# ♦ 電位 (Electric Potential)

- >電位與位能有密切關係,即每單位電荷的位能。
- ▶電位為純量,運算不需考慮向量問題。

$$W_{EXT} = +\Delta U = U_f - U_i = -W_c \ (\because v = const. \implies W_{net} = \Delta K = 0 = W_{EXT} + W_c)$$

●電位(electric potential)之定義:

$$\Delta V = \frac{\Delta U}{q} \implies \Delta V = \frac{W_{EXT}}{q} = -\frac{W_c}{q} = \frac{\vec{F}_c \cdot \Delta \vec{s}}{q} \quad \text{(SI $\mathbb{q}$ $\delta$ $\delta$ $1$ $V = 1$ J/C)}$$

考慮微量變化
$$\Rightarrow dV = \frac{dU}{q} = -\frac{W_c}{q} = -\frac{\bar{F}_c \cdot d\bar{s}}{q}$$

$$W_c$$
以靜電力作功表示 $\Rightarrow dV = -\frac{q\bar{E}\cdot d\bar{s}}{q} = -\bar{E}\cdot d\bar{s}$ 

$$\Rightarrow \Delta V = V_{\scriptscriptstyle B} - V_{\scriptscriptstyle A} = -\int_{\scriptscriptstyle A}^{\scriptscriptstyle B} \vec{E} \cdot d\vec{s}$$

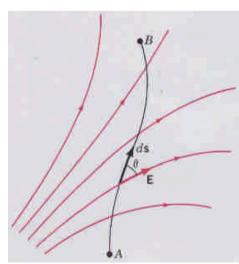


Fig.25.2

重力位能 $\Rightarrow U_g = mgy$ ; 電位能 $\Rightarrow U_E = qEy$ 

重力位
$$\Rightarrow U_g = gy$$
; 電位 $\Rightarrow V_E = Ey$ 

### ●均勻電場(uniform field)

$$\Delta V = -\int \vec{E} \cdot d\vec{s} = -\vec{E} \cdot \int d\vec{s} = -\vec{E} \cdot \Delta \vec{s}$$

電荷沿等位線移動不會造成電位差。 電位沿電場方向呈線性遞減。

如 Fig. 25.3  $\Rightarrow \Delta V = \pm Ed$  電場E的等效單位  $\Rightarrow$  1 V/m = 1 N/C

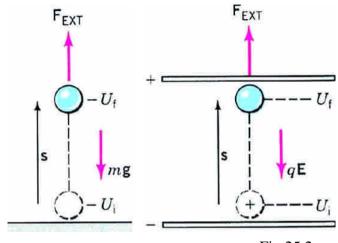


Fig.25.2

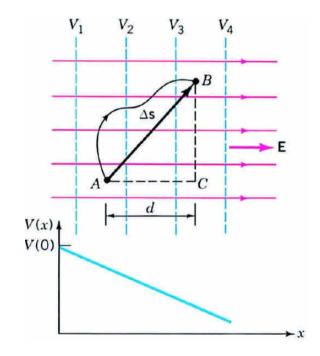


Fig.25.3

- ●等位線或等位面(equipotential)
  - □ \ \bigg\{ \bigs\} \bigg\} \frac{\partial 1. \partial \partial
- 带電粒子運動的能量

$$\Delta K + \Delta U = 0 \implies \Delta K = -\Delta U = -q\Delta V$$
$$\Rightarrow \Delta K = e\Delta V \quad (1 \ eV = 1.602 \times 10^{-19} \ J)$$

●點電荷的電位(potential of point charge)

$$\begin{split} \vec{E} &= E_r \hat{r} = \frac{kQ}{r^2} \hat{r} \\ V_B - V_A &= -\int_A^B \vec{E} \cdot d\vec{s} = -\int_A^B E_r dr = -\int_A^B \frac{kQ}{r^2} dr \\ &= -\left[ -\frac{kQ}{r} \right]_A^B = kQ \left( \frac{1}{r_B} - \frac{1}{r_A} \right) \end{split}$$
 考慮 $V_B = 0$  at  $r \to \infty$  , 則: $V = \frac{kQ}{r}$ 

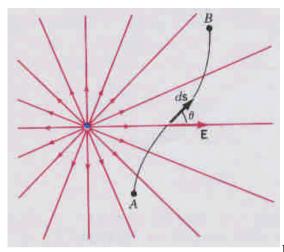
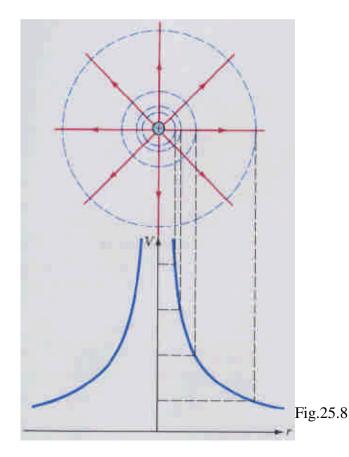


Fig.25.7



## •多個點電荷的電位

— 利用疊加原理(電位為純量,可直接進行加減) 
$$\Rightarrow V = \sum \frac{kQ_i}{r_i}$$

ightharpoonupCase (A)  $\Rightarrow$ V= 0 (如Fig.25.9),但E $\neq$  0 (如Fig.25.10)

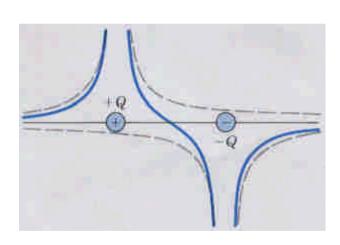


Fig.25.9

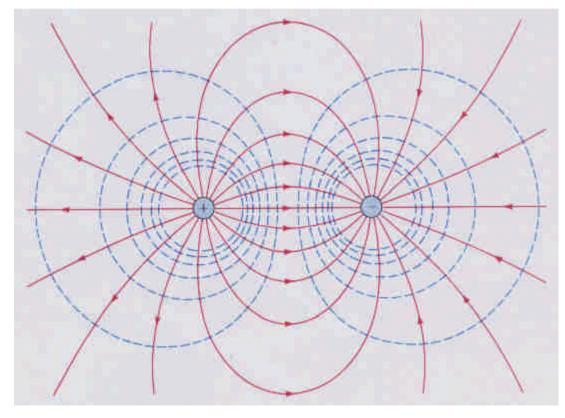
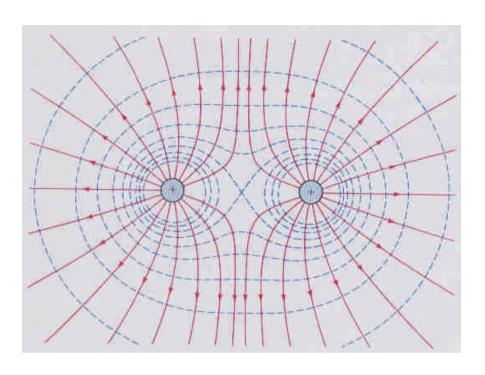


Fig.25.10

#### ightharpoonupCase (B) $\Rightarrow$ E= 0 (如Fig.25.11),但V $\neq$ 0 (如Fig.25.12)



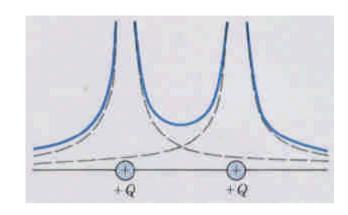


Fig.25.12

Fig.25.11

#### •雨點電荷的電位能

 $\Rightarrow U = qV = q(\frac{kQ}{r}) = \frac{kqQ}{r} \begin{cases} 若極性相同,則U>0,表外力作正功(即保守力作負功) \\ 若極性相異,則U<0,表外力作負功(即保守力作正功) \end{cases}$ 

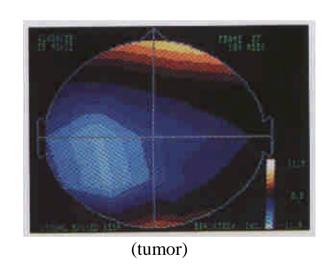
(相當於將兩電荷自無窮遠處等速移至相距 r 處外力所作的功)

$$\Delta U = U(r) - U(\infty) = q\Delta V = q(-\int_{\infty}^{r} \vec{E} \cdot d\vec{r}) = -q\int_{\infty}^{r} \frac{kQ}{r^{2}} dr = \frac{kqQ}{r} \implies U(r) = \frac{kqQ}{r} \quad (\because U(\infty) = 0)$$

### •多個點電荷的電位能

$$U_{ij} = \frac{kq_iq_j}{r_{ij}}$$
, but  $i \neq j$  (※計算總電位能須注意 $i \neq j$ )

▶腦部經閃光刺激後,可激發其電位的分佈



(Epilepsy)

Fig.25.14

### ●電位推導電場

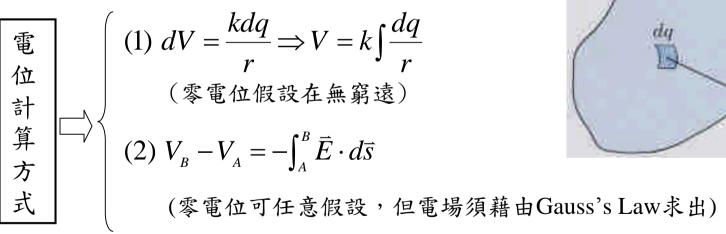
$$dV = -\vec{E} \cdot d\vec{s} = -Eds \cos \theta = -E \cos \theta ds = -E_s ds$$

$$\Rightarrow E_s = -\frac{dV}{ds}$$

考慮三維直角座標系⇒ 
$$dV = -\vec{E} \cdot d\vec{s} = -(E_x \hat{i} + E_y \hat{j} + \vec{E}_z \hat{k}) \cdot (dx \hat{i} + dy \hat{j} + dz \hat{k})$$
  
=  $-(E_x dx + E_y dy + E_z dz)$ 

其中 
$$E_x = -\left(\frac{dV}{dx}\right)_{y,z=\ const.} = -\left(\frac{\partial V}{\partial x}\right) \longrightarrow \vec{E} = -\left(\frac{\partial V}{\partial x}\right)\hat{i} - \left(\frac{\partial V}{\partial y}\right)\hat{j} - \left(\frac{\partial V}{\partial z}\right)\hat{k}$$

●連續電荷分佈(continuous charge distribution)



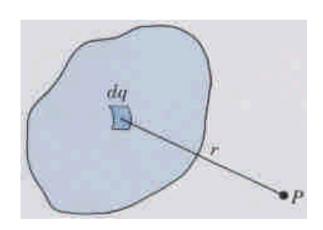


Fig.25.15

### Example 25.5:

單位環形面積所帶電荷 $\Rightarrow$   $dq = \sigma(2\pi x dx)$ 

$$dV = \frac{kdq}{r} = \frac{k\sigma(2\pi x dx)}{(x^2 + y^2)^{1/2}}$$

$$V = 2\pi k\sigma \int_0^a \frac{xdx}{(x^2 + y^2)^{1/2}} = 2\pi k\sigma \int_0^a \frac{(1/2)dx^2}{(x^2 + y^2)^{1/2}}$$
$$= 2\pi k\sigma \left[ \left( x^2 + y^2 \right)^{1/2} \right]_0^a$$
$$= 2\pi k\sigma \left[ \left( a^2 + y^2 \right)^{1/2} - y \right]$$

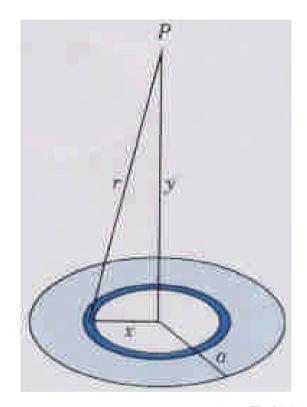


Fig.25.16

$$(\because \Rightarrow H = x^2 + y^2 \& dH = dx^2 \Rightarrow \int (\frac{1}{2})H^{-1/2}dH = H^{1/2} + c)$$

討論:

1.有限圓盤在無窮遠處可近似點電荷,即  $y>>a \rightarrow V \approx \frac{kQ}{y}$ 

2.推導電場(習題 Ex.47)

$$E_{y} = -\frac{\partial V}{\partial y} = -\frac{\partial}{\partial y} \left\{ 2\pi k\sigma \left[ \left( a^{2} + y^{2} \right)^{1/2} - y \right] \right\} = -2\pi k\sigma \frac{\partial}{\partial y} \left[ \left( a^{2} + y^{2} \right)^{1/2} - y \right]$$

$$= -2\pi k\sigma \left[ y \left( a^{2} + y^{2} \right)^{-1/2} - 1 \right] = 2\pi k\sigma \left[ 1 - y \left( a^{2} + y^{2} \right)^{-1/2} \right]$$
(Figure 1) (Figure 23.8 states as the proof of the pro

### Example 25.6:

When 
$$r > R \implies E = \frac{kQ}{r^2}$$
;  $V(r) - V(\infty) = -\int_{\infty}^{r} \vec{E} \cdot d\vec{r}$   

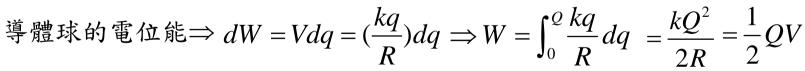
$$= -\int_{\infty}^{r} (\frac{kQ}{r^2} \hat{r}) \cdot d\vec{r} = -\int_{\infty}^{r} \frac{kQ}{r^2} dr = -kQ \left[ -\frac{1}{r} \right]_{\infty}^{r} = \frac{kQ}{r}$$

$$\therefore V(\infty) = 0 \implies V(r) = \frac{kQ}{r}$$

When 
$$r < R \implies E = 0$$
 ;  $V(r) - V(R) = 0$ 

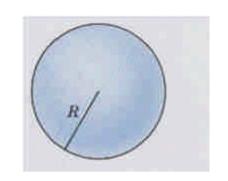
$$V(R) = \frac{kQ}{R} \implies V(r) = \frac{kQ}{R}$$

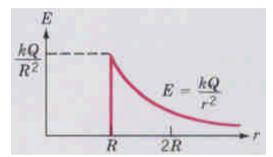
## Example 25.7:

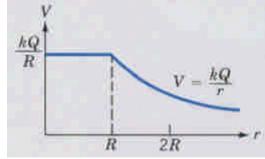


(考慮外力將dq自無窮遠移至導體球上所作的功)

**Disscussion**: U=QV 表單一電荷 ; U=1/2 QV 表系統電荷









# ♦ 導體(conductors)

- ●在靜電平衡狀態下,導體內部與表面的電位皆相同。
  - ▶導體內部空腔之電場為0,即所謂的屏蔽效應。

$$V_{\scriptscriptstyle B} - V_{\scriptscriptstyle A} = -\int_{\scriptscriptstyle A}^{\scriptscriptstyle B} \vec{E} \cdot d\vec{s}$$
 ; If  $V_{\scriptscriptstyle B} = V_{\scriptscriptstyle A} \Longrightarrow \vec{E} = 0$ 

▶在均勻電場中的電中性導體,接近球面等位面為 圓形,電力線呈輻射狀。

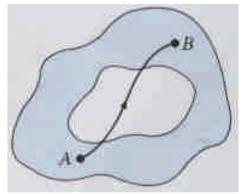


Fig.25.18

- ●導體曲率半徑愈小,則電荷密度愈大。
  - > 導線相連的導體球

$$V_1 = V_2 \implies \frac{Q_1}{R_1} = \frac{Q_2}{R_2} \implies \frac{4\pi R_1^2 \sigma_1}{R_1} = \frac{4\pi R_2^2 \sigma_2}{R_2}$$

$$\Rightarrow \frac{\sigma_1}{\sigma_2} = \frac{R_2}{R_1} \Rightarrow \sigma_1 R_1 = \sigma_2 R_2$$

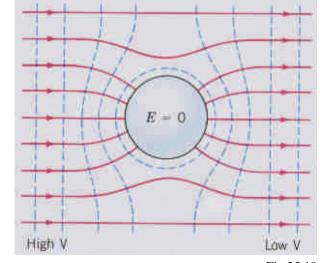


Fig.25.19



Fig.25.20

#### ▶尖端放電(discharge)

因靠近導體表面  $E=\sigma/\varepsilon_0$ , 由此推知,愈尖 銳處會有較大的電場E, 若電場足夠大  $(\sim 3\times 10^6~V/m)$ , 則在空氣中造成放電現 象。

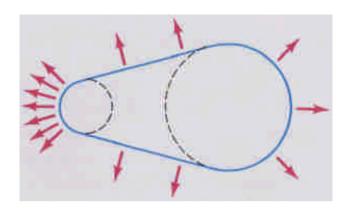


Fig.25.21

#### 崩潰(breakdown)電場的發生

一因宇宙射線及大地輻射導致空氣分子部份解離,而電場作用會導致已解離的電子加速撞擊其他分子形成更多離子,致使空氣失去絕緣特性變成導體,造成電量放電 (corona discharge)。

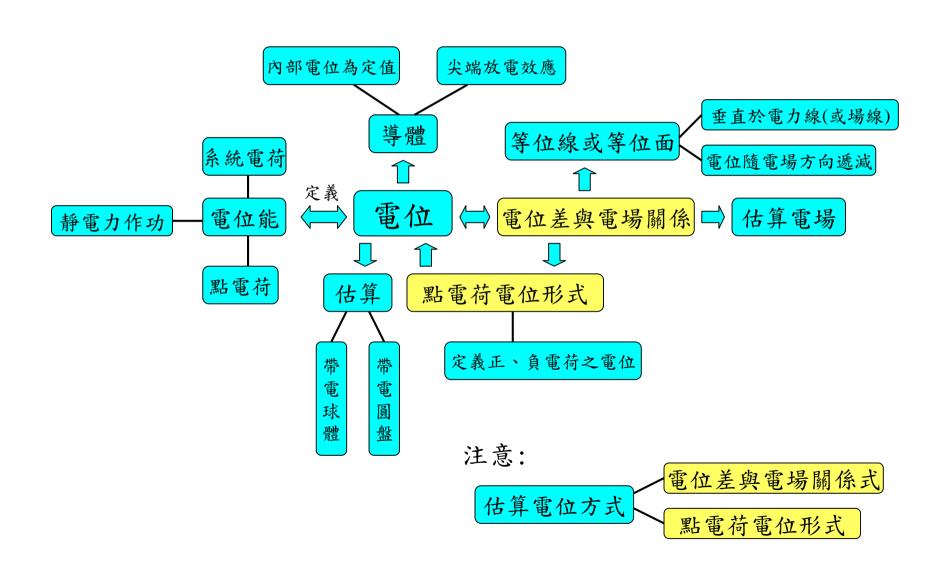
#### 應用

避雷針(lightning rod)、飛機機翼的拖曳短線、場離子顯微鏡(field-ion microscopy)、高壓設備的平緩表面(防止放電)。

塵爆(dust explosion)—半徑0.05 mm的灰塵粒子在150V即能放電。

V=kQ/R,  $E=kQ/R^2 \Rightarrow V=ER \Rightarrow V \propto R$ 

# 本章重要觀念發展脈絡彙整



## 習題

●教科書習題 (p.503~p.508)

Exercise: 5,11,15,17,21,23,25,31,35,37,43,45,47,51,57,61,65,69,73

Problem: 5,7,10,11,12,13

**%**Hint: Problem 12 Ans. (b)  $E_r = 2kp \cos\theta/r^3$ ;  $E_{\theta} = kp \sin\theta/r^3$ 

#### •基本觀念問題:

- 1.請寫出電位差與電場關係式
- 2.請說明導體尖端放電原理。

#### •延伸思考問題:

1.請探討Example 25-5帶電圓盤表面的電位。

# ◆電容器(Capacitor)

儲存電荷

來登瓶 (Leyden jar)

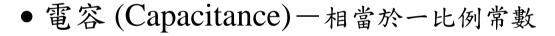
金屬平 板電容 Water (a)

(Von Kleist)





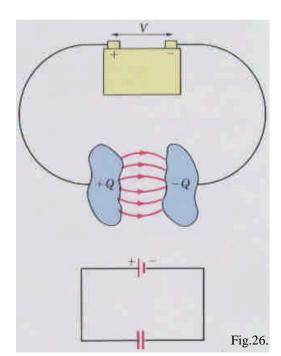
- 1.Radios & Tvs (濾波器應用)



$$Q = C\Delta V$$
 一儲存電荷(Q)正比於兩板間的電位差 $\Delta V$  =  $CV$  (將 $\Delta V$ 視為一參數 $V$ )

$$\Rightarrow C = \frac{Q}{V}$$
  $\Rightarrow$  SI unit: 1 farad=1 coulomb/volt

一般電容器的電容值約 $1pF(10^{-12}F)$ 或  $1\mu F(10^{-6}F)$ 。



## ● 平行電板電容(Parallel-Plate Capacitor)

$$E = \frac{\sigma}{\varepsilon_0} = \frac{Q}{\varepsilon_0 A} \qquad (\because \sigma = \frac{Q}{A})$$

$$C = \frac{Q}{V} = \frac{Q}{Ed} = \frac{Q}{(\frac{Q}{\varepsilon_0 A})d} = \frac{\varepsilon_0 A}{d}$$

電容C與電容的幾何性質有關:

$$\begin{cases} If \ \ V = const. \ \Rightarrow \ C \propto Q \ \Rightarrow \ \begin{cases} Q = \sigma A \Rightarrow Q \propto A \\ Q = \varepsilon_0 EA = \varepsilon_0 VA/d \Rightarrow Q \propto 1/d \end{cases}$$

$$If \ \ Q = const. \ \Rightarrow \ C \propto 1/V \Rightarrow V = Ed \ \ (\because E = \frac{Q}{\varepsilon_0 A} = const.) \Rightarrow V \propto d \Rightarrow C \propto 1/d$$

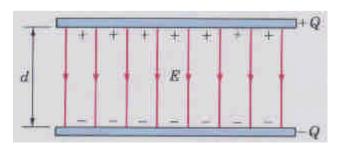
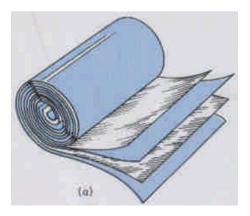


Fig.26.4



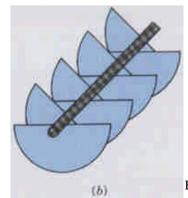


Fig.26.5

## Example 26.3:孤立導體球的電容?

假設導體球表面帶電+Q,而地面為電容的另一面

$$C = \frac{Q}{V} = \frac{Q}{|V(R) - V(\infty)|} = \frac{Q}{kQ/R} = \frac{R}{k} = 4\pi\varepsilon_0 R \qquad (\because k = \frac{1}{4\pi\varepsilon_0})$$

Example 26.4: 球形電容器(spherical capacitor)

$$V_{2} - V_{1} = -\int_{R_{1}}^{R_{2}} E_{r} dr = -\int_{R_{1}}^{R_{2}} \frac{kQ}{r^{2}} dr = -\left[-\frac{kQ}{r}\right]_{R_{1}}^{R_{2}} = kQ\left(\frac{1}{R_{2}} - \frac{1}{R_{1}}\right)$$

$$C = \frac{Q}{V} = \frac{Q}{|V_{2} - V_{1}|} = \frac{Q}{kQ\left(\frac{1}{R_{1}} - \frac{1}{R_{2}}\right)} = \frac{R_{1}R_{2}}{k(R_{2} - R_{1})}$$

Fig.26.6

#### Discussion:

(a) If 
$$R_2 >> R_1 \Rightarrow C = \frac{R_1 R_2}{k(R_2 - R_1)} \approx \frac{R_1 R_2}{kR_2} = \frac{R_1}{k} = 4\pi\epsilon_0 R_1$$
 (近似孤立導體球電客)

(b) If 
$$R_2 \approx R_1 = R$$
,  $R_2 - R_1 = d \implies C = \frac{R_1 R_2}{k(R_2 - R_1)} \approx \frac{R^2}{kd} = \frac{4\pi \varepsilon_0 R^2}{d} = \frac{\varepsilon_0 A}{d}$  (::  $A = 4\pi R^2$ )

(近似乎行電板電容)

Example 26.5: 圓柱形電容器(cylindrical capacitor)

$$C = \frac{Q}{|V_b - V_a|} = \frac{\lambda L}{2k\lambda \ln(b/a)} = \frac{L}{2k\ln(b/a)} = \frac{2\pi\varepsilon_0 L}{\ln(b/a)}$$

$$V_b - V_a = -\int_a^b E_r dr = -\int_a^b \left(\frac{2k\lambda}{r}\right) dr = -2k\lambda \int_a^b \frac{dr}{r} = -2k\lambda \ln \frac{b}{a}$$

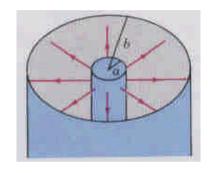
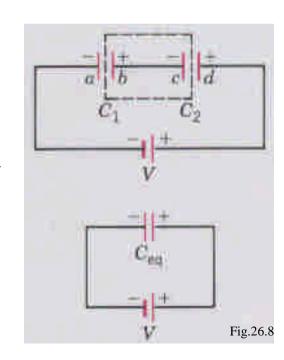


Fig.26.7

•電容串聯(series) 
$$\begin{cases} Q = Q_1 = Q_2 \\ V = V_1 + V_2 \end{cases}$$

$$\Rightarrow V = V_1 + V_2 \Rightarrow \frac{Q}{C_{eq}} = \frac{Q_1}{C_1} + \frac{Q_2}{C_2} \Rightarrow \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$
(series) 
$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \cdots + \frac{1}{C_N}$$



•電容並聯(parallel) 
$$\begin{cases} V = V_1 = V_2 \\ Q = Q_1 + Q_2 \end{cases}$$
$$\Rightarrow Q = Q_1 + Q_2 \Rightarrow C_{eq}V = C_1V_1 + C_2V_2 \Rightarrow C_{eq} = C_1 + C_2$$
$$(parallel) \quad C_{eq} = C_1 + C_2 + \cdots + C_N$$

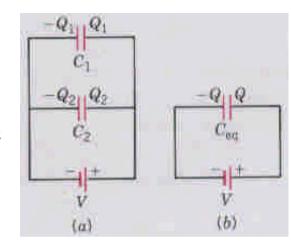


Fig.26.9

●電容儲存的能量(Energy stored in a capacitor)

dW = Vdq = (q/C)dq (假設dq 經導線自負極板移至正極板)

$$\Rightarrow W = \int_0^Q \frac{q}{C} dq = \frac{Q^2}{2C} = \frac{1}{2}QV = \frac{1}{2}CV^2 = U_E$$

考慮平行電板電容 $\Rightarrow C = \frac{\varepsilon_0 A}{d}, V = Ed$ 

$$U_E = \frac{1}{2}CV^2 = \frac{1}{2}\frac{\varepsilon_0 A}{d} \cdot (Ed)^2 = \frac{1}{2}\varepsilon_0 E^2(Ad)$$

$$u_E(energy\ density) = U_E / Ad(體積) = \frac{1}{2}\varepsilon_0 E^2$$

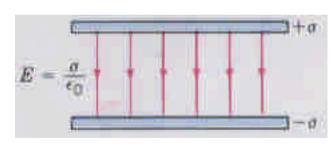


Fig.26.12

(能量以電場形式儲存,亦 即電容係儲存電能。) Example 26.5: 如Fig.26.11, 求初始狀態(a)及末狀態(b)的兩電容器上 的電荷、電位差及其儲存能量大小。

$$\begin{cases} Q_1 = C_1 V_1 = 5\mu \times 12 = 60\mu C \\ Q_2 = C_2 V_2 = 3\mu \times 12 = 36\mu C \end{cases}$$

$$\begin{cases} W_1 = V_2 = 12V \\ U_1 = \frac{1}{2}Q_1 V_1 = \frac{1}{2}(60\mu C)(12V) = 360\mu J \\ U_2 = \frac{1}{2}Q_2 V_2 = \frac{1}{2}(36\mu C)(12V) = 216\mu J \end{cases}$$

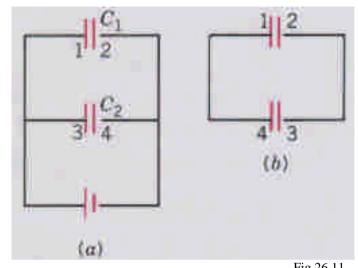


Fig.26.11

重新組合並聯後,假設兩電容的電荷分別為 Q',Q'

末 
$$Q'_1 + Q'_2 = 60\mu C - 36\mu C = 24\mu C$$
 (1)  $\Rightarrow Q'_1 = V'_2 \Rightarrow \frac{Q'_1}{C_1} = \frac{Q'_2}{C_2} \Rightarrow \frac{Q'_1}{5\mu F} = \frac{Q'_2}{3\mu F} \Rightarrow 3Q'_1 - 5Q'_2 = 0$  (2)  $\Rightarrow Q'_1 = 15\mu C, \ Q'_2 = 9\mu C$  (b)  $V'_1 = V'_2 = \frac{Q'_2}{C_2} = \frac{9\mu C}{3\mu F} = 3V$  ; 
$$\begin{cases} U_1 = \frac{1}{2}Q'_1V'_1 = \frac{1}{2}(15\mu C)(3V) = 22.5\mu J \\ U_2 = \frac{1}{2}Q'_2V'_2 = \frac{1}{2}(9\mu C)(3V) = 13.5\mu J \end{cases}$$

Example 26.9: 孤立金屬球的電位能

$$dU_{E} = u_{E}(dV_{volume}) = \frac{1}{2}\varepsilon_{0}E^{2}(4\pi r^{2}dr)$$

$$= \frac{1}{2}\varepsilon_{0}\left(\frac{kQ}{r^{2}}\right)^{2}\left(4\pi r^{2}dr\right) = \frac{kQ^{2}}{2r^{2}}dr$$

$$\left[\because E = \frac{kQ}{r^{2}}, \quad as \quad r > R\right]$$

$$U_{E} = \frac{kQ^{2}}{2}\int_{R}^{\infty} r^{-2}dr = \frac{kQ^{2}}{2}\left[-\frac{1}{r}\right]_{R}^{\infty} = \frac{kQ^{2}}{2R}$$

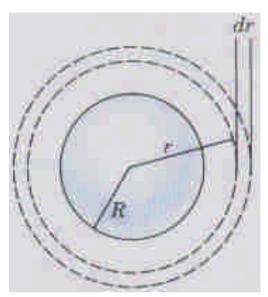
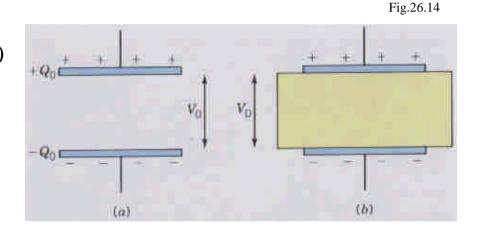


Fig.26.13

# ♦介電質(Dielectrics)

- 一將電容兩平板間插入非導電物質會導致電容增加,而此非導電物質即介電質,但也有例外,如:水。
  - (i)未接電池⇒電位差V會改變,電荷Q不變。

$$\Rightarrow V_D = \frac{V_0}{\kappa} \quad (\kappa A \Lambda)$$
 電質常數  $, \kappa \ge 1$  
$$\Rightarrow E_D = \frac{E_0}{\kappa} \quad (\because V = Ed)$$
 
$$\Rightarrow C_D = \frac{Q_0}{V_D} = \frac{Q_0}{V_0/\kappa} = \kappa C_0$$



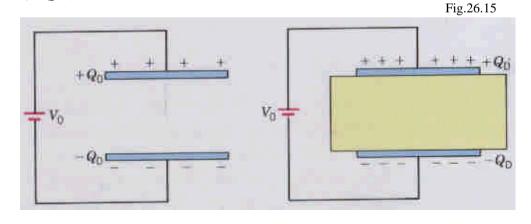
(ii)連接電池⇒電位差V不變,電荷Q會改變。

$$\Rightarrow Q_D = \kappa Q_0$$

$$\Rightarrow C_D = \frac{Q_D}{V_0} = \frac{\kappa Q_0}{V_0} = \kappa C_0$$

$$(\because E = \sigma / \varepsilon_0 \Rightarrow E = \kappa E_0 ,$$

$$\therefore E_D = E / \kappa = \kappa E_0 / \kappa = E_0)$$



#### •介電質的優點:

- 1.可增加電容。
- 2.可減小電容的體積。
- 3.可增加臨界電位差(或介電強度),使電容 不致放電崩潰。



一使介電質喪失絕緣特性而崩潰放電的 最大電場強度。

### ●介電質的原子觀點(Atomic view of dielectrics)

- ▶介電質常數(Dielectric Constant) K相當於該電介質內部電荷對外部電場的反應程度。
- ▶一般分子密度較低,其介電質常數 K 亦較小,如氣體。
- ▶介電質若為非極性分子,則由於外加電場的作用會形成感應電偶極矩 (induced dipole moment)。

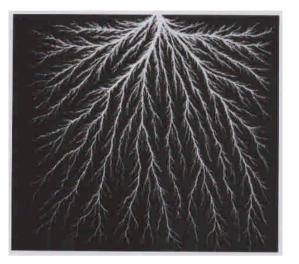
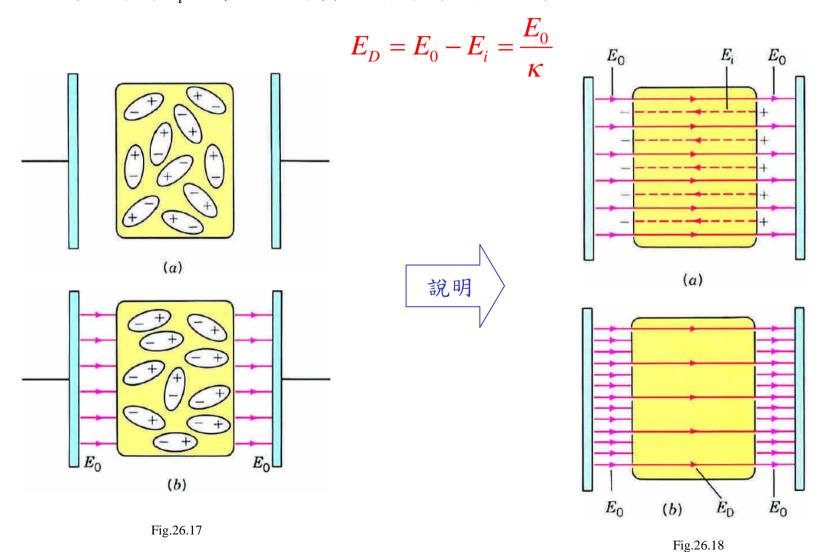


Fig.26.16

STRENGTHS		
Material	Dielectric Constant	Dielectric Strength (106 V/m)
Air	1.00059	3
Paper	3.7	16
Glass	4-6	9
Paraffin	2.3	11
Rubber	2-3.5	30
Mica	6	150
Water	80	_

 $\blacktriangleright$  感應電偶極矩及永久電偶極矩皆會沿外加電場方向排列,最後在介電質兩端造成電荷區隔現象,即所謂的電極化(polarization)現象,如Fig.26.17。其中區隔的感應電荷極性與平板極性相反,在介電質內部形成與外部電場 $E_0$ 指向相反的感應電場 $E_i$ ,導致介電質的淨電場減小,即:



Example 26.10 已知介電質的厚度 t、介電質常數κ、平行電板的面積A及分隔距離d,求Fig.26.19的電容?

$$E_{0} = \frac{\sigma}{\varepsilon_{0}} \quad \text{and} \quad E_{D} = \frac{E_{0}}{\kappa}$$

$$\Rightarrow V = E_{0}(d-t) + E_{D}t$$

$$= \frac{\sigma}{\varepsilon_{0}} \left[ (d-t) + \frac{t}{\kappa} \right]$$

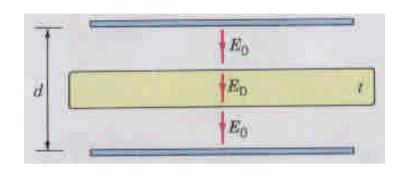


Fig.26.19

$$C = \frac{Q}{V} = \frac{\sigma A}{\frac{\sigma}{\varepsilon_0} \left[ (d - t) + \frac{t}{\kappa} \right]} = \frac{\varepsilon_0 A}{d + t(\frac{1}{\kappa} - 1)}$$

(note: If 
$$\kappa = 1$$
, then  $C = \frac{\varepsilon_0 A}{d}$ )

• 考慮介電質的高斯定律  $\Rightarrow \oint \bar{E} \cdot d\bar{A} = \frac{Q_f}{\varepsilon}$  (※以下推導證明僅供參考,不列入考試範圍)

$$E_{D} = E_{0} - E_{i} = \frac{E_{0}}{\kappa} \Rightarrow \frac{\sigma_{f}}{\varepsilon_{0}} - \frac{\sigma_{b}}{\varepsilon_{0}} = \frac{\sigma_{f}}{\kappa \varepsilon_{0}} \Rightarrow \sigma_{f} A - \sigma_{b} A = \frac{\sigma_{f} A}{\kappa} \Rightarrow Q_{f} - Q_{b} = \frac{Q_{f}}{\kappa}$$

考慮如右圖虛線的封閉曲面積分:

$$\begin{split} \oint \vec{E} \cdot d\vec{A} &= \int \vec{E}_D \cdot d\vec{A} = (E_0 - E_i)A = (\frac{\sigma_f}{\varepsilon_0} - \frac{\sigma_b}{\varepsilon_0})A \\ &= \frac{1}{\varepsilon_0} (\sigma_f A - \sigma_b A) = \frac{1}{\varepsilon_0} (Q_f - Q_b) = \frac{Q_f}{\kappa \varepsilon_0} = \frac{Q_f}{\varepsilon} \end{split}$$

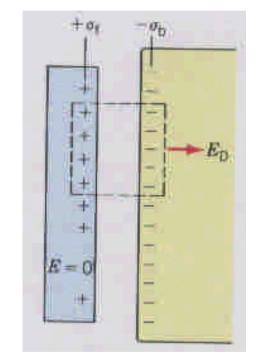
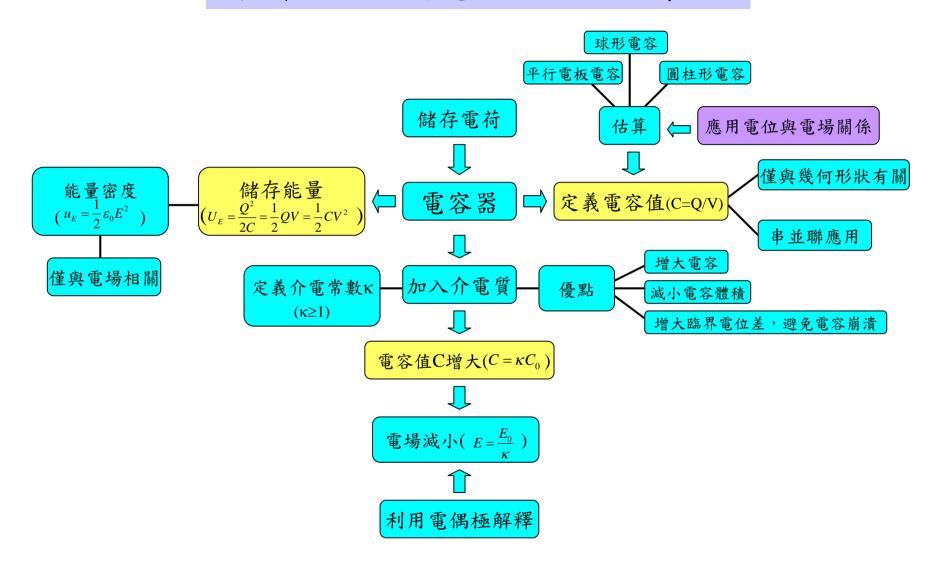


Fig.26.20

# 本章重要觀念發展脈絡彙整



# 習題

●教科書習題 (p.525~p.529)

#### Exercise:

7,11,13,15,19,21,25,29,31,33,34,35,41,42,43,47,53,57,59,63

Problem: 1,8,9,11,13

#### **※**Hint:

Ex34 Ans. (a)None; (b)Halved; (c)Halved

Ex42 Ans. 
$$\frac{2\kappa_1\kappa_2C_0}{\kappa_1+\kappa_2}$$

Problem 8 Ans. CV<sup>2</sup>/2κ (題目修訂:....constant κλ修訂為κ)

#### •基本觀念問題:

- 1.請問電容器加入介電質的優點為何?
- 2.請問電容器崩潰放電的原因為何?