

SECTION-A

Answer all the questions. Each carries two marks

10 x 2 = 20

Note: Write the answers in orderly at one place

1. The general solution of the differential equation $(D^3 - 3D - 2)y = 0$ is ...

A. $y(x) = (c_1 + c_2x)e^{-x} + c_3e^{2x}$

B. $y(x) = (c_1 + c_2x)e^{-2x} + c_3e^{-x}$

C. $y(x) = (c_1 + c_2x)e^x + c_3e^{2x}$

D. $y(x) = (c_1 + c_2x)e^x + c_3e^{-2x}$

2. The general solution of differential equation $4x^2y'' + y = 0$ is ...

A. $y(x) = (c_1 + c_2 \ln x)x^{-1/2}, x > 0$

B. $y(x) = (c_1 + c_2x)e^{x/2}, x > 0$

C. $y(x) = (c_1 + c_2x)e^{x/2}, x > 0$

D. $y(x) = (c_1 + c_2 \ln x)x^{1/2}, x > 0$

3. The particular Integral of $y'' + y = 6 \sin x$ is ...

A. $y_p = 3x \cos x$

B. $y_p = -3x \cos x$

C. $y_p = -3x \sin x$

D. $y_p = 3x \sin x$

4. By changing the order of integration, the integral $\int_{-a}^a \int_0^{\sqrt{a^2-y^2}} f(x,y) dx dy$ transformed to ...

A. $\int_{-a}^a \int_{-\sqrt{a^2-x^2}}^{\sqrt{a^2-x^2}} f(x,y) dy dx$

B. $\int_0^a \int_0^{\sqrt{a^2-x^2}} f(x,y) dy dx$

C. $\int_0^a \int_{-\sqrt{a^2-x^2}}^{\sqrt{a^2-x^2}} f(x,y) dy dx$

D. $\int_{-a}^a \int_0^{\sqrt{a^2-x^2}} f(x,y) dy dx$

5. The value of the integral $\int \int_R x^2 dx dy$ over the region R bounded by the hyperbola $xy=4, y=0, x=1, x=4$ is...

A. $-16/3$

B. $16/3$

C. -30

D. 30

6. The value of the integral $\int \int \int (x+y+z) dz dy dx$ over the volume bounded by the planes $x=0, x=1, y=0, y=1, z=0, z=1$ is...

A. $\frac{5}{2}$

B. $\frac{3}{2}$

C. $\frac{-3}{2}$

D. $\frac{-5}{2}$

7. The gradient of a scalar point function $\ln(x+y+z)$ at $(1,2,-1)$ is...

A. $\frac{i+j+k}{2}$

B. $\frac{i-j+k}{2}$

C. $\frac{i-j-k}{2}$

D. $\frac{-i-j-k}{2}$

8. The value of the integral $\int \int \frac{1}{xy} dx dy$, over the region bounded by $1 \leq x \leq 2, 1 \leq y \leq 2$ is...

A. $\log 2^2$ B. $2\log 2$ C. $\log 4$ D. $(\log 2)^2$

9. If $f(x, y, z) = x \sin(x + y + z)$, then $\text{Curl}(\text{grad} f)$ is...

A. 0 B. $\vec{0}$ C. 1 D. -1

10. If $f(x, y, z) = x^2 - y^2$, C is the closed curve $x = 3\cos t, y = 3\sin t, 0 \leq t \leq 2\pi$ then $\int_C f(x, y, z) ds = \dots$

A. $\frac{2}{3}$ B. $-\frac{2}{3}$ C. 0 D. $\frac{5}{3}$

SECTION-B

Answer any two of the following questions.

2 x 5

=10

11. [2+3]

(a) Find the equation of the tangent plane to the surface $z = 16 - x^2 - y^2$ at $(1, 3, 6)$.

(b) Find the directional derivative of xyz at $(1, 4, 3)$ in the direction of the line from $(1, 2, 3)$ to $(1, -1, -3)$.

12. [2+3]

(a) Find the particular Integral of $(D^3 + 1)y = \cos(2x - 1)$

(b) Solve $y'' + 16y = 32\sec 2x$ by the method of variation of parameters

13. [5]

Find the volume of the solid in the first octant bounded by the paraboloid

$$z = 36 - 4x^2 - 9y^2$$

14. [2+3]

(a) Evaluate the integral $\int \int_R e^{x^2} dx dy$, where R is the region given by $R = \{(x, y) : 2y \leq x \leq 2, 0 \leq y \leq 1\}$

(b) Evaluate $\int \int r^3 dr d\theta$ over the area included between the circles $r = 2\sin\theta$ and $r = 4\sin\theta$.

End os the MT Question paper