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## Search algorithms implemented

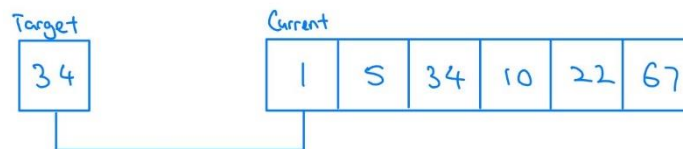
### Linear Search

Linear search appears as a simple search method that often referred to as sequential search. It starts the search by visiting all the elements one by one from the beginning of a collection of elements. The search will go through the whole collection until the desired value is found.

Figure 1.1 is a visualization of how Linear Search functions with the provided array and target value:

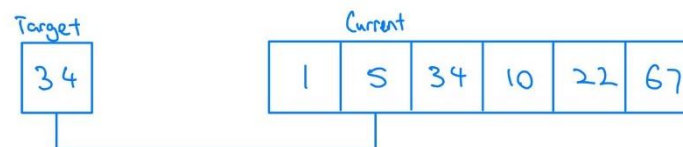
Target : 34      Arr[] = { 1 , 5 , 34 , 10 , 22 , 67 }

First Iteration:



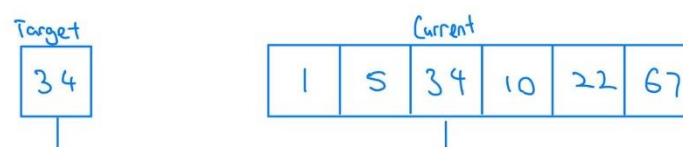
Target  $\neq$  current. Moving to next element.  
34  $\neq$  1

Second Iteration:



Target  $\neq$  current. Moving to next element.  
34  $\neq$  5

Third Iteration:



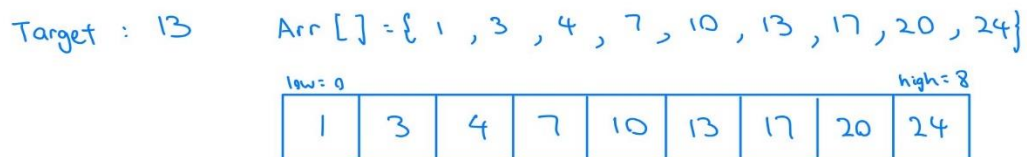
In this iteration, target and current have the same value which means that the target has been found from the array. The search will end.

Figure 1.1 – Example Linear Search

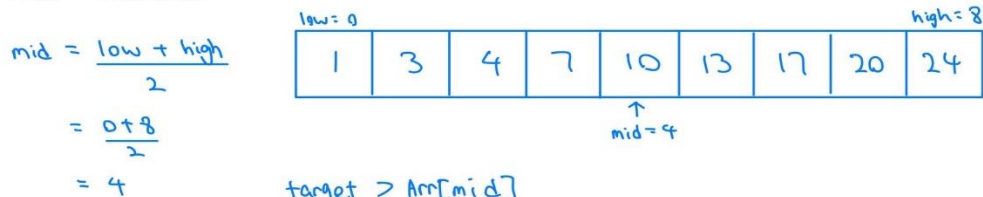
## Binary Search

Binary Search algorithm looks for a certain value in a sorted array. It will divide the search array in half to find the middle index (GeeksforGeeks, 2024). It will then compare this value with the target value if they have the same value means that the target is found and the process will terminate. If not, the algorithm will decide between the divided arrays to continue the search. The left array will be used for the next search if the target has a smaller value than the middle element, and vice versa. The search will continue to work until the target value is found.

Figure 1.2 is a visualization of how Binary Search functions with the provided sorted array and target value:



First Iteration:



target > Arr[mid]  
13 > 10 .

Since the target value is greater than the middle element, the right array of the middle element will be used for the following search.

Second Iteration:



target < Arr[mid]  
13 < 17 .

Since the target value is smaller than the middle element, the left array of the middle element will be used for the following search.

Third Iteration:

$$\begin{aligned} \text{mid} &= \frac{\text{low} + \text{high}}{2} \\ &= \frac{5 + 5}{2} \\ &= 5 \end{aligned}$$

$\text{low} = \text{high} = 5 = \text{mid}$

1	3	4	7	10	13	17	20	24
---	---	---	---	----	----	----	----	----

$$\begin{aligned} \text{target} &= \text{Arr}[\text{mid}] \\ 13 &= 13. \end{aligned}$$

In this iteration, there is only one element left and it is also same with the target value. The target value has been found and the search will stop.

Figure 1.2 – Binary Search

### **Sort algorithms implemented**

#### **Merge Sort**

Merge sort is a divide and conquer method that works by iteratively dividing the array into smaller subarrays until each subarray has only 1 element. The sub-arrays are then combined back together in sorted order.

Figure 1.3 is a visualization of how Merge Sort functions with the provided array:

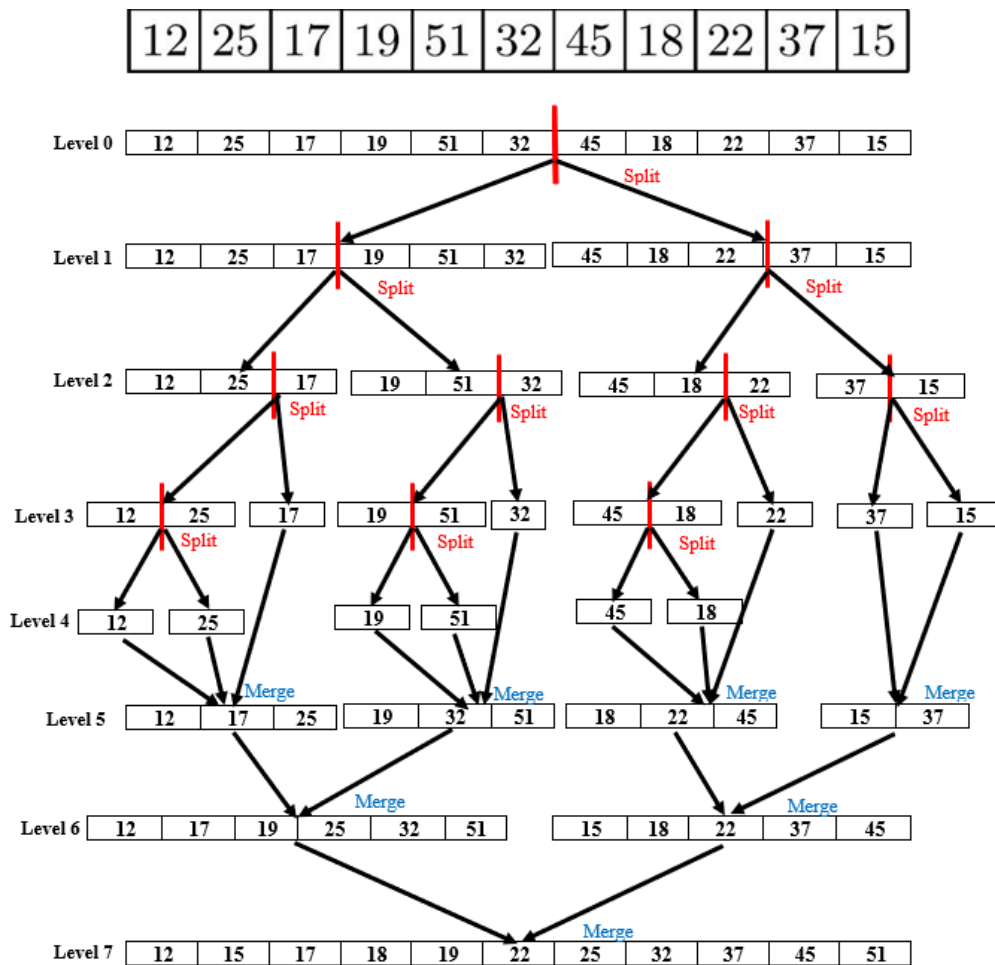


Figure 1.3 – Merge Sort

At Level 0, an array of 11 elements is split in half using the middle of the array found by applying the following formula:

$$mid = \frac{a[i]}{2}$$

$$mid = \frac{a[11]}{2}$$

$$= a[5]$$

Following the formula, we found that the middle lies at a [5], then we split the array into two halves:

Left half: [12, 25, 17, 19, 51, 32]

Right half: [45, 18, 22, 37, 15]

Subsequently, every array is split in half recursively until it reaches just one element.

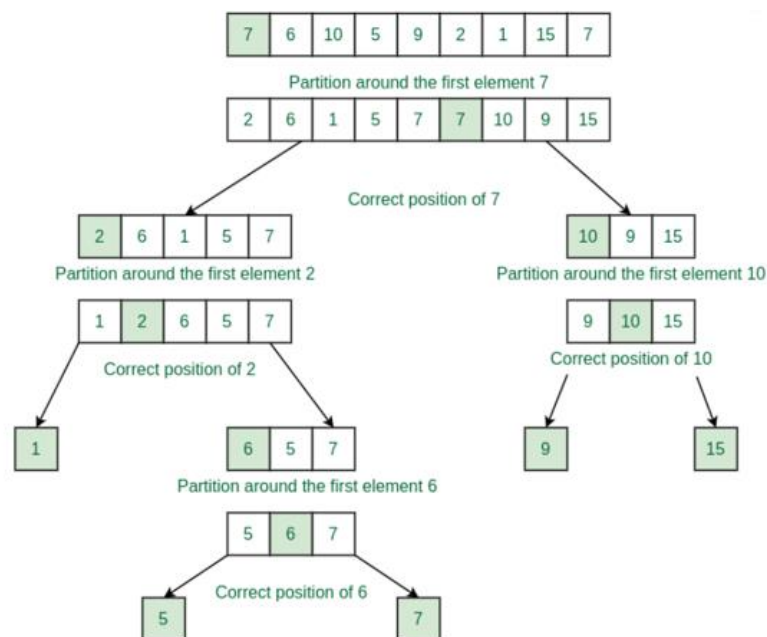
At Level 4, every element has been divided into a single element. Then at level 5, they are all merged together in a sorted order. Three rounds of merging will occur until level 7, at which point each element in the array is sorted.

## Quicksort

Quicksort is also a divide-and-conquer algorithm by dividing the array into sections centered on the pivot element. Multiple varieties of quick sort apply different algorithms to identify the pivot.

- The first element as pivot
- The last element as pivot
- A random element is chosen as pivot
- The median is chosen as pivot

Figure 1.4 is a visualization of how Quicksort performs by selecting the first element as a pivot:



Output:

1	2	5	6	7	7	9	10	15
---	---	---	---	---	---	---	----	----

Figure 1.4 – Quick Sort

A partition serves as a Quicksort's main function. If the array is sorted, partitioning

aims to place the pivot in the correct place; place elements that have a smaller value or equal to the pivot to the left of the array, place elements that have a greater value than the pivot to the right array and accomplish this all-in linear time.

The example above shows that the first element is selected as the pivot. After that, each element is compared to the pivot; if it is smaller than the pivot, it is positioned to the left of the array's partition, and if it is greater than the pivot, it is positioned to the right array's partition. The process will end until every element in the array has been sorted (GeeksforGeeks, 2024).

### Bubble Sort

Bubbles sort compares the current elements to the nearby elements in the array. In the first iteration, it will compare the first element of the array to the next element. If the initial element is greater than the adjacent elements, it will swap their position. This process will keep repeating for each pair of adjacent entries until it reaches the end of the list. After first iteration, the largest element will be move to the end which is the correct position.

In the second iteration, the last element will not be compared since it is in the correct position. This process will be repeated until no more swaps are needed which means it is sorted (GeeksforGeeks, 2024).

Below is a visualization of how Bubble Sort functions with the provided array:

The unsorted array:

[45, 21, 48, 67, 32]

Array	45	21	48	67	32
Index	0	1	2	3	4

In 1<sup>st</sup> iteration, it will start from index 0 and compare to its adjacent index. If index  $i$  is greater than  $i+1$  then it will swap. Since 45 is greater than 21 then it will swap.

Array	21	45	48	67	32
Index	0	1	2	3	4



Now it will compare between 45 and 48. Since 48 is greater, it will not carry out the swapping operation. Then it will continue to compare between 48 and 67. Since 67 is still greater than 48 then it will move to the next index to do the comparison. Now it will compare between 67 and 32. 67 is greater than 32 then it will swap.

Array	21	45	48	32	67
Index	0	1	2	3	4

In the second iteration, the last elements in the array will not be compared because it was already in the correct position. It will now start from index 0 again and compare. The swapping process in the second iteration is on the comparison between 48 and 32.

Array	21	45	32	48	67
Index	0	1	2	3	4

48 and 67 are in the right position so both will not be sorted again. The swapping process in the third iteration is between 45 and 32.

Array	21	32	45	48	67
Index	0	1	2	3	4

Lastly, our array is in the sorted form where the swapping process in that iteration is not carried out. Therefore, it comes out with the final sorted result.

[21, 32, 45, 48, 67]

### **Best search algorithms implemented**

Between these two search methods, I think Binary Search is better than Linear Search. There are several reasons for me to prove that Binary Search is better.

First of all, in terms of time complexity, Binary Search achieves time complexity of  $O(\log n)$  and Linear Search has a time complexity of  $O(n)$ . We can see that this is quite obvious that Binary Search is faster than Linear Search, especially for the huge datasets. It can save a lot of time and be quite effective. Whereas Linear Search requests that every element be checked, Binary Search remains a somewhat steady efficiency even in the worst of circumstances.

In terms of pre-processing and indexing, Binary Search can be used in conjunction with pre-processing and indexing procedures to further improve search efficiency. For instance, multi-level index structures such as Binary trees can be utilized to increase search performance on large-scale data sets. However, it is difficult for Linear Search to achieve significant performance improvements through pre-processing or indexing in unordered data.

Therefore, I believe that Binary Search is the best search algorithm due to its effectiveness.

### **Best sorting algorithms implemented**

In my opinion, Merge sort is the best sorting algorithm among all the sorting algorithms we've created. This is because it applies the concept of divide and conquer by recursively dividing an array into half and then sorting the divided array. After that, it will combine all the sorted arrays.

Besides, I choose merge sort as the best sorting algorithm as it is more stable due to its ability to preserve the relative order of records with equal keys. Moreover, its performance does not degrade with specific input patterns. Therefore, it is more suitable for handling large datasets because of its consistent time complexity of  $O(n \log n)$  for all cases.

Moving on, merge sort is inherently easier to parallelize. Since each half array is sorted independently, it is an excellent candidate for parallelize processing. This can be beneficial in dealing with large files that do not fit entirely into memory. In my opinion, it can sort various data that come from different files which is a common requirement in external sorting scenarios.

I believe that merge sort is a valuable tool for many practical applications due to its robustness, reliability and consistent performance despite the additional space required by the temporary arrays. Its stability, consistency and ability to be parallelized enhance its

effectiveness in various scenarios. That's all the reasons why I think that merge sort is a much superior sorting algorithm compared to the other two sorting algorithms.

## **Time & Space Complexity of Search Algorithms**

### **Linear Search**

Best case: It happens when the target value is the first element in the datasets. Therefore, there will only one comparison is required, and the time complexity is  $O(1)$ .

Worst case: The target value is at the last position in the collections of datasets or doesn't exist in the dataset, hence all elements need to be checked. The time complexity is  $O(n)$ .

Average case: Assuming that the target element is equally likely to be at any position in the dataset, on average  $\frac{n}{2}$  elements need to be checked. Therefore, the average time complexity is  $O(n)$ .

A linear search has a very small space complexity since it is only used for the variable to go through the whole list (GeeksforGeeks, 2024). So, the space complexity of the Linear Search is  $O(1)$ . This indicates that the size of the input dataset does not affect the space complexity of the Linear Search.

### **Binary Search**

Best case: When the target is in the middle of the sorted array, the time complexity in the best case is  $O(1)$  which means that it can find the target value by doing one comparison.

In average case,

Initial range:  $n$ - the size of datasets.

First search: The dataset is divided into two parts, each of which is  $\frac{n}{2}$ .

Second search: Divided into two parts again, and the search range becomes  $\frac{n}{4}$ .

And so on: After  $k$  divisions, the search range's size is  $\frac{n}{2^k}$ . When the search range is narrowed down to only one element, that is  $\frac{n}{2^k} = 1$ , we get  $k = \log_2 n$  from the equation.

Therefore, the time complexity of binary search is  $O(\log n)$ .

Worst case: The worst case happens when the target is the first element of the sorted array (GeeksforGeeks, 2024). The time complexity is  $O(\log n)$ .

Binary Search only uses several additional variables to store indexes and bounds such as low, high and mid, and not require additional space other than the dataset itself (GeeksforGeeks, 2024). The size of the input array didn't affect that. Therefore, the space Complexity of Binary Search is  $O(1)$ .

## **Time & Space Complexity of Sorting Algorithms**

### **Merge Sort**

The Merge Sort achieves time complexity of  $O(n \log n)$  in both average and worst cases. In addition, it's space complexity of  $O(n)$ . Let's prove it.

$T(K)$  = time taken to sort k elements

$M(K)$  = time taken to merge k elements

So, it can be written as:

$$\begin{aligned} T(N) &= 2 * T\left(\frac{N}{2}\right) + M(N) \\ &= 2 * T\left(\frac{N}{2}\right) + \text{constant} * N \end{aligned}$$

These  $N/2$  elements are further divided into two halves. So,

$$\begin{aligned} T(N) &= 2 * \left[ 2 * T\left(\frac{N}{4}\right) + \text{constant} * \frac{N}{2} \right] + \text{constant} * N \\ &= 4 * T\left(\frac{N}{4}\right) + 2 * N * \text{constant} \\ &\dots \\ &= 2^k * T\left(\frac{N}{2^k}\right) + k * N * \text{constant} \end{aligned}$$

The divided maximum will be converged to 1, therefore  $\frac{N}{2^k} = 1$ ,  $k = \log_2 N$

$$\begin{aligned} T(N) &= N * T(1) + N * \log_2 N * \text{constant} \\ &= N + N * \log_2 N \end{aligned}$$

Therefore, the time complexity is  $O(N * \log_2 N)$ .

The space complexity of Merge Sort is  $O(n)$ . This is because it combines the sorted halves of the input array into an auxiliary array of size n. The combined result is saved in the auxiliary array and the sorted result is reprinted in the input array (GeeksforGeeks, 2024).

## Quicksort

The Quicksort has the time complexity of  $O(n \log n)$  on the average case and best case, but when it comes to the worst case, the time complexity will be  $O(n^2)$ . For the space complexity, Quicksort has  $O(n \log n)$  for the best case and average case, but it becomes  $O(n)$  due to unbalanced partitioning. Let's prove it.

$T(K)$ : time complexity of Quicksort of  $K$  elements

$P(K)$ : time taken for finding the position of pivot among  $K$  elements

Let's have a look at the best-case time complexity for Quicksort. It occurs when the mean is selected as the pivot. So here,

$$T(N) = 2 * T\left(\frac{N}{2}\right) + N * \text{constant}$$

Now,  $T\left(\frac{N}{2}\right)$  is also  $2 * T\left(\frac{N}{4}\right) + \frac{N}{2} * \text{constant}$ . So,

$$\begin{aligned} T(N) &= 2 * \left[ 2 * T\left(\frac{N}{4}\right) + \frac{N}{2} * \text{constant} \right] + N * \text{constant} \\ &= 4 * T\left(\frac{N}{4}\right) + 2 * \text{constant} * N \end{aligned}$$

Therefore, we can say that

$$T(N) = 2^k * T\left(\frac{N}{2^k}\right) + k * \text{constant} * N$$

$$\text{Then, } 2^k = N$$

$$k = \log_2 N$$

So  $T(N) = N * T(1) + N * \log_2 N$ . Therefore, the time complexity is  $O(N * \log N)$ .

Next, let's have a look at the worst-case time complexity for Quicksort. It occurs when the array is split into two halves, one of which is  $N-1$  elements and the other, and so forth. Thus,

$$\begin{aligned}
T(N) &= T(N-1) + N * \text{constant} \\
&= T(N-2) + T(N-1) * \text{constant} * N * \text{constant} \\
&= T(N-2) + 2 * N * \text{constant} - \text{constant} \\
&= T(N-3) + 3 * N * \text{constant} - 2 * \text{constant} - \text{constant} \\
&\quad \dots \\
&= T(N-k) + k * N * \text{constant} - (k-1) * \text{constant} - \dots - 2 * \text{constant} - \text{constant} \\
&= T(N-k) + k * N * \text{constant} - \text{constant} * \frac{k * (k-1)}{2}
\end{aligned}$$

If we put  $k = N$  in the above equation, then

$$\begin{aligned}
T(N) &= T(0) + N * N * \text{constant} - \text{constant} * \frac{N * (N-1)}{2} \\
&= N^2 - \frac{N * (N-1)}{2} \\
&= \frac{N^2}{2} + \frac{N}{2}
\end{aligned}$$

Therefore, the worst-case complexity is  $O(N^2)$ .

The best case for space complexity for Quicksort is  $O(\log n)$ , due to balanced partitioning, which produces a balanced recursion tree with an  $O(\log n)$  call stack. Furthermore, for the worst case for space complexity for Quicksort is  $O(n)$ , due to uneven partitioning that produced a skewed recursion tree and an  $O(n)$  call stack (GeeksforGeeks, 2024).

### Bubble Sort

Best case	$O(n)$
Worst case	$O(n^2)$
Average case	$O(n^2)$

The best case is when the input is sorted. So, it will only pass through the array only once. The worst case scenario occurs when the input array is sorted in decreasing order. So, it will go through the array and make  $n$  comparison for each element. This results in quadratic time complexity (Alake, 2023).

Space complexity is  $O(1)$ , which requires just a constant amount of extra space for the switching procedure. Bubble sorts require minimal space requirements where it only uses a single additional space for swapping the elements. This will benefit those systems that have very limited memory.

### **Additional search algorithm and comparison**

#### **Jump Search** (VIDHVAN, 2021)

Jump Search is an improved linear search algorithm that can function within sorted arrays. This search has combined the ideas of Linear Search and Binary Search, quickly narrowing the search range by jumping fixed-size blocks and then performing a Linear Search within the found blocks. The performance of the Jump search is better than the Linear Search but worse than the Binary Search (GeeksforGeeks, 2024).

Below is a visualization of how Jump Sort functions with the provided sorted array and the target value,

$\text{Arr}[] = [1, 3, 4, 5, 7, 8, 12, 14, 16, 18, 21, 24, 27, 35, 40, 44, 48]$

$\text{target} = 18$

Step 1: The block size  $m$  is usually close to be  $\sqrt{n}$ , where size of the array is  $n$ . In this example, the array size is 17, so the block size is

$$m = \sqrt{n} = \sqrt{17} = 4.1231 \approx 4$$

Step 2: This step is also the jumping phase where it will start from the first element of the array, compare the target value with the first element, jump 4 elements at a time and compare the element in the jump position with the target value.

1	3	4	5	7	8	12	14	16	18	21	24	27	35	40	44	48
---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----

$\text{Arr}[0] = 1 < 18$ . Since it is not a match, then jump to the next block to do the following comparison.

First jump: Jump to  $\text{Arr}[4]$

1	3	4	5	7	8	12	14	16	18	21	24	27	35	40	44	48
---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----

$\text{Arr}[4] = 7 < 18$ . Since it is not a match, then jump to the next block to do the following comparison.

Second jump: Jump to  $\text{Arr}[8]$

1	3	4	5	7	8	12	14	16	18	21	24	27	35	40	44	48
---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----

Arr[8] = 16 < 18. Since it is not a match, then jump to the next block to do the following comparison.

Third jump: Jump to Arr[12]

1	3	4	5	7	8	12	14	16	18	21	24	27	35	40	44	48
---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----

Arr[12] = 27 > 18. However, the next jump position has a larger value than the target value.

Therefore, this jump will not be taken and the Linear Search will be applied on the current block.

Step 3: In this step, the Linear Search is applied to compare the current block with the target value.

1	3	4	5	7	8	12	14	16	18	21	24	27	35	40	44	48
---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----

After that, the pointer increments from 8<sup>th</sup> to 9<sup>th</sup>. Arr[9] = 18 where it is equal to the target. Returns the 9<sup>th</sup> index as the output and the search stops.

### Comparison of Linear Search, Binary Search and Jump Search

	Linear Search	Binary Search	Jump Search
Algorithm type	Sequential	Divide and conquer	Block Search
Time complexity	Best Case: $O(1)$ Average Case: $O(n)$ Worst Case: $O(n)$	Best Case: $O(1)$ Average Case: $O(\log n)$ Worst Case: $O(\log n)$	Best Case: $O(1)$ Average Case: $O(\sqrt{n})$ Worst Case: $O(\sqrt{n})$
Sorted Array needed	No	Yes	Yes
Search Approach	Compare one by one	Divide the search range repeatedly	Jump few blocks, then Linear Search
Datasets suitable	Small datasets	Large and sorted datasets	Large and sorted datasets

Each of them has their advantages. The search approach of Linear Search makes it inefficient when dealing with large datasets, however, it is very easy to implement. Binary Search and Jump Search have better performance when handling large datasets but they can only work with sorted arrays.



### Interpolation Search (G Bhat, 2020)

Interpolation Search is an improved search algorithm that is suitable for uniformly distributed sorted arrays. This search combines the idea of Binary Search and linear interpolation. Unlike Binary Search, Interpolation Search uses interpolation formulas to estimate the target element's position, thereby quickly narrowing the search range.

Below is a visualization of how Interpolation functions with the provided sorted array,

$Arr[] = [10, 20, 30, 40, 50, 60, 70, 80, 90, 100]$        $target=80$

Initialization:

$low = 0$ : The first index of the array.

$high = 9$ : The last index of the array.

$target = 80$ : The target value we want to find.

First Iteration:

Step 1: Calculate the estimated position

Use the interpolation formula to estimate the position of target:

$$pos = low + \frac{(target - arr[low]) \times (high - low)}{arr[high] - arr[low]}$$

Substitute the initialized values into the formula:

$$pos = 0 + \frac{(80-10) \times (9-0)}{100-10} = 0 + \frac{70 \times 9}{90} = 0 + 7 = 7$$

The estimated position is 7.

Step2: Compare and adjust

Compare  $Arr[7]$  and target value:

$$Arr[7] = 80, target = 80$$

$Arr[7]$  is equal to the target, we found the target value, return index 7 and the algorithm exit.

Now, one more example that the target value does not exist in the sorted array, hence, we can further adjust the search range.

Second example

$Arr[] = [10, 20, 30, 40, 50, 60, 70, 80, 90, 100]$        $target=65$

Initialization:

$low = 0$ : The first index of the array.

$high = 9$ : The last index of the array.

$target = 65$ : The target value we want to find.

First Iteration:

Step1: Calculate the estimated position

$$pos = 0 + \frac{(65-10) \times (9-0)}{100-10} = 0 + \frac{55 \times 9}{90} = 0 + 5.5 \approx 6$$

The estimated position is 6.

Step2: Compare and adjust

$$Arr[6] = 70, target = 65$$

Since  $Arr[6] > target$ , adjust the search range:

$$high = pos - 1 = 6 - 1 = 5$$

Second Iteration:

Step1: Calculate the estimated position

$$pos = 0 + \frac{(65-10) \times (5-0)}{60-10} = 0 + \frac{55 \times 5}{50} = 0 + 5.5 \approx 5$$

The estimated position is 5.

Step2: Compare and adjust

$$Arr[5] = 60, target = 65$$

Since  $Arr[5] < target$ , adjust the search range:

$$low = pos + 1 = 5 + 1 = 6$$

At this time, the position of  $low > high$ , the search ends and the target value 65 is not in this array.

### Comparison of Linear Search, Binary Search and Interpolation Search

	Linear Search	Binary Search	Interpolation Search
Algorithm type	Sequential	Divide and conquer	Based on the position
Time complexity	Best Case: $O(1)$ Average Case: $O(n)$ Worst Case: $O(n)$	Best Case: $O(1)$ Average Case: $O(\log n)$ Worst Case: $O(\log n)$	Best Case: $O(1)$ Average Case: $O(\log \log n)$ Worst Case: $O(n)$
Sorted Array needed	No	Yes	Yes
Search Approach	Compare one by one	Divide the search range repeatedly	Estimate the position
Datasets suitable	Small datasets	Large and sorted datasets	Large and uniformly distributed sorted datasets

Interpolation Search is a search algorithm that has high requirements on the datasets. It is more efficient than Binary Search when searching the uniformly distributed datasets (GeeksforGeeks, 2023). However, it performs poorly which similar to linear search when dealing with non-uniformly distributed data.

### Additional sorting algorithm and comparison

#### Tim Sort (GeeksforGeeks, 2023)

Tim Sort combines the design of Merge Sort with Insertion Sort. It was designed to work well with a wide range of real-world data formats. The major purpose of it is to minimize the amount of comparisons and swaps by using the data current order. This is performed by first separating the array into small and pre-sorted subarrays called runs. Then it will then combine using modified merge sort algorithms (GeeksforGeeks, 2023).

Below is a visualization of how Tim Sort functions with the provided array,

$\text{arr}[] = \{4, 2, 8, 6, 1, 5, 9, 3, 7\}$ :

#### Step 1: Define the size of the run

We have to set the minimum run size, for example, 32. (In our case we will ignore this step as our array is small).

#### Step 2: Divide the array into runs

In this step, insertion sort is used to sort the small subsequence within the array. In the initial array: [ 4, 2, 8, 6, 1, 5, 9, 3, 7], no initial runs are present, so runs are created using insertion sort.

Sorted runs: [2, 4], [6, 8], [1, 5, 9], [3, 7]

Updated array: [2, 4, 6, 8, 1, 5, 9, 3, 7]

#### Step 3: Merge the runs

In this step, a modified merge sort is being used to merge the sorted runs. The process will merge the runs until the entire array is sorted.

Merged runs; [2, 4, 6, 8], [1, 3, 5, 7, 9]

Updated array: [2, 4, 6, 8, 1, 3, 5, 7, 9]

#### Step 4: Adjust the run size

We double the run's size after every merge operation until it exceeds the length of the array. For example, the run size doubles: 32, 64, 128. (In our case we will ignore this step as our array is small).

#### Step 5: Continue merging

The merging process is repeated until the entire array is sorted.

Final merged run: [1, 2, 3, 4, 5, 6, 7, 8, 9]

Besides, the time complexity for Tim Sort is  $O(n)$  in the best case,  $O(n * \log n)$  in both average and worst case.

#### Comparison of Tim Sort, Merge Sort and Quicksort

	Tim Sort	Merge Sort	Quicksort
Algorithm type	Hybrid (Combination of Merge Sort and Insertion Sort)	Divide and conquer	Divide and conquer
Time complexity	Best Case: $O(n)$ Average Case: $O(n \log n)$ Worst Case: $O(n \log n)$	Best Case: $O(n \log n)$ Average Case: $O(n \log n)$	Best Case: $O(n \log n)$ Average Case: $O(n \log n)$ Worst Case: $O(n^2)$

		Worst Case: $O(n \log n)$	
Space complexity	$O(n)$	$O(n)$	$O(\log n)$
Stability	Stable	Stable	Not stable
Typical use cases	Utilized in standard libraries like Python and Java for sorting and in practice for real-world data. It also works well with large datasets that have a certain degree of order.	Utilized in situations where space complexity is unimportant and stable sorting is necessary.	Frequently used in general-purpose sorting because of its in-place sorting and average-case efficiency. Utilized frequently in embedded systems and system programming.

### Heap Sort (GeeksforGeeks, 2024)

The Heap Sort algorithm is a comparison-based sorting method based on the binary heap. It is an upgraded version of the selection sort that makes use of the heap data structure to efficiently identify the maximum or minimum element (GeeksforGeeks, 2024).

There are a few steps in the heap sort algorithm. For example, we use an unsorted array with a size of 6.

2	8	5	3	9	1
---	---	---	---	---	---

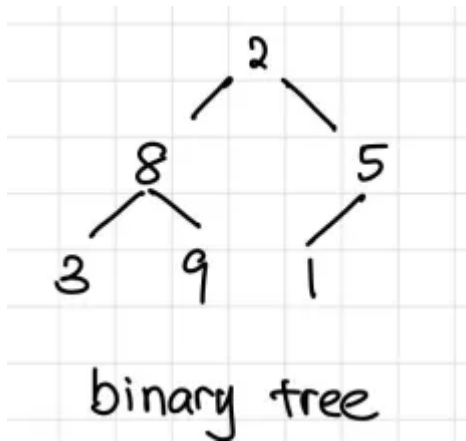
#### Step 1: Build a complete binary tree

First, we will convert an array into a complete binary tree. A complete binary tree is a binary tree in which all levels are fully filled and from left to right except for the last levels. The nodes will follow the sequence of the array where it is unsorted.

Array:

2	8	5	3	9	1
---	---	---	---	---	---

Tree:



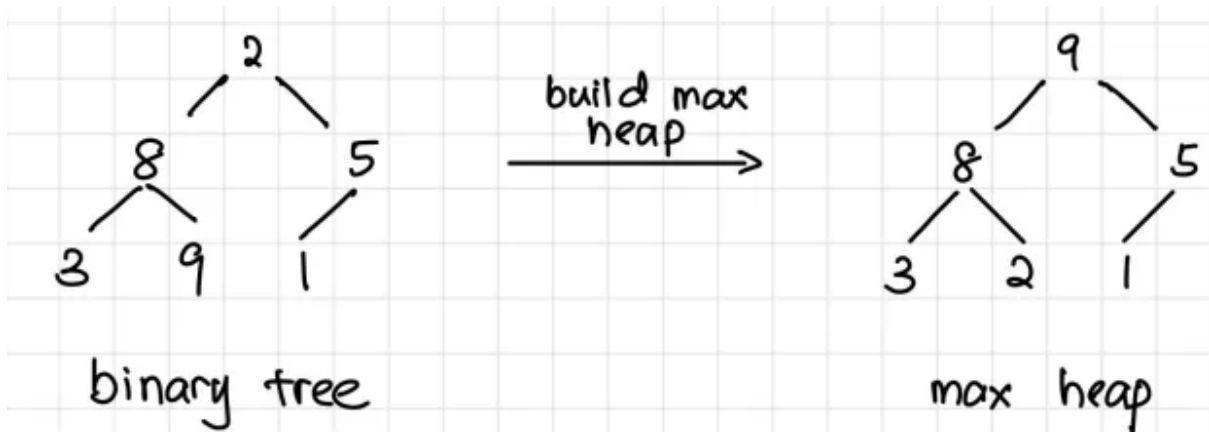
### Step 2: Max-Heapify Constructed Binary Tree

It will then convert the entire binary tree into the maximum heap. A Max heap is a tree in which the parent node is greater than or equal to its offspring. The heapification process begins with the last non leaf node and progresses upwards. It uses the heapify procedure to verify that the subtree rooted at each node meets the maximum heap property

Array:

9	8	5	3	2	1
---	---	---	---	---	---

Tree:



### Step 3: Remove Maximum from the root and max-heapify

After the max heap tree is constructed, the root node will be the largest element among all the elements. The root node will be removed and swapped with the last element in the heap. Then the heap's size will be reduced by 1 and call the max heapify on the root node.

This is to make sure the tree satisfies the max heap property. Process repeatedly working to sort all the elements.

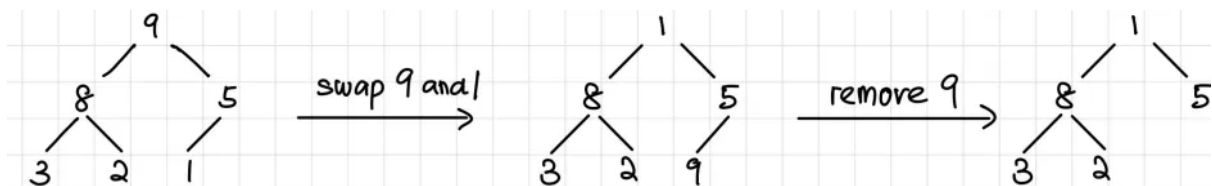
From the example above, the 9 is the maximum among all the elements. So, 9 will be swapped with the last element in the tree then only remove 9 from the tree.

Array:

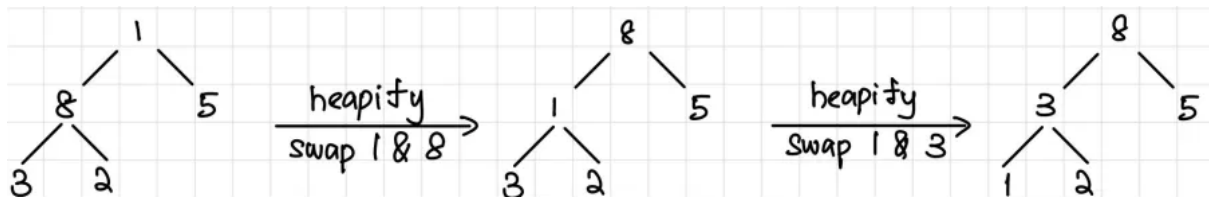
9	8	5	3	2	1
---	---	---	---	---	---

Swap the position of 9 and 1 in the array

1	8	5	3	2	9
---	---	---	---	---	---



Now, we need to make sure that the tree satisfies the max heap property. So, we will heapify the tree by swapping the largest child of the parent node (1) to be the parent.

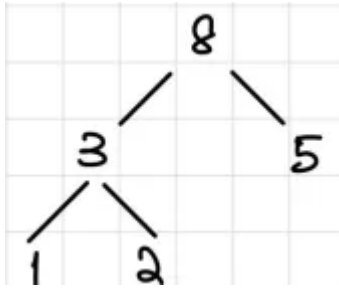


Before we carry on to the next iteration, the array and tree will be used for the next iteration will be:

Array:

8	3	5	1	2	9
---	---	---	---	---	---

Tree:



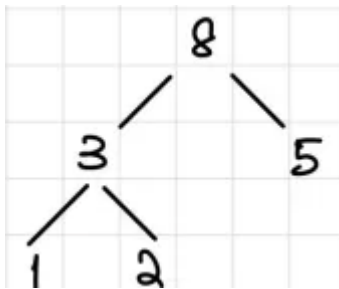
Step 3 will be repeated until only 1 element is in the tree.

## 2<sup>nd</sup> iteration

Array:

8	3	5	1	2	9
---	---	---	---	---	---

Tree:



Swap 2 and 8.

Array:

2	3	5	1	8	9
---	---	---	---	---	---

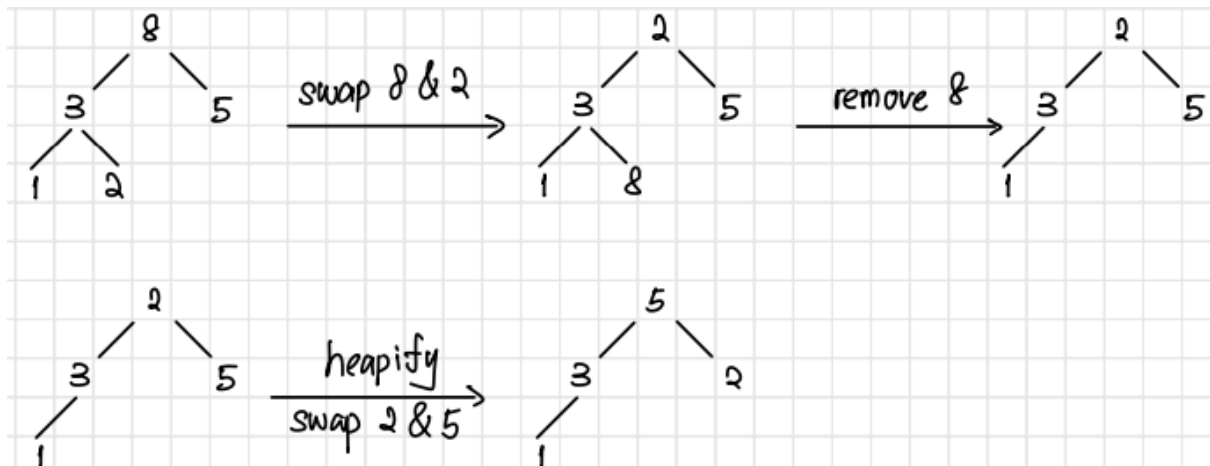
Then carry out heapify

Array:

5	3	2	1	8	9
---	---	---	---	---	---

Tree:



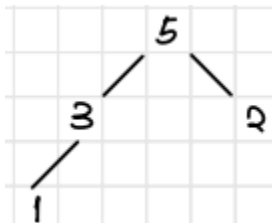


### 3<sup>rd</sup> iteration

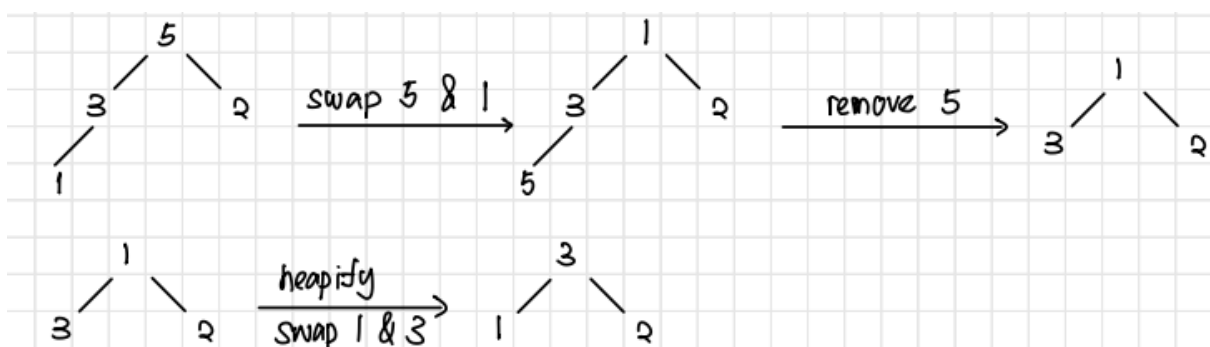
Array:

5	3	2	1	8	9
---	---	---	---	---	---

Tree:



Swap 5 and 1 then carry heapify

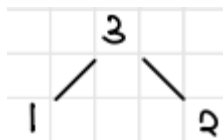


### 4<sup>th</sup> iteration

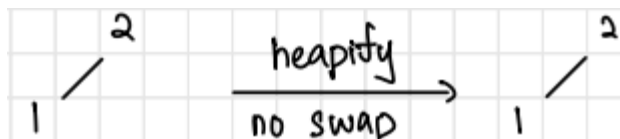
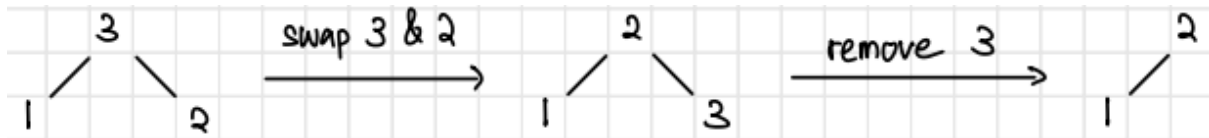
Array:

3	1	2	5	8	9
---	---	---	---	---	---

Tree:



Swap 3 and 2

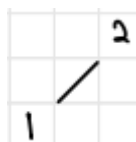


**5<sup>th</sup> iteration**

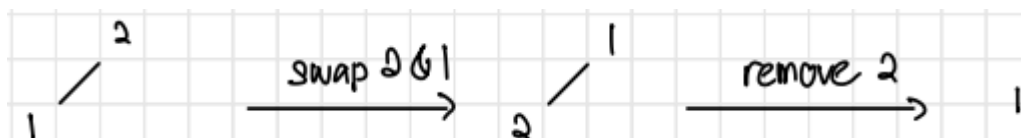
Array:

2	1	3	5	8	9
---	---	---	---	---	---

Tree:



Swap 2 and 1 then heapify



Step 4: Remove the last elements and return the sorted array

Since 1 is the last element in the tree, it will just return where it is the smallest number. Then it will return the sorted array.

Sorted Array:

1	2	3	5	8	9
---	---	---	---	---	---

Comparison of Heap Sort, Merge Sort and Quicksort

Heap Sort, Merge Sort and Quick Sort are 3 different sorting algorithms each with unique advantages that suit different use cases. Heap sort has a space complexity of only  $O(1)$  because it relies on binary heap data structure. It makes it extremely efficient in terms of space. This is because quick sort uses a recursion stack that requires only  $O(\log n)$  additional space. It can lead to good cache performance and faster than merge sort and heap sort. Merge sort is a powerful divide and conquer algorithm that reliably separates the array into halves sorts each half then combines the sorted halves back together.

Heap Sort performs very unstable as it does not preserve the relative order of equal elements, which tends to make it slower for most practical applications; whereas Quick Sort is also an unstable algorithm since its sorting algorithm's performances are highly dependent on pivot position selections; consequently, Merge Sort establishes stable relationships between equals which come very handy when order matters in some applications.

In a nutshell, Heap Sort is advantageous due to its space efficiency, merge sort is advantageous because it is stable and long-lasting when working with large datasets, and quick sort is advantageous because it is practical and efficient.

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## **Appendix Section**

// Class to store and manage order details

```
class OrderDetails{
private:
    int orderNumber;
    vector<string> VIPList = {"ADM123", "NAJ123"};
    string buyerName;
    string buyerId;
    string carId;
    string carBrand;
    string modelName;
    string carColor;
```

```

int productionYear;
double carPrice;
double totalPrice;
double discount;
time_t timeValue; // Time value for the current date
static vector<int> numbers; // List to store generated order numbers to ensure uniqueness
struct tm ltm = {0}; // Local time structure
struct tm currentDate = {0}; // Current date structure

// Generate unique order number
void generateOrderNumber(){
    orderNumber = rand()%(1001);
    for(auto& n : numbers){
        if(n == orderNumber){
            generateOrderNumber();
            return;
        }
    }
    numbers.push_back(orderNumber);
}

// Check if the buyer is eligible for a discount
void isDiscount(){
    for(auto& vip : VIPList){
        if(vip == buyerId){
            discount = 0.1;
            totalPrice = carPrice - (carPrice * discount);
        }
        else{
            totalPrice = carPrice; // No discount for non-VIP buyers
        }
    }
}

```

```

public:
    // Constructor to initialize order details
    OrderDetails(string name, string id, string cid, string brand,
                 string model, string color, int py, double price){
        time_t now = time(0);
        buyerName = name;
        buyerId = id;
        carId = cid;
        carBrand = brand;
        modelName = model;
        carColor = color;
        productionYear = py;
        carPrice = price;
        generateOrderNumber();
        isDiscount();
        ltm = *localtime(&now);
        currentDate.tm_year = ltm.tm_year; // Year since 1900
        currentDate.tm_mon = ltm.tm_mon;   // Month (0-11)
        currentDate.tm_mday = ltm.tm_mday; // Day of the month
        timeValue = mktime(&currentDate);
    }

    // Get the customer ID
    string getCustomerId(){
        return buyerId;
    }

    // Get the car ID
    string getCarId(){
        return carId;
    }

    // Get the final price after discount
    double getFinalPrice(){
        return totalPrice;
    }

```

```

// Get the local time structure
struct tm getTime(){
    return ltm;
}

// Get the current date as time_t
time_t getCurrentDate(){
    return timeValue;
}

// Display detailed order information
void displayDetails(){
    cout << endl;
    cout << "Bill ID: " << orderNumber << endl;
    cout << "Customer ID: " << buyerId << endl;
    cout << "Customer Name: " << buyerName << endl;
    cout << "Car ID: " << carId << endl;
    cout << "Car Brand: " << carBrand << endl;
    cout << "Car Model: " << modelName << endl;
    cout << "Car Color: " << carColor << endl;
    cout << "Production Year: " << productionYear << endl;
    cout << "Price: RM" << fixed << setprecision(2) << carPrice << endl;
    cout << "Discount : " << discount * 100 << "%" << endl;
    cout << "Total Price: RM" << fixed << setprecision(2) << totalPrice << endl;
    cout << "Date:" << ltm.tm_mday << "/" <<
    1 + ltm.tm_mon << "/" <<
    1900 + ltm.tm_year << endl;
    cout << "Time (00:00, 24-hour time): " << ltm.tm_hour << ":";
    cout << ltm.tm_min;
    cout << endl << endl;
}

// Display a summary report for the order
void displayReport(){
    cout << endl;
    cout << "Car ID: " << carId << endl;
    cout << "Car Brand: " << carBrand << endl;

```

```

        cout << "Car Color: " << carColor << endl;
        cout << "Customer Name: " << buyerName << endl;
        cout << "Date:" << ltm.tm_mday << "/" <<
            1 + ltm.tm_mon << "/" <<
            1900 + ltm.tm_year << endl;
        cout << "Price: RM" << fixed << setprecision(2) << totalPrice << endl;
        cout << endl << endl;
    }
};

// Class to store and manage car details
class Car{
private:
    string carID;
    string brand;
    string model;
    string color;
    string manufactureCountry;
    int manufactureYear;
    double price;
    int Sales;
    bool bestSeller;

    // Generates a random digit
    string generateNumber(){
        int num;
        num = rand()%10;
        return to_string(num);
    }

    // Generate a random car ID
    void randomID(){
        carID = brand.substr(0,3);
        for(int i = 0; i<9; i++){
            carID += generateNumber();
        }
    }
};

```



```
    }  
}
```

public:

```
    Car() = default; // Default constructor  
    Car(string b, string m, string c, string country, int year, double p, int s = 0){  
        brand = b;  
        model = m;  
        color = c;  
        manufactureCountry = country;  
        manufactureYear = year;  
        price = p;  
        Sales = s;  
        randomID();  
    }  
    // Get methods  
    string getCarId(){  
        return carID;  
    }  
    string getBrand(){  
        return brand;  
    }  
    string getModel(){  
        return model;  
    }  
    string getColor(){  
        return color;  
    }  
    string getManufactureCountry(){  
        return manufactureCountry;  
    }  
    int getManufactureYear(){  
        return manufactureYear;  
    }  
}
```

```

double getPrice(){
    return price;
}
int getSales(){
    return Sales;
}
// Check if the car is a best seller
bool isBestSelling(){
    if (Sales > 8){
        bestSeller = 1;
    }
    else{
        bestSeller = 0;
    }
    return bestSeller;
}
// Set methods
string setBrand(string b){
    if(b!="-1")
        brand = b;
}
string setModel(string m){
    if(m!="-1")
        model = m;
}
string setColor(string c){
    if(c!="-1")
        color = c;
}
string setManufactureCountry(string country){
    if(country!="-1")
        manufactureCountry = country;
}
int setManufactureYear(int year){

```

```

        if(year!=-1)
            manufactureYear = year;
    }
    double setPrice(double p){
        if(p!=-1)
            price = p;
    }
    void increaseSales(){
        Sales += 1; // Increment sales count
    }
};

```

// Class to manage user information

```

class User{
    private:
        string userID;
        string userName;
        string userPassword;
        string status;
    public:
        User() = default; // Default Constructor
        User(string id, string name, string password){
            userID = id;
            userName = name;
            userPassword = password;
        }

        // Get methods
        string getUserId(){
            return userID;
        }
        string getUserName(){
            return userName;
        }
}

```

```

    string getUserPassword(){
        return userPassword;
    }
    string getUserStatus(){
        return status;
    }

    // Set methods
    void setUserStatus(string s){
        status = s;
    }
};

// Class to manage the system, including users, cars, orders
class System{
private:
    vector<User> userList;
    vector<User> adminList;
    vector<Car> carList;
    vector<Car> temp; // temp vector to stored sorted cars
    vector<OrderDetails> orderList;
    vector<OrderDetails> reportList;
    User currentUser;
    int taskOption;
    double totalPrice;

    // Function to register a new user
    void registerFunc(){
        string userId;
        string name;
        bool valid;
        string password;
        cin.ignore();
        cout << endl;

```

```

cout << "Registration" << endl;

do{
    valid = 1;
    cout << "Enter unique Id >";
    getline(cin, userId);
    for(auto& user : userList){
        if (userId == user.getUserId()){
            cout << "ID existed, please try another id" << endl;
            valid = 0;
        }
    }
    if(userId == "-1"){
        cout << "Invalid ID" << endl;
        valid = 0;
    }
}while(!valid);
cout << "Enter your name >";
getline(cin, name);
cout << "Enter your password >" ;
getline(cin, password);
cout << "Register successfully!" << endl << endl;
registeredUser(User(userId, name, password));
}

// Add an order to the order list and increases car sales
void addOrder (OrderDetails order){
    for(auto& car : carList){
        if (car.getCarId() == order.getCarId()){
            car.increaseSales();
        }
    }
    orderList.push_back(order);
}

```

```

// Handles the purchases of a car
void purchase(int x){
    int choice;
    cout << "(type in '-1' to exit selection)> ";
    cin >> choice;
    bool status = true;
    while(status){
        try{
            digitInputValidation();
            status = false;
        }
        catch(string errorMsg){
            cout << endl;
            cout << "Error: " << errorMsg << endl;
            cout << endl;
            cout << endl;
            cout << "(type in '-1' to exit selection)> ";
            cin >> choice;
        }
    }
    if (x == 1){ // If purchasing from the main car list
        if(choice == -1){
            cout << endl;
            cout << "Return to Main Page" << endl;
        }
        else if(choice < 1 || choice > carList.size()){
            cout << endl;
            cout << "Option out of range" << endl;
            purchase(x);
        }
        else{
            OrderDetails    order(currentUser.getUserName(),    currentUser.getUserId(),

```

```

carList[choice-1].getCarId(),
                    carList[choice-1].getBrand(),carList[choice-1].getModel(),
carList[choice-1].getColor(),
                    carList[choice-1].getManufactureYear(),          carList[choice-
1].getPrice());
        addOrder(order);
        order.displayDetails();
    }
}
else if(x == 2){ // If purchasing from the temporary list
    if(choice == -1){
        cout << endl;
        cout << "Return to Main Page" << endl;
    }
    else if(choice < 1 || choice > temp.size()){
        cout << endl;
        cout << "Option out of range" << endl;
        purchase(x);
    }
    else{
        OrderDetails    order(currentUser.getUserName(),    currentUser.getUserId(),
temp[choice-1].getCarId(),
                    temp[choice-1].getBrand(),temp[choice-1].getModel(),
temp[choice-1].getColor(),
                    temp[choice-1].getManufactureYear(), temp[choice-1].getPrice());
        addOrder(order);
        order.displayDetails();
    }
}

}

// Search Car id by using binary search
int Binary_Search_ID(vector<Car> carList, int low_arr, int high_arr, string id){

```

```

while(low_arr <= high_arr){
    int middle_arr = ( ( high_arr - low_arr ) / 2 ) + low_arr ;

    if(carList[middle_arr].getCarId() == id)
        return middle_arr;

    if(carList[middle_arr].getCarId() <= id)
        low_arr = middle_arr + 1;

    else
        high_arr = middle_arr - 1;
}
return -1;
}

// Search best selling cars using binary search
int Binary_Search_bestSelling(vector<Car> carList, int low_arr, int high_arr, bool best){
    while(low_arr <= high_arr){
        int middle_arr = ( ( high_arr - low_arr ) / 2 ) + low_arr ;

        if(carList[middle_arr].isBestSelling() == best)
            return middle_arr;

        if(carList[middle_arr].isBestSelling() <= best)
            low_arr = middle_arr + 1;

        else
            high_arr = middle_arr - 1;
    }
    return -1;
}

// Search report within specific period using binary search
int Binary_Search_report(vector<OrderDetails> orderList, int low_arr,

```



```

        int high_arr, struct tm startTime, struct tm endTime){
time_t start_time_t = mktime(&startTime);
time_t end_time_t = mktime(&endTime);
while(low_arr <= high_arr){
    int middle_arr = ( ( high_arr - low_arr ) / 2 ) + low_arr ;
    if(orderList[middle_arr].getCurrentDate()      >=      start_time_t      &&
orderList[middle_arr].getCurrentDate() <= end_time_t)
        return middle_arr;

    if(orderList[middle_arr].getCurrentDate() < start_time_t)
        low_arr = middle_arr + 1;

    else
        high_arr = middle_arr - 1;
}
return -1;
}

```

// Sort best selling car according to brand using bubbles sort

```

void bubbleSort(vector<Car>& arr){
    for(int i =0; i < arr.size(); i++){
        for(int j =0; j<arr.size()-i-1; j++){
            if(arr[j].getBrand() > arr[j+1].getBrand()){
                swap(arr[j], arr[j+1]);
            }
        }
    }
}

```

// Linear search for bills by customer ID

```

void linearSearch_Bills(){
    for (int i = 0; i < orderList.size(); i++){
        if(orderList[i].getCustomerId() == currentUser.getUserId()){
            orderList[i].displayDetails();

```

```

    }
}
}
// Linear search for bills by date
void linearSearch_Bills_Date(tm date){
    for (int i = 0; i < orderList.size(); i++){
        if (orderList[i].getTime().tm_mday == date.tm_mday &&
            orderList[i].getTime().tm_mon == date.tm_mon &&
            orderList[i].getTime().tm_year == date.tm_year){
            orderList[i].displayDetails(); // Display bill details if date matches
        }
        else{
            cout << endl;
            cout << "No bill issued that day." << endl;
            cout << endl;
        }
    }
}
// Partition function for quick sort
int partition(vector<OrderDetails> &v, int low, int high){
    double pivot = v[high].getFinalPrice(); // Pivot element is the final price of the high
element
    int i = low - 1;
    for(int j = low; j < high; j++){
        if(v[j].getFinalPrice() < pivot){
            i++;
            swap(v[i], v[j]);
        }
    }
    swap(v[i+1], v[high]);
    return (i+1);
}
// Quick sort function
void quickSort(vector<OrderDetails> &v, int low, int high){

```

```

if (low < high){
    int pi = partition(v, low, high); // Partitioning index

    quickSort(v, low, pi - 1); // Recursively sort elements before partition
    quickSort(v, pi+1, high); // Recursively sort elements after partition
}
}

// merge two halves by brand
void mergeBrand(vector<Car>& arr, int left, int mid, int right) {
    int n1 = mid - left + 1;
    int n2 = right - mid;
    vector<Car> LeftArray(n1);
    vector<Car> RightArray(n2);

    // The Mid element is saved in LeftArray
    for (int i = 0; i < n1; i++)
        LeftArray[i] = arr[left + i];
    for (int i = 0; i < n2; i++)
        RightArray[i] = arr[mid + 1 + i];

    int i = 0; // Initial index of first subarray
    int j = 0; // Initial index of second subarray
    int k = left; // Initial index of merged subarray

    while (i < n1 && j < n2) {
        if (LeftArray[i].getBrand() <= RightArray[j].getBrand()) {
            arr[k] = LeftArray[i];
            i++;
        } else {
            arr[k] = RightArray[j];
            j++;
        }
        k++;
    }
}

```

```

while (i < n1) {
    arr[k] = LeftArray[i];
    i++;
    k++;
}

// Copy the remaining elements of Right array
while (j < n2) {
    arr[k] = RightArray[j];
    j++;
    k++;
}
}

// merge two halves for merge sort by price
void mergePrice(vector<Car>& arr, int left, int mid, int right) {
    int n1 = mid - left + 1;
    int n2 = right - mid;

    vector<Car> LeftArray(n1);
    vector<Car> RightArray(n2);

    // The Mid element is saved in LeftArray
    for (int i = 0; i < n1; i++)
        LeftArray[i] = arr[left + i];
    for (int i = 0; i < n2; i++)
        RightArray[i] = arr[mid + 1 + i];

    int i = 0; // Initial index of first subarray
    int j = 0; // Initial index of second subarray
    int k = left; // Initial index of merged subarray

    while (i < n1 && j < n2) {
        if (LeftArray[i].getPrice() <= RightArray[j].getPrice()) {

```

```

        arr[k] = LeftArray[i];
        i++;
    } else {
        arr[k] = RightArray[j];
        j++;
    }
    k++;
}

while (i < n1) {
    arr[k] = LeftArray[i];
    i++;
    k++;
}

while (j < n2) {
    arr[k] = RightArray[j];
    j++;
    k++;
}
}

// merge two halves for merge sort by ID
void mergeId(vector<Car>& arr, int left, int mid, int right) {
    int n1 = mid - left + 1;
    int n2 = right - mid;

    vector<Car> LeftArray(n1);
    vector<Car> RightArray(n2);

    // The Mid element is saved in LeftArray
    for (int i = 0; i < n1; i++)
        LeftArray[i] = arr[left + i];
    for (int i = 0; i < n2; i++)
        RightArray[i] = arr[mid + 1 + i];

```

```

int i = 0; // Initial index of first subarray
int j = 0; // Initial index of second subarray
int k = left; // Initial index of merged subarray

while (i < n1 && j < n2) {
    if (LeftArray[i].getCarId() <= RightArray[j].getCarId()) {
        arr[k] = LeftArray[i];
        i++;
    } else {
        arr[k] = RightArray[j];
        j++;
    }
    k++;
}

while (i < n1) {
    arr[k] = LeftArray[i];
    i++;
    k++;
}

while (j < n2) {
    arr[k] = RightArray[j];
    j++;
    k++;
}
}

// Function to implement merge sort
void mergeSort(vector<Car>& arr, int left, int right) {
    if (left >= right)
        return;

```

```

int mid = left + (right - left) / 2;

// Sort first and second halves
mergeSort(arr, left, mid);
mergeSort(arr, mid + 1, right);

// Merge the sorted halves based on taskOption
if(taskOption == 2){
    mergePrice(arr, left, mid, right); // Merge by price
}
else if(taskOption == 3){
    mergeBrand(arr, left, mid, right); // Merge by brand
}
else if(taskOption == 4){
    mergeId(arr, left, mid, right); // Merge by ID
}
}

// Validation for digit input
void digitInputValidation(){
    if(cin.fail()){
        cin.clear();
        cin.ignore(numeric_limits<streamsize>::max(), '\n');
        string msg = "Please enter digits.";
        throw msg;
    }
}

// Validation for date input
void dateInputValidation(){
    if(cin.fail()){
        cin.clear();
        cin.ignore(numeric_limits<streamsize>::max(), '\n');
        string msg = "Please enter proper date.";
        throw msg;
    }
}

```

```
}
```

public:

```
//constructor for system class
```

```
System(){
```

```
    cout << "Welcome to Car Dealership" << endl;
```

```
}
```

```
// Function to register a user
```

```
void registeredUser(User user){
```

```
    userList.push_back(user);
```

```
}
```

```
// Function to register an admin
```

```
void registeredAdmin(User admin){
```

```
    adminList.push_back(admin);
```

```
}
```

```
// Function to register a car
```

```
void registeredCar(Car car){
```

```
    carList.push_back(car);
```

```
}
```

```
// Function to get the current user's status
```

```
string getStatus(){
```

```
    return currentUser.getUserStatus();
```

```
}
```

```
// Function to add a new car
```

```
void addNewCar(){
```

```
    string brand;
```

```
    string model;
```

```
    string color;
```

```
    string country;
```

```
    int year;
```



```
double price;
cout << endl;
cout << "Please enter new car information." << endl;
cout << "Car Brand: ";
getline(cin, brand);
cout << "Car Model Name: ";
getline(cin, model);
cout << "Car Color: ";
getline(cin, color);
cout << "Manufacture country: ";
getline(cin, country);
cout << "Manufacture Year: ";
cin >> year;
```

```
// Validate digit input for year
bool status = true;
while(status){
    try{
        digitInputValidation();
        status = false;
    }
    catch(string errorMsg){
        cout << endl;
        cout << "Error: " << errorMsg << endl;
        cout << endl;
        cout << endl;
        cout << "Manufacture Year: ";
        cin >> year;
    }
}
```

```
cout << "Price: ";
cin >> price;
```

```

// Validate digit input for price
status = true;
while(status){
    try{
        digitInputValidation();
        status = false;
    }
    catch(string errorMsg){
        cout << endl;
        cout << "Error: " << errorMsg << endl;
        cout << endl;
        cout << endl;
        cout << "Price: ";
        cin >> price;
    }
}

// Register the new car
registeredCar(Car(brand, model, color, country, year, price));
cout << "New car added successfully." << endl << endl;
cin.ignore();
}

// Function to remove a car
void removeCar(){
    if (!carList.empty()){
        displayAllCars();
        int option;
        cout << endl;
        cout << "Choose a car to delete: ";
        cin >> option;
        // Validate digit input for option
        bool status = true;
        while(status){
            try{

```

```

        digitInputValidation();
        status = false;
    }
    catch(string errorMsg){
        cout << endl;
        cout << "Error: " << errorMsg << endl;
        cout << endl;
        cout << endl;
        cout << "Choose a car to delete: ";
        cin >> option;
    }
}

// Check if the option is within range
if (option > 0 && option <= carList.size()){
    carList.erase(carList.begin()+(option -1));
    cout << "Car removed successfully." << endl << endl;
}
else{
    cout << endl;
    cout << "Option out of range" << endl;
    cout << endl;
}
}

// Function to modify a car's details
void modifyCar(){
    string id;
    cout << endl;
    cout << "Enter the car id to modify: ";
    cin >> id;
    string brand;
    string model;
    string color;
    string country;

```

```

int year;
double price;

// Search for the car by id and modify its details
for (auto& car : carList){
    if (car.getCarId() == id){
        cout << "Enter -1 if you do not wish to modify this section." << endl;
        cout << "Enter new brand: ";
        cin >> brand;
        car.setBrand(brand);
        cout << "Enter new model name: ";
        cin >> model;
        car.setModel(model);
        cout << "Enter new color: ";
        cin >> color;
        car.setColor(color);
        cout << "Enter new Manufacture Country: ";
        cin >> country;
        car.setManufactureCountry(country);
        cout << "Enter new Manufacture Year: ";
        cin >> year;
        bool status = true;
        while(status){
            try{
                digitInputValidation();
                status = false;
            }
            catch(string errorMsg){
                cout << endl;
                cout << "Error: " << errorMsg << endl;
                cout << endl;
                cout << endl;
                cout << "Enter new Manufacture Year: ";
                cin >> year;
            }
        }
    }
}

```

```

    }
}

car.setManufactureYear(year);
cout << "Enter new price: ";
cin >> price;
status = true;
while(status){
    try{
        digitInputValidation();
        status = false;
    }
    catch(string errorMsg){
        cout << endl;
        cout << "Error: " << errorMsg << endl;
        cout << endl;
        cout << endl;
        cout << "Enter new price: ";
        cin >> price;
    }
}

car.setPrice(price);

cout << "Changes made." << endl << endl;
return;
}
}

cout << "No such car exist." << endl << endl;
}

// Function to handle user login
bool loginFunc(){

```

```

string userId;
string password;
char x;

while(true){
    cout << "Please Login (-1 to quit)" << endl;
    cout << "Enter User Id >" ;
    getline(cin, userId);
    if (userId == "-1"){
        return 0;
    }
    cout << "Enter Password >" ;
    getline(cin, password);

    // Check user credentials
    for(auto& user : userList){
        if(userId == user.getUserId() && password == user.getUserPassword()){
            currentUser = User(user.getUserId(),user.getUserName(),
user.getUserPassword());
            currentUser.setUserStatus("user");
            cout << endl;
            cout << "Login Successful" << endl;
            cout << "Welcome, " << currentUser.getUserName() << endl;
            cout << endl;
            return 1;
        }
    }

    // Check admin credentials
    for(auto& admin : adminList){
        if(userId == admin.getUserId() && password == admin.getUserPassword()){
            currentUser = User(admin.getUserId(),admin.getUserName(),
admin.getUserPassword());
            currentUser.setUserStatus("admin");
            cout << endl;

```

```

        cout << "Login Successful" << endl;
        cout << "Welcome, " << currentUser.getUserName() << "(Admin)" << endl;
        cout << endl;
        return 1;
    }
}

// Prompt user for registration if login fails
cout << endl;
cout << "Invalid login" << endl;
cout << "Do you wish to register? (Y/N)" << endl;
cin >> x;
if (x == 'Y' || x == 'y'){
    registerFunc();
}
else{
    cout << endl;
    cin.ignore();
}
}

// Display available tasks
int availableTasks(){
    cout << endl;
    cout << "Please choose a task to continue: " << endl;
    cout << "1) Display all cars" << endl;
    cout << "2) Display cars sorted by price" << endl;
    cout << "3) Display cars sorted by brand" << endl;
    cout << "4) Display cars sorted by ID" << endl;
    cout << "5) Display best selling cars" << endl;
    cout << "6) Search car by ID" << endl;
    cout << "7) Search issued bills" << endl;
    if (currentUser.getUserStatus() == "admin"){
        cout << "8) Add new car" << endl;
        cout << "9) Modify car" << endl;
    }
}

```

```

        cout << "10) Remove car" << endl;
        cout << "11) Generate Report" << endl;
        cout << "12) Exit" << endl;
    }
    else{
        cout << "8) Exit" << endl;
    }
    cout << "> ";
    cin;
    cin >> taskOption;

    bool status = true;
    while(status){
        try{
            digitInputValidation();
            status = false;
        }
        catch(string errorMsg){
            cout << endl;
            cout << "Error: " << errorMsg << endl;
            cout << endl;
            cout << endl;
            cout << "> ";
            cin >> taskOption;
        }
    }

    // Validate task option based on user or admin status
    if (((taskOption < 1 || taskOption > 8) && currentUser.getUserStatus() != "admin")
        || ((taskOption < 1 || taskOption > 12) && currentUser.getUserStatus() == "admin")){

        availableTasks();

    }

```



```

else{
    cin.ignore();
    return taskOption;
}
}

// Display all cars or sorted cars based on task option
void displayAllCars(){
    int i = 1;
    cout << endl << "Car options" << endl;
    if (taskOption == 1){
        if (carList.empty()){
            cout << endl;
            cout << "No car available for now." << endl;
            cout << endl;
        }
        else{
            cout << endl;
            for(auto& car : carList){
                cout << i << " ";
                cout << car.getBrand() << endl;
                cout << "Car ID: " << car.getCarId() << endl;
                cout << "Car Model Name: " << car.getModel() << endl;
                cout << "Color: " << car.getColor() << endl;
                cout << "Manufacture Country: " << car.getManufactureCountry() << endl;
                cout << "Manufacture Year: " << car.getManufactureYear() << endl;
                cout << "Price: RM" << fixed << setprecision(2) << car.getPrice() << endl;
                cout << "Sales: " << car.getSales() << endl << endl;
                ++i;
            }
            purchase(1);
        }
    }
    else if(taskOption == 10){
        cout << endl;
    }
}

```

```

for(auto& car : carList){
    cout << i << " ";
    cout << car.getBrand() << endl;
    cout << "Car ID: " << car.getCarId() << endl;
    cout << "Car Model Name: " << car.getModel() << endl;
    cout << "Color: " << car.getColor() << endl;
    cout << "Manufacture Country: " << car.getManufactureCountry() << endl;
    cout << "Manufacture Year: " << car.getManufactureYear() << endl;
    cout << "Price: RM" << fixed << setprecision(2) << car.getPrice() << endl;
    cout << "Sales: " << car.getSales() << endl << endl;
    ++i;
}
}
else{
    if (temp.empty()){
        cout << endl;
        cout << "No car available for now." << endl;
        cout << endl;
    }
    else{
        cout << endl;
        for(auto& car : temp){
            cout << i << " ";
            cout << car.getBrand() << endl;
            cout << "Car ID: " << car.getCarId() << endl;
            cout << "Car Model Name: " << car.getModel() << endl;
            cout << "Color: " << car.getColor() << endl;
            cout << "Manufacture Country: " << car.getManufactureCountry() << endl;
            cout << "Manufacture Year: " << car.getManufactureYear() << endl;
            cout << "Price: RM" << fixed << setprecision(2) << car.getPrice() << endl;
            cout << "Sales: " << car.getSales() << endl << endl;
            ++i;
        }
    }
    purchase(2);
}

```

```

    }
}

// Sort cars using merge sort and display
void sortCar_MergeSort(){
    temp = carList;
    mergeSort(temp, 0, temp.size()-1);
    displayAllCars();
}

// Search for a car by its ID
void searchCarByID(){
    int found;
    string id;
    if (!carList.empty()){
        temp = carList;
        cout << endl;
        cout << "Enter Car ID: ";
        cin >> id;
        // Sort for binary search algorithm
        sort(temp.begin(), temp.end(), [](Car& a, Car& b) {
            return a.getCarId() < b.getCarId();
        });
        found = Binary_Search_ID(temp, 0, temp.size()-1, id);
        if (found != -1){
            Car elementToKeep = temp[found];
            temp.clear();
            temp.push_back(elementToKeep);
            displayAllCars();
        }
        else{
            cout << endl;
            cout << "Car with this ID does not exist." << endl << endl;
        }
    }
}

```

```

    }
    else {
        cout << endl;
        cout << "No car available." << endl << endl;
    }

}

// Search for best selling cars
void searchBestSelling(){
    int found;
    temp.clear();
    if (!carList.empty()){
        vector<Car> searchList = carList;
        // sort for binary search algorithm
        sort(searchList.begin(), searchList.end(), [](Car& a, Car& b) {
            return a.isBestSelling() < b.isBestSelling();
        });
        found = Binary_Search_bestSelling(searchList, 0, searchList.size()-1, 1);
        if (found == -1){
            cout << endl;
            cout << "No Best Selling Cars for now." << endl << endl;
        }
        else{
            while (found != -1){
                temp.push_back(searchList[found]);
                searchList.erase(searchList.begin()+found);
                found = Binary_Search_bestSelling(searchList, 0, searchList.size()-1, 1);
            }
            bubbleSort(temp); // bubbleSort function is used to sort best selling cars
            displayAllCars();
        }
    }
}

```

```

    }
    else {
        cout << endl;
        cout << "No car available." << endl << endl;
    }

}

// Search issued bills by customer ID or date
void searchIssuedBills(){
    int choice;
    cout << endl << "Issued bills by: " << endl;
    cout << "1)Customer ID " << endl;
    cout << "2)Date of bill issued " << endl;
    cout << "> ";
    cin >> choice;
    bool status = true;
    while(status){
        try{
            digitInputValidation();
            status = false;
        }
        catch(string errorMsg){
            cout << endl;
            cout << "Error: " << errorMsg << endl;
            cout << endl;
            cout << endl;
            cout << "> ";
            cin >> choice;
        }
    }
    if (choice == 1){
        if (orderList.empty()){
            cout << endl << "You have no previous purchase.";
            cout << endl << endl;
        }
    }
}

```

```

    }
    else{
        linearSearch_Bills(); // linearSearch_Bills function is used for searching bills by
customer ID
    }
}
else if (choice == 2){
    if (orderList.empty()){
        cout << endl << "You have no previous purchase.";
        cout << endl << endl;
    }
    else{
        struct tm date;
        char dash;
        cout << endl;
        cout << "Enter bill data (day/month/year): ";
        cin >> date.tm_mday >> dash >> date.tm_mon >> dash >> date.tm_year;
        bool status = true;
        while(status){
            try{
                dateInputValidation();
                status = false;
            }
            catch(string errorMsg){
                cout << endl;
                cout << "Error: " << errorMsg << endl;
                cout << endl;
                cout << endl;
                cout << "Enter bill data (day/month/year): ";
                cin >> date.tm_mday >> dash >> date.tm_mon >> dash >> date.tm_year;
            }
        }
        date.tm_mon -= 1;
        date.tm_year -= 1900;
    }
}

```

```

        cout << endl;
        linearSearch_Bills_Date(date); // linearSearch_Bills_Date function is used for
searching bills by date
    }
}

}
// Generate a report of orders within a specific period
void generateReport(){
    struct tm startTime = {0}; // Struct to hold starting time
    struct tm endTime = {0}; // Struct to hold ending time
    char dash;
    int found;
    totalPrice = 0;
    vector<OrderDetails> tempList = orderList; // Copy of orderList for temporary
operations
    // Input and validation for starting date
    cout << "Enter specific period range" << endl;
    cout << "Please type according to the format and include '/' " << endl;
    cout << "Starting Date (day/month/year): ";
    cin >> startTime.tm_mday >> dash >> startTime.tm_mon >> dash >>
startTime.tm_year;
    bool status = true;
    while(status){
        try{
            dateInputValidation();
            status = false;
        }
        catch(string errorMsg){
            cout << endl;
            cout << "Error: " << errorMsg << endl;
            cout << endl;
            cout << endl;
            cout << "Starting Date (day/month/year): ";

```

```

        cin >> startTime.tm_mday >> dash >> startTime.tm_mon >> dash >>
startTime.tm_year;
    }
}

```

```

startTime.tm_mon -= 1; // Adjust month for tm struct (0-based)
startTime.tm_year -= 1900; // Adjust year for tm struct (years since 1900)
// Input and validation for ending date
cout << "Ending Date (day/month/year): ";
cin >> endTime.tm_mday >> dash >> endTime.tm_mon >> dash >> endTime.tm_year;
status = true;
while(status){
    try{
        dateInputValidation();
        status = false;
    }
    catch(string errorMsg){
        cout << endl;
        cout << "Error: " << errorMsg << endl;
        cout << endl;
        cout << endl;
        cout << "Ending Date (day/month/year): ";
        cin >> endTime.tm_mday >> dash >> endTime.tm_mon >> dash >>
endTime.tm_year;
    }
}

```

```

endTime.tm_mon -= 1;
endTime.tm_year -= 1900;
// Convert struct tm to time_t for comparison
time_t start_time_t = mktime(&startTime);
time_t end_time_t = mktime(&endTime);
// Validate and process the entered period

```



```

if (end_time_t >= start_time_t) {
    reportList.clear(); // Clear previous report entries

    // Search for orders within the specified period
    found = Binary_Search_report(tempList, 0, tempList.size()-1, startTime, endTime);
    if (found == -1){
        cout << endl;
        cout << "No purchase within this period." << endl << endl;
    }
    else{
        // Gather all matching orders into reportList
        while (found != -1){
            reportList.push_back(tempList[found]);
            tempList.erase(tempList.begin()+found);
            found = Binary_Search_report(tempList, 0, tempList.size()-1, startTime,
endTime);

        }
        // Sort reportList for chronological order
        quickSort(reportList, 0, reportList.size()-1);
        // Display each order's details in the report
        for (auto& order : reportList){
            order.displayReport();
            totalPrice += order.getFinalPrice(); // Accumulate total price
        }
        cout << "Total price of all sold cars: RM" << fixed << setprecision(2) <<
totalPrice;
        cout << endl << endl;
    }

} else {
    cout << endl;
    cout << "Period is invalid" << endl;
    cout << endl;
}

```

```

    }

}

};

//static member initialization
vector<int> OrderDetails :: numbers;

int main()
{
    srand(time(0)); // for generate random car ID
    int optionTask;
    char running;

    System system;// Initialize the car dealership system
    // Initialize existing users and admins
    system.registeredAdmin(User("ADM123", "Ang Yi Xun", "Cho030909$"));
    system.registeredUser(User("NAJ123", "Dr Najla'a Ateeq M. Draib", "najla2024"));
    system.registeredUser(User("AIT935", "Choo Qie Sheng", "QS030208"));
    system.registeredUser(User("AIT974", "Khoo Song Hao", "SH050503"));

    // Initialize cars
    system.registeredCar(Car("Audi", "R8", "black", "Germany", 2021, 1200000, 5));
    system.registeredCar(Car("Toyota", "Prius", "Purple", "Japan", 2020, 200000, 10));
    system.registeredCar(Car("Peroduo", "MyVi", "Red", "Malaysia", 2022, 80000, 12));
    system.registeredCar(Car("Proton", "X70", "White", "China", 2023, 400000, 6));
    system.registeredCar(Car("BYD", "Seal", "black", "China", 2024, 400000, 11));
    system.registeredCar(Car("Honda", "Civic", "black", "Japan", 2022, 600000, 7));
    // Main program loop
    while(system.loginFunc()){
        running = 'y';

```

```
while(running == 'y'){
    switch(system.availableTasks()){
        case 1:
            system.displayAllCars();
            break;
        case 2:
            system.sortCar_MergeSort();
            break;
        case 3:
            system.sortCar_MergeSort();
            break;
        case 4:
            system.sortCar_MergeSort();
            break;
        case 5:
            system.searchBestSelling();
            break;
        case 6:
            system.searchCarByID();
            break;
        case 7:
            system.searchIssuedBills();
            break;
        case 8:
            if(system.getStatus() == "admin")
                system.addNewCar();
            else{
                cout << endl;
                running = 'n';
            }
            break;
        case 9:
            system.modifyCar();
            break;
```

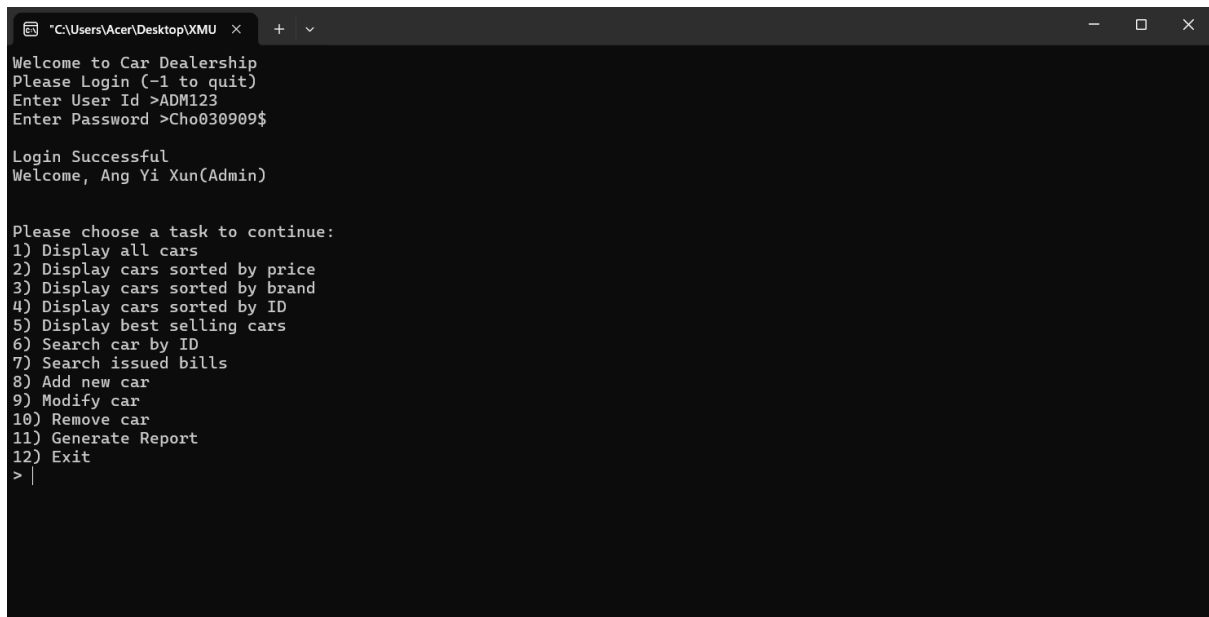
```
    case 10:
        system.removeCar();
        break;
    case 11:
        system.generateReport();
        break;
    case 12:
        cout << endl;
        running = 'n';
        break;
    default:
        cout << "Invalid Input" << endl;
    }
}
}
cout << endl;
cout << "Thank you for visiting." << endl;
cout << "Hope to see you again." << endl;
return 0;
}
```

Other resource:

<https://www.hackerearth.com/practice/notes/validating-user-input-in-c/>

## Running results

### Login for admin

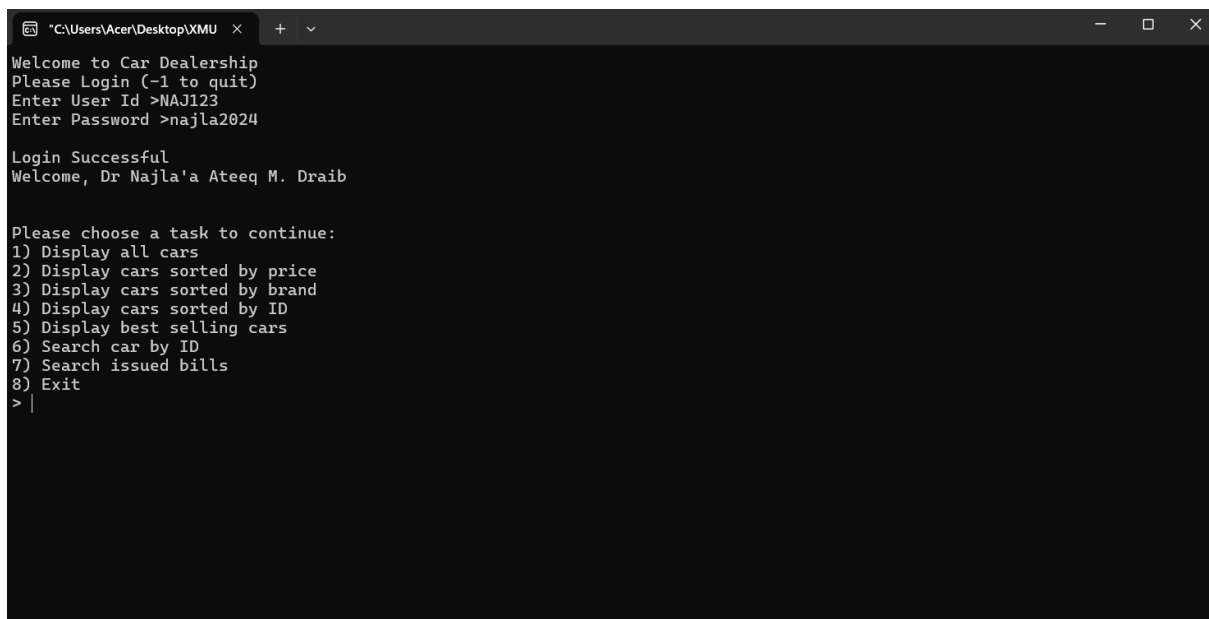


```
*C:\Users\Acer\Desktop\XMU x + v
Welcome to Car Dealership
Please Login (~1 to quit)
Enter User Id >ADM123
Enter Password >Cho030909$

Login Successful
Welcome, Ang Yi Xun(Admin)

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> |
```

### Login for user



```
*C:\Users\Acer\Desktop\XMU x + v
Welcome to Car Dealership
Please Login (~1 to quit)
Enter User Id >NAJ123
Enter Password >najla2024

Login Successful
Welcome, Dr Najla'a Ateeq M. Draib

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Exit
> |
```

### Task 1

```
"C:\Users\Acer\Desktop\XMU x + v

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Exit
> 1

Car options

1)Audi
Car ID: Aud116421095
Car Model Name: R8
Color: black
Manufacture Country: Germany
Manufacture Year: 2021
Price: RM1200000.00
Sales: 5

2)Toyota
Car ID: Toy263135113
Car Model Name: Prius
Color: Purple
Manufacture Country: Japan
Manufacture Year: 2020
Price: RM200000.00
Sales: 10

3)Peroduo
Car ID: Per460302754
Car Model Name: MyVi
Color: Red
Manufacture Country: Malaysia
Manufacture Year: 2022
Price: RM80000.00
Sales: 12

4)Proton
Car ID: Pro833307319
Car Model Name: X70
Color: White
Manufacture Country: China
Manufacture Year: 2023
Price: RM400000.00
Sales: 6

5)BYD
Car ID: BYD350277531
Car Model Name: Seal
Color: black
Manufacture Country: China
Manufacture Year: 2024
Price: RM400000.00
Sales: 11

6)Honda
Car ID: Hon426764212
Car Model Name: Civic
Color: black
Manufacture Country: Japan
Manufacture Year: 2022
Price: RM600000.00
Sales: 7

(type in '-1' to exit selection)> |
```

## Task 2

```
"C:\Users\Acer\Desktop\XMU x + v

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Exit
> 2

Car options

1)Peroduo
Car ID: Per442596424
Car Model Name: MyVi
Color: Red
Manufacture Country: Malaysia
Manufacture Year: 2022
Price: RM80000.00
Sales: 12

2)Toyota
Car ID: Toy975367705
Car Model Name: Prius
Color: Purple
Manufacture Country: Japan
Manufacture Year: 2020
Price: RM200000.00
Sales: 10

3)Proton
Car ID: Pro620689368
Car Model Name: X70
Color: White
Manufacture Country: China
Manufacture Year: 2023
Price: RM400000.00
Sales: 6

4)BYD
Car ID: BYD274696780
Car Model Name: Seal
Color: black
Manufacture Country: China
Manufacture Year: 2024
Price: RM400000.00
Sales: 11

5)Honda
Car ID: Hon639367797
Car Model Name: Civic
Color: black
Manufacture Country: Japan
Manufacture Year: 2022
Price: RM600000.00
Sales: 7

6)Audi
Car ID: Aud961695202
Car Model Name: R8
Color: black
Manufacture Country: Germany
Manufacture Year: 2021
Price: RM1200000.00
Sales: 5

(type in '-1' to exit selection)> |
```

## Task 3

```
"C:\Users\Acer\Desktop\XMU" x + v

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Exit
> 3

Car options

1)Audi
Car ID: Aud961695202
Car Model Name: R8
Color: black
Manufacture Country: Germany
Manufacture Year: 2021
Price: RM1200000.00
Sales: 5

2)BYD
Car ID: BYD274696780
Car Model Name: Seal
Color: black
Manufacture Country: China
Manufacture Year: 2024
Price: RM400000.00
Sales: 11

3)Honda
Car ID: Hon639367797
Car Model Name: Civic
Color: black
Manufacture Country: Japan
Manufacture Year: 2022
Price: RM600000.00
Sales: 7

4)Peroduo
Car ID: Per442596424
Car Model Name: MyVi
Color: Red
Manufacture Country: Malaysia
Manufacture Year: 2022
Price: RM80000.00
Sales: 12

5)Proton
Car ID: Pro620689368
Car Model Name: X70
Color: White
Manufacture Country: China
Manufacture Year: 2023
Price: RM400000.00
Sales: 6

6)Toyota
Car ID: Toy975367705
Car Model Name: Prius
Color: Purple
Manufacture Country: Japan
Manufacture Year: 2020
Price: RM200000.00
Sales: 10

(type in '-1' to exit selection)> |
```

## Task 4

```
"C:\Users\Acer\Desktop\XMU" x + v

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Exit
> 4

Car options

1)Audi
Car ID: Aud961695202
Car Model Name: R8
Color: black
Manufacture Country: Germany
Manufacture Year: 2021
Price: RM1200000.00
Sales: 5

2)BYD
Car ID: BYD274696780
Car Model Name: Seal
Color: black
Manufacture Country: China
Manufacture Year: 2024
Price: RM400000.00
Sales: 11

3)Honda
Car ID: Hon639367797
Car Model Name: Civic
Color: black
Manufacture Country: Japan
Manufacture Year: 2022
Price: RM600000.00
Sales: 7

4)Peroduo
Car ID: Per442596424
Car Model Name: MyVi
Color: Red
Manufacture Country: Malaysia
Manufacture Year: 2022
Price: RM80000.00
Sales: 12

5)Proton
Car ID: Pro620689368
Car Model Name: X70
Color: White
Manufacture Country: China
Manufacture Year: 2023
Price: RM400000.00
Sales: 6

6)Toyota
Car ID: Toy975367705
Car Model Name: Prius
Color: Purple
Manufacture Country: Japan
Manufacture Year: 2020
Price: RM200000.00
Sales: 10

(type in '-1' to exit selection)>
```

## Task 5

```
"C:\Users\Acer\Desktop\XMU" x + v
Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Exit
> 5

Car options

1)BYD
Car ID: BYD274696780
Car Model Name: Seal
Color: black
Manufacture Country: China
Manufacture Year: 2024
Price: RM400000.00
Sales: 11

2)Peroduo
Car ID: Per442596424
Car Model Name: MyVi
Color: Red
Manufacture Country: Malaysia
Manufacture Year: 2022
Price: RM80000.00
Sales: 12

3)Toyota
Car ID: Toy975367705
Car Model Name: Prius
Color: Purple
Manufacture Country: Japan
Manufacture Year: 2020
Price: RM200000.00
Sales: 10

(type in '-1' to exit selection)> |
```

## Task 6

```
Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Exit
> 6

Enter Car ID: Aud791257749

Car options

1)Audi
Car ID: Aud791257749
Car Model Name: R8
Color: black
Manufacture Country: Germany
Manufacture Year: 2021
Price: RM1200000.00
Sales: 5

(type in '-1' to exit selection)>
```

## Task 7



```

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> 7

```

```

Issued bills by:
1)Customer ID
2)Date of bill issued
> 1

```

```

Bill ID: 167
Customer ID: ADM123
Customer Name: Ang Yi Xun
Car ID: Aud647605097
Car Brand: Audi
Car Model: R8
Car Color: black
Production Year: 2021
Price: RM1200000.00
Discount : 10.00%
Total Price: RM1200000.00
Date:6/7/2024
Time (00:00, 24-hour time): 20:0

```

```

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> 7

```

```

Issued bills by:
1)Customer ID
2)Date of bill issued
> 2

```

```

Enter bill data (day/month/year): 6/7/2024

```

```

Bill ID: 167
Customer ID: ADM123
Customer Name: Ang Yi Xun
Car ID: Aud647605097
Car Brand: Audi
Car Model: R8
Car Color: black
Production Year: 2021
Price: RM1200000.00
Discount : 10.00%
Total Price: RM1200000.00
Date:6/7/2024
Time (00:00, 24-hour time): 20:0

```

## Task 8 (admin)

```

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> 8

```

```

Please enter new car information.
Car Brand: Ferrari
Car Model Name: Super123
Car Color: Red
Manufacture country: Italy
Manufacture Year: 2023
Price: 2000000
New car added successfully.

```

```

7)Ferrari
Car ID: Fer467025238
Car Model Name: Super123
Color: Red
Manufacture Country: Italy
Manufacture Year: 2023
Price: RM2000000.00
Sales: 0

```

## Task 9 (admin)

```

Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> 9

```

```

Enter the car id to modify: Fer467025238
Enter -1 if you do not wish to modify this section.
Enter new brand: Lambo
Enter new model name: Super345
Enter new color: White
Enter new Manufacture Country: Germany
Enter new Manufacture Year: 2024
Enter new price: 3000000
Changes made.

```

```

7)Lambo
Car ID: Fer467025238
Car Model Name: Super345
Color: White
Manufacture Country: Germany
Manufacture Year: 2024
Price: RM3000000.00
Sales: 0

```

## Task 10 (admin)

```
"C:\Users\Acer\Desktop\XMU" x + v
Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> 10

Car options

1)Audi
Car ID: Aud146707036
Car Model Name: R8
Color: black
Manufacture Country: Germany
Manufacture Year: 2021
Price: RM1200000.00
Sales: 5

2)Toyota
Car ID: Toy381151404
Car Model Name: Prius
Color: Purple
Manufacture Country: Japan
Manufacture Year: 2020
Price: RM200000.00
Sales: 10

3)Peroduo
Car ID: Per667364626
Car Model Name: MyVi
Color: Red
Manufacture Country: Malaysia
Manufacture Year: 2022

4)Proton
Car ID: Pro988627551
Car Model Name: X70
Color: White
Manufacture Country: China
Manufacture Year: 2023
Price: RM400000.00
Sales: 6

5)BYD
Car ID: BYD164718945
Car Model Name: Seal
Color: black
Manufacture Country: China
Manufacture Year: 2024
Price: RM400000.00
Sales: 11

6)Honda
Car ID: Hon846627597
Car Model Name: Civic
Color: black
Manufacture Country: Japan
Manufacture Year: 2022
Price: RM600000.00
Sales: 7

7)Lambo
Car ID: Fer467025238
Car Model Name: Super345
Color: White
Manufacture Country: Germany
Manufacture Year: 2024
Price: RM3000000.00
Sales: 0

Choose a car to delete: 7
Car removed successfully.
```

```
"C:\Users\Acer\Desktop\XMU" x + v
Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> 1

Car options

1)Audi
Car ID: Aud146707036
Car Model Name: R8
Color: black
Manufacture Country: Germany
Manufacture Year: 2021
Price: RM1200000.00
Sales: 5

2)Toyota
Car ID: Toy381151404
Car Model Name: Prius
Color: Purple
Manufacture Country: Japan
Manufacture Year: 2020
Price: RM200000.00
Sales: 10

3)Peroduo
Car ID: Per667364626
Car Model Name: MyVi
Color: Red
Manufacture Country: Malaysia
Manufacture Year: 2022

4)Proton
Car ID: Pro988627551
Car Model Name: X70
Color: White
Manufacture Country: China
Manufacture Year: 2023
Price: RM400000.00
Sales: 6

5)BYD
Car ID: BYD164718945
Car Model Name: Seal
Color: black
Manufacture Country: China
Manufacture Year: 2024
Price: RM400000.00
Sales: 11

6)Honda
Car ID: Hon846627597
Car Model Name: Civic
Color: black
Manufacture Country: Japan
Manufacture Year: 2022
Price: RM600000.00
Sales: 7

(type in '-1' to exit selection)> |
```

Task 11 (admin)

```
Please choose a task to continue:
1) Display all cars
2) Display cars sorted by price
3) Display cars sorted by brand
4) Display cars sorted by ID
5) Display best selling cars
6) Search car by ID
7) Search issued bills
8) Add new car
9) Modify car
10) Remove car
11) Generate Report
12) Exit
> 11
Enter specific period range
Please type according to the format and include '/'
Starting Date (day/month/year): 3/7/2020
Ending Date (day/month/year): 7/7/2024

Car ID: Aud647605097
Car Brand: Audi
Car Color: black
Customer Name: Ang Yi Xun
Date:6/7/2024
Price: RM1200000.00

Total price of all sold cars: RM1200000.00
```