

Due at 1700, Fri. Mar. 20 in homework box under stairs, first floor Cory .

Note: up to 2 students may turn in a single writeup. Reading Nise 10.

1. (20 pts) Nyquist Exercise (Nise 10.5)

Consider a close loop system with unity feedback. For each $G(s)$ below, hand sketch the Nyquist diagram, determine $Z = P - N$, algebraically find the closed-loop pole location, and show that the closed loop pole location is consistent with the Nyquist diagram calculation.

a) $G(s) = \frac{5}{s+1}$

b) $G(s) = \frac{5}{s-1}$

2. (25 pts) Nyquist Plot (Nise 10.5)

Consider a closed loop system with unity feedback. The open loop transfer function is:

$$G(s) = \frac{k(s-2)}{(s+10)(s+2)}$$

- a) Hand sketch the asymptotes of the Bode plot magnitude and phase for the open-loop transfer functions.
- b) Hand sketch Nyquist diagram.
- c) From Nyquist diagram, determine range of k for stability.
- d) Verify sketches with MATLAB (`bode()` and `nyquist()`) and hand in.

3. (25 pts) Nyquist Plot (Nise 10.5)

Consider a closed loop system with unity feedback. The open loop transfer function is:

$$G(s) = \frac{k(s+4)^2}{(s+1)^4}$$

- a) Hand sketch the asymptotes of the Bode plot magnitude and phase for the open-loop transfer functions.
- b) Hand sketch Nyquist diagram.
- c) From Nyquist diagram, determine range of k for stability.
- d) Verify sketches with MATLAB (`bode()` and `nyquist()`) and hand in.

4. (30 pts) Gain and phase margin (Nise 10.7, 10.10)

A closed loop system with unity gain has open loop transfer function

$$G(s) = \frac{2(s+5)}{s(s^2+2s+8)}$$

- a) Plot the Bode magnitude and phase plots for the open loop system (MATLAB ok).
- b) Determine the gain and phase margin.
- c) Assuming a second order approximation for the closed loop system, estimate the transient response for a step input from the phase margin and gain margin. (That is estimate ξ , overshoot, peak time, and settling time.)
- d) Compare the actual closed loop step response from MATLAB with the estimates from c).