14.5) Determinated punchelor de extrem land precenditional, liberte, foro legaturi) En coul fundiçõe de n-savaloide Carol: M=1(C1 12 = 12 : Fic ) f: D = 12 - 22 o functio de dont ou devisabile que donne vivel de def D Vocan sã de termina un punchele de estrem local ale funçtici " f" Lesponetile els minim | maxim Agairtuel de levous (lives, d'axia) a) cutabelul demnistie a funției 1(x) ++0-- 0++0--0++0+++ for 1 for & for 1 for 1 for 1 for 1 fin fine fine fine fine fine fine b) as a justonal deminateller de ordinal I i it als function "fais. 0 coloniam devivata de ord. I: for =? 2) resultion ecuação: for = 0 ou solutido ( ) - punto critic ( atationare) de function for 5) redcular devivata de and Ti: \$(x)=? 4) ababitus semuel de vivalei de orde à m fire ese dinte puntele de toure. Date: (a) f(x;) >0 so x pand & mining (Cood) - { b) \$ (c) <0 => of panet de maxim (focal) (c) \$ (21)=0 => no se goate abolile valore purdadui (21). b') ou gutorel diferentiale br de ord. I vi I ale function , for, 1) calculan diferentiala de ord. I: df co = fix dx =? 2) reacher egolilature: decent co cos flord = oc flores ou solution ( salica ( salica ) 3) calculou diferentiala de ord T: de Los = 4" codx =? is addition semme diferentials; so not is in fiscare divite purches obtioners. Date: (a) of top > 0 (a) of the 100 100 to co fix 1 >0 => 0 ( - pand de minim (bod) ( p) gotal) <0 (e, t/x) ( so co t, al) so => x! -banet or maxim (pool) c) of facil so (=) facilar = 0(=) facil=0 => in bottom go forming infrare for "12"

```
Obs: fundia for one o singuis derivate de ord I in o singuis devivate de ord I;
the country to the country one ("" of the country backing good I ( 3th : i=111)
a realiza abapela i)-iv) din mebda b) trabaia so folimin diferentiable de ord I ni II adapate aasteia & ove sunt unice: df(x,-,x,) ni df(x,-,x,)
Defi: Fie It: DER" - IR
                                      o finitie de (al pefie) dous on anisolate in espert au
  porto nocumos creper ( & CSD) in X0 = (x1, x2, -, x8) ED. Stornen co:
a) Xo osto parot de visión (book) perteu fanção "f", dace:
       b) to ste punt de maxim (local) pentru functia " f ", dace:
      (132) (3) N(K) = S(X, r) ⊂ D a.7: $(X) > $(X) - (A) X ∈ 4(K)
 (i) evident on get to me enter punct de copiem (Pord) (=) Xo - pet de vivien son de masion

(ii) evident on get to me ente punct de copiem (Pord) (=) (A) V(X) = S(Xo, r) CD, (A) X1,X8
                                                              (3x) 2< (2x) 2 (2x) > (2x) > (2x)
Toto Lie (t: Delle, - Delle

    pendie de dos C'(δ) (†ε C'(δ)) η χο=(x; x; -,x; ) ε·δ.

        Atoma Xo este punct stationer (oritic) portue funcția "f", dacă:
   (18.5) af(x0) = 0 = 0 (18.81) \ \frac{\text{gs}(x) = 0}{\text{gs}(x) = 0}
                                      8x5 (X)=0
 Tessemal de caracterizar a paritebr de extrem Ocal) - conditi me ficiente ma ji mossare
 File & ECSOD on DER" in XOED in punct who from our (oritic) forther " for Admicil dave:
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Fig & C(D) on D \(\int\) \(\text{N}\) \(\tex

(pertue ai puta statili semnul aasteia) tookna 1 pati li reformulato artfel:

## Tearema I (de caracter sare a printe br de artem local cu metada lui tardri)

Fix \$ \in Co D \in D \in R" in X & \in D un print replicated ( or ye) benten tingia " \in (X)" in

 $g_5 t(x^o)_{\text{pol}} = \sum_{x}^{(z)} \frac{2z}{x} \frac{\partial x(yx)}{\partial z^{\text{c}}} (x^o) q x(qx), \quad \tilde{z} \sum_{x} \sum_{x}^{(z)} \tilde{z}_x^{(z)} q x(qx).$ ) respective brassiana atorreta valaj (=aji)

and ans- and - and

Condici "f" in principle obalismos Xo=(x,x,-,x): H(x) = | and one - and EMM(R)

Notand on: An Asi-, Air-, An minoria diagonali moning.

Notand on: Dr. Dr. -- Dig -- Du minorii diagonalii principali ai matricei H(xo), adica:

$$\Delta_{s} = \begin{vmatrix} \alpha_{11} & \alpha_{12} \\ \alpha_{21} & \alpha_{22} \end{vmatrix}$$

$$\Delta_{s} = \begin{vmatrix} \alpha_{11} & \alpha_{12} \\ \alpha_{21} & \alpha_{22} \end{vmatrix}$$

$$\Delta_{s} = \begin{vmatrix} \alpha_{11} & -\alpha_{12} \\ \alpha_{11} & -\alpha_{12} \\ \alpha_{11} & -\alpha_{12} \end{vmatrix}$$

$$\Delta_{s} = \begin{vmatrix} \alpha_{11} & -\alpha_{12} \\ \alpha_{11} & -\alpha_{12} \\ \alpha_{12} & -\alpha_{12} \end{vmatrix}$$

$$\Delta_{s} = \begin{vmatrix} \alpha_{11} & -\alpha_{12} \\ \alpha_{11} & -\alpha_{12} \\ \alpha_{12} & -\alpha_{12} \end{vmatrix}$$

atunei, avem pentru:

- a) \$1 >0; \$2 >0; -184 >0 (+,+,-,+) => X0 este perch de minim (ocal) pritue function f(x);
- b) Do CO, Os so; OsCo, -- (-,+,-,+, -) => Xo ate provet de maxion (bod) pertre familia (K)
- c)(V) bito, i= I'm in in once also combination de service do cot in casul a) over b) => Xoust - punct do in faxione (good pa) pontru functia (XX);
- ababase (E)(b) b):=0, ietis, wi => nu re poate precisa natura punctului Xa (wooda Qu' lacoln' na "functionera")
- i) in Te, toma potratio : def(X) = = = a; dx; dx; a fort aduate la forma removiro tolorand formula bei lawoloi: deplo) = Dody + Didy + - + Didy + - + Du do (am notest ac: dy:=bilda:+bizdaz+-+bildam ; i=Tin)
- ú) evident in comel d) peto ur foldri medoda lui Gans (vou aduce matricea HKo) la forma triunglinlar superioare cu T.F.)

Don deft oi e respectiv (TI m) Te resulto unuaborul algoritu de determinare a puntilo-de extrem Exol partru funcții de "u "vorialnici": Algorithm de de terminare a punch lor de octron local (libera) reconditionate Men Egitasi I) casal general (ID") Pentru a determina punchelo da extrem lord alse unes functio (f. DER -R), procedem astfel: O Calculan ale "" quivate bastiale de ory I ap Cantrei : 32, 32, -, 32 Determinam puncted stationare (vilia) ele funtia, resolvand vistames: ale corni solutii Pe (23, 23, -, 23) sunt printele stationere (visha) contate 34 = 0 @ Calculan cale "", derivate partiale de ord " ale funçãoi: 3x,3x; 6) Sociem herriana atapaté function fin  $H(\alpha^{1/3}x^{3}-1,x^{\alpha}) = \begin{cases} \frac{9x^{4}9x^{1}}{35t} \frac{9x^{2}9x^{2}}{35t} & \frac{9x^{2}}{35t} \\ \frac{9x^{2}9x^{4}}{35t} \frac{9x^{2}}{35t} & \frac{9x^{2}9x^{\alpha}}{35t} \end{cases}$ 6 Coloulan harring in junctul abolioner (oute) 7, (x1, -1x1): HP(1) = a21 022 - 024 © Calculan minorii diagonali principali ai lui H(Pr); Δn = | 0, -0, | Δn = | 1 | = det H(Pr)

( pa tour) grandly is abteny - 19 (= (duco (a tasse some do siterialmos stle in in 117) (+) & (B)

1) B) Bi => pt i e {1.5, - , u} => me proter processe where (polde vivin) maxim/infarines) get P1

(8) Reposion edopale O-O pertur toate all lalk private deficione (ailia): B, B, -, Pe

( sea) minim ab. ty-, 9 c= (+1-,+1+) ocub1 ---- 10000 10010

B) B1 CO, B2 201 B3 CO, ---- (-1+1-1+1-)=> P1-12+ de maxim (Bral)

```
II) carul particular (4=2 (=1 P2)
Perton a de tomina punctele de extrem boal ele unei functi: {1:DER2-12
O Calculan derivable partial de ord I: 20, 20;
@ pe perminent bance opinione (origine) of tendio, tout sesopiery visiting
       (A) \ \frac{34}{3\frac{1}{2}} = \frac{ago cour acente (102) \frac{1}{2} (22) \frac{1}{2} \rightarrow \text{ and baneted retionace (config.) courtest? } \frac{1}{2} (22) \frac{1}{2} \frac
@ Calculan garinappe barliage go end is op leg test test): 355 / 356 , 350 = 355
@ Essient promiant apology timber tout): Hail = (35 35 35)
(3) Calculan hasinna in primal pand with Praise! Her! = Haritel = (an ass
(6) Calculam minorii diagonali principali $1,150 ai lui HA): ∫$1=011 ✓
          bace: (a) $10; 620 (+1+) => Pr-pot de maxim (Gcal)
61 4(0; 600 (-1+) => Pr-pot de maxim (Gcal)
                              C) ($1>0; $2<0(4,-) => P1-pal. de inflamme (punct pa)
                              (d) $100 san $200 => ha pakus procisa notura puntului osità P.
   & Reportan edapole 6-6 poutru al Palk puncte onitice: P3, P3, -, Fe
              Ex: So se distanción took prochet de citron anal ale finifici: [ F. R - R
    DEM.
                                                                        Obs deriver handis a un produs followed while ((1) - 1 + 1)
   0 3x = (2+1) (02+2+1)
         137 = (X+1) (X+5A+1)
                                                                                   \frac{cabeer \text{ or } (x)}{g_{\frac{\pi}{4}}} = \left[ (2\pi i)(3x + 2\pi i) \right]^{X} = \left[ (2\pi i)(3x + 2\pi i) \right]^{X}
\frac{2x}{g_{\frac{\pi}{4}}} = \left[ (2\pi i)(2\pi i)(3x + 2\pi i) \right]^{X} = \left[ (2\pi i)(3x + 2\pi i) \right]^{X}
                                                                                                841=0 (=1) B(-1)-1)
                                                                                                                                                                                   כיבל שמם בכם כים לים (יוֹ
                                                                                                      24 5 4 1 =0 (=) By (-3 1-2)
```

$$\frac{9xg4}{8xt} = \frac{94gx}{8xt} = \sigma(x+14x)$$

$$\frac{94x}{8xt} = \sigma(x+1)$$

$$\frac{94x}{8xt} = \sigma(x+1)$$

## III cazul particular N=3 (123)

Benton a de permina bruspe es estrem pares es tembres (4: PELS - 15 becaga in artel:

$$\frac{1}{2} = 0 \quad \text{observed of the state of t$$

(oridice) contate

$$H(x) \frac{350}{35} = \frac{950}{35} \frac{955}{35} = \frac{955}{35}$$

$$H(x) \frac{3}{3} \frac{1}{5} = \frac{950}{35} = \frac{955}{35}$$

$$\frac{955}{35} = \frac{955}{35} = \frac{955}{35}$$

(alculou minorii diagonali principali: Ander 12 conspantatiri lui H(A):

Dace!

a) 200 minim so top - 19 (+1+1+) coco (00 col ocid)

6) A, <0, A250, A3<0 (-,+,-) => P, - got de manime local

(3a) (4) 1/20, i=13 in alto ambination de semme dest assaub) => 7, -pot de inflocione (3a)

18 Sino, ichora = 1 me putam precisa natura punchelui orità PI

De repete etopole ⊕ -@ pertru allelatte punte aritea: 3, 3, -. R

Ex: Deberminati punded do cotram land ala función: It is se

$$\frac{\partial x}{\partial t} = -85$$

$$\frac{\partial x}{\partial t} = e^{2}A - e$$

$$\frac{\partial x}{\partial t} = e$$

$$\frac{\partial x}{\partial t} = e^{2}A - e$$

$$\frac{\partial x}{\partial t} = e$$

$$\frac{\partial x}{\partial t} = e$$

$$(3a)$$

$$H(P) = H(1,1,0) = \begin{cases} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{cases} = \begin{cases} \Delta_3 = -54 & \frac{1}{4c} \\ \Delta_3 = 192 & \frac{1}{4c} \end{cases}$$
Poste panet de inflicacione (3a)

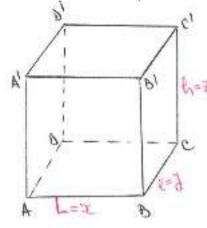


abstrite deselve interruper in farmitarea apei industriale, societa a schilitatia deside sa si arigine o seserta (suficiente phi destesurarea activitati timp de o este sopriamina) construind un basin descopsit, de forma unui parablipipal desphinglia (prismo pakulatera dregto) ou capacitatea (volumul) de 1000 m³. Flind co preful (fix) de construcție este de 500 timo/m² so se se de termine soluție caustructio captime."

## Dom:

solutie contrativa optima a costul bold de contractie to fe minim

Os costed depinde de cat se construinte (suprefora construità trebecie sa fie minima)



$$\begin{cases} N = xA \le 1000 \text{ (Mz)} \rightarrow 600\text{ april (abov.)} \rightarrow 6000 \text{ april (abov.)} \rightarrow 6000 \text{ april (abov.)} \end{cases} \rightarrow 6000 \text{ april (abov.)} \rightarrow 6000 \text{ april (ab$$

Model natematic

on conspiger ( pategora): 2525=1000

objusted o (none) fantise case depinde door de x, y or un are legaturi (restrictii:

Vrem so detecninam valorile lui (x=? a.r. Lixi3) sã aitre valoasea minima (=1 no determinos practed (practices de minima al funçãos « + «

Aplican als. de de terminare a puncte los de extram boral fundiai froy:

$$\int_{\overline{Q}} \left(\frac{\lambda_{S}}{T}\right)_{i}^{z} = -\frac{\lambda_{S}}{S}$$

$$\overline{Qpe}_{i} \left\{ \left(\frac{x}{T}\right)_{i}^{z} = -\frac{\lambda_{S}}{T} \right\}$$

 $\frac{3d}{3t} = 3$   $\frac{3d}{3t}$  $(=) x_3 - (\sqrt{3}\sqrt{2})^2 = 0 = (2 - (\sqrt{2} + (\sqrt{2} + (\sqrt{2} + \sqrt{2} + \sqrt{2}))^2) = 0 = (\sqrt{2} + (\sqrt{2} + \sqrt{2} + \sqrt{2}))^2 = 0 = (\sqrt{2} + (\sqrt{2} + \sqrt{2} + \sqrt{2}))^2 = 0 = (\sqrt{2} + (\sqrt{2} + \sqrt{2} + \sqrt{2}))^2 = 0 = (\sqrt{2} + (\sqrt{2} + \sqrt{2} + \sqrt{2}))^2 = 0 = (\sqrt{2} + (\sqrt{2} + \sqrt{2} + \sqrt{2}))^2 = 0 = (\sqrt{2} + (\sqrt{2} + \sqrt{2} + \sqrt{2}))^2 = 0 = (\sqrt{2} + \sqrt{2} + \sqrt{2}) = (\sqrt{2} +$ (1) P(10/2) 10 (2) - punt on fic (stationer) unic (N=-300 Th<0)

A: - 49 loved wining storted sto I see Souristud on marine boal ph-, to

Comparie 
$$(3.4)^2 = \frac{3.94}{9.35} = 1$$

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Condusie

Lundia Land is aginte reported minimo in banega Blogs ing)

Conducio economica

Poliția constructiva optima (ou al mai vice ost toste date de:

(x=101/2 m) share beginsher its un patret (2 = 5 \$\frac{1}{2} m → mothings brainchie este junichete deu Palana patrabli de la bare

Dos 5 = 1000 = 1000 = 2001 = 315 (W)

Vight 260) = 552 + 525 + 525 = 100 gt + 100 gt + 100 gt = 300 gt (mg) 5 136 mg Chin = 200 E/Ms. 4 (Ms) on 200x440 = 538000 Enes (costal potal minim de constructio al womenly)

Obs - date construiour bosinal ca au cab as leture de 10 m, volumal acestacia as fi fost de 1000 mº, dor supre fosto construità as fi fost de = fekx now = = = on we, dea contact to tol as fi fort de 250.000 sun (mai more at 12.000 Euro!!!) sente este efectul unui valad makuntic