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Curs 4
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I.5) Forme limare

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Def Fie (V,+, ) un epotiu liniar conecus pi corpul combotis al m. real (R,+, ). Numin forma liniara pe V aplicatio: \f: V -oR care satisface proprietofile:

(4.1) (i) f(u+6) = fu+for); (4) w, self (=> (4.1) f(u+pa) = a fu+pfe); (4) u, self

(ii) f(xx) = x f(u); (4) xeR (=> (4.1) f(u+pa) = a fu+pfe); (4) xeR
```

000.

i) proprietable de aviantete (41) se peate generalità pertur casul a """ vectori, adico:
(4A) fixiu,+x2 v2+ +x, vn) = x, fru)+x2 five)+ +x, fru) (4) v, ve, -, vn ex
"" a l'all te ve to en to en

ii) an constitular I = 12" (signal con in interspect), avon una barra tecrema de carac-

Teorema (de caract a formaler liviare def pote")

O aplication (f: R) - R sote forma limiter (=> (4.2) (f: R) - R

{f(x) = p(x,x,...,x_n) = x_1x_1 + c_2x_2 + - + c_4x_n

on e(ER, is In M/X = (x_1x_2,...,x_n) = R)

(1) (4) 4 - forma limpe 12", over : from = from --, 0) = 0

il) does when: $C = (x_1 x_2 - - x_1) \in \mathcal{U}_{(0)}^{(2)}$ (42) $(4.2') \mathcal{L}(X) = C \times - \text{bairned matricials}$ a unei $X = \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = (x_1, x_2, -, x_1, x_2) = (4.2') \mathcal{L}(X) = C \times - \text{bairned matricials}$ forme liviane.

 $\begin{cases} f(x_1, x_2) = 2x_1 - 3x_2 \end{cases} \begin{cases} c = (2_{\bullet} - 3) \Rightarrow \text{ metrices conficientillor formed livings} \\ (x_1, x_2)^T = (x_1) \end{cases}$

I(X) = C. X = (5 -3) (x1) = 5x1-3x5

 $\begin{cases} \{\cot^{(2)}x^{(1)}x^{2}\} = 2x^{2} + 5x^{2} - \mu x^{2} \\ \begin{cases} x^{2} \\ (2 - \mu) \end{cases} \Rightarrow \begin{cases} x = (x^{(2)}x^{2})^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu) \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{2} \\ (x^{2} - \mu)^{2} \end{cases} \Rightarrow \begin{cases} x^{2} + (x^{2} - \mu)^{$

- 3) {f: 24 → 12 for) = 200, + 300,203 -4 -> musto forme liniarà (!!) (aven producel 4306 23 n)
- 4) Analog, my mut for we livian, arm = toasele aplicati (functi)

 (i) f: R²→R; f(x1,x2,x3) = 2x2 + 3x2 x1x3+4

 (ii) fe: R²→R; fo(x1,x2) = 6x1+x2-1

 (ii) fo: R²→R; fo(x1,x2) = 6x1+x2-1

 (iii) fo: R²→R; fo(x1,x2)=6x1+x2-1

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III Elemente de proframera liniara fontada aler desse fase
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III Notimi indroductive Modela economica generale.

Ze ministe 3 ropogemes que budianos maganatica (332) a desprima go torna:

(Im) (min/max) I= f(201,200,..., xx) - fundia objectiv (este o fanctie correcare) [gacx,,x2,...,xk] \$5,

an/ (8, ca, x, ..., x,) \$ b2 24(2123,) 28) € pm

(energy (emplie de montales de 1927 - 19 mont fares de

(3m) x3 EB, 3=1x

A resolva (P.P.M) acsoamura a afle traste soluțiile richemului de restrictii (2m) (aasta admite. in general o infinitet de voluții) ni apoi sã o determinana (destre acestra) pe acesa (ace lea-pot fi mai mulbe) care face ca função directir das (10) são ia valvara minima/maxima. O avida de soluție se nu nește colutie optime a (P.P.M)

Dava cute-o (3.7m) atat funcția obioctio, fu och și funcții le "grzer-13m" care définer votristifé (201) runt forme liniere, obtiven cosul posticular (dar extrem de important in facile des intélluit en apricatifé économia al problematir de programare liviate (PPL) avand forma urma-bore:

((1) (min/max) fixeras,..., xx) = x1x1+x2x2+...+xxxx - functio drivetiv (functio cost/profit)

(aux1+015x5+---+018x8/2pl

(21) Jana + 0 35 ast - + + 10 35 as 2 2 2 ps 12 regristri economico

000

Favofill " g, go, --, gm, care defined patriotile der richeral (2m) au in a ast cas, urmo -- baredo expreso:

2(x1)21-1-124)=011x1+015x5+-+01x5 - forme liniare (cf 62) 95(x1) x21 , xK) = 051x1+055x3+ ... + 05kxK

(3m(x1,x21----, xx)=amx1+amxx2+---+amxxx

nodel madematic etc (P.P.L)

```
1) Problema planificarii productioi (folosirea optimo) eficiente a resursabir limitate)
"O companie /firma disque de resursele limitet (moderni prime, Garde de muna, bariate):
  Risks ..... 18m (Per 15 in) in contidation bists ..... ibu for int
   ni donoste são fabrico (oblivão) produced (obricto, manini, servicii, etc.):
  Rigging Bk (Bij= 15k) in cantidatile: across -- 1xx & 2; j= 1xx } recommanded
    Stind ca:
  a) consumal unidor den roseroa "P; " penten a se fabrico un produs "Fi" ate contiletar "a j'e i-tra
  6) profital (not/boat) unitar poulsa vansara unici produs , 3, ste , 3, 1, 5-1,2
Do se desermine un plan de productie explin (est so se fabrice des frecase produce a?
 profibul total realizat são fie maxim si no se madouse on contitação limitade de
  resurve anute la diaposité)
    Modellel matematic al acestei probleme economice ate o (P.P.L) de forme:
(1) (max) $ (x1, x2, -1, xx) = x1x1+x2x2+ -1 xxx - vegocour prof. fulli (Lunifice prof. t)
  (2) Son x1 + 0 12 x2 + ... + 0 16 x6 
(41) - rotricti economia (nu pot follosi mai mult dint-0

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(2) Son x1 + 0 12 x2 + ... + 0 16 x6 
(41) - rotricti economia (nu pot follosi mai mult dint-0

(2) Son x1 + 0 12 x2 + ... + 0 16 x6 
(5) Son x1 + 0 12 x2 + ... + 0 16 x6 
(6) Son x1 + 0 12 x2 + ... + 0 16 x6 
(7) Son x1 + 0 12 x2 + ... + 0 16 x6 
(8) Son x1 + 0 12 x2 + ... + 0 16 x6 
(9) Son x1 + 0 12 x2 + ... + 0 16 x6 
(9) Son x1 + 0 12 x2 + ... + 0 16 x6 
(10) Son x1 + 0 12 x2 + ... + 0 16 x6 
(11) Son x1 + 0 12 x2 + ... + 0 16 x6 
(12) Son x1 + 0 12 x2 + ... + 0 16 x6 
(13) Son x1 + 0 12 x2 + ... + 0 16 x6 
(14) Son x1 + 0 12 x2 + ... + 0 16 x6 
(15) Son x1 + 0 12 x2 + ... + 0 16 x6 
(16) Son x1 + 0 12 x2 + ... + 0 16 x6 
(17) Son x1 + 0 12 x2 + ... + 0 16 x6 
(18) Son x1 + 0 12 x2 + ... + 0 16 x6 
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(18) Son x1 + 0 12 x2 + ... + 0 16 x6 
(18) Son x1 + 0 12 x2 + ... + 0 16 x6 
(18) Son x1 + 0 12 
(0) oc; >0 1 7= 1x
                                       · contideple core unesso a fi produse mugot fue valori registive.
  Exemple
i) veri primal exemple (on gentile de laptop den annul introductio (aureul 00)
ii) U.F. a lancat a competitive priving Ginantarea projectible all arcatare privind energia
    alberrature (la combentitoilei forili) en un buget total ale un miliard de tiro. Comina
     de evaluare a retinut den all poste 200 de projecte dequos dans 6 partir a le tinanta.
     Fiscore din ale 6 projecte a fast evaluat in punctat in resport a viterial: "bushaid
      (profital) not definat pentru frecon Euro invotif, representant beneficial (profital)
      potential partir o perioacto de mani de aplicare a projectului. Intobalul de mai
        305 de génera projectile, punale maxime policidete de audor à beneficiel net estimet de
c. Tipul projectului projection inter source mains role cité to
l. Energie adaré (I) 446 200 milioure Euro
     Hr. Tipul projectului
      1. Every's where (I)
       2. Emilie colore (1)
                                                                    180 mil. E
                                                 385
       3. andustibili midetici
                                                                    250 mil 5
                                                 4,15
                                                                     120 mil E
       4 Bio-combustiloili
                                                 3,50
                                                                     400 mil 5
       5. Energie michagos
                                                 5,16
       6. Evergie gro-brondo
                                                                     les will E
                                                 3,2€
                                               Total firmfor= 1.320.000.000 Euro
```

Propositional Cominies European a reliabet as provided din somewill militar not princave cal putin 60% du rema maximo policidato, motivand en importante strategica a commin la vivalul U.E. Datorita lobby-ului intens foont de O.N.E-uville pe donnevial ecologic, d' ma provis acestora aborava a minimal 250 milioant Euro partre finantare projectibre "versi" adica a alor dans projects de energie solars in cel primad energia gestermala. Sa se destrinive pland optim de aboare a banifor (cost bani sã princace fiecase project a.? teneficial pokulial oblinat prin application for so be maxim) Modelul madernatic not: 2; i = 1.6 - sumed (or milioun de Euro) care nemente a l'alacate prosentului ? (omy max) 2006 + 50019+ 2005 6+ 60010+ 3086+ 12044=(30,700,000,000,000) (1). (x,+x;+x3+x,+x5+x6 & 1.000 bund bolds aboats alor 6 project un peats deport 1 millard 6 mo) X €2307 (2) < x2 ≤ 180 93 € 250 - sumb alocali abor 6 projects m pot dapor valores maximo ordicito pun project JA 5120 275 400 £ € 120] 25 ≥ 240 (summe aloo at projectable medear at the minim sof toom# = \$40 mil. Euro)

2) Problema diesei

" În verma unui studiu biologic efectuat ampra animabler de la o Germa n-a stabilit ca rația silvice de brane a aastora telacie ne antivo elementel netribire:

(x1+x2+x6 > 220 (totaled minular appears being tolor "nows" or lie minin 520 mil. Ecas)

 $(3) x_{j \ge 0}$, j = 1,6 (Aumak almak on pet avec valor regative)

Ferma dispuse de furajele:

E, F2, --, Fe (F, j= Te) to le laborator efectuate) contin pe unitake de furaj F j= to eartitate a; din almental nutritor N; i= T, m. estind ca proper unitar al furaj lei F; oste F; j= Te to se determine ratio aplina vilnice a animal bor ladice so se determine componenta of contitate vecesario din ficcore furaj astilitate accosta so cartiva toade de mentele untritive indicate in macar cartitatile minimo indicate oi care so coste est mai putin)

not: 21, 22, -, 26 - canhitatea de furaj de tipul Fr. Fz, -, Fe care ur mease a fifolóxido en

063

- i) problemale substanting generale (40) in (43) se numere forme canonice a unei (4.8.6); assiful pende. de ((max) are boate restrictive din (3) de forma " &"

 (min) are boate restrictive de de forma " >"
- ii) problembe real economice me our modelel madematic associat lor rest forma canonica de cat foorte var (sour de bc). De doicei reidennel de restrictii, economice (2) our ji incuatii de lip " \ " pi " \ " dar " ei ecuatii (deci cu amul "=").
- iii) à probleme diétei nu out spécificate contidates de funcj F 15-tre disposibile, est ce ni oun ferme an dispuse de contidété velimitate. Donc motion au : fin for -, fre contité d'él (limitate) de funcj F, F, -, Fe pe care le ane forma le disposible atuni la médemul (e) mai telouie adonyate ni inquatiile.

minarel restriction overcand de la "m" la "m+x" !!

3) Probleme de transport (P.T)

Acout tip de problème ste o close particulare de (P.P.L) promote la finabel acordii capital pe lorg. Model lor de resolvare este similar ou al al (P.P.L) generale, don nu identic. Di ferența majore destre cele devie close de problème este me, melt mai more de ecuații ri bau incurofii precum ri de recunosaite care apor in (P.T).

11.2 Diverse forme (de sovere) a unei (P.P.L)

A) Forma generale a unei P.P.L

As) Forma generala voisa explicit (our forma generala a unei TR voisa sub-forma

(18) (min max) & (20, 25, -126) = 8,26 + 82 25+ --+ 8226 (33) x330 1 7= 1/8

(33) x330 1 7= 1/8

(33) x330 1 3= 1/8

(34) x300 1 3= 1/8

(35) x

i) este ferma esuale a modelalui unci (P.P.L.) conomice; se past cere sau velocrea minimo race ora maxima a funcției obniecțiu iar mothicțiile pot quea pemnele " ¿,,, »>" par "=")

ys) Lorma dine colo sanza ma pricial

 $(PPL_{2}^{m}) \begin{cases} (y_{1}(min/max) f(x) = C x \\ (y_{2}) A \times \xi B \end{cases}$ $(x_{2}) X \Rightarrow 0$

Am followit urmadowsele notation meatriciale: $A = (a_{ij})_{i=n,m} = \begin{vmatrix} a_{ii} & a_{i2} & ... & a_{ik} \\ a_{ij} & a_{im} & a_{im} & ... & a_{ik} \end{vmatrix}$ $B = \begin{pmatrix} b_{i} \\ b_{2} \end{pmatrix} ; C = (c_{i}c_{2} ... c_{k}); X = \begin{pmatrix} x_{i} \\ x_{i} \\ x_{i} \end{pmatrix}$

As) Forme general source vectorial

(18) (min max) fear 20 -- 20) = 100 2+ 0 25+-- +0 20

(3) x 30 12=11x

unde an notat ar 3,3, - 12 nestorii salonie ai netuici A, adira: A = an are --- are be iar ar 20 colonia torno ni con leborii din asstern.

iar an Po coloana tornanion le bori den asbem.

B = (001) = (011) a = 1 - 2011 EB 1 35 | 000 = (010) a = 1 - 2000 | = (010) a = 1 - 2000 |

Obsignationed sub forme matriciale our rectoriale ne agritation defining uner concepta it in demonstrarea tecremalor care fundamentos adquitmed de resoluce al (7.7.L) i) intot diauna modebal matematic al unei problème economica reale (consede este sais obtinut mub forma explicità

B) Forma standard a unei P.P.L.

Bi) Forma wandard voisse explicit (!!!)

Oos: ovice inconstic (restricte economics) der risteme linear or Coma generale (2g), pooks &. transformata entre caratie adminded/scatand o nova variabile (necuresante), numite variabile de componeure (san "écat" (Pr.) san "slack variabel." (ongel), adica:

a)
$$a_{i_1}x_{i_1} + a_{i_2}x_{i_2} + \dots + a_{i_k}x_k \le b_i \xrightarrow{+x_i^c} a_{i_1}x_{i_1} + a_{i_2}x_{i_2} + \dots + a_{i_k}x_k + x_i^c = b_i$$
 (de compandate)

b) $a_{i_1}x_{i_1} + a_{i_2}x_{i_2} + \dots + a_{i_k}x_k \ge b_i \xrightarrow{-x_i^c} a_{i_1}x_{i_1} + a_{i_2}x_{i_2} + \dots + a_{i_k}x_k + x_i^c = b_i$ (de compandate)

 $a_{i_1}x_{i_1} + a_{i_2}x_{i_2} + \dots + a_{i_k}x_k \ge b_i \xrightarrow{-x_i^c} a_{i_1}x_{i_1} + a_{i_2}x_{i_2} + \dots + a_{i_k}x_k + x_i^c = b_i$ (de compandate)

i) find autimore, or modele of demonstrate (+ det, bourse) non atilisa notatia portra noise volicinal de consocional (+ det, bourse) non atilisa notatia portra noise volicinal. de consequence: 2xx1, 2xx2, --- 12x1p, coea ce esseanne co pp.) inificie, and format generale are .K. vaidnile initiale (20, 20, -, 20) of noi are mai introdus un monde , 7 & m voright of combensors (xm, xms, -... xm my am note in sold in the

(2) (4)(PP) Cu forma generale ((2) - when case are in inscrafii) posts (: adusa la forma wandar (BET): (PP) - (B2) (Wighmy (S2) grante without go sociation) but agostance up novietage go combon

(88) x11x31--1xx1 xx11xx121-1xx >0

Forma standard explicité a una (PPL)

<u>055:</u>

ii) date tu vegemb (inited) de estricti vas terms denenge drem.

a) to to trestriction and forms de imagelie, us trebuie se admien predan in forme incuration o varioris le de compensare (desi z=w) de i m nitremel sub forme c'andord (25) vom avec in black N = K+M varioris ;

b) doce den cale " " " restrictio dein miet. (29) doce PKm ment inconstii (cestal para le " " Fiind constii) atuna met adandard (80) us avea: N= K+p variabale;

c) dace took cole "m" restidis den est (2g) sent constri, etuni el este deja in forme standor deci mu trebanie se mai adarytem variation de compensare (p=0 m K=N)

(3) $\begin{cases} x_1 + x_2 + 2x_3 \le 6 \\ (3) \begin{cases} 3x_1 - x_2 + 3x_3 \le 6 \end{cases}$ $(2s) \begin{cases} x_1 + x_2 + 2x_3 + 3x_1 = 6 \\ 3x_1 - x_2 + 3x_3 = 6 \end{cases}$ Aid $\begin{cases} p = 2 (mm) \cdot 3 \cdot m \cdot 6k \cdot consponence \\ m \in k + p = 5 \cdot 5 \cdot m \cdot bird \cdot dk \cdot consponence \end{cases}$

in) expense function direction to make accept in in forma abandant (ca in in forma generale initiale)

such to fi egelt on 0: $C_{KH} = C_{KH} = - = C_{K} = 0$, activa:

Les ordered function of $C_{KH} = C_{KH} = - = C_{K} = 0$, activa:

= fran x 52 -- 1xx) =0 = fran -3x2 = 0 xxx + 0

```
e are vasarea optima minuma
    (i) Such down aring perstra o B.P.L) < se core valores optime marine. Metode de ractione (algoritm
            Simplex) ste rivilara dar <u>me idantico</u> pt. ale done tipuri de probleme. Pontre a ne
             invada a algorituri diferiti (ac periolel de a face confutir la focare edopo de resolvare)
             non studia doar (P. 1) de nivir. Aast lucue ste posibil, decora ovice problème
             de maxim se poste reduce la o problème de minier conform relation:
              (e.1) (max) f(xx1x2) - - (xx1) = - (min) - f(xx1x2) - 1 xn) ; (1) f(x1x2) - 1x1 = x1x1x2 x + - 401x4
        Datorito relatici (6.1) (max) f= - min(f) nom omidera, intotaleanne (P.P.L) out forma
          standard de forma:
            (00) | and + and 25+ --- + and 26+ + and 20+ + -- + and 20+ -- + and 2
      Ex: Sã se aduce la forma solandard, urmatoarea (P.P.L.), soción explicit sub forma ganerale:
             ((13) (max) fran x5/25/20) = 301-05+300+3001
                 (32) colos 120 121 20
         Postar a adua (PPL) y la forma standard (PPL), trebuie ou travel. problème de marin
     idrang de minim, iar sist. de rechitii (23) sã-Raduam le forme Mondord (25) sadire:
                 (10) (min) - f(x1)x51x31x11x61x61x61x61x6)=581-x3+3x3+3x4+0.x6+0.x6+0.x6+0.x6
(30) x, 1x6 20, 20, x6 x6 x6 x2 x2 x2 20

(x, -x2 -x2+ x6 = 3

x, 4x5 + 5x2 + 3x4 = 8

5x5 + x2 + 3x4 - x5 = 2

3x1 - x3 + 5x4 - x6 = 5

x, -x5 + 5x4 - x6 = 5
                                 (x,-x2+8x2+xx+xx=6
```

B2) Forma standard societ sub forma matriciale

ar notating:
$$A = \begin{pmatrix} a_{11} & a_{22} & \cdots & a_{nk} & a_{nkn} & \cdots & a_{nk} \\ a_{21} & a_{22} & \cdots & a_{2k} & a_{2kn} & \cdots & a_{nk} \\ a_{2n} & a_{2n} & \cdots & a_{nk} & a_{nkn} & \cdots & a_{nk} \end{pmatrix}$$

$$B = \begin{pmatrix} b_{21} \\ b_{22} \\ b_{23} \\ b_{2n} \end{pmatrix}$$

Ba) Forma shouldard source undonal

(25) 18/3 = x2 P2 + ... + 22/2 = P0 = x(24+C2) = x (24+C2) = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = 20 = 20 = (011) = (011) = (011) = 20 = 20 = (011) (30) x1321-1261 (20) x1321-120

$$\beta_{i} = \begin{pmatrix} \alpha_{i1} \\ \alpha_{21} \\ \alpha_{mi} \end{pmatrix} = \begin{pmatrix} \alpha_{i(1)}\alpha_{2(1)} - \beta_{mi} \\ \alpha_{mi} \end{pmatrix} \in \mathbb{R}^{m}$$

Obs: Heavitatea introducerii formai standard people o PPL raids dis.

(consideration of set) is a boson sole his beautiful to the form general to the form general to the form of the fo 167 forance de mai 205

leavene Solutia optima a unei (PPL) out 10 forme governote (initials) we obtine also solition oplime a (P. R.L.) sub forme standard din

case se elimina variabilele de compensore

Mai jos et presentate " schema de resolvare, a unei PPL) ;

(PPL) = txi (PPL) = KRg. SIMPLEX X standard divineuro Xophina Vaplina Vaplina Vaplina