## I.I.) Balinbarea acordonatelor unui rector la solimbarea basei

Fie (1,+,.) un spatin liniar agresse an dim von if fie (B) ilB) Louis base den 0;

Fre well un vector conscione, care admite in cele dout love descompaniele:

Vom nami: (B) - prime bada basa inifata basa vedra (B') + a dava box | baza finals | baza mova

Davin são garin o Ogoduro (alatre) dintre cale dono seturi de acordanate (mg ni mg) ale acoluiani vedor "" In one about bose diferite: (B) of (B')!

Decouse B ≤ J => (B)-5.6 ph. 4 acouse \$ 15 = 1 = > (E) (E) = (5= 1/4 a.s. :

dem " sii " and coordonatele verbriller 2: EB' fato

Atuna relatible (3.3) (case expresenta legatura dentre acipario parci (B) di necpre, basei (B) ) se pot socie sub forma matriciata:

Torreno: Matrissa solimbari de basa S (= SB1B) este o matrice inversabile Dem: (m.r.a)

Pp. ca Sellu@) we ste inversabile ((XS)) (=) det 3=0 (3 ste degenerate) (=) mys < n (=) cale " " " livii (san caleane) ale mariasi S " no ant independent (=) cal patin una dintre livi se poste soie a o combinatio liviaro de a lolde (=) al putir une deira vectorii de , ietu se poste saie ce o combinație aniare de coileți vectori (= 3 8'-LD (fele decrea B'& I) (a) presuper rea fearle eté felse (=) Sete inversain le f(3)5 Ella (R)

Vom inComi expressible (descompanente) ledonibr 4,081, istra din rel. (3.3) in expression vectoralii ut din relația (32) și obficom:

(xxx) W= Pr ( 1211 11 + 1212 + ... + 1211 11 ) + B2 ( 121 11 + 122 12 + ... + 121 11 1 ) + ... + Bu ( 121 11 + 122 12 + ... + 121 11 11 ) = = (Bobs + Bo Der --- + Burgue) M+ (Bross + Bopson + Bopso

of university accordentallow universetor entres passe, du relative : (32), + (44), detiran:

(3.5) | d= b11 p1+ b21 p2+ --- + b41 p4 - Egatune (relative) divita coordonable W of WH.

pour internación matricis schimboni de bata 5 (du= Drugs + Danget --- + Dun Bu

can soire sub forma naticialà:

(35') WB = 5"WB' (=) (3.5") WB = (5") WB

Don: \$00m. -06 (3.5")}

Doonea: 151+0 600 det (5)+0 (1)(5))+0 (1)(5)) a.s: 37.(5))=(3)/-5=1, (1)

Inneltin exalitatea (3.5), la starya, an (5) " of obficer:

(3,), m= (2,), 3, m, (=) (2,), m= In, m, (=) (2,), m= m)

i) relative (formula) (35) sau(3.5) respective (3.5) so mines of formulate do solimbero a aprobnaklor uni vector la soliun barea basei, prin intermedial matrice salintarii de basta

ii) pentu a le aplica in problème prochère, trebuir son de terminan mai cità i motiona administrati de basia \$ (de hapt 5º pi(5º)"!!!)

iii) dava in los são descompanem velocii &; &(B'), is in in bata (B), procedem viavorsa, adecidencempaneam vectorii basei inidiale 4; &(B), is in fato de vestorii basei finale (B), on fi obtinut nigle relații vimilare lui (B.B) au (B.B), respective:

## Exemple:

1) Fre in spatial liniar conscare (1,+,1) basele: B= { Unas, us } in B'a { Us, vo, vs, vs} } (desi dim 1=3). Stim co:

Se core são se determine coordanable vectorulai. " in base (B).

## Dem.

Der not (m) => often coordonable lui "1", in base (B'): (1) 188 = [3,2,1]

Der not (m) => S (= SB18)= (2 1-1)

10 -12 (2) => S= (2 1 0)

1 3 1 (2) => S= (2 1 0)

1 3 -1 (2)

Conform rolation (3.5°), aven;

$$\frac{1}{m^{B}} = \frac{2}{2} \cdot m^{B_{1}} = \frac{8}{2} \cdot m^{B_{1}} = \frac{1}{2} \cdot m^{B_{2}} = \frac{1}{2} \cdot m^{B} = \frac{$$

9-9.0

Dog: duce in booked problemai am fi dat coordonabale lui, u, in book (B)(211082[4,3])

of am fi count coord. lui, u on tooke (B) (wg1=?), am fi aplicat relation (35")

day to build not calcula in (3) -!!! , aslica and fi allient:

$$\frac{1}{m^{\mathcal{O}_{i}}} = (\partial_{\underline{J}})_{\underline{J}}, m^{\mathcal{B}} = \left((\partial_{\underline{J}})_{\underline{J}} \circ \widetilde{S}\right) \left(\frac{1}{I^{\mathcal{O}_{i}}}\right) = \left(\frac{1}{3}\right)$$

$$\begin{cases} \delta u - \Delta_{12} = 2 & \text{mod-lini} \\ -\Delta_{11} + 2\Delta_{12} = 3 & \text{mod-lini} \\ \delta u - \Delta_{12} = 2 & \text{mod-lini} \\ \delta u + \Delta_{12} = 3 & \text{mod$$

b) trebuie no determinam mai intai 5" ni (5") phr. a pritea aplica formule le (8.5") ni (3.5").

De 3= 3 = (5-8) (x) Debruiron (5) cu T. E, adi à:

Lema substitution (cas particular, calle dona base Bri B' difere printern singur vator Fie B= {un, ..., Min, Min, ..., unis st of vectorii v, we I as discompanionid in B: (87) [V=8,21+ ...+ Xin 2in + 8; 21+ 8; 1) [1+ 2 -- + 8 12 24 [= ) (3.7) [3] [2] [2] = [2] -- > 8in -- > 8in ]

[14] [V=8,21+ -- + din 2in + 8; 21+ 8; 21+ 2in 2in + -- + du 2n fee (3.7) [2] [2] = [2] -- > 8in -- > din ] a) B'= { U, --, U, -1, V, Wi+1, --, 2W } < 4 (=) \$ ( +0 b) dace B' & t, alunci W= prait -+ prit piva pinini+- pour fermo = [An-pinpa] unde noile coordonate "pi, izin ale lui ut sunt dak de reletible: (81= 41 - 41 81 Wind of in! 18/10 - pivotal banefallen. المنا طنها 5,11 grobs: Demarkle Lin eminful Pin = din - 418,41 lama subst. gream si U BI Lormale a (3.8) de schir. Bucdn - di En - bose a coordonatelor mu Win Bus trebeuge memorate dans Win Bith sunt pure out forme Derifice in in a condidi B' sole (sou nu) L.I. Fie occloris a; ER, i= III. Impuni Condida: (1) a; v; + a; v; + a; v + a; v; + - ia v; -a. condida: (1) a, v,+ - a, v, v, + a, + + a, + + a, v,+ + - + a, v, = 0. Inbaind expression ari " " " gin (3.7)" in relation (1) optimen: 0, 21+ --- + 0, 1/41+ 0, (8, 21+ --+ 8;-, 21-1+8; 11+8; 11, 21+1+ 8, 24) + 0; 11/41+ --+ 0, 24 = 0, (=) (a) (a, +a; 8; /2,+--+ (a; +a; 8; ) 2; + + a; 8; 2; + (a; +a; 8; 1) 22+ + -+ (au +a; 8u) un = 0 a } det decourace BEV=> vectorii x1, -- , 21, - , 24, -Li a1+0; 8,=0 (i)  $\underline{g}(\underline{+0} \Rightarrow \alpha_i = 0 \xrightarrow{(3)} \alpha_i z - z \alpha_{i+1} = \alpha_{i+2} = \alpha_{i+2} \Rightarrow b_i - L.1$ 0:1+0:8770 0=18;0 - 0 = 18;0 = 0 o so trufts in iset, ser in some if stood C= N8;B+NO

b) Eulocian in relative: w=p(U+++pi)Ui-1+pi V+pin Vii+++ pnun I ar expresse din (3.7), in vom obline:

00= 30114--18111111 + Bilgint - + girnit 4. Nit girnit +-+ 8000) + Birnit +-- 1 BNNN (=)

(4) m= (21-4) 1/2 + --+ ( pi-1+pik; ) xi-1+ pi& xi+ + (pin+pi&in) xin+--+ (pinpi & ) xu Din (8.7) 2 m; (4), conform unicide hi wordonatelor in bara B, oblinen:

Ex:

Fie B= { N1, U2, U3 } & \$ fu=[1,-1,2]+ in vectorii ( 1= 14, -12+243 & WB=[3,1,6]}

Deservinati coordonade le lui, vo, in basele:

al B'= { W1, 4, 234 c) B"= } 47 22 203 } P) B = { u, uz, & }

social detele moble mei red forme tobelore. Den: Aplican lana salod

-	3	Committee of the Commit
w	0	
3	1	aty
+4	1-1	1(41/-1/27
D	2,	4
4	0	*
2	0	
T		
Wal	121-	-V+2N3
F.	esecut.	
	3 1 0 4 2 2 3 2 2	

WB1 = [4,-1,2]

B	w	4	
U	3	A	* t
U2	1	-1	44
-las	0	2	1/2/1/2/(2)
4,	3	0	
uz	1	0	
4	0	1	
Ų	U	ł	
W	-34	,+U;	L+0v
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W.	7 - 0-	3,1	Ta.

B	w	H
-U	3	回行格
uz	A	-1 41
Us	0	200
1	3	1
Uz	4	0
U3	-6	0
$\sim$	1	
WE	214	+ 4212 - 6212

WBm=[3,4,-6]

i) Lema substituțiai (L.S.) poate f. aplicate iterativ a.i. putem a fla coordenatele unui voctor (sau a mai multora) rut-o nove bare B care difere de bara inițiale pun 2,3,-.. sau toți voctorii

ii) cand nouse borse B' difere prin to l' voctorii de veches sorte B, pentre a putes aplica L.S. trebuie são stim matricea eduimberii de baro: (asse eum vode fi in tabebul de mai jos); evident co in acest car art. mult mai nimplu no aplicam formulet de adimbere a coord. la solimbere a borei (18 = 5, 18 1 sau 18 1= (5) 18)

B w 1 1 1 1 1 20 --- Don sunt componendale matrice ST (!!!)

Obs: pentru a se evide calculul matricci S (vecesa Te en primul dabul dint. S) se va lua intetel -una ca baza initiale = bara camu

and as posto impare = post among

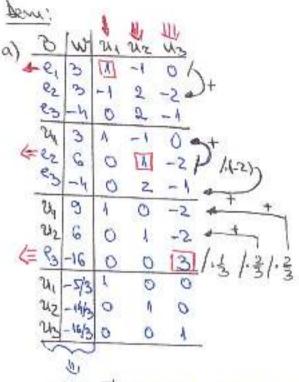
iii) Cema subst. poete fi foloside ni atunai cand dorim ne aftem coord.
uni vector Titr-o baza Vom considere an acest caz:

Bara initialie: Be + bara cononice

Bara finalie: B -> bara in care se cur coord. vect.

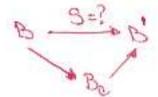
Ex: Fie (B) ( & = (1,-1,0) = 3 | W3 = (-1,2,2) = (B) ( W3 = (0,-2,-1) = (B)

Se are: (a) no= (3,3,4) => ==? (b) 2B=[211,1]=> ==?



W=-5/301-14/302-16/303(=) WB=[-5/3-14/3-16]

iv) atuna and down sã after its amoscand its (sau invers), dar nu stim matricea 3, vom folosi intot de anna ca bata initiali baza caronica Bc.



B S=? B' adire: UB ??? NB'

Bo NB = M

in alfa on man band courts ignification is a law de la laifini bulselot (ii coord and rector W= (dide, - , du) = 12" in both B= {u, ue, - , un} 41 rectorii si icim avand componentele: [si=(a11012)-1011) - na fi 65 95 018 055 --- 0" (ST = (0" 0x5) -- 10")

61 × 10 11 051 --- 10 1

51 × 10 11 051 --- 10 1

51 × 10 11 051 --- 10 1

51 × 10 11 051 --- 10 11

51 × 10 11 051 --- 10 11

endnom azn -- ann