SEMINAR I TRANSFORMARI ELEMENTARE (T.E.) - APLICATIO

Def: Fie matricea NEMMIN, Munim transformane elementaria (t.e.) una dintre urmatoarele aporatri efectuate asupra liviilor accoleia:

(Ti) Inmultirea (elementelor) unei livii en un scalar neuel (40);

wtația AnA' represente foptul ce matricea A' a foot oblinate den matricea Aprien t.e. (spa--nem ce matricile Ani A' sund <u>eclinaluite</u> depolu al 1.e)

Ex:

a)
$$\lambda = \begin{pmatrix} 2 & 3 - 1 \\ 1 & 0 & 2 \\ 2 & -2 & 0 \end{pmatrix}$$
 $\sim \begin{pmatrix} 6 & 9 - 9 \\ 1 & 0 & 2 \\ 2 & -2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$ $\sim \begin{pmatrix} 6 & 9 - 3 \\ 1 & 0 & 2 \\ 2 & 2 & 0 \end{pmatrix}$

b)
$$B = \begin{pmatrix} 1 & 2 \\ 0 & 1 \\ -3 & 5 \end{pmatrix} / \left(\frac{1}{2}\right) \sim \begin{pmatrix} 1 & 2 \\ 0 & -1/2 \\ -3 & 5 \end{pmatrix} / \left(-2\right) \sim \begin{pmatrix} 1 & 2 \\ 0 & -1/2 \\ 6 & -10 \end{pmatrix}$$

(2) Turnelfirea (abmarkar) unci Pini ar un evalar neval (x40) je admarea ci la o este livi

₩:

Obs: pubu aplica (12) simultan asupra mai multor livii:

(18) Schimbara (elementeter) a done livii intre ele:

Li (011 a12----am)

Li ais aiz----ain

Ex A = (1 2 3) 1 N (1 2 3 4) 1 N (0 -5 4) 1 2 2 -1 (1 2 3) 2 2 2 -1 (1 2 2 2)

(1) In toak aplication do pe paranoul acostus curs services, vom folosi t.e. pontu a transforma una san mai mulk coloane a unei matrice corecore, in abanel nationi unitate.

 $\begin{array}{lll}
\underline{Cbg} & \underline{T}_{8} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & * \text{matrices unitate de order } & \underbrace{T_{1} \begin{pmatrix} 1 & 0 & --- & 0 \\ 0 & 1 \end{pmatrix}}_{L_{8}} & * & --- & 0 \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & &$

Obs: Reschare a nistemator de ec. lin. cu e sau e reassosante (ni accelor un de scurtii à mist. patratia de tip (na mor) ou metoda climinari, inscruna sã in basin sistemal initial an mai mor met. limar, ou accelor solutii ou sist. initial (sibus colimbrate) dar mai

F: (1) { 21, +222 = 5 1.2] (=)

(=) { x1 + 2x5 = 2 /(4) / 5 (=)

(=) { \(\alpha\) = 25 \(\alpha\) = -3 \(\alpha\) = \(\alpha\) A=(2 2 5)1.27 ~

~ (0 ED 0)10015 ~

~ (0 0 1-9) => { x1=23 + solutionie (nich name)

b) $\begin{cases} x_1 + x_2 - 2x_3 = 3 & 1/c-0 \\ -x_1 - 2x_2 + 3x_3 = -1 & + \\ x_1 & -x_3 = 6 \end{cases}$ (a)

(e) $\begin{cases} -x^5 + x^2 = 3 \\ -x^5 + x^2 = 5 \end{cases} = \begin{cases} -x^5 + x^2 = 3 \\ x^1 + x^5 - 5x^2 = 3 \end{cases} = \begin{cases} -x^5 + x^2 = 3 \\ x = 1 \end{cases}$

(e) { = 30 = 5 = 5 = 5 = 601. luin

(0,1) se inmulfate o ecuação (sou mai multe) ou un ocalor remil (+0);

(Or) se inmelfagte o amatic on in scalar rend in se admir la o alle constie;

(03) se solimbé intre ele dons carati;

Prin ante operatii, soluția (ile) sist. liu. nu se modifice. Oblinem alte sistem care sunt educabate as rist initial (on author solutio) dar care on a forma mai muglie de resolvat.

Asa am no quoto deserva in din example de mai sus all tra operatio efect - ate acupia ec. Que dis viden munt de fapt ale trai transf. elen. (Ti) to) save re efectuease anyone matriai extince A atazak sistemului

Obs: pentre a rifelige model de lucre on t.e. vou anota 4 aplicații ale acestora (drai dilutre ele le dif ristatil la licu, dar afi fobrit o alte motode de resolure, a descrimenti)

Aplication ale T.E.

1) Determinarea rangului ansi matria; persona

21 Deferminance imorsee unei matrici (pa teatra);

31 Roso Granca nist. de consti Ginione (moboda lui Garros!!)

41 Determinarea soluții Por de bază ale unui vist. Diviar (compatital nedeterminat)

1) Determinarea rangului anei matrice cut e

Det Fre matricea A = Mm, (R) Humin rangul matricei A (" rang A = (a) numarul natural rem ou proprietatile:

(i) existe an minor de ordin " " (1/2: Mr) al matrici A, noul (40) 4(3) Mr 40)

(a) pope minorii que ordin underior gri "L" vant mari (=0) (A) ME=0 (A) TE > QE)

a) (4) LE Mum (12) det 0 5 CA 5 min fmin }

b) 7,=0 (=> A= (0 ... 0) =0 of 0 of 0 on triang orde

c) w. minoribe de ordie sup. bui, in each eyel ou: = Cm . Cu + Cm . Cu - ---

Ex Fine to Ellerotte) cu Tr=4. Cf. def. trebesie in anotein on existe un Mid O pi tot minori de ord. 5 mi G sunt serro, adice: (m. min. de ord 5 este C. C. = 61272=1572 for Mo ate: (6. Co = 1x210 = 210

desi un total de 1722 de misson de ord. 5 m 6!!!

Obs: nr. Minoralor de ordinal voi" ste egal en: Com. Con

Ex: in easel exemplului precedent aven de calculat door cui 1582 minori de ord. 5 m n'

Te: rang A = ~ (=> Si)(I)Mr #0

(Hote minori de ord. "+1" objeint prin fordarga minoralece!

de ord. ~ nevel, sout well!)

Obs: wr. Man ste equal on: (m-17-(n-1)

Ex to cook preparated trebasic no colarteur: (m-17/11-1) = (6-4)(6-4) = 2.6=12 union de ord 5 objection prac bordores minorable de ord. 4 mul (vi me 1.512!!)

Obs (!!!) Rangeel unei matrice no spure cade livii (respectiv colo ane) sent inde-pendente dir totalel de livii (colorne) ale matricei, adrice me se pot sonce
ca ni combinatii liviare de colo labe livii (colorne).

<u>009</u>:

is in cools with live do co., ranged matriced to (1) to cope with live do co., ranged matriced to (1) to cook deposed de a coste (1000m re create coste divise constituent independent (principale) of cook de posed de a coste (1000m de constituent) de constituent porte de constituent de const

ca ji combinatii (Briana) de acestoa.

(ii) pritra a avita calculele lungi ala rangulai fabried mison (determinanti) ne basar pe urmatoara travensa:

B: Transformatile alementore applicate unes matrici, mei modifice rangel. Adica state:

(I.A) ANB = T_= TB som mai general: (I.A) +, N+2N ... N+2 => T_= T_2 - ... - The

<u> 068:</u>

" pertue a foliosi To, va trebesie sã adreau mátrica vantre la o forma (mai nint pertur care varquel mátricai são me trebuiancã são fie calarelat (ou Te) ci são valla discort don expression acestria. La esta formão o vom mumi forma Gaurs-Fordas

<u>000-8:</u>

i) un car particular, ste forma Gouss-Jordan reduce (canonice) (# ARJ), unde coloanel matricii unitate and primale (ocupo primale « parifii) Jadise a ne expuria:

ii) o matrice Aculary, carrang to the or unite forma Gaus-Jordan, ai poal avea maxim: Cu for 1 (puter alega or, div cela, ny coloane ale matricei pentur a a transforma (ca te) a coloane le matricei unitati a Cu moduni)

iii) este evident et eff. rangului moi motuice (sau Is) es range & = = rang he] =

: more ET 20, southe; Taline is intered to enough so (nam) on =

Er: Determinate roughl armatearelor matrice, tolorind to.

Dan: evident 0 & 1 x & min (3,3) => 1 & 1 x & 2 Admos u A le Morma Games - Jordan, Low.

Sau :

Obs: Evident, der forma naturai B -> 1563

Dem:

Sau

(Piviare) de alle lace lace!

9.2.0