

## CSci 4511W: Intro To AI

### Homework 2

[Google Colab](#)

1. The A\* algorithm sorts the nodes in the frontier by increasing value of  $f$ . When multiple nodes have the same value, the order in which they are sorted is arbitrary. Could you suggest a better way of sorting the nodes that have the same value? Explain your reasoning.

A better way of sorting the nodes that have the same value would be to prioritize nodes with a lower  $g(n)$  which is the cost from the start node to  $n$ . This is because a lower  $g$ -value means the node has reached its position with less cost, which may lead to a more optimal path. Additionally, we can use the heuristic value to prioritize the nodes (prioritize the nodes with lower  $h$ -value), as a lower  $h$ -value signifies that the node is estimated to be closer to the goal, reducing the number of nodes explored.

2. You want to reduce the memory used by A\*. You come up with the following idea: you keep in the queue only the  $N$  best nodes (i.e, the nodes with lower costs), for some positive value of  $N$ . When the queue is full and a new node has to be stored, the worst node is deleted from the queue and removed from consideration.

- a. If you use an admissible heuristic, will the modified algorithm find the optimal solution? Explain why (or why not). Are there any additional constraints? [hint: consider what can happen depending on the value of  $N$ ].

No, with an admissible heuristic, the modified algorithm may not find the optimal solution. A\* search algorithm guarantees optimality because it explores all possible optimal paths. If we remove nodes, we risk discarding a necessary step in the optimal path, especially if the  $N$  value is too small.

- b. If you use a perfect heuristic, i.e. for all  $n$   $h(n)=h^*(n)$  , where  $h^*(n)$  is the cost of the optimal path from  $n$  to goal, will the modified algorithm find the optimal solution?

Yes, with a perfect heuristic, the modified algorithm will find the optimal solution if  $h(n)=h^*(n)$ , because A\* will expand the best possible path without backtracking. Since we effectively implement greedy best-first search with guaranteed correctness, removing worse nodes does not impact the result.

3. Answer the following questions briefly but precisely:

- a. Why the cost of an optimal solution to a relaxed problem is an admissible heuristic for the original problem?

A relaxed problem is one where constraints are removed, making it easier than the original problem. Since the cost of an optimal solution to a relaxed problem is

always less than or equal to the cost of the optimal solution to the original problem, it never overestimates the true cost, making it admissible.

- b. Does the fact that A\* is "optimally efficient" mean that A\* will never expand more nodes than any other algorithm? Explain precisely.**

No, A\* is optimally efficient in the sense that no other algorithm using the same heuristic function will expand fewer nodes while guaranteeing optimality.

However, another algorithm using a better heuristic (closer to the true cost) could expand fewer nodes.

- c. Why is it that any node in the frontier with  $f(n) < f^*(n)$  (the cost of the optimal solution path) will eventually be selected for expansion by A\*?**

A\* expands nodes in increasing order of  $f(n)$ . If a node has  $f(n) < f^*(n)$ , it means the node has a lower estimated cost than the optimal path. Since A\* explored nodes with the lowest  $f$ -values first, it must eventually expand that node before reaching the goal.

**4. This question is on genetic algorithms.**

- a. What is the role of the fitness function used in genetic algorithms?**

The fitness function evaluates how good a candidate solution is. It helps guide evolution by selecting individuals that perform better according to the problem's objective.

- b. Could genetic algorithms be used without a fitness function? Why or why not?**

No. Without a fitness function, there would be no way to determine which individuals are better suited for survival and reproduction. The algorithm would evolve randomly without direction, making it ineffective.

- c. What happens if the crossover point is not the same for all the individuals of the population? Explain.**

If crossover points vary, it increases the genetic diversity, potentially leading to a more effective search of the solution space. However, it can also introduce randomness that disrupts beneficial genetic structures, making convergence to an optimal solution slower or less predictable.

Note: Used Grammarly for sentence structure, and grammar purposes.