

- (1) (1.0 pt.) Consider a dataset of 100 examples with exactly 40% noisy examples. What is the probability of having more than half the noisy examples, in a sample of 50 drawn uniformly from the dataset.

Hint 1: you need to compute probability of having more than 25 noisy examples in the drawn sample of size 50

Hint 2: You will be needed to sum up Binomial trials, where each example drawn for the sample can be either from the noisy examples or not

Hint 3: You can compute it by hand, but it could be faster computationally

1- 0.06

2- 0.15

3- 0.10

- (2) (0.5 pt.) Based on PAC theory for the hypothesis class of axis parallel rectangles, the lower bound of the sample size ($T(\epsilon, \delta) = 4/\epsilon \log 4/\delta$) has a stronger dependence on:

1- error (ϵ)

2- confidence level ($1 - \delta$)

3- both the same effect

- (3) (0.5 pt.) Which option is not considered as an assumption in PAC theory:

1- the data are sample from a uniform distribution

2- the underlying distribution is fixed but unknown

3- the examples should be independently drawn from an identical distribution

- (4) (0.5 pt.) The expected generalization error with respect to generalization error bound, usually has:

1- higher value

2- lower value

3- the same value

- (5) (1.0 pt.) Based on the generalization bound relying on the size of the hypothesis class using boolean conjunctions, and the following information, what is the lower bound on the number of examples:

(Formula: $m \geq \frac{1}{\epsilon} (\log(|\mathcal{H}|) + \log(\frac{1}{\delta}))$)

Dataset : 3 binary features and one binary label

error bound : 10%

confidence level : 95% ($\delta = 5\%$)

1- 86

2- 157

3- 63

- (6) (1.0 pt.) Based on the generalization bound for true error, using the empirical error : $R(h) \leq \hat{R}(h) + \sqrt{\frac{\log \frac{2}{\delta}}{2m}}$, if we change δ , from 0.1 to 0.2, how many example will be needed to keep the same bound as before.

1- 0.5m

2- 1.6m

3- 0.8m

(7) (0.5 pt.) Which option is not correct based on the Bayes error

- 1- there might be a learner with a lower error than the Bayes error
- 2- Bayes error can be reduced by reducing the overlap between class distributions in the input space
- 3- Bayes error gives the expected noise level

(8) (2.0 pt.) What is the vector of coefficients for linear regression model, for the given inputs (x) and outputs (y). [computational work]

x = [0, 1, 3, 4, 6, 8, 9]

y = [2, 5, 7, 6, 8, 14, 12]

1- [2.70 1.13]

2- [2.01 1.56]

3- [1.59 1.96]

(9) (1.5 pt.) For the above information, which option is the result of $\frac{\text{covariance}(x,y)}{\text{variance}(x)}$. [computational work]

covariance: $\text{cov}_{x,y} = \frac{\sum_{i=1}^N (x_i - \bar{x})(y_i - \bar{y})}{N}$

variance: $\text{var}_x = \frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N}$

1- 1.59

2- 2.01

3- 1.13

(10) (1.5 pt.) What is the predicted outputs for input test vector [2,7], based on the built LR model in question

8. [computational work]

1- [6.13, 13.72]

2- [4.97, 10.62]

3- [5.01, 11.25]