

- (1) (1.0 pt.) In the hard-margin SVM we have the constraints  $y_i \mathbf{w}^T \mathbf{x}_i \geq 1$  for all  $i = 1, \dots, m$ . For a pair,  $(y, \mathbf{x})$ , of a new sample example we have  $y_i \mathbf{w}^T \mathbf{x}_i < 1$  but  $y_i \mathbf{w}^T \mathbf{x}_i > 0$ . What does it mean?
- 1- This example is wrongly classified.
  - 2- This example is classified correctly but it is within the margin.
  3. We can not decide on which class contains this example.
- (2) (1.0 pt.) In the soft-margin SVM we have the constraints  $y_i \mathbf{w}^T \mathbf{x}_i \geq 1 - \xi_i$  for all  $i = 1, \dots, m$ . If a pair,  $(y, \mathbf{x})$ , of a new sample example is classified correctly what could be the value of the corresponding slack variable  $\xi$ ?
- 1-  $0 \leq \xi < 1$
  - 2-  $\xi = 0$
  3.  $\xi < 0$
- (3) (3.0 pt.) What happens if all labels are positive in an SVM problem? It is called as one-class classification problem. What does the SVM do in this case?
- Hint: Think about what the constraints could force in this case.
- 1- It separates all the examples from the origin.
  - 2- The result has no any meaning.
  3. All slacks will be 0.
- (4) (5.0 pt.)
- Let 6 points be given in the plane,  $X = \{(0, 1), (2, 1), (2, -1), (0, -1), (-2, -1), (-2, 1)\}$ , and the corresponding labels in the same order  $y = \{1, 1, 1, -1, -1, -1\}$ . Compute  $\mathbf{w}$  by the algorithm given by Slide 20 of Lecture 7 by taking the examples in the given fix order instead of randomly drawing them. Let  $\lambda = 1$ , and the learning speed  $\eta = 0.1$ . Which of these coordinates can give the solution for  $\mathbf{w}$ ? Round the numbers up to 2 decimals, and take the closest one.
- 1- (0.54, -0.07)
  2. (0.66, 0.12)
  - 3- (-0.66, -0.12)