

Processes-1

A Formal View

Processes
Flow Graphs
Determinancy

Definitions

- The notion of a **sequential process** helps to cope with structuring.
- It captures the notion of:
 - Non-determinism
 - Parallel activities
- A process consists of:
 - **Program** (the text segment)
 - **Data** (the data segment)
 - **A Thread of Execution** (i.e., runtime information such as program counter and stack)

Informally, a **sequential process** or **task** is the activity resulting from the execution of a program by a sequential CPU

In general: A *process* is a *program whose execution has started and not yet terminated!*

A simplified view....

- A process may be in any one of several states:
 - **Running** → the process is using the processor to execute an instruction.
 - **Ready** → the process is executable but other processes are executing and all CPUs are in use.
 - **Blocked** → the process awaits an event to occur:
 - Resource availability
 - Messages
 - Signals
- Concurrent processes are individually scheduled to use the CPU.
- Concurrent processing results from multiple instantiations (creation) of a set of processes
$$P = \{p_1, p_2, p_3 \dots p_n\}$$
- Each process p_i may execute a different program!

A System of Processes

Let $P = \{p_1 \dots p_n\}$ a set of processes in the system.

We define the following:

- $D(p_i)$ is the domain of p_i
- $R(p_i)$ is the range of p_i

We can view process p_i as a function $p_i = D(p_i) \rightarrow R(p_i)$ that maps memory to memory.

Given two processes, p_i and p_j , we must consider the possibility of interference.

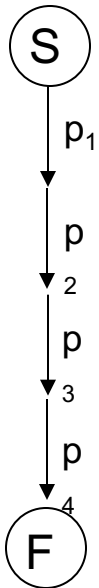
i.e., the order of execution of p_i and p_j may matter!

We can prescribe the execution order of p_i and p_j by a precedence relation " \rightarrow ".

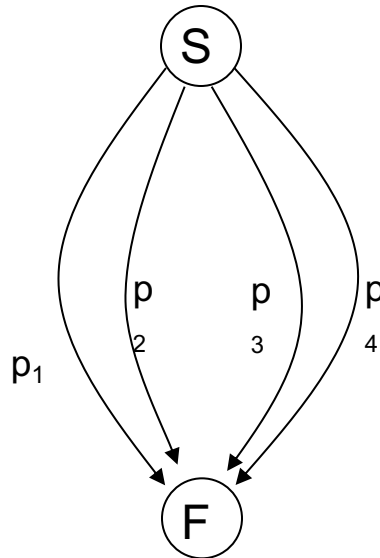
$\rightarrow = \{(p_i, p_j) : p_i \text{ must complete before the start of } p_j\}$

Process Flow Graph

The precedence constraints among a set of processes can be visualized by a **process flow graph**.



$S(p_1, p_2, p_3, p_4)$



$P(p_1, p_2, p_3, p_4)$

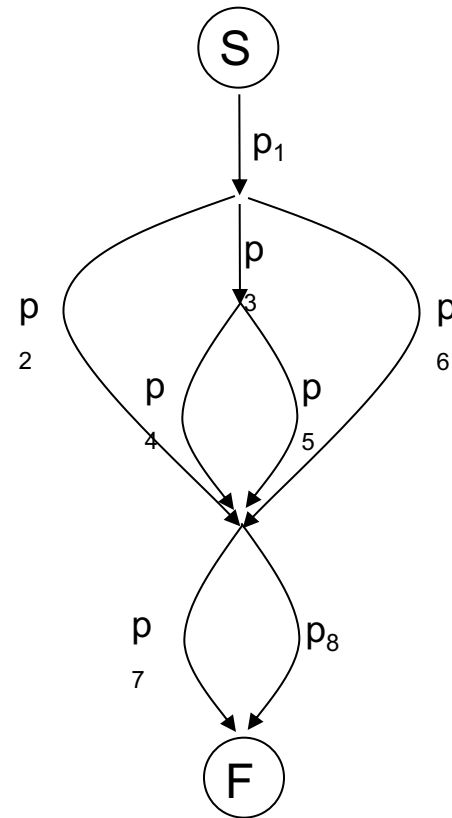
- S and F denote the start and finish of the flow graph, respectively.
- Every PFG is a directed acyclic graph (DAG) [why?]
- $S(p_1, p_2, \dots, p_n)$ denotes the **sequential** execution of processes.
- $P(p_1, p_2, \dots, p_n)$ denotes the **parallel** execution of processes.

...more flow graph

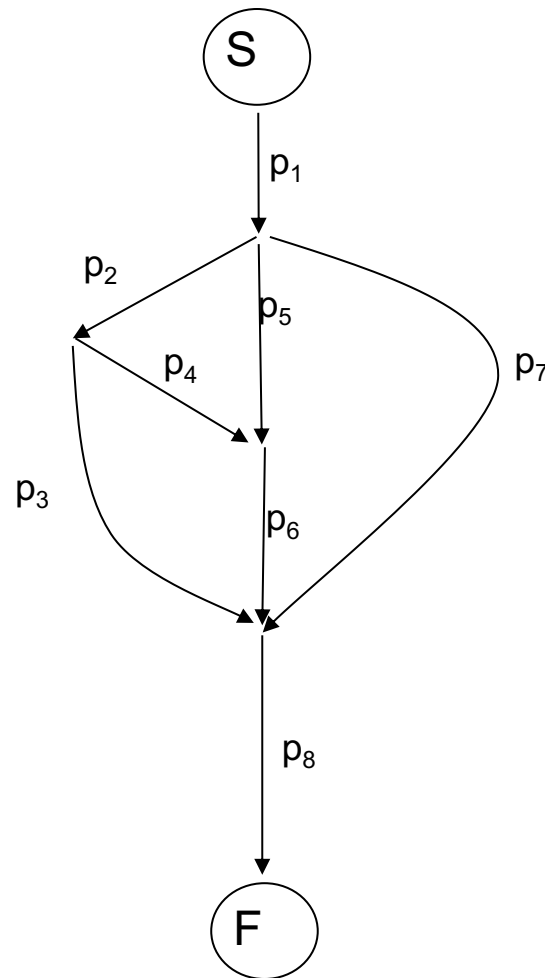
A process flow graph is **properly nested** if it can be described by the functions S and P and only function composition.

Example:

$S(p_1, P(p_2, S(p_3, P(p_4, p_5)), p_6), P(p_7, p_8))$



...general precedence..

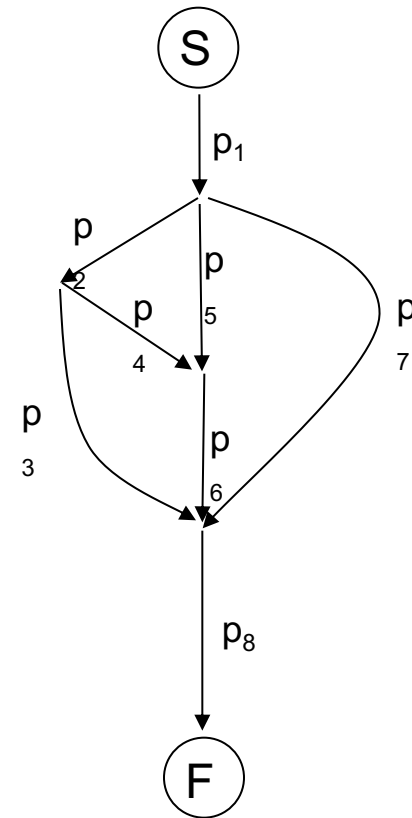


...general precedence..

Note that not all flow graphs are properly nested.

i.e., the precedence relation may not be expressible though *S* and *P* operations in conjunction with function composition.

Nevertheless, it is still possible to express the process precedence by using *fork()* and *join()* operations. (see example on page 49)



Why is this not properly nested ?

Determinancy

Recall the **precedence relation**:

$\rightarrow = \{(p_i, p_j) : p_i \text{ must complete before the start of } p_j\}$

Determinancy: if all executions allowed under " \rightarrow " relation result in the same values for all memory cells, then the system is said to be **determinate**.

Example (non-determinate):

$P_1: C(M_1)+1 \rightarrow M_2 ; C(M_2)-1 \rightarrow M_3$ (concurrent)

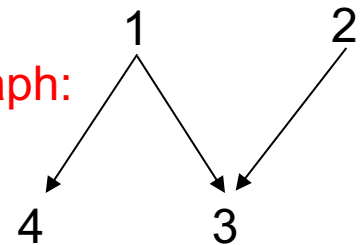
$P_2: 2 * C(M_2) \rightarrow M_4$

$P_3: C(M_3)+C(M_4) \rightarrow M_5$

$P_4: C(M_2)+1 \rightarrow M_6$

$\rightarrow = \{ (1,3), (2,3), (1,4) \}$

Precedence Graph:



p_1 and p_2 are **independent** since (p_1, p_2) is not in \rightarrow

Example...

Example (non-determinate):

Initialize: $0 \rightarrow M_1..M_6$

P_1 : $C(M_1)+1 \rightarrow M_2$; $C(M_2)-1 \rightarrow M_3$ (concurrent)

P_2 : $2 * C(M_2) \rightarrow M_4$

P_3 : $C(M_3)+C(M_4) \rightarrow M_5$

P_4 : $C(M_2)+1 \rightarrow M_6$

Conflict

p_1 and p_2 conflict if:

$(D(p_1) \cap R(p_2)) \cup$

$(D(p_2) \cap R(p_1)) \cup$

$(R(p_1) \cap R(p_2)) \neq \emptyset$

| | M_1 | M_2 | M_3 | M_4 | M_5 | M_6 |
|--------------------------|-------|-------|-------|-------|-------|-------|
| if $p_1 \rightarrow p_2$ | 0 | 1 | -1 | 2 | 1 | 2 |
| if $p_2 \rightarrow p_1$ | 0 | 1 | -1 | 0 | -1 | 2 |

...more determinancy

In summary: A set of processes is **determinate**, if, given the same input, the **same results** are produced regardless of the relative **speeds** of executions of the processes or the **legal overlaps** in execution.

However, determinancy is not a particularly useful property as it is difficult to determine whether a large system of processes is indeed determinate.

Recall that a process can be viewed as a function:

$$f_p = D(p_i) \rightarrow R(p_i)$$

Supplying f_p is referred to as giving an **interpretation**.



This requires the use of a stronger condition on a system of processes:
mutual non-interference

mutual non-interference

Two processes p_i and p_j are **mutually non-interfering** if:

- \rightarrow^* means ordered directly or indirectly by \rightarrow

$P_i \rightarrow^* p_j$ or $P_j \rightarrow^* p_i$ or

$(D(p_i) \cap R(p_j)) \cup$

$(D(p_j) \cap R(p_i)) \cup$

$(R(p_i) \cap R(p_j)) = \emptyset$

These conditions are known as
Bernstein Conditions!

A system of processes is mutually non-interfering if any two processes meet the above conditions!

Important Theorems

Theorem 1:

A mutually non-interfering
(MNI) system of processes is
derminate (DET)

$MNI \rightarrow DET$

However, the converse is not
true: $DET \not\rightarrow MNI$

Theorem 2:

Consider a system of processes in which,
for each process p_i , $D(p_i)$ and $R(p_i)$ are
given but the interpretation f_p is left
unspecified. If the system is
derminate for all interpretations, then
all processes are MNI.

PROOF IT !!!

(I mean you in the back row.....)

Maximally Parallel Systems (MPS)

A maximally parallel system of processes is a DET system in which the removal of any (p_i, p_j) from \rightarrow would cause p_i and p_j to interfere.

We need to define the transitive closure of \rightarrow :

$$\text{cl}(\rightarrow) = (\rightarrow \cup \{(p_i, p_k) \mid (p_i, p_j) \& (p_j, p_k) \text{ forall } p_i, p_j, p_k \in \rightarrow\})^*$$

Example (non max. parallel):

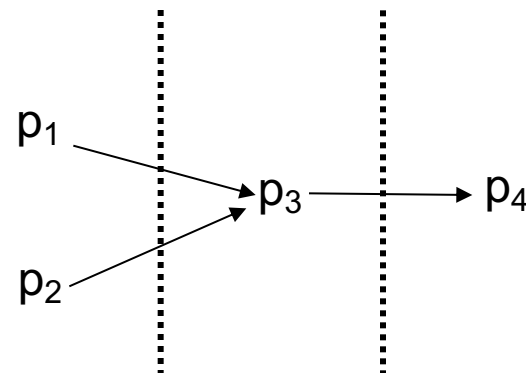
$p_1: M_1 \rightarrow M_2$

$p_2: M_1 \rightarrow M_3$

$p_3: M_2, M_3 \rightarrow M_4$

$p_4: M_2, M_3 \rightarrow M_5$

$$\rightarrow = \{(1,3), (2,3), (3,4)\}$$



Constructing an MPS

Theorem 3:

Given a DET system of processes with precedence relation \rightarrow , construct another system with the same processes and **new** precedence relation \rightarrow' defined by:

$$\rightarrow' = \{(p_i, p_j) \in \text{cl}(\rightarrow) \mid \underbrace{p_i, p_j}_{\text{conflict}}\}$$

From Bernstein Conditions

Note: \rightarrow' is unique

In the example:

$$\rightarrow = \{(1,3), (2,3), (3,4)\}$$

$$\rightarrow' = \{(1,3), (1,4), (2,3), (2,4), \cancel{(3,4)}\}$$

