Example 4

$$\sum_{n=0}^{\infty} n! \, x^n = 1 + x + 2! \, x^2 + \ldots$$