Assessed coursework: Integrating R and C++

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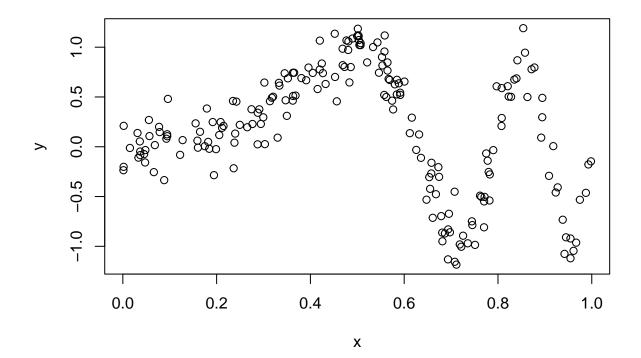
Adaptive kernel regression smoothing

We will consider data generated from the model

$$y_i = \sin(\alpha \pi x^3) + z_i$$

where $z_i \sim N(0, \sigma^2), i \in \{1, ..., n\}.$

```
set.seed(998)
# n = 200
nobs <- 200
x <- runif(nobs)
# alpha = 4, sigma = 0.2
y <- sin(4*pi*x^3) + rnorm(nobs, 0, 0.2)
plot(x, y)</pre>
```



We want to model this data using a kernel regression smoother (KRS) by estimating $\mu(x) = \mathbb{E}(y|x)$. The KRS estimator is given by

 $\hat{\mu}(x) = \frac{\sum_{i=1}^{n} \kappa_{\lambda}(x, x_i) y_i}{\sum_{i=1}^{n} \kappa_{\lambda}(x, x_i)}$

where κ is a kernel function with bandwidth $\lambda > 0$. The following R function uses the Gaussian kernel function with variance λ^2 :

```
meanKRS <- function(y, x, x0, lam){

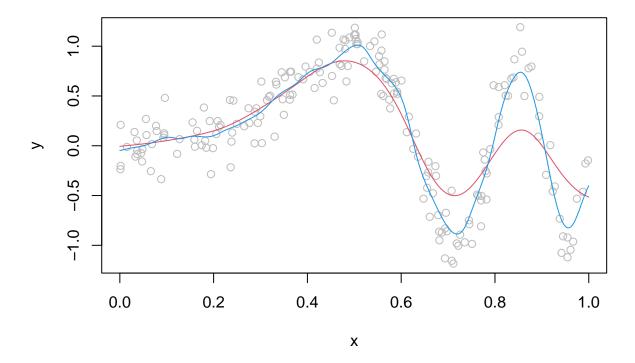
n <- length(x)
n0 <- length(x0)

out <- numeric(n0)
for(ii in 1:n0){
  out[ii] <- sum( dnorm(x, x0[ii], lam) * y ) / sum( dnorm(x, x0[ii], lam) )
}

return( out )
}</pre>
```

We can compare the performance of the KRS estimator with different bandwidths:

```
xseq <- seq(0, 1, length.out = 1000)
muSmoothLarge <- meanKRS(y = y, x = x, x0 = xseq, lam = 0.06)
muSmoothSmall <- meanKRS(y = y, x = x, x0 = xseq, lam = 0.02)
plot(x, y, col = "grey")
lines(xseq, muSmoothLarge, col = 2)
lines(xseq, muSmoothSmall, col = 4)</pre>
```



Q1a

We want to write a C++ version of the meanKRS function. The function is as follows:

```
#include <R.h>
#include <Rinternals.h>
#include <Rmath.h>

SEXP meanKRS_C(SEXP y_vec, SEXP x_vec, SEXP x0_vec, SEXP lambda_param)
{
   int n = length(x_vec);
   int n0 = length(x0_vec);
   SEXP out = PROTECT(allocVector(REALSXP, n0));

   double *y = REAL(coerceVector(y_vec, REALSXP));
   double *x = REAL(coerceVector(x_vec, REALSXP));
   double *x0 = REAL(coerceVector(x0_vec, REALSXP));
   double lambda = REAL(lambda_param)[0];

for (int i = 0; i < n0; i++)
{
   double sum_dens_norm_y = 0;
   double sum_dens_norm = 0;
}</pre>
```

```
for (int j = 0; j < n; j++)
{
    double dens_norm = dnorm(x[j], x0[i], lambda, 0);
    sum_dens_norm_y += dens_norm * y[j];
    sum_dens_norm += dens_norm;
}

REAL(out)[i] = sum_dens_norm_y / sum_dens_norm;
}

UNPROTECT(1);
return out;
}</pre>
```

We can compile the code and then load the function as follows:

```
# Compile the code
system(pasteO("R CMD SHLIB ", here("portfolios/02_interfacing_r_with_c++/meanKRS_C.c")))
# Load the binary code
dyn.load(here("portfolios/02_interfacing_r_with_c++/meanKRS_C.so"))
# Check if the function is loaded
is.loaded("meanKRS_C")
```

[1] TRUE

Next, we can call it using .Call and compare the results with the R function:

[1] TRUE

```
# Compare computing time
krs_R \leftarrow function() meanKRS(y = y, x = x, x0 = xseq, lam = 0.06)
krs_C \leftarrow function() .Call("meanKRS_C", y = y, x = x, x0 = xseq, lambda = 0.06)
library(microbenchmark)
microbenchmark(krs_R(), krs_C(), times = 500)
## Unit: milliseconds
       expr
                 min
                                             median
                            lq
                                     mean
                                                           uq
                                                                     max neval
## krs_R() 9.952303 10.658409 11.226581 10.766600 11.309105 15.967211
                                                                           500
## krs_C() 2.621224 3.035951 3.150422 3.088098 3.219024 3.849808
                                                                           500
```

The C version of the function is over 3.5 times faster than the R version on average.

Q1b

We now want to implement k-fold cross-validation for selecting the bandwidth λ . We can first do so in R:

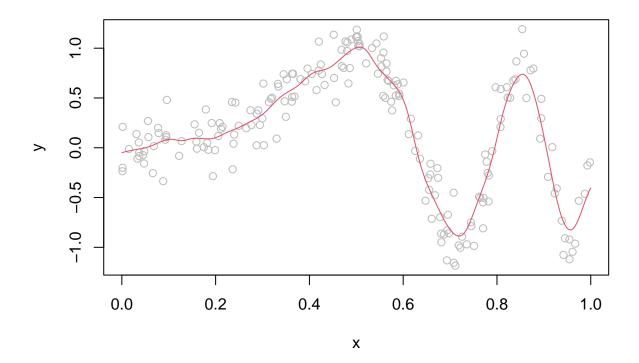
```
krsCV <- function(y, x, k, lam_seq){</pre>
  n <- length(x)
  groups <- sample(rep(1:k, length.out = n), size = n)</pre>
  mse_table <- data.frame(lambda = rep(lam_seq, each = k),</pre>
                            fold = rep(1:k, length(lam_seq)),
                            mse = NA)
  for (lambda in lam_seq) {
    for (i in 1:k) {
      # Set up training and testing sets
      x_train <- x[groups != i]</pre>
      y_train <- y[groups != i]</pre>
      x_test <- x[groups == i]</pre>
      y_test <- y[groups == i]</pre>
      # Fit the model on the training set and get values for x_test
      mu_pred <- meanKRS(y = y_train, x = x_train, x0 = x_test, lam = lambda)</pre>
      # Calculate MSE on the testing set
      mse <- mean((mu_pred - y_test)^2)</pre>
      mse_table$mse[mse_table$lambda == lambda & mse_table$fold == i] <- mse</pre>
    }
  }
  mean_mse <- mse_table %>%
    group_by(lambda) %>%
    summarise(mean_mse = mean(mse))
  best lambda <- mean mse$lambda[which.min(mean mse$mean mse)]
  return(best_lambda)
}
```

Using this R function, we can find the value of λ with the lowest average mean squared error (MSE) over 5-fold cross-validation:

```
best_lambda <- krsCV(y = y, x = x, k = 5, lam_seq = seq(0.01, 0.1, by = 0.01))
# See the best lambda value from 5-fold CV
best_lambda

## [1] 0.02

xseq <- seq(0, 1, length.out = 1000)
mu_best_lambda <- meanKRS(y = y, x = x, x0 = xseq, lam = best_lambda)
plot(x, y, col = "grey")
lines(xseq, mu_best_lambda, col = 2)</pre>
```



We can see the fit above using $\lambda = -0.0485553, -0.0474475, -0.0463246, -0.0451891, -0.0440435, -0.0428904, -0.0417327, -0.01074, 9.4738068 \times 10^{-4}, 0.002222, 0.0035456, 0.0049191, 0.0063434, 0.0078192, 0.0093466, 0.0109258, 0.0125564, 0.0142377, 0.012564, 0.0142377, 0.0$

```
# dyn.unload(here("portfolios/02_interfacing_r_with_c++/krsCV_Cpp.so"))
# Compile the code
system(paste0("R CMD SHLIB ", here("portfolios/02_interfacing_r_with_c++/krsCV_Cpp.cpp")))
# Load the binary code
dyn.load(here("portfolios/02_interfacing_r_with_c++/krsCV_Cpp.so"))
# Check if the function is loaded
is.loaded("krsCV_Cpp")
```

[1] TRUE

We can now use the C++ function to perform 5-fold cross-validation and return the value of λ yielding the highest average MSE across the 5 folds.

[1] 0.02

We can compare the computational performance of krsCV_Cpp to our R function krsCV:

```
# Compare computing time
krsCV_R <- function() krsCV(y = y,</pre>
                             x = x,
                             k = 5,
                             lam_seq = seq(0.01, 0.1, by = 0.01))
krsCV_Cpp <- function() .Call("krsCV_Cpp",</pre>
                       y_{vec} = y,
                       x_{vec} = x,
                       k_val = as.integer(5),
                        lambda_sequence = seq(0.01, 0.1, by = 0.01))
microbenchmark(krsCV_R(), krsCV_Cpp(), times = 500)
## Unit: milliseconds
           expr
                      min
                                  lq
                                          mean
                                                   median
                                                                 uq
                                                                          max neval
##
      krsCV_R() 19.270213 20.537017 21.680641 21.466783 22.017895 28.495935
                                                                                 500
   krsCV_Cpp() 4.708349 5.233496 5.432359 5.409505 5.606198 8.414248
```

Once again, the C++ version is much faster than the R version, this time around 4 times faster.

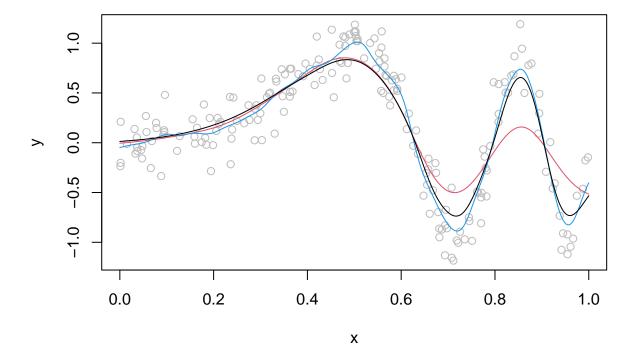
$\mathbf{Q2}$

The following R function allows the bandwidth to depend on x, i.e. $\lambda = \lambda(x)$:

```
return( out )
}
```

We can see the results here, where the red and blue lines show the fits from earlier where $\lambda = 0.06$ and $\lambda = 0.02$, respectively, and the black line shows the fit using the adaptive bandwidth function mean_var_KRS:

```
xseq <- seq(0, 1, length.out = 1000)
muSmoothAdapt <- mean_var_KRS(y = y, x = x, x0 = xseq, lam = 0.06)
plot(x, y, col = "grey")
lines(xseq, muSmoothLarge, col = 2) # red
lines(xseq, muSmoothSmall, col = 4) # blue
lines(xseq, muSmoothAdapt, col = 1) # black</pre>
```



We now want to write a version of mean_var_KRS in C++ and compare the results and performance with the R function. Code for the C++ function can be found on GitHub here.

```
# dyn.unload(here("portfolios/02_interfacing_r_with_c++/mean_var_krs_Cpp.so"))
# Compile the code
system(paste0("R CMD SHLIB ", here("portfolios/02_interfacing_r_with_c++/mean_var_krs_Cpp.cpp")))
# Load the binary code
dyn.load(here("portfolios/02_interfacing_r_with_c++/mean_var_krs_Cpp.so"))
# Check if the function is loaded
is.loaded("mean_var_krs_Cpp")
```

[1] TRUE

We can use the C++ function to fit the model and compare the results with the R function:

[1] TRUE

```
## Unit: milliseconds
## expr min lq mean median uq max neval
## var_krs_R() 21.187948 23.813029 24.563429 24.138163 24.486816 66.225953 500
## var_krs_C() 5.909083 6.808422 6.970961 6.976432 7.055845 9.482412 500
```

Once again, the implementation in C++ is much faster than in R, a little over 3.5 times faster.