

194.050 Social Network Analysis

Topic 04: Equivalence-based role mining

Intermediate presentation

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Content

Motivation

Theoretical background

- Definition of role equivalences
- Techniques for finding or quantifying equivalences

Proposed approach

- Which edge lists to use
- Methods for role mining
- Expected results

Motivation and Task Description

Task: Grouping users into equivalence classes that define roles

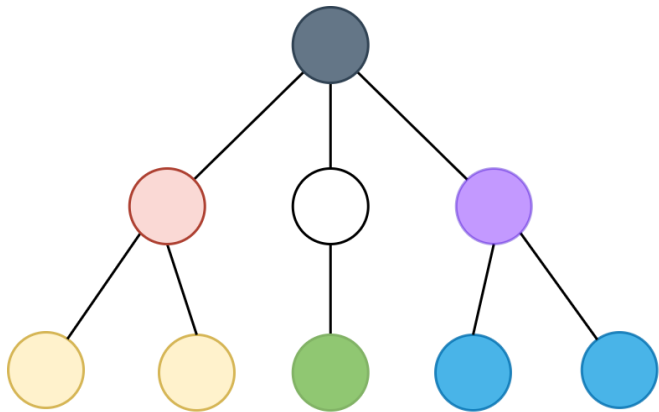
No prior knowledge of user roles

Equivalences are designed in a way that the results may carry a sociological interpretation [1]

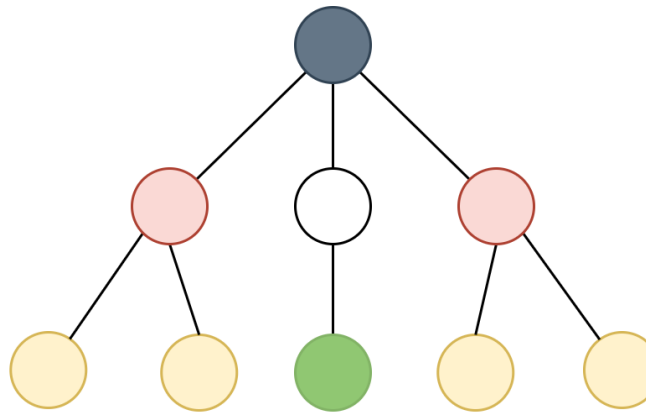
Theoretical background – Equivalence definitions

Comparing Positions: how nodes are embedded in its ego-network [2]

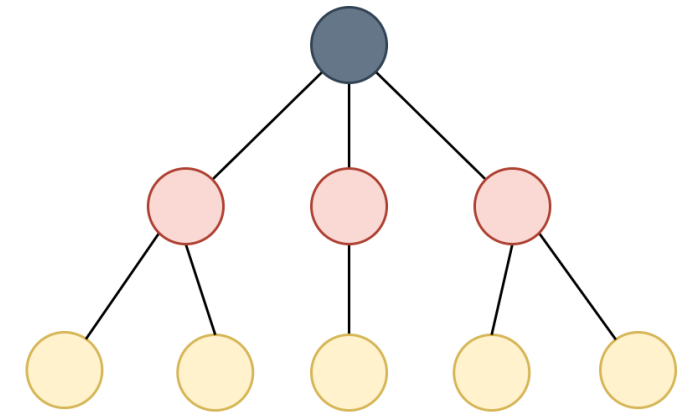
Structural equivalence



Automorphic equivalence



Regular equivalence



Most
restrictive

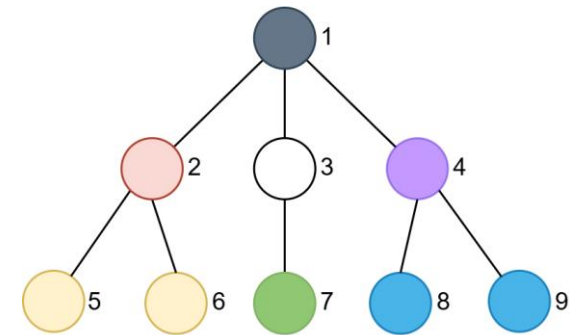
Least
restrictive

Theoretical background – Structural equivalence

Exactly identical composition of neighbourhood

e.g. {5, 6}

{8, 9}



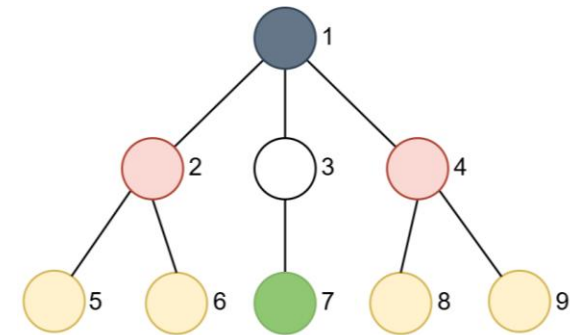
Approximated by K-means with compatible similarity measure
(corrected Euclidian or Manhattan distance function)

Theoretical background – Automorphic equivalence

Identically-shaped neighbourhoods with same degree

The connected neighbours can be different entities

e.g. {5, 6, 8, 9}



RoleSim [3]

Compute RoleSim score matrix of maximal weighted matching of the two vertices' neighbourhood

Iterate until convergence of the maximal weighted matching value

Output: a similarity matrix for performing clustering

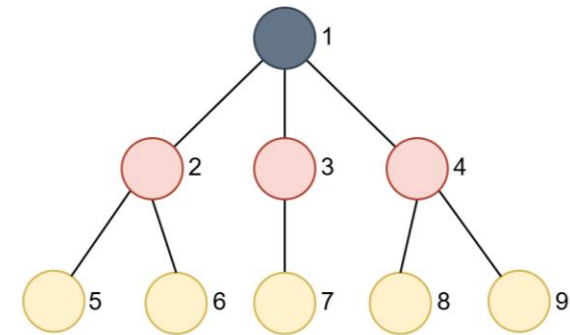
Theoretical background – Regular equivalence

Existence of connections with neighbour(s) of the same class

The connected neighbours can be different entities

The degree can be different

e.g. {5, 6, 7, 8, 9}



REGE [4]

Compute similarity score matrix that quantifies matching edge type (incoming/outgoing/bidirectional) exists in the two vertices' neighbourhood

Iteratively update matrix with the previous matching score as a weight for fixed iteration

Output: a similarity matrix for performing clustering

Proposed approach – Graphs to create

We will create 3 directed graphs with users as nodes as follows:

Network of Users Who Vote on Postings

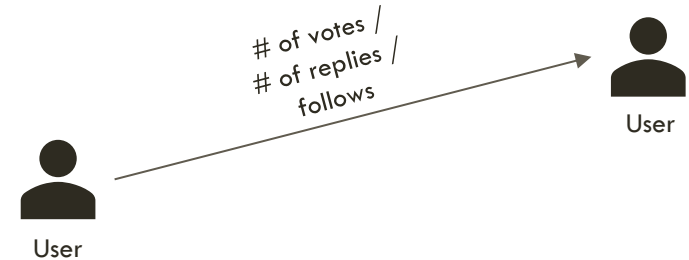
- Edge list: `df_edge_list_directed_users_votes_to_postings_net.parquet`
- Edge weights: Number of votes

Network of Users Who Reply to Postings

- Edge list: `df_edge_list_directed_users_postings_replies.parquet`
- Edge weights: Number of replies

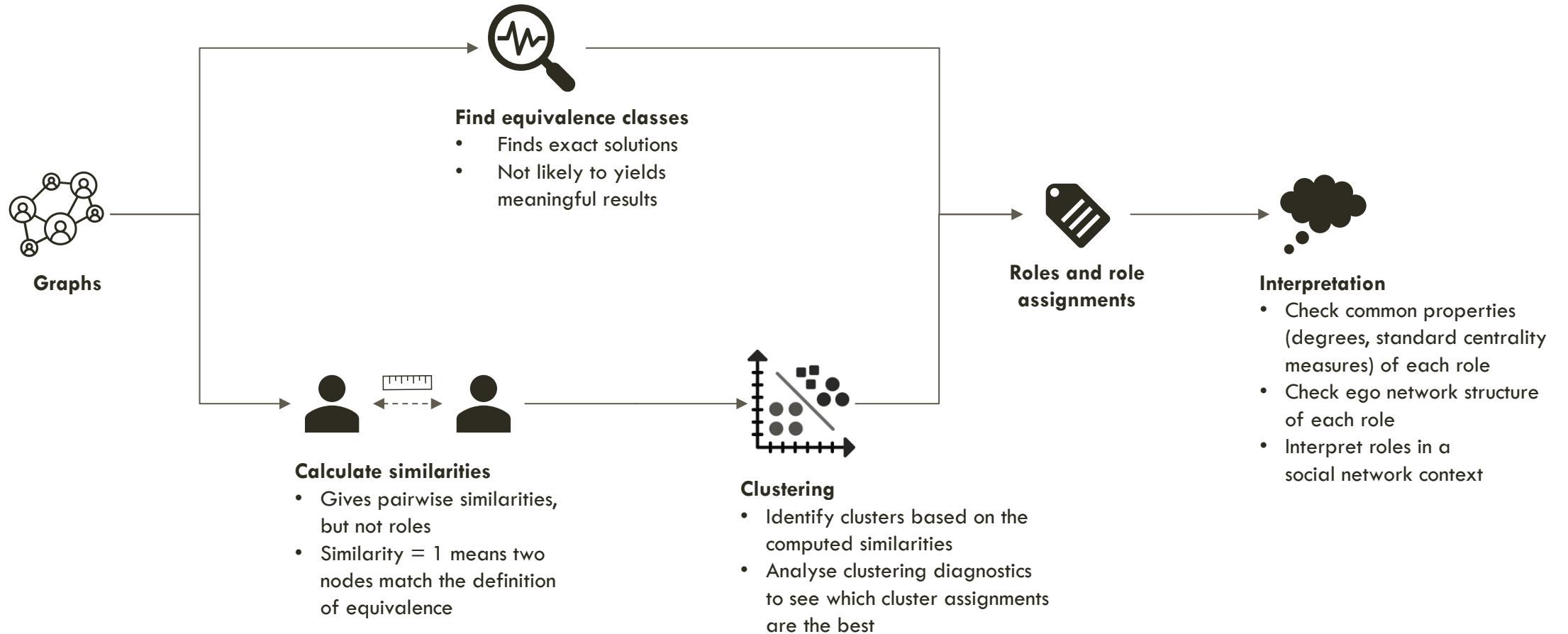
Network of Users Who Follow Other Users

- Edge list: `df_edge_list_directed_users_combined_postings_replies_and_votes_to_postings_net_and_follow_connections.parquet`
- Edge weights: 1 (Unweighted)



We do not plan to use the `weight_total` column in the edge lists since it hides the nature of user interactions

Proposed approach – Role mining



Role Identification

- ✓ Use equivalence clustering metrics to determine if distinct roles emerge

Role Interpretation

- ✓ **Activity Patterns:** Voting, replying, following
- ✓ **Ego-Network Structure:** Neighborhood composition and characteristics

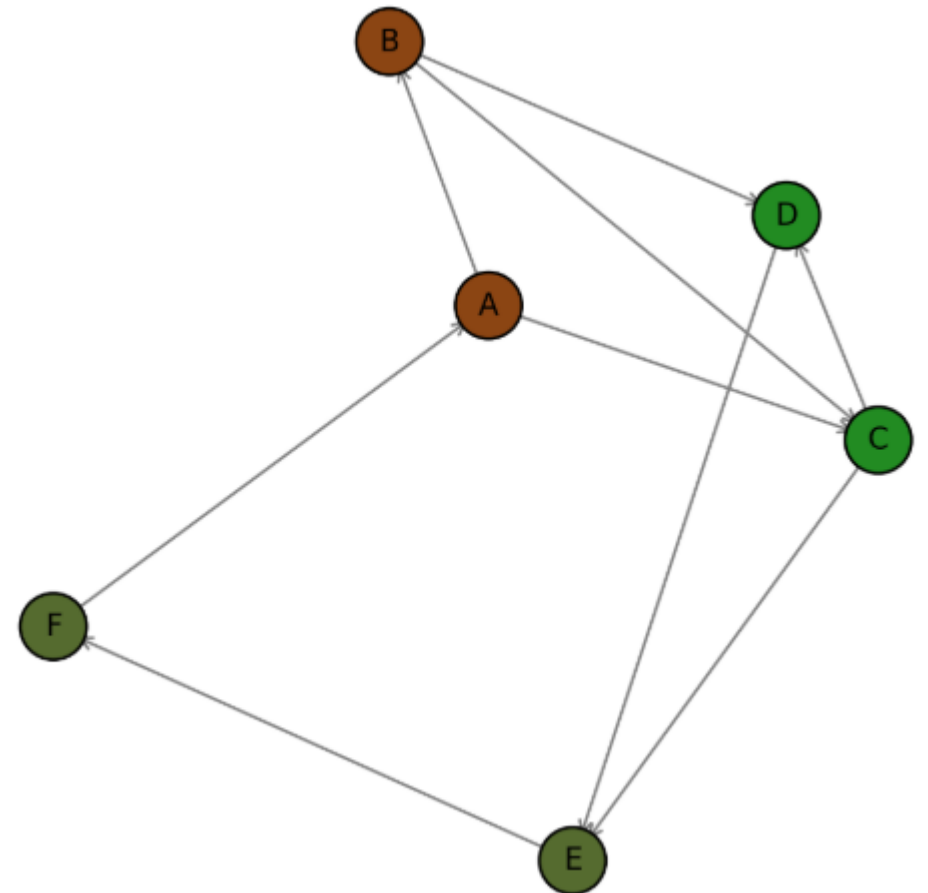
Role Characteristics

- ✓ **Degree Distributions:** In-degree, out-degree
- ✓ **Network Metrics:** Centrality, connectivity
- ✓ **Equivalence Properties:** Structural, automorphic, regular

Common Features

- ✓ **Neighborhood Structure:** Connections and configurations
- ✓ **Behavioral Patterns:** Interactional or functional similarities

Expected Results



References

- [1] Doran, D. (2017). *Network Role Mining and Analysis*. Springer International Publishing, p. 31.
- [2] Doran, D. (2017). Equivalence-Based Role Mining. *Network Role Mining and Analysis*. Springer International Publishing.
- [3] Jin, R., Lee, V. E., & Hong, H. (2011). Axiomatic ranking of network role similarity. In *Proceedings of the 17th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, 922–930. ACM.
- [4] Borgatti, S. P., & Everett, M. G. (1993). Two algorithms for computing regular equivalence. *Social Networks*, 15(4), 361–376.