

2.1. Problem Statement: STATISTICS 1

3. In a class on 100 students, 80 students passed in all subjects, 10 failed in one subject, 7 failed in two subjects and 3 failed in three subjects. Find the probability distribution of the variable for number of subjects a student from the given class has failed in.

For a random student,

The probability of failing in 0 subjects, $P(X=0) = 0.8$

The probability of failing in 1 subjects, $P(X=1) = 0.1$

The probability of failing in 2 subjects, $P(X=2) = 0.07$

The probability of failing in 3 subjects, $P(X=3) = 0.03$

The probability distribution can be shown as:

X	0	1	2	3
P(X)	0.8	0.1	0.07	0.03

2.2. Problem Statement: STATISTICS 2

1. A test is conducted which is consisting of 20 MCQs (multiple choices questions) with every MCQ having its four options out of which only one is correct. Determine the probability that a person undertaking that test has answered exactly 5 questions wrong.

$$n = 20, n - k = 5, k = 20 - 5 = 15$$

- The probability of success = probability of giving a right answer = $s = 14$
- The probability of failure = probability of giving a wrong answer = $1 - s = 1 - 14 = 34$

When we substitute these values in the formula for Binomial distribution we have,

$$P(\text{exactly 5 out of 20 answers incorrect}) = C(20, 5) * (1/4)^{15} * (3/4)^5$$

$$P(5 \text{ out of } 20) = (20 \cdot 19 \cdot 18 \cdot 17 \cdot 16) / (5 \cdot 4 \cdot 3 \cdot 2 \cdot 1) \cdot (1/4)^5 \cdot (3/4)^{15} = \mathbf{0.0000034}$$

Thus the required probability is 0.0000034 approximately.

2. A die marked A to E is rolled 50 times. Find the probability of getting a “D” exactly 5 times.

$$n = 50, k = 5, n - k = 45.$$

The probability of success = probability of getting a “D” = $s = 1/5$

The probability of failure = probability of not getting a “D” = $1 - s = 4/5$.

3. Two balls are drawn at random in succession without replacement from an urn containing 4 red balls and 6 black balls. Find the probabilities of all the possible outcomes.

First determine the probabilities of the events.

Events	Probability
RR	$= (4/10)(3/9) = 2/15$
RB	$= (4/10)(6/9) = 4/15$
BR	$= (6/10)(4/9) = 4/15$
BB	$= (6/10)(5/9) = 1/3$

The probability of 0 blue balls (RR) is $2/15$

The probability of 1 blue ball is (RB or BR) is $4/15 + 4/15 = 8/15$

The probability of 2 blue balls (BB) is $1/3$

So the probability distribution is: $Z \quad p(Z)$

$$0 = \mathbf{2/15}$$

$$1 = \mathbf{8/15}$$

$$2 = \mathbf{1/3}$$