Taylor series - Special cases

Practice Quiz, 5 questions

✓ Congratulations! You passed!

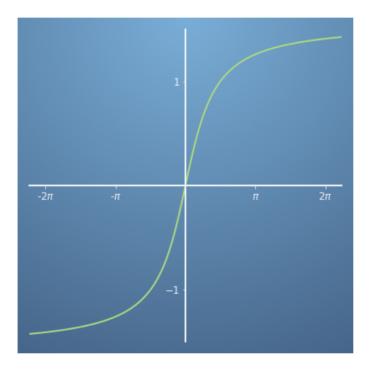
Next Item



1/1 points

1.

The graph below shows the function $f(x) = an^{-1}(x)$



By using the Maclaurin series or otherwise, determine whether the function shown above is even, odd or neither.



Odd

Correct

For an odd function, -f(x)=f(-x). We can also determine if a function is odd by looking at its symmetry. If it has rotational symmetry with respect to the origin, it is an odd function.

Even

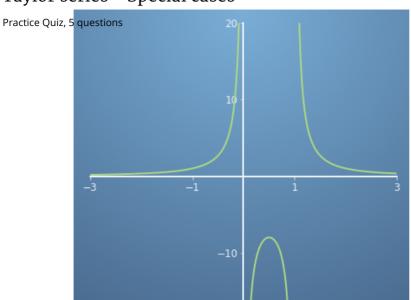
Neither odd nor even

0.75 / 1 points

2.

The graph below shows the discontinuous function $f(x)=rac{2}{(x^2-x)}$. For this function, select the

starting points that will allow a Taylor approximation to be made. Taylor series – Special cases



$$x = -3$$

Correct

A Taylor approximation centered at x=-3 will allow us to approximate f(x) for x<0 only.

$$x = 1$$

Un-selected is correct

$$x = 2$$

Correct

A Taylor approximation centered at x=2 will allow us to approximate f(x) for $x>1 {
m only}.$

$$x = 0.5$$

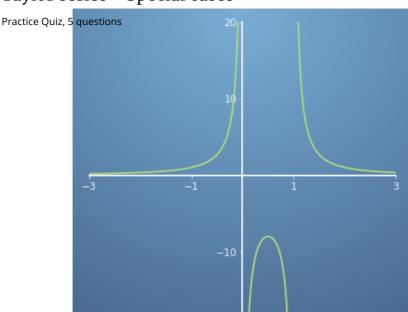
This should be selected

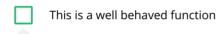
0.40 / 1 points

3.

For the same function as previously discussed, $f(x)=rac{2}{(x^2-x)}$, select all of the statements that

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Un-selected is correct

Approximation ignores segments of the function

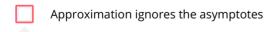
Correct

Due to the discontinues function and the range of \boldsymbol{x} values in which it remains well behaved, the starting point of the Taylor series dictates the domain of the function we are trying to approximate.



This should not be selected

Often the case with similar functions and as mentioned in the previous chapter video, there is often a sign flip in the approximation, showing very slow convergence however, this is not always the case.



This should be selected

Approximation accurately captures the asymptotes

This should not be selected

Taylor series approximations often find it difficult to capture asymptotes correctly. For example, the zeroth and first order terms cut directly through an asymptote in most cases.

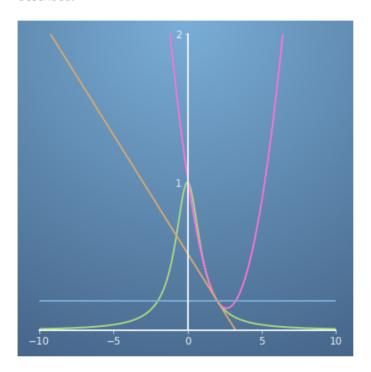
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4.

The graph below highlights the function $f(x)=rac{1}{(1+x^2)}$ (green line), with the Taylor expansions for the first 3 terms also shown about the point x=2. The Taylor expansion is

 $f(x)=rac{1}{5}rac{4(x-2)}{25}+rac{22(x-2)^2}{125}+\dots$ Although the function looks rather normal, we find that the Taylor series does a bad approximation further from its starting point, not capturing the turning point. What could be the reason why this approximation is poor for the function described.



None of these options

Un-selected is correct

Function does not differentiate well

Un-selected is correct

Asymptotes are in the complex plane

Correct

Although this function is well behaved in the real plane, in the imaginary plane, the asymptotes limit its convergence and the behaviour of the Taylor expansion, which is shown to behave badly for functions that are discontinuous.

The function has no real roots

Un-selected is correct

It is a discontinuous function in the complex plane

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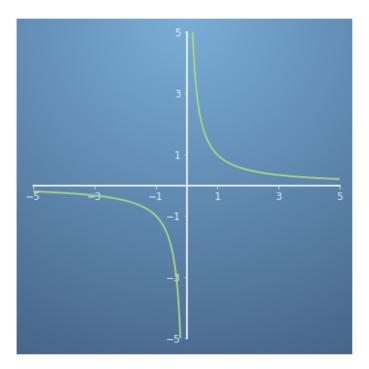
Practice Quiz, 5 questions
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1/1 points

5.

For the function $f(x)=rac{1}{x}$, provide the linear approximation about the point x=4, ensuring it is second order accurate.



$$f(x) = 1/4 + x/16 - O(\Delta x^2)$$

Correct

Second order accurate means we have a first order Taylor series. All the terms above are sufficiently small, assuming Δx is small.

$$f(x) = 1/4 - x/16 + O(\Delta x^2)$$







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