5/5 points (100%)

Practice Quiz, 5 questions

✓ Congratulations! You passed!

Next Item



points

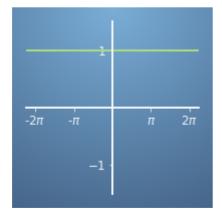
1.

As mentioned in the previous video, the Taylor series approximation can also be viewed as a power series, in which these approximations are used to build functions that are often simpler and easier to evaluate, particularly when using numerical methods. In the following questions, we are looking at developing our understanding of how the increasing order of a power series allows us to develop further information of a function.

Below are three graphs highlighting the zeroth, second and fourth order approximations of a common trigonometric function. Observe how increasing the number of approximations in the power series begins to build a better approximation, and determine which function these approximations represent.

Zeroth order approximation:

$$f_0(x) = 1$$



Second order approximation:

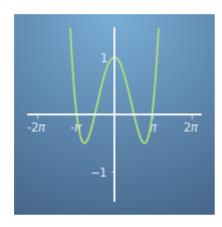
$$f_2(x)=1-\frac{x^2}{2}$$

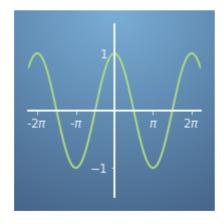
Matching functions and approximations Practice Quiz, 5 questions $\frac{1}{-2\pi} - \pi = \frac{\pi}{2\pi}$

5/5 points (100%)

Fourth order approximation:

$$f_4(x) = 1 - \frac{x^2}{2} + \frac{x^4}{24}$$



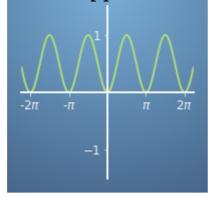


Correct

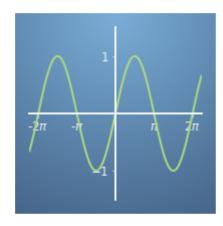
The function $f(x)=\cos(x)$ is symmetric about the line x=0. Furthermore our approximation of this function is when x=0, known as a Maclaurin series. At the point x=0, f(0)=1 which is shown in the zeroth order approximation.

$$\bigcirc \quad f(x) = \sin^2(x)$$

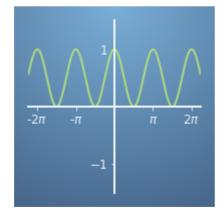
Practice Quiz, 5 questions



5/5 points (100%)



$$\int f(x) = \cos^2(x)$$





1/1 points 2.

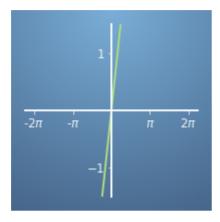
Below are three graphs highlighting the first, third and fifth order Matching functions approximations function. Observe how the

5/5 points (100%)

Practice Quiz, 5 questions power series begins to build the function, and determine which function these approximations represent.

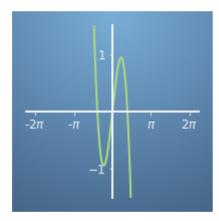
First Order:

$$f_1(x)=2x$$



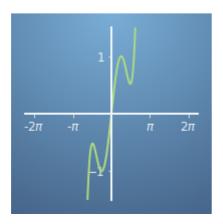
Third Order:

$$f_3(x)=2x-\frac{4x^3}{3}$$



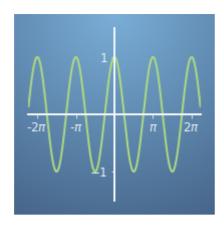
Fifth Order:

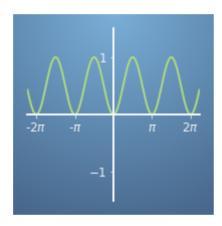
$$f_5(x) = 2x - rac{4x^3}{3} + rac{4x^5}{15}$$

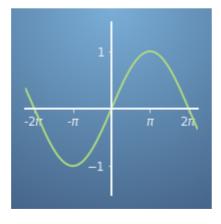


5/5 points (100%)

Practice Quiz, 5 questions







$$\bigcap \quad f(x) = \sin(2x)$$

Matching functions and approximations

Practice Quiz, 5 questions

5/5 points (100%)

Correct

The function $f(x)=\sin(2x)$ has rotational symmetry about the origin. Furthermore, we can see that the period is much shorter, also evident from the three approximations shown.



1/1 points

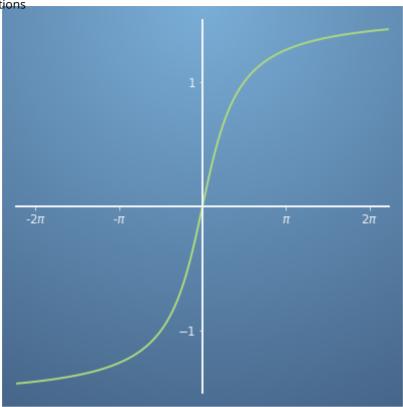
3.

The graph below shows the function $f(x) = \tan^{-1}(x)$, select all the power series approximations that can be used to obtain an

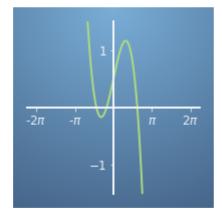
power series approximations that can be used to obtain an Matching functions approximations

5/5 points (100%)

Practice Quiz, 5 questions



$$f(x)=rac{1}{2}+x-rac{x^3}{3}\dots$$



Un-selected is correct

$$f(x) = x \dots$$

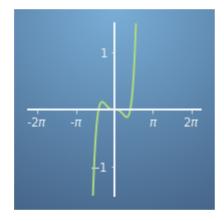
Practice Quiz, 5 questions

5/5 points (100%)



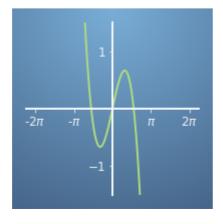
We can see this approximation goes through the origin and also looks as if it fits the function well between -0.5 < x < 0.5. As this is a linear function, this is a first-order approximation.

$$f(x)=-rac{x^3}{3}+rac{x^5}{5}\dots$$



Un-selected is correct

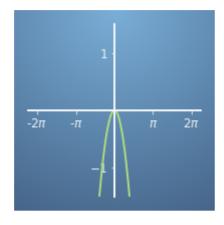
$$f(x) = x - rac{x^3}{3} \cdots$$



5/5 points (100%)

Practice Quiz, 5 question. We can see this approximation goes through the origin and also looks as if it fits the function well between -0.5 < x < 0.5.

$$f(x) = -x^2 \dots$$



Un-selected is correct

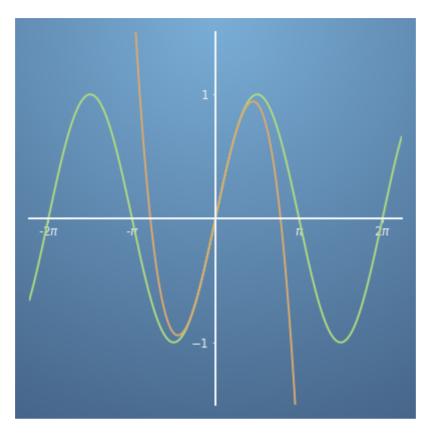


1/1 points

The sinusoidal function $f(x)=\sin(x)$ (green line) centered at x=0 is shown in the graph below. The approximation for this function is shown

Matching functions and approximations line). Determine what 5/5 points (100%)

Practice Quiz, 5 quest polynomial order is represented by the orange line.



Zeroth	Order

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 LII 21	i Onuei



Correct

The highest power of x in the approximation is 3, therefore this approximation is a third order approximation.

Fifth Order

None of the above



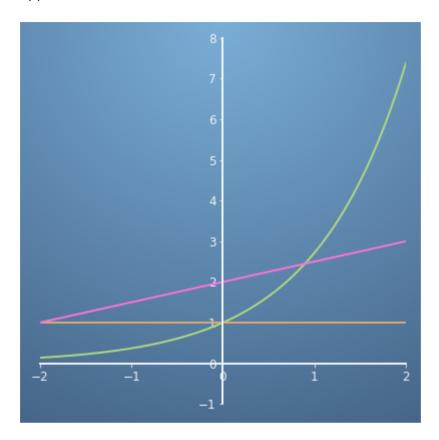
1/1 points

5.

The graph below shows the function $f(x) = e^x$ (green line), the exponential function so widely used in science and mathematics today. Matching functions in an approximation for the exponential function, centred at x = 0. Determine if the pink line show

5/5 points (100%)

Practice Quiz, 5 questions exponential function, centred at x=0. Determine if the pink line shown on the graph is, in fact, an approximation and if so, what order is this approximation.





- Second Order
- Third Order
- Not a correct approximation

Correct

The approximation shown is not tangent to this point and is, therefore, a poor approximation of the function.







5/5 points (100%)

Practice Quiz, 5 questions