Taylor Series Assessment

6/6 points (100%)

Quiz, 6 questions

✓ Congratulations! You passed!

Next Item

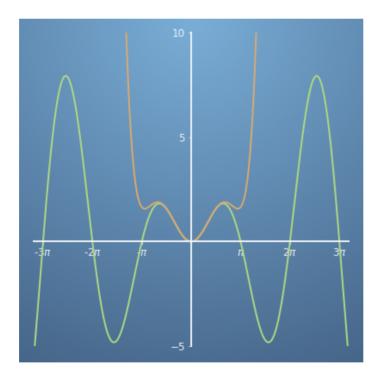


1/1 points

1.

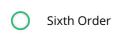
Now that we have completed the set of Taylor series lectures and answered all the quiz questions, we now need to test our understanding of Taylor series. We have looked at the derivation of Taylor series, broken it down into a power series approximation, explored special cases and developed the idea of multivariant Taylor series, that is required in order for us to develop a good grounding for the next chapters in this course.

For the function $f(x)=x\sin(x)$ shown below, determine what order approximation is shown by the orange curve, where the Taylor series approximation was centered about x=0.



\bigcirc	Second	Order

Third	Order



Correct

The sign of the sixth order term is positive, which dominates over the fourth order term and is particularly the reason why the approximation for f(x) is always

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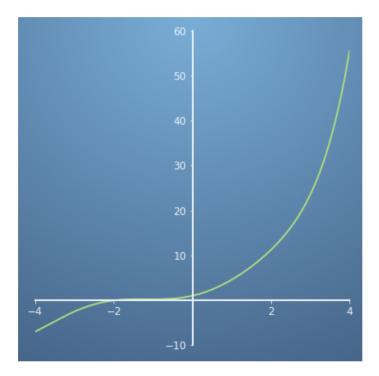
None of the above



1/1 points

2.

Find the first four non zero terms of the Taylor expansion for the function $f(x)=e^x+x+\sin(x)$ about x=0. The function is shown below:



$$f(x) = 1 + 3x + rac{x^2}{2} + rac{x^3}{6} + \dots$$

$$f(x) = 1 + 3x + \frac{x^2 + x^4}{2 + 24} + \dots$$



As there is a variety of functions here i.e. $\sin(x)$ and an exponential, we are not likely to get expansions that are often only for odd or even powers of x.

$$f(x) = 3x + rac{x^2}{2} + rac{x^4}{4} + rac{x^6}{720} + \dots$$

 \bigcirc

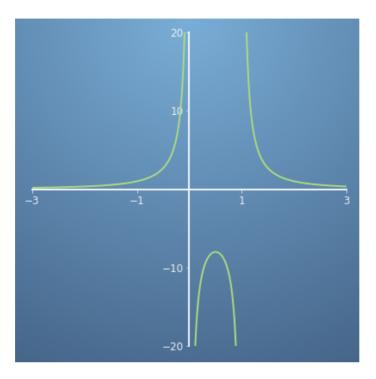
$$f(x) = 1 + 3x - \frac{x^2 + x^4}{2 + 24} + \dots$$

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Quiz, 6 questions 3.

The graph below shows the discontinuous function $f(x)=\frac{2}{(x^2-x)}$. Approximate the section of this function that covers the domain 0< x<1. Use the Taylor series forumla and x=0.5 as your starting point, find the first two non zero terms.



$$f(x) = -4 - 16(x - 0.5)^2 \dots$$

$$f(x) = -8 - 32(x - 0.5)^2 \dots$$

Correct

This second order approximation is only valid within the domain 0 < x < 1, and is, therefore, a poor approximation for the entire function, but behaves well within the defined domain.



$$f(x) = -8 - 32x^2\dots$$

$$f(x) = -8 + 32(x - 0.5)^2 \dots$$



1/1 points

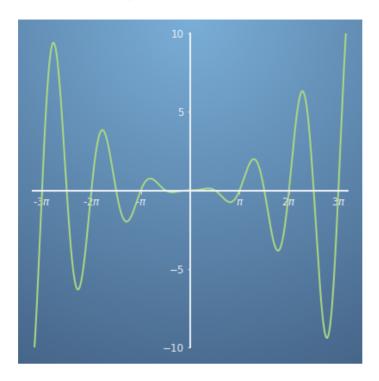
4.

Determine if the function:

Taylor Series Assessment = $\left(\frac{x}{2}\right)^2 \frac{\sin(2x)}{2}$

6/6 points (100%)

Quiz, 6 questions shown below is odd, even or neither.



0

Odd

Correct

For an odd function, -f(x)=f(-x). We can also determine if a function is odd by looking at its symmetry. If it has rotational symmetry with respect to the origin, it is an odd function.

Even

Neither odd nor even



1/1 points

5.

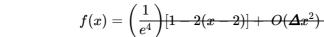
Take the Taylor expansion of the function

$$f(x)=e^{-2x}$$

about the point x=2 and subsequently linearise the function.

$$f(x) = \left(\frac{1}{e^4}\right)[1 + 2(x-2)]$$

$$f(x)=igg(rac{1}{e^2}igg)[2(x-2)]+O({ extstyle \Delta} x^2)$$



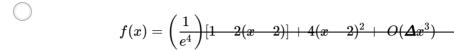
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6/6 points (100%)

Quiz, 6 questions

Correct

Here we are taking a complicated function and simplifying it into its linear components, making sure to still note down its level of accuracy.

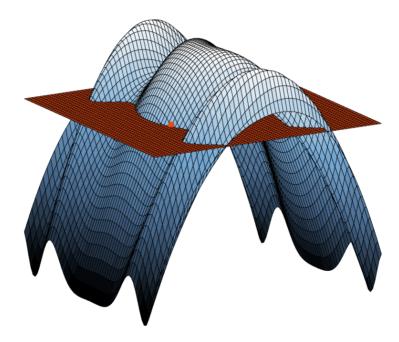


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1/1 points

6.

The figures below feature functions of two variables with proposed Taylor series approximations in red, expanded around the red circle. Which of the following features a valid second order approximation?

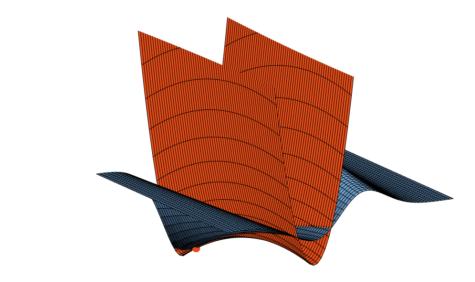


$$\bigcirc \quad f(x,y) = x^2 - xy + \sin(y)$$

6/6 points (100%)



$$\int f(x,y) = xe^{-x^2+y/4}$$



Correct

The red surface has a gradient which changes with x and y, and both the function and its approximation have the same behaviour near the point of expansion, unlike the other second order red surface in this question. It is therefore the second order Taylor series approximation.

$$\int f(x,y) = (x^3 + 2y^2)e^{-x^2 - y^2}$$

