

Today's Quote →

**YOU DON'T HAVE
TO BE GREAT TO START,
BUT YOU HAVE TO
START TO BE GREAT**

Good Morning !!

Today's content

$\text{arr}[5] = \boxed{\begin{array}{|c|c|c|c|c|} \hline 5 & 7 & 4 & 3 & 11 \\ \hline 0 & 1 & 2 & 3 & 4 \\ \hline \end{array}}$ indices: $[0, N-1]$

$\text{arr}[2], \text{arr}[4], \underline{\text{arr}[i]}$ $T.C \rightarrow O(1)$

How to print all elements in the array ⇒

```
void printArr( arr, N){           i: [0, N-1]
    for( i = 0 ; i < N ; i++) {      ; N iterations
        cout << arr[i];
    }
}
```

$T.C \rightarrow O(N)$
 $S.C \rightarrow O(1)$

Q1) Given N array elements, count no. of elements, having at least one element greater than itself.

Eg → arr[7] : { -3 ₀ 2 ₁ 6 ₂ 8 ₃ 4 ₄ 8 ₅ 5 ₆ }
count : +1 +1 +1 +1 +1 = 5.

arr[8] : { 2 ₀ 3 ₁ 10 ₂ 7 ₃ 3 ₄ 2 ₅ 10 ₆ 8 ₇ }
count : +1 +1 +1 +1 +1 +1 +1 ans = 6

arr[10] : { 2 ₀ 5 ₁ 1 ₂ 4 ₃ 8 ₄ 0 ₅ 8 ₆ 1 ₇ 3 ₈ 8 ₉ }
count : +1 +1 +1 +1 +1 +1 +1 +1 +1 ans = 7.

arr[5] : { 8 ₀ 8 ₁ 8 ₂ 8 ₃ 8 ₄ } ans = 0

observation: for maximum element, we don't have any element greater than itself.

find count of how many times max element is appearing.
 $\Rightarrow C$

$$\underline{\text{ans.}} = \text{total no. of elements} - C$$

pseudocode →

```
put    countGreater ( arr , N ) {  
    max = arr [ 0 ] ;  
    for ( i = 1 ; i < N ; i ++ ) {  
        if ( arr [ i ] > max ) {  
            max = arr [ i ]  
        }  
    }  
    c = 0 ;  
    for ( i = 0 ; i < N ; i ++ ) {  
        if ( arr [ i ] == max ) {  
            c += 1  
        }  
    }  
    return N - c ;  
}
```

T.C $\rightarrow O(N)$
S.C $\rightarrow O(1)$

todo : try to solve this by iterating only once .

Q1) Given N array elements , check if there exists a pair (i,j) such that $\text{arr}[i] + \text{arr}[j] == k$ & $i \neq j$

Note→ i and j are index value , k is given sum.

$\text{arr}[] : \{ 3, -2, 1, 4, 3, 6, 8 \} : \{ \text{true} \}$

$K=10$

$\text{arr}[] : \{ 2, 4, -3, 7 \} : \{ \text{false} \}$

$K=5$

$\text{arr}[] : \{ 2, 4, -3, 7 \} : \{ \text{false} \}$

$K=8$

$\text{arr}[] : \{ 3, 5, 2, 1, -3, 7, 8, 15, 6, 13 \}$

sum → 10 $(3, 7), (2, 8), (-3, 13) : \{ \text{true} \}$

$\text{arr}[] : \{ 2, 3, 7, -4, 3 \} : \{ \text{true} \}$

$K=6$

idea-1 check all the pairs . If any pair (i, j) is having their sum = K \Rightarrow return true.

boolean checkPairs (arr, N, K) {

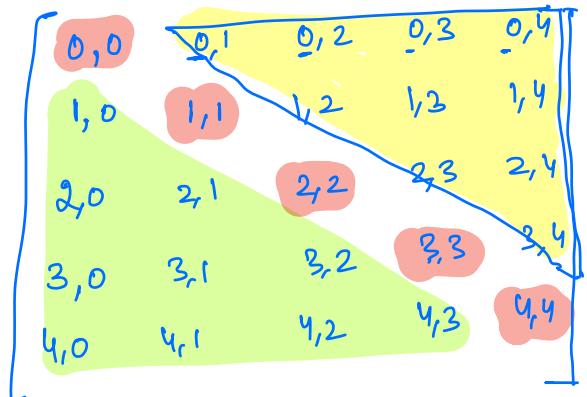
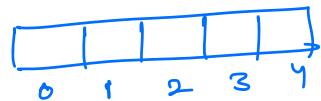
```

    for( i=0 ; i < N ; i++) {
        for( j=0 ; j < N ; j++) {
            if( i != j ) {
                if (arr[i] + arr[j] == K) {
                    return true;
                }
            }
        }
    }
    return false;
}

```

3

$$\begin{array}{|l|l|} \hline T.C \rightarrow O(N^2) \\ S.L \rightarrow O(1) \\ \hline \end{array}$$



all the pairs.

initially.

$$\begin{array}{ll} i = 0, & j \rightarrow [1, 4] \\ i = 1, & j \rightarrow [2, 4] \\ i = 2, & j \rightarrow [3, 4] \\ i = 3, & j \rightarrow [4, 4]. \\ \vdots & \quad j \rightarrow [i+1, N-1] \end{array}$$

Idea-2

boolean checkPairs (arr, N, K) {

 for(i=0 ; i < N ; i++) {

 for(j=i+1 ; j < N ; j++) {

 if (arr[i] + arr[j] == K) {

 return true;

 }

 }

}

table

i	j	iterations.
0	[1, N-1]	N-1
1	[2, N-1]	N-2
2	[3, N-1]	N-3
⋮	⋮	⋮
<u>N-1</u>	[N, N-1]	0

$$\# \text{ total no. of iterations} = (N-1) + (N-2) - \dots - 2 + 1 + 0$$

$$= \frac{N(N-1)}{2}.$$

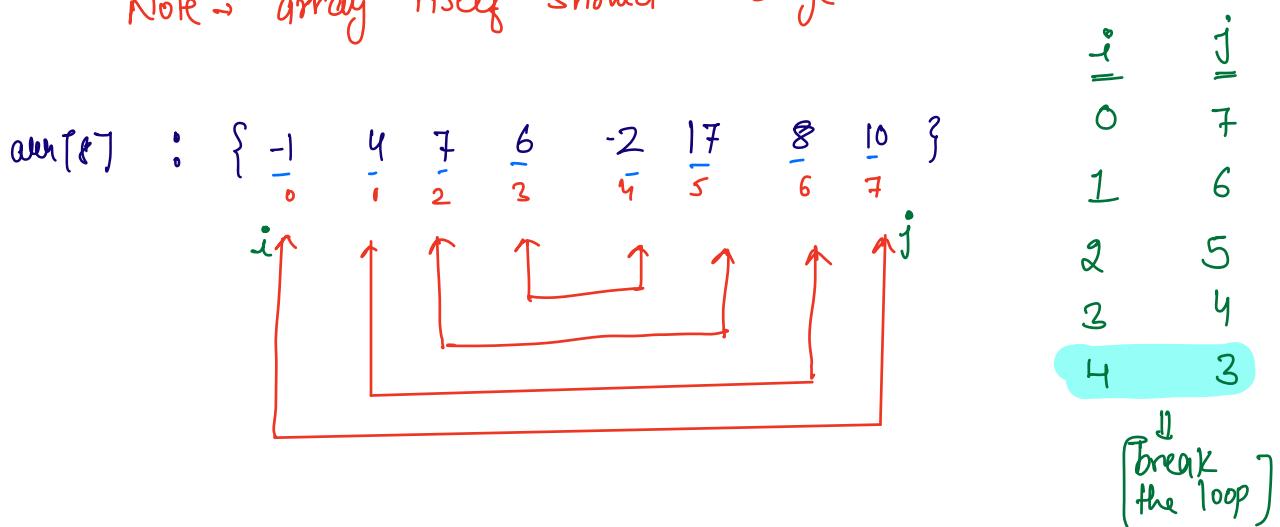
$$\frac{N(N+1)}{2}$$

$$\Rightarrow \frac{(N-1)(N+1)}{2}$$

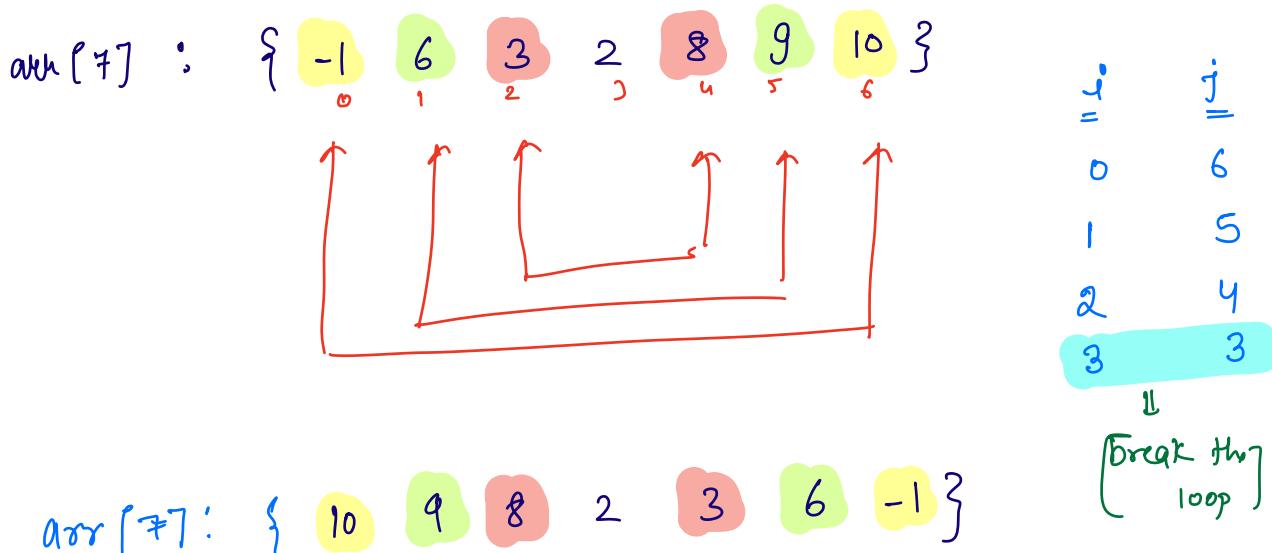
$$\Rightarrow \frac{N(N-1)}{2}.$$

T.C $\rightarrow O(N^2)$
S.C $\rightarrow O(1)$

Q1) Given an array : Reverse entire array . [s.c $\rightarrow O(1)$]
 Note \rightarrow array itself should change .

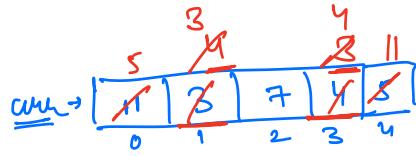


$$arr[8] : \{ 10_0, 8_1, 17_2, -2_3, 6_4, 7_5, 4_6, -1_7 \}$$



pseudo-code.

```
void reverse ( arr, N){  
    i = 0 , j = N-1  
    while ( i < j ) {  
        int temp = arr[i]  
        arr[i] = arr[j]  
        arr[j] = temp  
        i += 1  
        j -= 1  
    }  
}
```



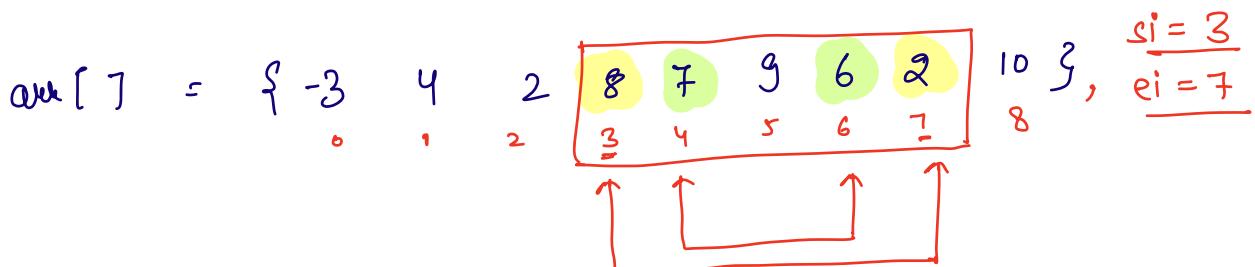
$$\begin{aligned} i &= \emptyset \times 2 \leq 3 \\ j &= 4 \times 3 \geq 1 \end{aligned}$$

→ swapping
ith & jth
idx value

$$\begin{array}{r} 0, 3 \\ 1, 2 \\ \hline 2, 1 \\ 3, 0 \end{array}$$

T.C → O(N)
S.C → O(1)

Q.) Given N array elements and $\underline{si \& ei}$.
 Reverse array from si to ei . Note $si \leq ei$



$arr[] : \{ -3, 4, 2, 2, 6, 9, 7, 8, 10 \}$

pseudo-code →

void reversePart (arr, N, si, ei) {

i = si , *j* = ei

 while (i < j) {

 int temp = arr[i]
 arr[i] = arr[j]
 arr[j] = temp

i += 1
 j -= 1

$O(ei - si)$

T.C $\rightarrow O(N)$

S.C $\rightarrow O(1)$

Q1) Given N array elements, Rotate array from last to first by K times.

[S.C → O(1)]



$\text{arr}[7]: \{ 3 \underset{0}{}, -2 \underset{1}{}, 1 \underset{2}{}, 4 \underset{3}{}, 6 \underset{4}{}, 9 \underset{5}{}, 8 \underset{6}{} \} \quad \times K=3$

K=1 $\{ 8 \underset{0}{}, 3 \underset{1}{}, -2 \underset{2}{}, 1 \underset{3}{}, 4 \underset{4}{}, 6 \underset{5}{}, 9 \underset{6}{} \}$

K=2 $\{ 9 \underset{0}{}, 8 \underset{1}{}, 3 \underset{2}{}, -2 \underset{3}{}, 1 \underset{4}{}, 4 \underset{5}{}, 6 \underset{6}{} \}$

K=3. $\{ 6 \underset{0}{}, 9 \underset{1}{}, 8 \underset{2}{}, 3 \underset{3}{}, -2 \underset{4}{}, 1 \underset{5}{}, 4 \underset{6}{} \}$

$\text{arr}[9]: \{ 4 \underset{0}{}, 1 \underset{1}{}, 6 \underset{2}{}, 9 \underset{3}{}, 2 \underset{4}{}, 14 \underset{5}{}, 7 \underset{6}{}, 8 \underset{7}{}, 3 \underset{8}{} \} \quad \times K=4$

$\text{arr}[9]: \{ 14 \underset{0}{}, 7 \underset{1}{}, 8 \underset{2}{}, 3 \underset{3}{}, 4 \underset{4}{}, 1 \underset{5}{}, 6 \underset{6}{}, 9 \underset{7}{}, 2 \underset{8}{} \}$

reverse.

$\{ \underset{\text{Reverse}}{\overbrace{3 \underset{0}{}, 8 \underset{1}{}, 7 \underset{2}{}, 14 \underset{3}{}}} \underset{2}{}, \underset{\text{Reverse}}{\overbrace{9 \underset{4}{}, 6 \underset{5}{}, 1 \underset{6}{}, 4 \underset{7}{}}} \}$

$\{ \underset{\text{Reverse}}{\overbrace{14 \underset{0}{}, 7 \underset{1}{}, 8 \underset{2}{}, 3 \underset{3}{}, 2 \underset{4}{}, 9 \underset{5}{}, 6 \underset{6}{}, 1 \underset{7}{}, 4 \underset{8}{}}} \}$

$\{ \underset{\text{Reverse}}{\overbrace{14 \underset{0}{}, 7 \underset{1}{}, 8 \underset{2}{}, 3 \underset{3}{}, 4 \underset{4}{}, 1 \underset{5}{}, 6 \underset{6}{}, 9 \underset{7}{}, 2 \underset{8}{}}} \}$

ans.

$\text{arr} \rightarrow \{ 3, 2, 7, 4, 6, 1, 9 \}$ K=5

$\text{arr} \rightarrow \{ 7, 4, 6, 1, 9, 3, 2 \}$

reverse.

$\rightarrow \{ 9, 1, 6, 4, 7, 2, 3 \}$

$\rightarrow \{ 7, 4, 6, 1, 9, 3, 2 \}$

ans.

$$\textcircled{1} \quad K = K \% N$$

\textcircled{2} Reverse the entire array $\rightarrow \text{reversePart}(\text{arr}, 0, N-1)$: (arr, 0, 6)

\textcircled{3} Reverse first K-elements $\rightarrow \text{reversePart}(\text{arr}, 0, K-1)$: (arr, 0, 7)

\textcircled{4} Reverse remaining elements $\rightarrow \text{reversePart}(\text{arr}, K, N-1)$

$\text{arr} \rightarrow [0, 1, 2, 3, 4, 5, 6]$, K=8, N=7

$K \geq N$

$T.C \rightarrow O(N)$
$S.L \rightarrow O(1)$

arr : $\{ 3, 2, 7, 5, 4 \}$ $N=5$

$$\begin{aligned} K &= N \\ K &= N \cdot N = 0 \end{aligned}$$

K=1 : $\{ 4, 3, 2, 7, 5 \}$

K=2 : $\{ 5, 4, 3, 2, 7 \}$

K=3 : $\{ 7, 5, 4, 3, 2 \}$

K=4 : $\{ 2, 7, 5, 4, 3 \}$

K=5 : $\{ 3, 2, 7, 5, 4 \}$

K=6 : $\{ 4, 3, 2, 7, 5 \}$

K=7 : $\{ 5, 4, 3, 2, 7 \}$

K=8 : $\{ 7, 5, 4, 3, 2 \}$

K=9 : $\{ 2, 7, 5, 4, 3 \}$

K=10 : $\{ 3, 2, 7, 5, 4 \}$

0 →	5	→ 10 → 15	---
1 →	6	→ 11 → 16	---
2 →	7	→ 12 → 17	—
3 →	8	→ 13 → 18	—
4 →	9	→ 14 → 19	—

→ ans is repeating after N iterations.

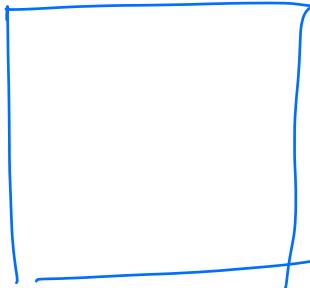
→ take modulo with N .

$$\Rightarrow K = K \% N$$



Doubts →

→ α no. of questions

- 
- similar to what we have discussed.
- [small variance].

loops

```

for ( i=0 ; i < (2n) ; i++ ) {
    j = i
    while ( j > 0 ) {
        j -= 1
    }
}
  
```

i	j	iterations
0	[0, 0)	0
1	[1, 0)	1
2	[2, 0)	2
3	[3, 0)	3
...		
1		1
1		1
2 ⁿ	[2 ⁿ , 0)	2 ⁿ

total no. of iteration = $0 + 1 + 2 + 3 + \dots + 2^n$.

$$\text{Sum of first } 2^n \text{ natural no.'s.} = \frac{2^n(2^n+1)}{2}$$

$$= \frac{2^{2n} + 2^n}{2} = \frac{4^n + 2^n}{2}$$

$$= \frac{4^n}{2} + \frac{2^n}{2}$$

T.C $\rightarrow O(4^n)$

```

for(i=1; i<=n; i++) {
    for(j=1; j*j <= i; j+=i) {
        }
}

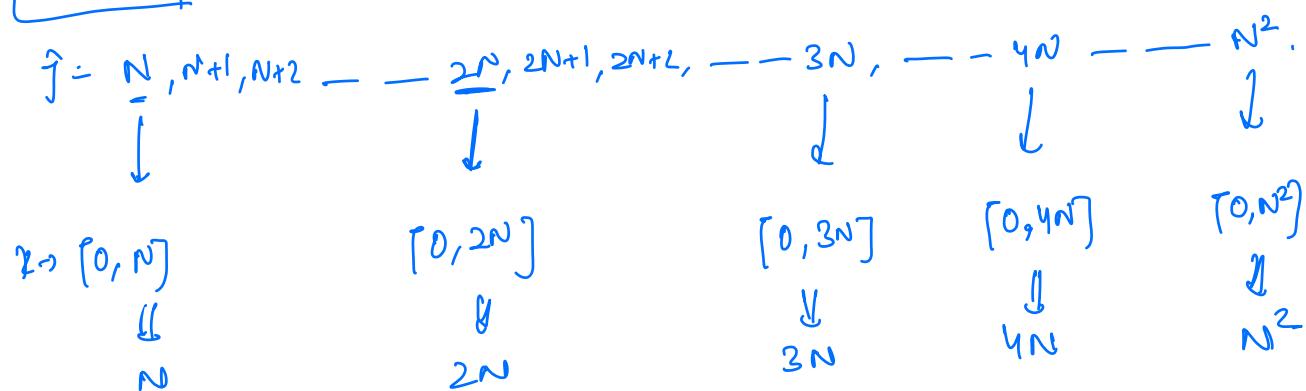
```

$$I \checkmark \\ (1+\sqrt{n})(1+\sqrt{n}) \leq \sqrt{n} .$$

i	j	iterations.
1	[1, 1]	1
2	[1, 1]	1
3	[1, 1]	1
4	[1, 1]	1
5	[1, 1]	1
...
\sqrt{N}	[1, 1]	1

$$\text{iteration} = \sqrt{N} .$$

$i = N$



$$\Rightarrow N + 2N + 3N + 4N + N^2$$

$$\Rightarrow N [(1 + 2 + 3 + 4 + \dots + N)]$$

$$\Rightarrow N \cdot \frac{N(N+1)}{2} \approx \underline{\underline{N^3}}$$

for ($i = 0 ; i \leq n ; i++$) {

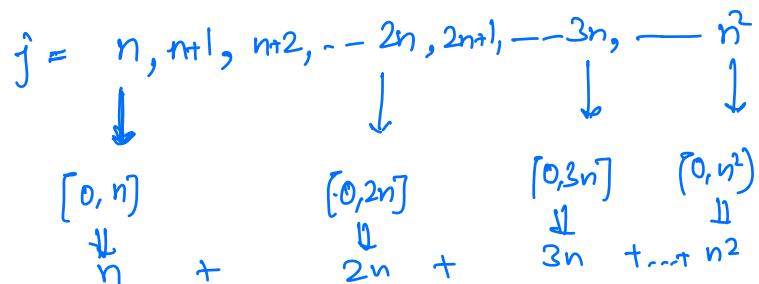
$i = \underline{\underline{n}}$

 for ($j = i ; j < i * i ; j++$) {

 if ($j \times i == 0$) {

 for ($k = 0 ; k < j ; k++$) {

 // print



$$\text{sum} = \underline{\underline{n^3}}$$

```

for( i = 3 ; i < n/3 ; i+=3) {
    for( j = 2 ; j < n/2 ; j+=2) {
        s
    }
}

```

$$i \rightarrow 3, \overset{+3}{\curvearrowright} 6, 9, 12, \dots - \frac{n}{3}$$

i	j	iterations.
3	[2, n/2]	$\frac{n}{4}$
6	[2, n/2]	$\frac{n}{4}$
9	[2, n/2]	$\frac{n}{4}$
12	[2, n/2]	1
$n/3$	[2, n/2]	$\frac{n}{4}$

total no. of iterations = $\underbrace{\frac{n}{4} + \frac{n}{4} + \dots}_{?} - \frac{n}{4}$

$$= \frac{n}{4} \cdot \frac{n}{9} = \frac{n^2}{36}$$

$T.C \rightarrow O(n^2)$

$\text{for } (i=3 ; i < \frac{n}{3} ; i+3) \{$

3

3, 6, 9, 12, 15, $\dots \frac{n}{3}$

$\frac{1}{3} \times \frac{n}{3}, \frac{1}{3} \times 6, \dots \frac{1}{3} \times \frac{n}{3} = \frac{n}{9}$

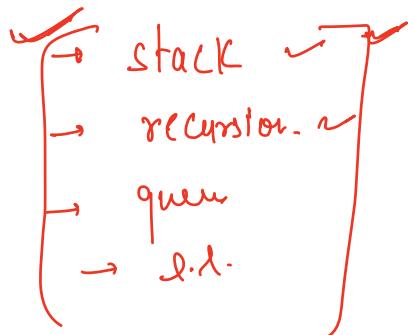
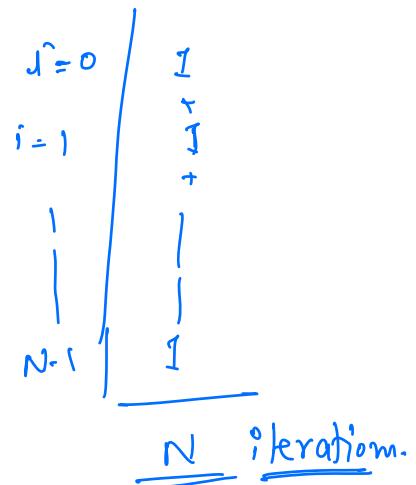
$$\frac{1}{3} \times \frac{n}{3} = \boxed{\frac{n}{9}}$$

$\text{for } (i=0 ; i < N ; i++) \{$

$\text{for } (j=i ; j < N ; j++) \{$

if, break

3



```

for( i=0 ; i < n ; i++) {
    for( j=0 ; j < n ; j++) {
        int sum = 0
        sum += 10
    }
}

```

$i = 0$
 $j = 0$
 $sum = 0$
12 bytes of space.

$S.C \rightarrow O(i)$