

# Supervised Learning

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CSIP5403 – Research Methods and AI Applications

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# Contents

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1. Introduction
2. Supervised Learning Methods
  - Regression
  - Classification
3. Evaluation Metrics
4. Practical Tips on Supervised Learning
5. Applications
6. Conclusion
7. References



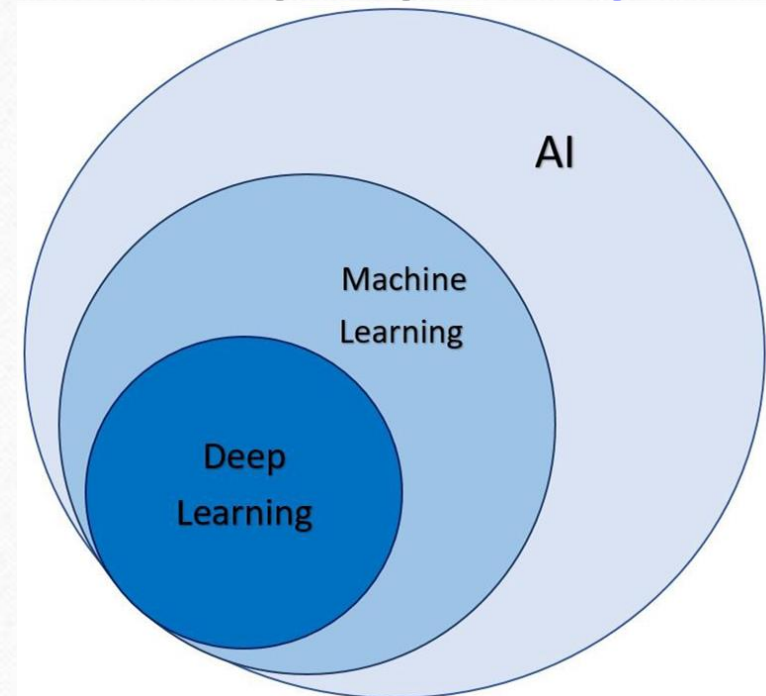
# Session Outcomes

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- Gain awareness of different ML branches.
- Acquire proper understanding of supervised learning methods.
- Understand how to apply supervised learning methods for different applications and how to properly evaluate their performance.

# 1. Introduction

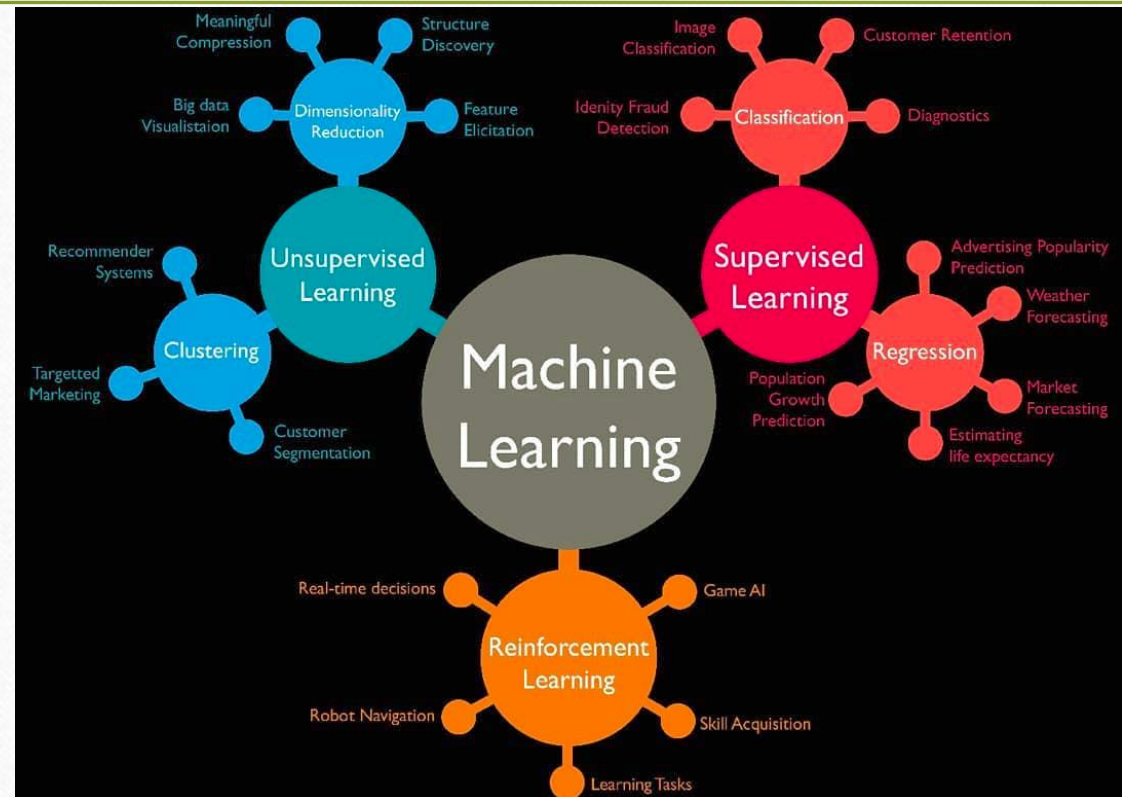
- ML is a branch of AI (a field concerned with designing **intelligent systems**).
- ML algorithms build **models** from training data to make predictions, **without** being explicitly programmed to do so.
- A ML algorithm has **parameters** (**weights**) whose values are learned from training data.





# 1. Introduction

- ML has 3 main branches for different applications:



## 2. Supervised Learning Methods

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- Dataset needs to be **labelled**.
- Each dataset should contain a **good selection of instances** to be representative of the application domain.
- Two types:
  - **Regression** - predicts **continuous** valued output.  
E.g. linear regression, non-linear regression, etc
  - **Classification** - predicts **discrete** valued output.  
e.g. logistic regression, decision trees and ensemble methods, SVM, Neural Networks (Perceptron, MLP, etc.), etc.



## 2. Supervised Learning Methods

- Supervised learning:

Functions  $\mathcal{F}$

$$f : \mathcal{X} \rightarrow \mathcal{Y}$$

Training data

$$\{(x_i, y_i) \in \mathcal{X} \times \mathcal{Y}\}$$

LEARNING

$$\begin{array}{l} \text{find } \hat{f} \in \mathcal{F} \\ \text{s.t. } y_i \approx \hat{f}(x_i) \end{array}$$

Learning machine



PREDICTION

$$y = \hat{f}(x)$$

New data

$x$

## 2. Supervised Learning Methods

- Learning is performed by optimizing a **cost function** using **optimization algorithms**, for instance, using **gradient descent**.

In general Minimize with respect to  $f \in \mathcal{F}$

$$\sum_{i=1}^N l(f(x_i), y_i) + \lambda R(f)$$

- Choose **loss function** for regression, classification, etc. such as MSE loss, CE loss (softmax loss), hinge loss, contrastive loss, etc.
- Choose **regularization function**:  
 $R(f) = \|\mathbf{w}\|_2^2$  for L2 (Ridge)  
 $R(f) = \|\mathbf{w}\|_1$  for L1 (Lasso) - sparse. 8



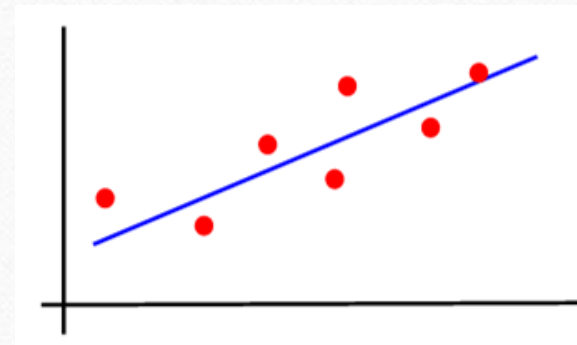
## 2. Supervised Learning Methods

- **Regression:**

- Given a training set of  $N$  observations  $(x_1, \dots, x_N)$  and  $(y_1, \dots, y_N)$ ,  $x_i, y_i \in \mathbb{R}$ , regression problem is to estimate  $f(x)$  from this data.

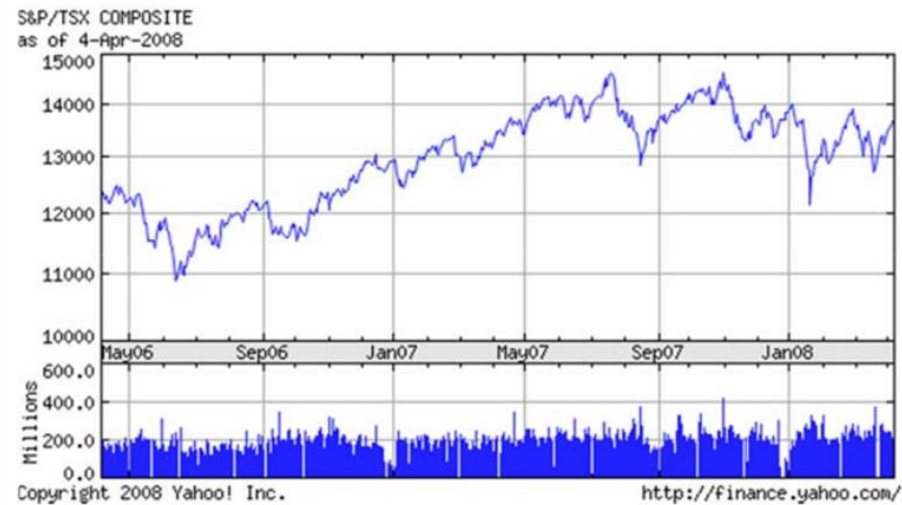
e.g. linear regression

$$f(\mathbf{x}) = \mathbf{w}^T \mathbf{x} + b$$



## 2. Supervised Learning Methods

- **Regression:**
  - Applications include **stock price prediction:**





## 2. Supervised Learning Methods

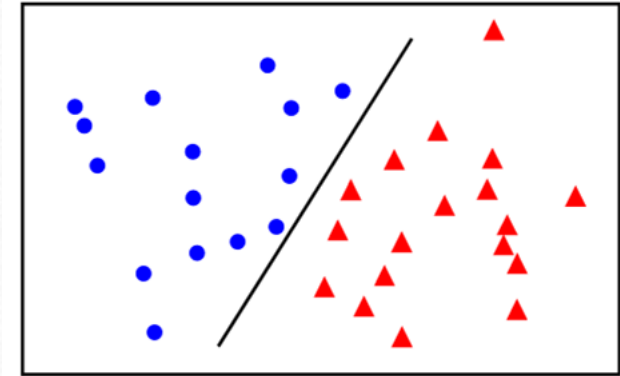
- **Classification:**

- Given a training set of  $N$  observations  $(\mathbf{x}_1, \dots, \mathbf{x}_N)$  and  $(y_1, \dots, y_N)$ ,  $\mathbf{x}_i \in \mathbb{R}^d$ ,  $y_i \in \{-1, 1\}$ , classification problem is to estimate  $f(\mathbf{x})$  from this data.

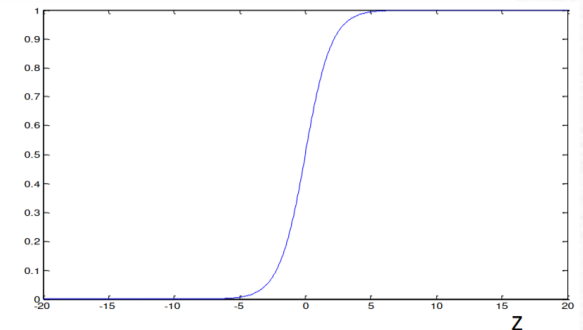
e.g. **logistic regression**

$$f(\mathbf{x}) = \sigma(\mathbf{w}^T \mathbf{x} + b)$$

$\sigma$  is logistic (sigmoid) function



$$\sigma(z) = \frac{1}{1 + e^{-z}}$$



## 2. Supervised Learning Methods

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- **Classification:**

- Multi-class classification - assign input vector  $\mathbf{x}$  into one of  $K$  classes  $C_K$ .
- Build from binary classifiers, e.g. logistic regression (LR). Learn  $K$  two-class **1-vs-the-rest** classifiers  $f_K(\mathbf{x})$  and choose class with most positive score.
- Use **Softmax** which generalizes LR for multiple classes.

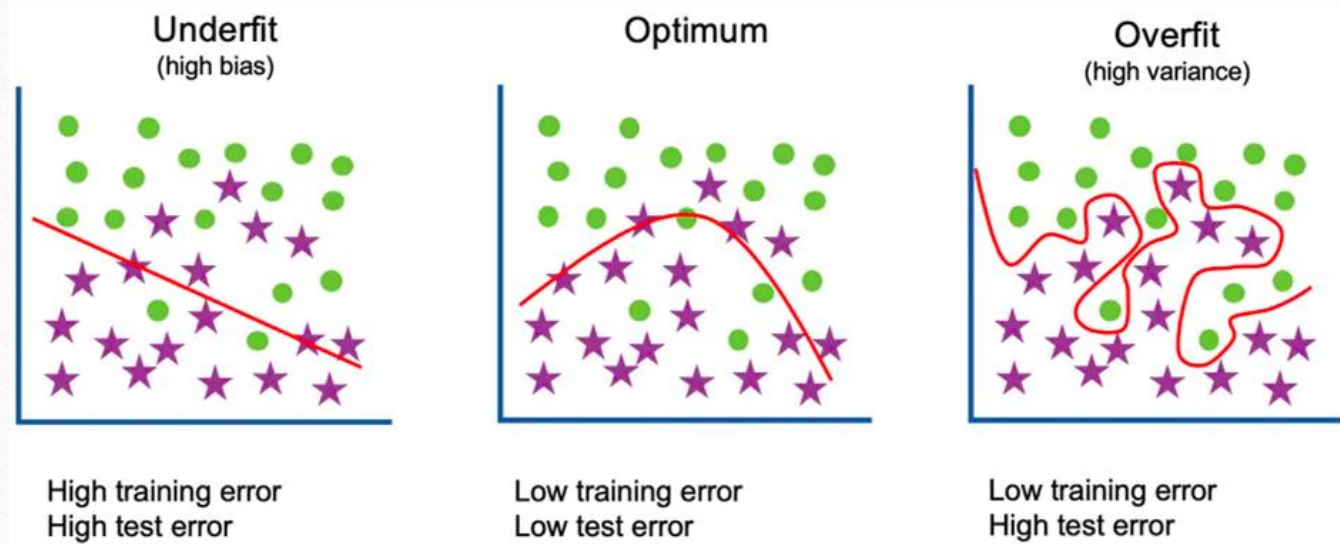
$$P(C_k|\mathbf{x}) = \frac{\exp(f_k(\mathbf{x}))}{\sum_j^K \exp(f_j(\mathbf{x}))} \quad \text{where } f_K(\mathbf{x}) = \mathbf{w}_K^T \mathbf{x} + b_K$$



## 2. Supervised Learning Methods

- **Classification:**

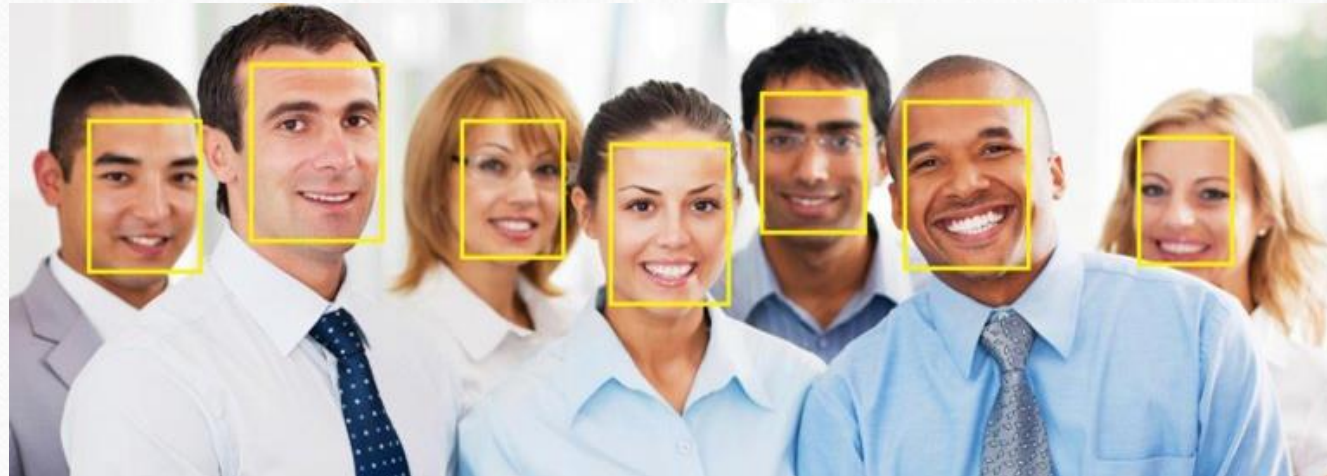
- The complexity of the (discriminant) function needs to be controlled to handle the **generalization** problem.



## 2. Supervised Learning Methods

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- **Classification:**
  - Applications include **face detection**.



→ Classify an image window into **face** and **non-face** classes.



# 3. Evaluation Metrics

- **Evaluation Metrics for Regression:**
  - Mean Squared Error (MSE) – the lower the better.
  - Root Mean Squared Error (RMSE) – the lower the better.
  - Mean Absolute Error (MAE) – the lower the better.
  - $R^2$ , pronounced 'R-squared', computes the **coefficient of determination**, which is the proportion of the variation in the dependent variable that is predictable from the independent variable(s). The higher the better.
- Read more on: <https://medium.com/analytics-vidhya/evaluation-metrics-for-regression-models-c91c65d73af>

# 3. Evaluation Metrics

- **Evaluation Metrics for Classification:**

- Accuracy
- Precision
- Recall
- F1-score
- Confusion matrix:

		Actual Values	
		Positive (1)	Negative (0)
Predicted Values	Positive (1)	TP	FP
	Negative (0)	FN	TN

- Read more on:

<https://medium.com/@impythonprogrammer/evaluation-metrics-for-classification-fc770511052d>



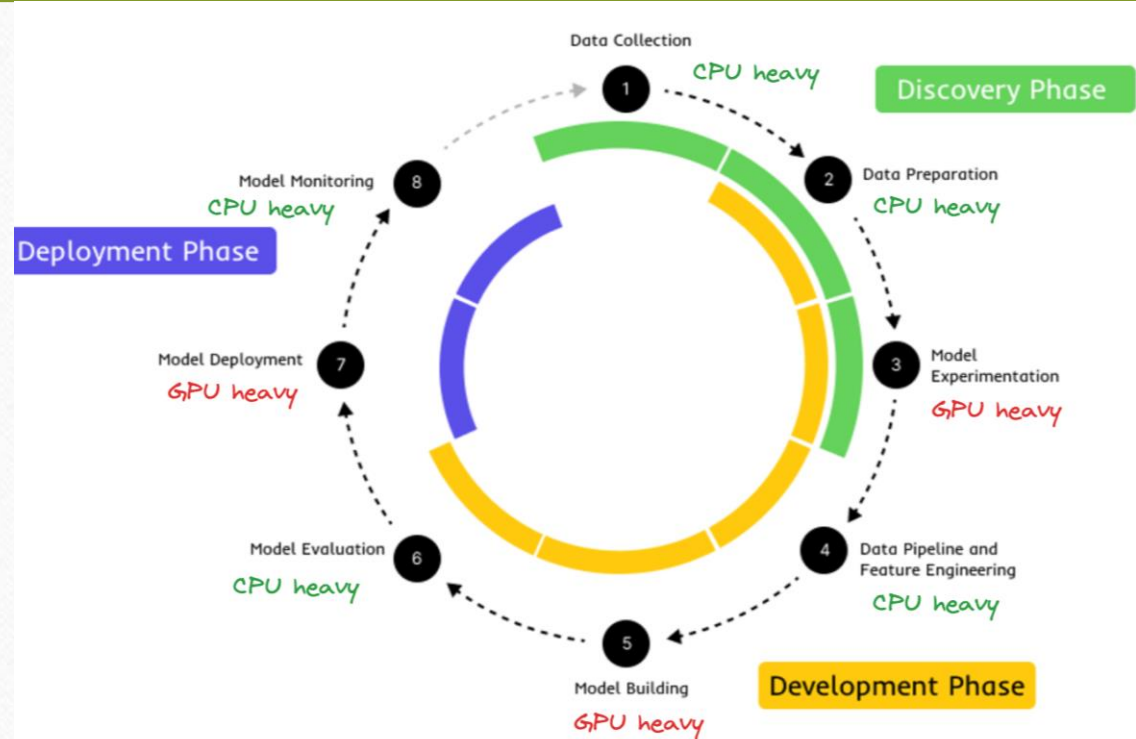
## 4. Practical Tips on Supervised Learning

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- Split the dataset into **training**, **validation** and **test** subsets.
- Choose parameters on **validation** set e.g. cross-validation. The validation and test sets should come from the **same distribution**.
- The aim of supervised learning is to do well on unseen **test data**.
- Handle overfitting using **regularization** (e.g. L1 regularization, L2 regularization) which penalizes **weights with large magnitudes**. Recently introduced regularization methods in deep learning include dropout, batch normalization, etc. **Preprocessing** of input data (normalization or standardization) is necessary in some methods.
- **ML tools**: Scikit-learn, PyTorch, TensorFlow, OpenCV, etc.

## 4. Practical Tips on Supervised Learning

- The **ML** and **Compute** Lifecycle:





# 5. Applications

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- Regression:
  - Stock price prediction,
  - Weather forecasting, ....
- Classification:
  - Face detection,
  - Identity fraud detection, ....
- Can you list **applications** of supervised learning?
- Discuss the **advantages** and **disadvantages** of supervised learning.

## 6. Conclusion

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- ML has 3 main branches for different applications: supervised, unsupervised and reinforcement learning.
- To effectively apply supervised learning methods to different applications, the dataset needs to be labelled and it should contain a good selection of instances to be representative of the application domain.
- It is crucial to properly handle overfitting using regularization methods.



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