

# Advanced Agribusiness Management

Rodney Beard

March 21, 2017

The Diet Problem

Feed-mix problems

Crop rotations

The MOTAD  
(Minimization of  
Total Absolute  
Deviations) model



- ▶ Stigler, George J. The Cost of Subsistence. *Journal of Farm Economics*, vol. 27, no. 2, 1945, pp. 303-314
- ▶ Dantzig, G. (1990). The Diet Problem. *Interfaces*, 20(4), 43-47. Retrieved from <http://www.jstor.org/stable/25061369>
- ▶ El-Nazer, T., McCarl, B. A., 1986. The choice of crop rotation: A modeling approach and case study. *American Journal of Agricultural Economics* 68 (1), 127-136. (available on <http://chla.mannlib.cornell.edu/>).
- ▶ Throsby, C.D. (1967) STATIONARY-STATE SOLUTIONS IN MULTI-PERIOD LINEAR PROGRAMMING PROBLEMS, *Australian Journal of Agricultural Economics*, Volume 11, Number 02, December 1967

## Rodney Beard

## Feed-mix problems

## Crop rotations

The MOTAD  
(Minimization of  
Total Absolute  
Deviations) model

◀ ◻ ▶ ◀ ◻ ▶ ◀ ≡ ▶ ◀ ≡ ▶ ≡

## Rodney Beard

The MOTAD  
(Minimization of  
Total Absolute  
Deviations) model

Nutrient	Daily Recommended Intake
Calories	3,000 Calories
Protein	70 grams
Calcium	.8 grams
Iron	12 milligrams
Vitamin A	5,000 IU
Thiamine (Vitamin B1)	1.8 milligrams
Riboflavin (Vitamin B2)	2.7 milligrams
Niacin	18 milligrams
Ascorbic Acid (Vitamin C)	75 milligrams

## How to mix feed at minimum cost

### Nutritive content and price of ingredients

Ingredient	Calcium (kg/kg)	Protein (kg/kg)	Fiber (kg/kg)	Unit Cost (cents/kg)
Limestone	0.38	0.0	0.0	10.0
Corn	0.001	0.09	0.02	30.5
Soybean meal	0.002	0.50	0.08	90.0

The mixture must meet the following restrictions:

- ▶ Calcium at least 0.8% but not more than 1.2%.
- ▶ Protein at least 22%.
- ▶ Fiber at most 5%.

[http://www.me.utexas.edu/~jensen/or\\_site/models/unit/lp\\_model/blending/blend1.html](http://www.me.utexas.edu/~jensen/or_site/models/unit/lp_model/blending/blend1.html)

## Rodney Beard

## Crop rotations

The MOTAD  
(Minimization of  
Total Absolute  
Deviations) model

Minimum calcium:	0.38L	+ 0.001C	+ 0.002S	> 0.008
Maximum calcium:	0.38L	+ 0.001C	+ 0.002S	< 0.012
Minimum protein:		+ 0.09C	+ 0.50S	> 0.22
Maximum fiber:		+ 0.02C	+ 0.08S	< 0.05
Conservation:	L	+ C	+ S	= 1

# Approaches to modelling crop rotations

- ▶ Multi-period linear programming
- ▶ Dynamic programming
- ▶ Repeated (annual timeless) cropping cycle (using LP)



# Crop rotations: Stationary Linear Programming

Problem a farm grows  $N$  crops and crop yield depends on what was grown on the farm in the previous three years.

Current year is  $i$ , previous years are  $j, k, r$ .

$$\max \sum_{i=1}^N \sum_{j=1}^N \sum_{k=1}^N \sum_{r=1}^N C_{ijkl} X_{ijkl}$$

subject to

$$\sum_{i=1}^N \sum_{j=1}^N \sum_{k=1}^N \sum_r X_{ijkl} \leq TA$$

$$\sum_{i=1}^N X_{ijkl} - \sum_{m=1}^N X_{jkrm} \leq 0, i, j, k = 1, \dots, N$$

$$X_{ijkl} \geq 0$$

The second constraint is a rotation constraint that is equal to zero when continuous cropping occurs, i.e. no rotation takes place.

## Rodney Beard

## Feed-mix problems

## Crop rotations

The MOTAD  
(Minimization of  
Total Absolute  
Deviations) model

[illegible]

Rodney Beard

## The Diet Problem

## Feed-mix problems

## Crop rotations

The MOTAD  
(Minimization of  
Total Absolute  
Deviations) model

Land	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	≤ TA
CCC	0	-1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	≤ 0
CCP	0	1	-1	-1	0	0	0	0	0	1	0	0	0	0	0	0	≤ 0
CPC	0	0	1	0	-1	-1	0	0	0	0	1	0	0	0	0	0	≤ 0
CPP	0	0	0	1	0	0	-1	-1	0	0	0	1	0	0	0	0	≤ 0
PCC	0	0	0	0	1	0	0	0	-1	-1	0	0	1	0	0	0	≤ 0
PCP	0	0	0	0	0	1	0	0	0	0	-1	-1	0	1	0	0	≤ 0
PPC	0	0	0	0	0	0	1	0	0	0	0	0	-1	-1	1	0	≤ 0
PPP	0	0	0	0	0	0	0	1	0	0	0	0	0	0	-1	0	≤ 0

# Solution and discussion

- ▶ Gives area of land to be planted to each crop for each sequence. so  $X_{CCCP}$  is the area of land to be planted to corn following two corn crops and one potato crop.
- ▶ i have not provided gross margins for this problem but nor do the authors.
- ▶ Think about where gross margins  $C_{ijkr}$  might be obtained from.
- ▶ How might one infer the rotation sequence in an area from aggregate data?
- ▶ How would you go about setting this model up in Jupyter using SciPy?

# E-V portfolio model

Start with a portfolio model (quadratic programming, can we turn it into a linear programming model)

$$\min \sum_{j=1}^n \sum_{k=1}^n x_j x_k \sigma_{jk}$$

such that

$$\sum_{j=1}^n f_j x_j = \lambda$$

$$\sum_{j=1}^n a_{ij} x_j \leq b_i$$

$$x_j \geq 0$$

The Diet Problem

Feed-mix problems

Crop rotations

The MOTAD  
(Minimization of  
Total Absolute  
Deviations) model

- ▶  $x_i$  level of the  $i$ -th farm activity
- ▶  $f_j$  the expected or forecast gross margin
- ▶  $\sigma_{jk}$  the covariance of the gross margin between the  $j$ -th and  $k$ -th farm activity
- ▶  $a_{ij}$  how much the  $j$ -th activity utilizes of the  $i$ -th resource
- ▶  $b_i$  availability of the  $i$ -th resource

# Advantages of the E-V model

- ▶ consistent with probability if gross margins are normally distributed
- ▶ subjective probability values may be used
- ▶ consistent with the separation theorem