# **UG9001**

# **FPGA FFT Library**

**User guide** 

v0.1

**DRAFT** 

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# Introduction

The OwOComm FFT library implements several FFT architectures including Single Path Delay Feedback (SPDF) and Bailey's 4-step FFT. Multiple architectures may be combined to form a hybrid FFT core. Large FFTs in external memory are supported. Cores are generated using a code generator.

### **Features**

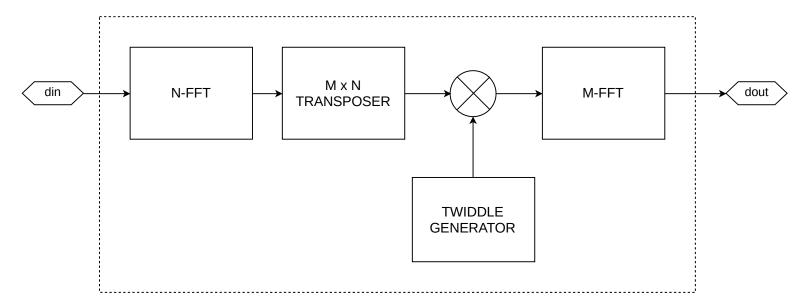
- Power of 2 FFT sizes
- Fixed point
- Scaling options: unscaled, divide by N, divide by sqrt(N)
- Rounding or truncation after each butterfly
- Large FFT sizes (up to 1G points) using external memory via AXI interface
- Automatically generated wrappers for natural order input/output
- Support for multiple interleaved channels in generated wrapper
- Optimized for data width up to 35 bits and twiddle width up to 24 bits
- Optimized for Xilinx® 7-series, Ultrascale, and Ultrascale+ FPGA families

# **Architectural overview**

# Bailey's 4-step FFT

The Cooley-Tukey algorithm can be most generally described as subdividing a size N\*M FFT into sub-FFTs of size N and M. M FFTs of size N are performed on the input data, the results are rotated by various angles (multiplication by roots of unity or twiddle factors), and finally N FFTs of size M are performed.

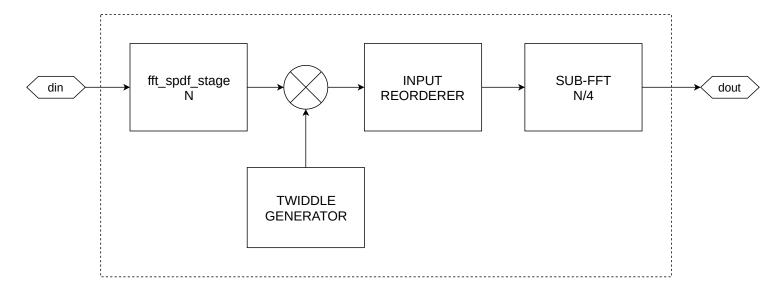
More precisely, the input data in natural order is put into a M columns by N rows matrix in row-major order. FFTs are performed on the columns, the resulting matrix is multiplied by twiddle factors, and FFTs are then performed on the rows. The results (in natural order) are read from the matrix in column major order.



Input and output transpose steps are omitted and data input/output are in transposed order. However because the sub-FFTs may take data in non-natural order, the final input and output order is best described as an address bit permutation. Generated FFT cores will have this permutation in the code comments, and generated reorderers will take care of correct data ordering.

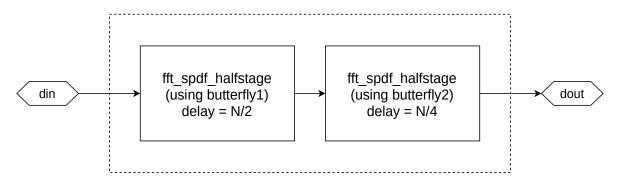
# Single Path Delay Feedback (SPDF)

The SPDF FFT architecture is conceptually similar to the Bailey's formulation in that input data is viewed as a M x 4 matrix, butterfly operations are performed on the columns, and a size M sub-FFT is performed.



#### fft\_spdf\_stage

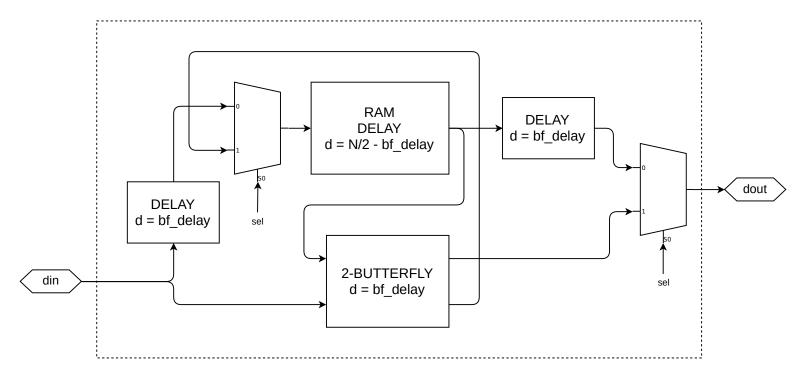
The SPDF butterfly stage is split into two stages, each regrouping its input data into a M  $\times$  2 matrix, performing 2-butterfly operations on its columns, and reading out the rows.



 Functionally equivalent to Nx4 transposer followed by 4-FFT followed by 4xN transposer

#### fft\_spdf\_halfstage

The SPDF half stage performs a 2-butterfly operation on the columns of a M  $\times$  2 matrix input in row major order, while also outputting the results in row major order.



During the first half of the frame (first N/2 cycles), sel is set to 0. Old data is flushed out while the first row of input fills the delay memory.

During the second half (next N/2 cycles) sel is 1 and the butterfly is active, reading the first row from the delay memory concurrently with the second row being input from din. The upper butterfly output (logically first row) is output to dout while the lower output (second row) is stored into the delay line, to be flushed out next frame.

# **Designing with the core**

# **Library primitives**

To use the library it is required to import the fft\_types package: use work.fft\_types.all;

#### **Data types**

Complex values throughout the library are represented using the complex type, which is defined as:

```
-- maximum supported bit width of the signed integers in a complex value.
constant COMPLEXWIDTH: integer := 48;

type complex is record
    re: signed(COMPLEXWIDTH-1 downto 0);
    im: signed(COMPLEXWIDTH-1 downto 0);
end record;
```

COMPLEXWIDTH limits the maximum precision of a complex value. In FFT cores the precision is further limited by a configurable data bits parameter.

The following operators are defined for the complex type:

```
function "+" (Left, Right: complex) return complex;
function "-" (Left, Right: complex) return complex;
function "-" (Right: complex) return complex;
function "*" (Left: complex; Right: integer) return complex;
function "/" (Left: complex; Right: integer) return complex;
function to_complex (re,im: integer) return complex;
function to_complex (re,im: signed) return complex;
function complex_re(val: complex; bits: integer) return signed;
function complex_im(val: complex; bits: integer) return signed;
```

# **Clocking and data framing**

The generated cores run from a single clock and has no clock enable input. To gate the operation of the core it is required to use clock gating (e.g. using a BUFGCE).

Data input is synchronized with and framed by the phase signal, which is required to be a monotonically increasing counter that wraps around at one frame length. When phase = 0, din should be set to the 0<sup>th</sup> complex value in this frame.

Data output follows data input after a fixed delay. The delay is documented in the code comments in all generated cores.

Phase is required to be monotonic for at least 32 cycles before the input of the first value in a frame, and remain monotonic until the output for that frame is complete for that frame to be considered valid. Violating this requirement can lead to incorrect data output but the core can be reset by restarting the phase counter at N-32.

# **Generating cores**

# gen\_fft.py

This is the main FFT core generator which generates cores, reorderers, and wrappers.

To generate the code for one of the layout definitions, run:

```
./gen_fft.py fft INSTANCE_TO_GENERATE
```

For example:

```
./gen_fft.py fft fft1024_wide
```

To generate input/output reorderers for a FFT core instance, run:

```
./gen_fft.py reorderer INSTANCE_TO_GENERATE
```

To generate natural order wrappers, run:

```
./gen_fft.py wrapper INSTANCE_TO_GENERATE
```

# **Composing FFT layouts**

There are several predefined layouts in gen\_fft\_layouts.py. You can add new FFT sizes or custom layouts by editing this file.

An example of a layout definition:

An FFT layout definition is simply an instance of one of the composite FFT classes, which are FFT4Step and FFTSPDF.

#### FFT4Step

FFT4Step represents a Bailey's 4-step FFT, which combines two sub-FFTs of size M and N to form a larger FFT of size M \* N.

#### **Constructor arguments**

- N integer FFT size.
- sub1 object sub-FFT instance 1. Can be a base FFT, FFT4Step, or FFTSPDF.
- sub2 object sub-FFT instance 2. Can be a base FFT, FFT4Step, or FFTSPDF.
- multiplier object multiplier type to use for twiddle multiplication. Must be an instance of gen\_fft\_modules.Multiplier. Built in instances are defaultMult (generic inferred RTL multiply) and largeMult (uses 2 DSP48E1s for a 25x35 multiplier). It is recommended to leave this unset and to set this value recursively using setMultiplier().
- twiddleBits integer precision of the twiddle generator. It is recommended to leave this unset. The default value is 'twBits' and twiddle precision takes on the value of the top level entity parameter 'twBits'.

#### Methods

- setMultiplier (multiplier, recursive=True) sets the twiddle multiplier. See above for a description of the multiplier argument. If recursive is true this will affect sub-FFT instances as well.
- delay() returns the total delay in clock cycles of this FFT core.
- inputBitOrder() returns the input data order as an address bit permutation (list of integers)
- outputBitOrder() returns the output data order as an address bit permutation (list of integers)

#### **FFTSPDF**

FFTSPDF represents a Single Path Delay Feedback FFT. The sub-FFT must have a size of N/4. The internal 4-butterfly does not do any scaling. If scaling is required it must be done in the sub-FFT.

#### **Constructor arguments**

- N integer FFT size.
- sub1 object sub-FFT instance 1. Can be a base FFT, FFT4Step, or FFTSPDF.
- multiplier object see FFT4Step
- twiddleBits object see FFT4Step

#### Methods

- setMultiplier(multiplier, recursive=True) sets the twiddle multiplier. See FFT4Step for a description of the multiplier argument.
- delay() returns the total delay in clock cycles of this FFT core.
- inputBitOrder() returns the input data order as an address bit permutation (list of integers)
- outputBitOrder() returns the output data order as an address bit permutation (list of integers)

#### **Base FFT instances**

These are to be used as the base cases when composing a larger FFT core.

The base FFT instances are:

- fft2\_scale\_none A size 2 FFT. No scaling is performed.
- fft2\_scale\_div\_n A size 2 FFT. Scales by ½.
- fft4\_scale\_none A size 4 FFT. No scaling is performed.
- fft4\_scale\_div\_sqrt\_n A size 4 FFT. Scales by ½.
- fft4\_scale\_div\_n A size 4 FFT. Scales by 1/4.

#### Methods

These methods apply to all base FFT instances:

- delay() returns the delay in clock cycles of this FFT butterfly.
- inputBitOrder() returns the input data order as an address bit permutation (list of integers)
- outputBitOrder() returns the output data order as an address bit permutation (list of integers)

#### **Layout recommendations**

When composing a new layout, the following should be considered:

- Is natural order input required? If both input and output are allowed to be in arbitrary order (defined by an address bit permutation) it is recommended to use FFT4Step throughout.
- Are multiple (interleaved) channels required? If so, reorder memory is required on both input and output side, and input/output reordering comes at no additional memory usage. Therefore using FFT4Step may still be indicated.
- FFTSPDF provides the lowest memory usage when input must be in natural order and is single channel.
- FFT4Step provides the lowest LUT usage but both data input and output are in non-linear order, therefore reorderers may be required.

When composing a natural order input single channel FFT, use one or two layers of FFTSPDF and switch to FFT4Step for the next sub-FFT.

When composing a layout using FFT4Step, the following should be considered:

- Keep the size of sub1 and sub2 close to sqrt(N) for minimal memory usage.
- If sub1 and sub2 must be different sizes (e.g. non-perfect-square N), sub2 should be the smaller sub-FFT. There is a reorderer before sub-FFT2 because the FFT4Step twiddle address generator requires linear column order (to avoid using a multiplier).

## **Generated FFT core description**

#### **Parameters**

• dataBits – integer

The input and output precision. A dataBits of 12 means 12 bits real and 12 bits imaginary.

• **twBits** – integer

The twiddle ROM precision.

The internal twiddle multipliers see a width of twBits + 1. If targeting a A\*B size multiplier, set twBits to A-1. For example to target a dual DSP48E1 25x35 multiplier implementation, dataBits should be <= 35, and twBits should be <= 24 (or vice versa).

• inverse – boolean

Set to true for inverse transform (twiddle phase  $2\pi ij/N$ ) or false for forward transform (twiddle phase  $-2\pi ij/N$ )

#### **Ports**

- **clk** std\_logic The input clock that all ports are synchronous to.
- din complex Input data
- phase unsigned A monotonically increasing counter that is synchronized with din
- dout complex Output data

# **Generated reorderer description**

Entity naming: INSTANCENAME\_ireordererN, where INSTANCENAME is the name of the FFT layout instance in the python file and N is the number of interleaved channels. ireorderer is the input reorderer and oreorderer is the output reorderer.

```
-- phase should be 0,1,2,3,4,5,6,...
-- delay is XXX
entity INSTANCENAME_ireorderer1 is
     generic(dataBits: integer := 24);
     port(clk: in std_logic;
           din: in complex;
           phase: in unsigned(...);
           dout: out complex
end entity;
-- phase should be 0,1,2,3,4,5,6,...
-- delay is XXX
entity INSTANCENAME_oreorderer1 is
     generic(dataBits: integer := 24);
     port(clk: in std_logic;
           din: in complex;
           phase: in unsigned(...);
           dout: out complex
           );
end entity;
```

#### **Parameters**

• dataBits – integer
The data width. A dataBits of 12 means 12 bits real and 12 bits imaginary.

#### **Ports**

- **clk** std\_logic The input clock that all ports are synchronous to.
- din complex Input data
- phase unsigned A monotonically increasing counter that is synchronized with din
- dout complex Output data