Advice for applying machine learning

Deciding what to try next

Debugging a learning algorithm:

Suppose you have implemented regularized linear regression to predict housing prices.

$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^{m} \theta_j^2 \right]$$

However, when you test your hypothesis on a new set of houses, you find that it makes unacceptably large errors in its predictions. What should you try next?

X1, X2, X3, ..., 7100

- -> Get more training examples
 - Try smaller sets of features
- -> Try getting additional features
 - Try adding polynomial features $(x_1^2, x_2^2, \underline{x_1}\underline{x_2}, \text{etc.})$
 - Try decreasing λ
 - Try increasing λ

Machine learning diagnostic:

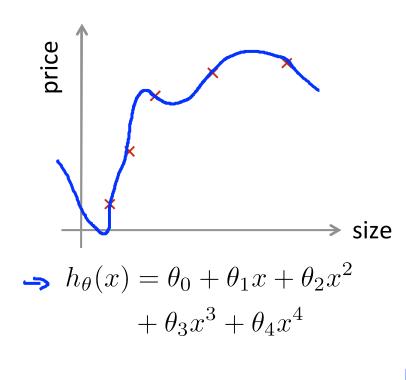
Diagnostic: A test that you can run to gain insight what is/isn't working with a learning algorithm, and gain guidance as to how best to improve its performance.

Diagnostics can take time to implement, but doing so can be a very good use of your time.

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Evaluating a hypothesis

Evaluating your hypothesis

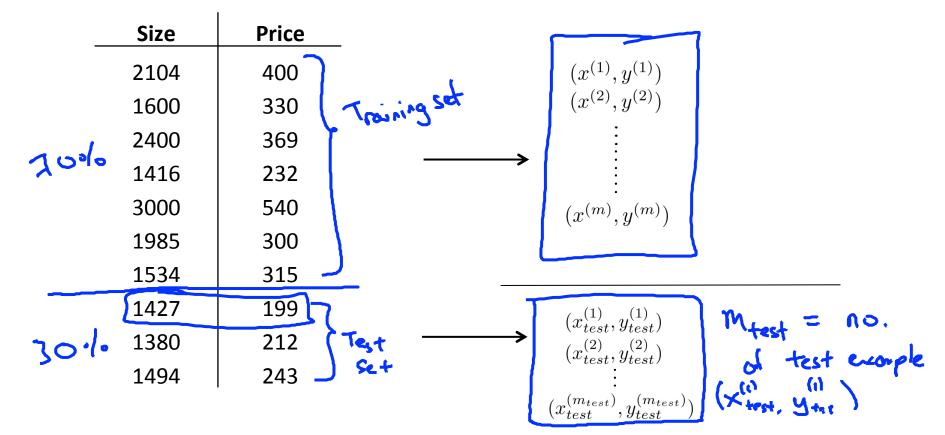


Fails to generalize to new examples not in training set.

```
x_1= size of house x_2= no. of bedrooms x_3= no. of floors
x_4 = age of house
x_5 =  average income in neighborhood
x_6 = kitchen size
```

Evaluating your hypothesis

Dataset:



Training/testing procedure for linear regression

 \rightarrow - Learn parameter θ from training data (minimizing training error $J(\theta)$)

- Compute test set error:

$$\frac{1}{1+est}(6) = \frac{1}{2m_{test}} \left(\frac{h_0(x_{test}) - y_{test}}{1+est}\right)^2$$

Training/testing procedure for logistic regression

- Learn parameter heta from training data
- Compute test set error:

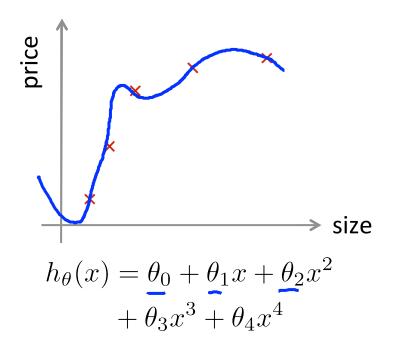
$$J_{test}(\theta) = -\frac{1}{m_{test}} \sum_{i=1}^{m_{test}} y_{test}^{(i)} \log h_{\theta}(x_{test}^{(i)}) + (1 - y_{test}^{(i)}) \log h_{\theta}(x_{test}^{(i)})$$

- Misclassification error (0/1 misclassification error):

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Model selection and training/validation/test sets

Overfitting example



Once parameters $\theta_0, \theta_1, \ldots, \theta_4$ were fit to some set of data (training set), the error of the parameters as measured on that data (the training error $J(\theta)$) is likely to be lower than the actual generalization error.

Model selection

d: degree of polynomial

3.
$$h_{\theta}(x) = \theta_0 + \theta_1 x + \cdots + \theta_3 x^3 \longrightarrow \mathfrak{I}_{\text{tot}}(\mathfrak{S}^{(n)})$$

$$\vdots$$

$$\vdots$$

$$h_{\theta}(x) = \theta_0 + \theta_1 x + \cdots + \theta_{10} x^{10} \longrightarrow \mathfrak{I}_{\text{tot}}(\mathfrak{S}^{(n)})$$

Choose
$$\theta_0 + \dots \theta_5 x^5$$

How well does the model generalize? Report test set

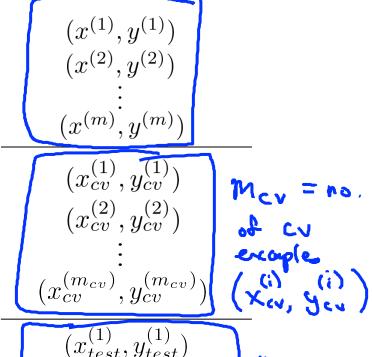
error $J_{test}(\theta^{(5)})$.

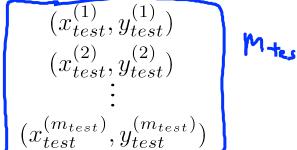
Problem: $J_{test}(\theta^{(5)})$ is likely to be an optimistic estimate of generalization error. I.e. our extra parameter $(\underline{d} = \text{degree of polynomial})$ is fit to test set.

Evaluating your hypothesis

Dataset:

	Size	Price	1
60%	2104	400	
	1600	330	
	2400	369 Trainy set	
	1416	232	
	3000	540	7
	1985	300	
20%	1534	315 7 Cross variation	
	1427	199	
70.1	1380	212 } test set	→
20 4	1494	243	





Train/validation/test error

Training error:

$$\rightarrow J_{train}(\theta) = \frac{1}{2m} \sum_{i=1} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$
 (6)

Cross Validation error:

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

Test error:

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{\infty} (h_{\theta}(x_{test}^{(i)}) - y_{test}^{(i)})^2$$

Model selection

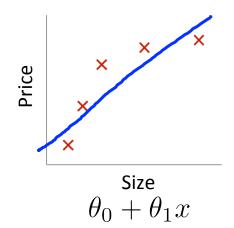
Pick
$$\theta_0 + \theta_1 x_1 + \dots + \theta_4 x^4 \leftarrow$$

Estimate generalization error for test set $J_{test}(\theta^{(4)})$ \longleftarrow

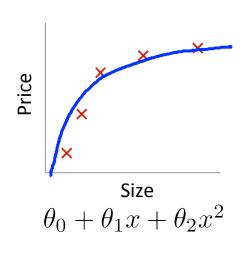
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Diagnosing bias vs. variance

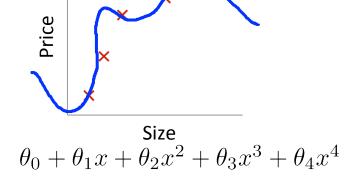
Bias/variance



High bias (underfit) 2=1



"Just right"

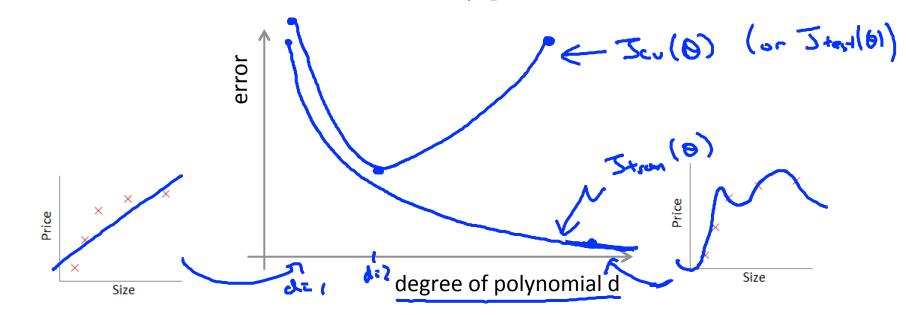


High variance (overfit)

Bias/variance

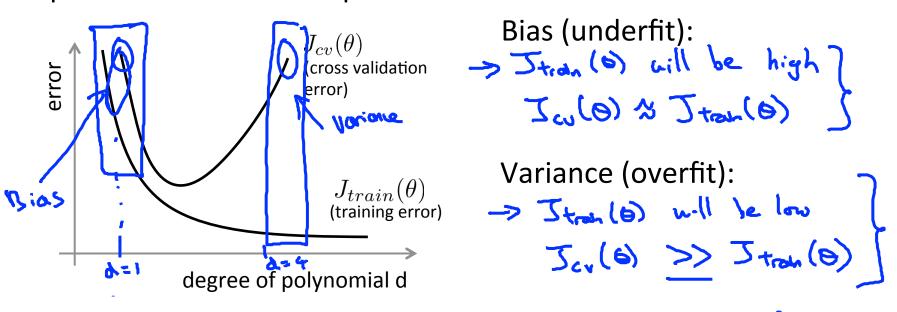
Training error:
$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{n} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Cross validation error:
$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$



Diagnosing bias vs. variance

Suppose your learning algorithm is performing less well than you were hoping. ($J_{cv}(\theta)$ or $J_{test}(\theta)$ is high.) Is it a bias problem or a variance problem?

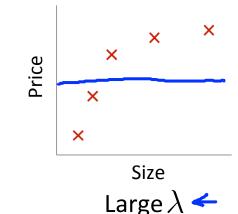


Advice for applying machine learning

Regularization and bias/variance

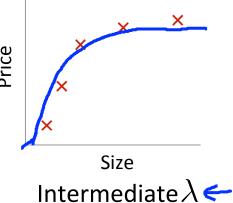
Linear regression with regularization

$$\text{Model: } \boxed{ h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4 } \\ = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \boxed{ \frac{\lambda}{2m} \sum_{j=1}^m \theta_j^2 } \\ <$$

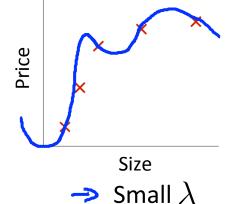


High bias (underfit)

 $\lambda = 10000. \ \theta_1 \approx 0, \theta_2 \approx 0, \dots$



"Just right"



High variance (overfit)

Choosing the regularization parameter λ

$$h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2m} \sum_{j=1}^{m} \theta_j^2$$

$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

7(0)

$$J_{cv}(\theta) = rac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

$$J_{test}(\theta) = rac{1}{2m_{test}} \sum_{m_{test}}^{m_{test}} (h_{\theta}(x_{test}^{(i)}) - y_{test}^{(i)})^2$$
Thus

$$\frac{1}{m_{test}} \sum_{m_{test}}^{m_{test}} (h_{\theta}(x_{test}^{(i)}) - y_{test}^{(i)})^2$$

Choosing the regularization parameter λ

Model:
$$h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2m} \sum_{i=1}^{m} \theta_j^2$$

1. Try
$$\lambda = 0 \leftarrow \gamma \longrightarrow \min J(\Theta) \rightarrow \Theta'' \longrightarrow J_{co}(\Theta'')$$

1. Try
$$\lambda = 0 \leftarrow 1$$
 \longrightarrow $\min \mathcal{I}(\Theta) \rightarrow \Theta^{(1)} \rightarrow \mathcal{I}_{Cu}(\Theta^{(11)})$
2. Try $\lambda = 0.01$ \longrightarrow $\Im_{Cu}(\Theta^{(1)}) \rightarrow \Im_{Cu}(\Theta^{(1)})$
3. Try $\lambda = 0.02$ \longrightarrow $\Im_{Cu}(\Theta^{(1)})$
4. Try $\lambda = 0.04$ \longrightarrow $\Im_{Cu}(\Theta^{(1)})$
5. Try $\lambda = 0.08$

4. Try
$$\lambda = 0.02$$

$$0.04$$

Try
$$\lambda = 0.08$$

:

Try $\lambda = 10$

Pick (say) $\theta^{(5)}$. Test error: $\mathcal{T}_{\text{test}} \left(\mathbf{S}^{(5)} \right)$

Bias/variance as a function of the regularization parameter $\,\lambda\,$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2} + \frac{\lambda}{2m} \sum_{j=1}^{m} \theta_{j}^{2}$$

$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

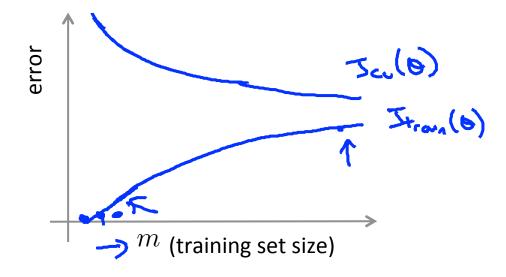
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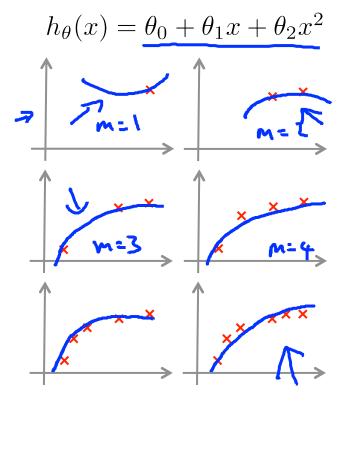
Learning curves

Learning curves

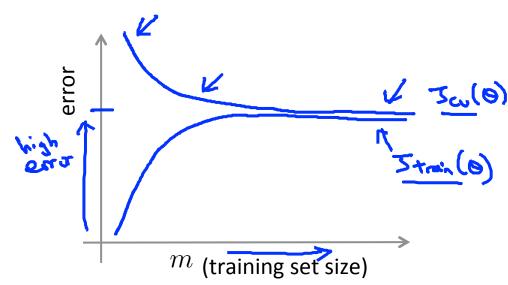
$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

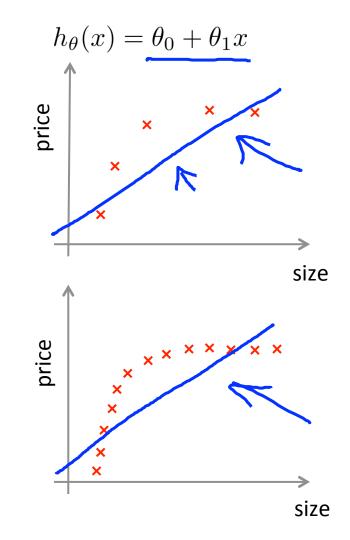




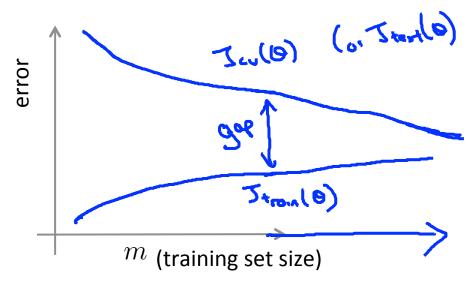
High bias



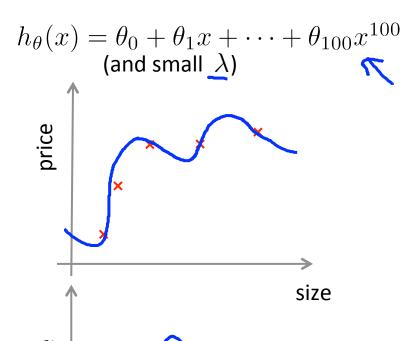
If a learning algorithm is suffering from high bias, getting more training data will not (by itself) help much.

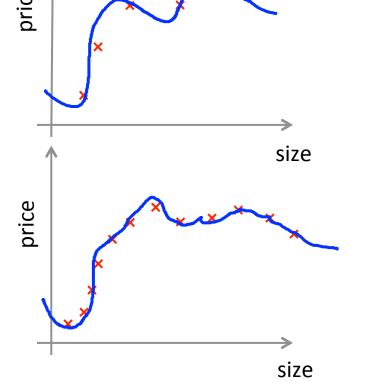


High variance



If a learning algorithm is suffering from high variance, getting more training data is likely to help. <





Advice for applying machine learning

Deciding what to try next (revisited)

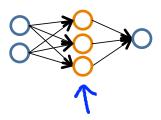
Debugging a learning algorithm:

Suppose you have implemented regularized linear regression to predict housing prices. However, when you test your hypothesis in a new set of houses, you find that it makes unacceptably large errors in its prediction. What should you try next?

- Get more training examples -> fixe high vorione
- Try smaller sets of features -> Fixe high voice
- Try getting additional features -> free high bias
- Try adding polynomial features $(x_1^2, x_2^2, x_1x_2, \text{etc}) \rightarrow \{$
- Try decreasing λ fixes high high
- Try increasing λ -> fixes high various

Neural networks and overfitting

"Small" neural network (fewer parameters; more prone to underfitting)



Computationally cheaper

"Large" neural network (more parameters; more prone to overfitting)

Computationally more expensive.

Use regularization (λ) to address overfitting.

