

# Probabilistic framework for integration of mass spectrum and retention time information in small molecule identification

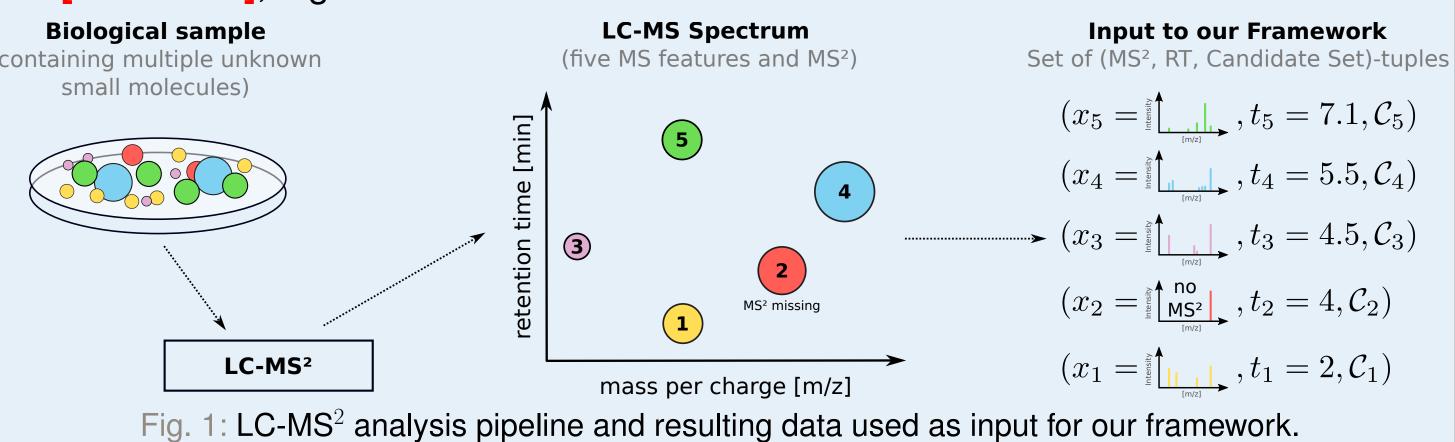


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# Small Molecule Identification in Untargeted Metabolomics

- Liquid chromatography (LC) coupled with tandem mass spectrometry (MS<sup>2</sup>) widely utilized in untargeted metabolomics studies
- Challenge: Annotation of LC-MS peaks with potential molecular structures
- Most automated machine learning based approaches utilize MS information only [CITATION]
- LC retention time (RT) is valueable additional information for the annotation [CITATION], e.g.



## Retention Time (RT) Utilization

- Multiple approaches to utilize RT for molecule annotation exist
- (utilization of RT information, scalable, cross laboratories (LC-systems), RT reference free)
- 1) Compare measured RTs with in-house reference RTs
- 2) Compare measured RTs with projected reference RTs
- 3) Compare measured RTs with predicted RTs
- 4) Compare measured RTs with predicted RTs proxies, e.g. LogP
- 5) Compare measured retention orders with predicted ones
- Fully supported: ✓, Partially supported: ●, Not supported: ✗
- RT comparison to prune candidate lists or (re)ranking [CITATION]

# **LC-MS Experiment Data and its Formal Representation**

- Assume data arises from LC-MS experiment (after peak-picking and alignment)
- Available information:  $MS^1$ , RT and (etwaige only for some peaks)  $MS^2$
- Molecular candidate lists are assumed to be given as well
- MS<sup>2</sup>scores, e.g. MetFrag [CITATION] or CSI:FingerID [CITATION], computed
- Data from LC-MS considered as set of N MS features:

$$\mathcal{D} = \{(x_i, t_i, \mathcal{C}_i)\}_{i=1}^{N}$$

- $x_i$ : MS<sup>2</sup> spectrum (or MS<sup>1</sup>, if no fragmentation available)
- t<sub>i</sub>: Measured RT
- $C_i$ : Potentail molecular annotations for feature i, e.g. exact mass search

# **Probabilistic Framework to integrate MS and Retention Orders**

- Definition of a probabilistic graphical model superimposed on the LC-MS data
- Let G = (E, V) be a complete graph
- Nodes  $i \in V$  represent the MS features, Edes  $(i, j) \in E$  the feature pairs
- Association of each node with discrete random variable  $z_i \in \mathcal{Z}_i = \{1, \dots, n_i\}$   $(n_i = |\mathcal{C}_i| \text{ number of candidates})$
- Molecule annotation for complete data  $\mathbf{z} = \{z_i \mid i \in V\} \in \mathcal{Z}_1 \times \ldots \times \mathcal{Z}_N = \mathbf{Z}_N$
- Intuitively: Random variable denotes which candidate is assigned to each feature.
- Pairwise Markov Random Field as probabilsitic model ?:

$$p(\mathbf{z}) = \frac{1}{Z} \prod_{i \in V} \psi_i(z_i) \prod_{(i,j) \in E} \psi_{ij}(z_i, z_j)$$

Ranking molecular candidates via max-marginals:

$$p_{\max}(z_i = r) = \max_{\{\mathbf{z}' \in \mathcal{Z} \mid z_i' = r\}} p(\mathbf{z}')$$

- Intuitively, maxmimum probabilsity a candidate assignment with  $z_i=r$  can achive
- Rank all candidates  $r \in \{1, \dots, n_i\}$  according to there max-marginals

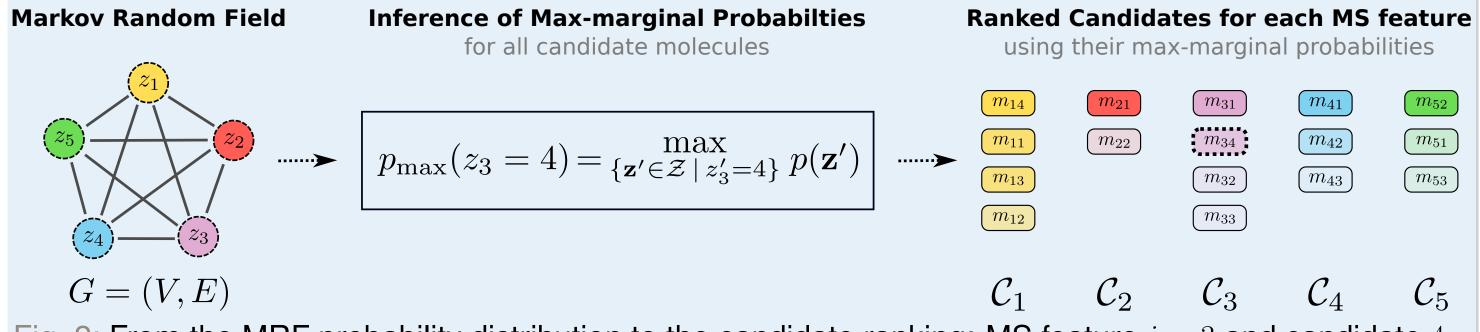


Fig. 2: From the MRF probability distribution to the candidate ranking: MS feature i=3 and candidate 4  $(m_{34})$ .

# **Node and Edge Potentials**

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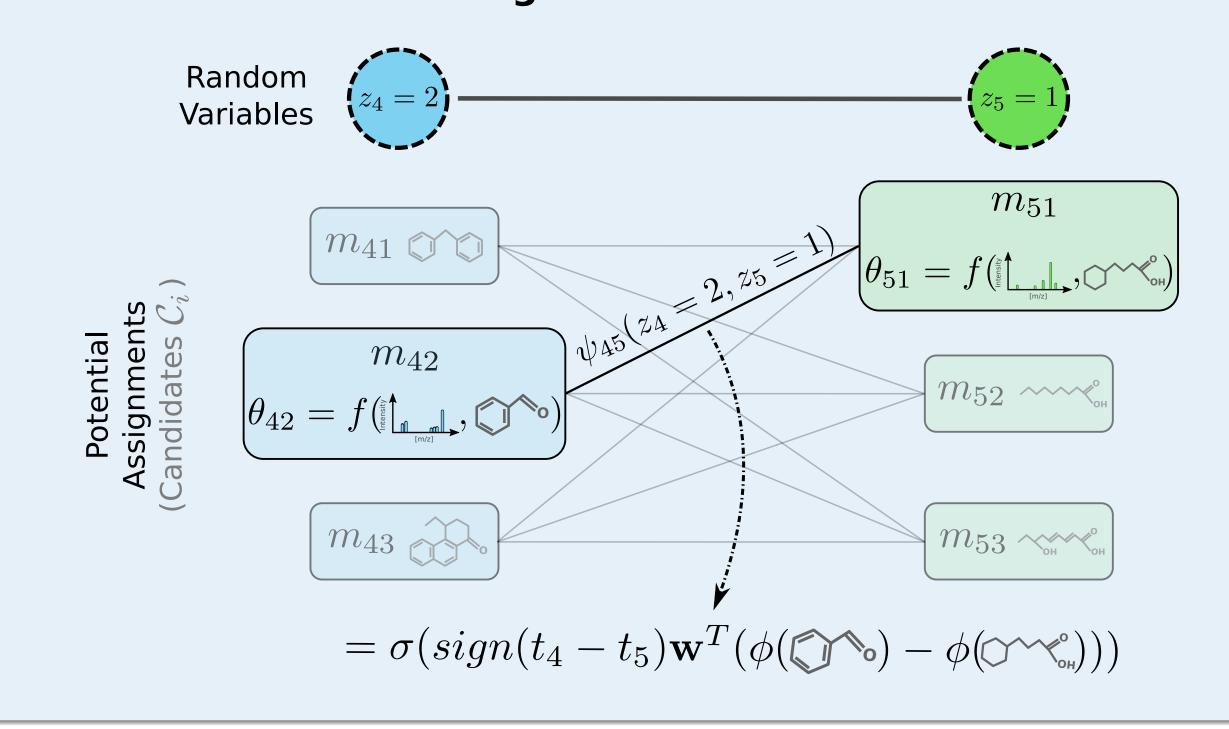
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- Node potential function  $\psi_i: \mathcal{Z}_i \to \mathbb{R}_{>0}$ : goodness of the match between measured spectrum  $x_i$  and candidates of feature i
- Edge potential function  $\psi_{ij}: \mathcal{Z}_i \times \mathcal{Z}_j \to \mathbb{R}_{>0}$ : consistency between the observed retention order of feature i and j with the predicted retention order of the candidates  $z_i$  and  $z_j$

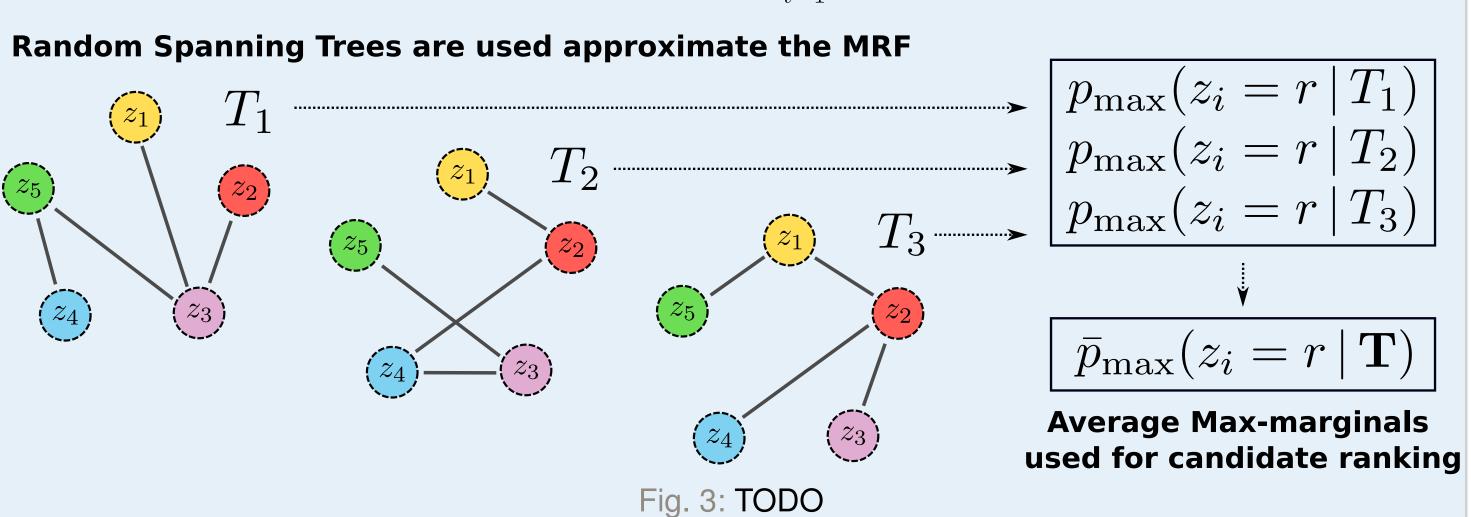
# Node and Edge Potential Calculation



### **Spanning Tree Approximation**

- $\bullet$  Marginal inference intractable in practice due to exponentail sized candidate assignment space  $\mathcal Z$
- Exact inference is feasible if G is tree-like [CITATION]
- Resort to infer the max-marginals a set of trees  $\mathbf{T} = \{T_t\}_{t=1}^L$  sampled from G
- Each tree  $T_t = (V, E_t)$  is connected graph with all nodes of G but reduces edges set  $E_t \subseteq E$
- Avergaged marginals used for ranking

$$\bar{p}_{\max}(z_i = r \mid \mathbf{T}) = \frac{1}{L} \sum_{t=1}^{L} p_{\max}(z_i = r \mid T_t)$$



# 5. Experiments and Results

- Dataset description
- Show table 4 from the paper
- Show figure 3 from the paper

#### References