

Recurrent Neural Networks

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A Bird's Eye View Of Classical Neural Networks

- ▶ The task is to model functions $f : A \rightarrow B$, where A and B are sets, using functions $\mathbb{R}^n \rightarrow \mathbb{R}^m$.
- ▶ A neural network is a fancy way to describe a class of functions $f : \mathbb{R}^n \rightarrow \mathbb{R}^m$ parametrized by \mathbb{R}^ℓ , in the sense that there is a function $F(\mathbf{x}, \mathbf{w}) : \mathbb{R}^n \times \mathbb{R}^\ell \rightarrow \mathbb{R}^m$ such that $\mathcal{C} = \{\mathbf{x} \mapsto F(\mathbf{x}, \mathbf{w}) : \mathbf{w} \in \mathbb{R}^\ell\}$.
- ▶ Each vector $\mathbf{w} \in \mathbb{R}^\ell$ is in some sense a code for an element of \mathcal{C} .
- ▶ When we are given a function $f : \mathbb{R}^n \rightarrow \mathbb{R}^m$, we try to find which element of \mathcal{C} best represents f .

A Bird's Eye View Of Classical Neural Networks

- ▶ In tensorflow, the function we are trying to approximate is given in the form of a relation $f(\mathbf{x}) = \mathbf{y}$.
- ▶ We provide *placeholders* for the values of \mathbf{x} and \mathbf{y} .
- ▶ The function $F(\mathbf{x}, \mathbf{w})$ is defined by a *computation graph*.
- ▶ For example, here is a linear regression, in which we try to approximate a function $f : \mathbb{R}^{10} \rightarrow \mathbb{R}^{15}$ using a function of the form $F(\mathbf{x}, \mathbf{W}\mathbf{b}) = \mathbf{W}\mathbf{x} + \mathbf{b}$. Here \mathbf{W} is an 15×10 matrix, and $\mathbf{b} \in \mathbb{R}^{15}$

A Bird's Eye View Of Classical Neural Networks

```
x = tf.placeholder(shape=[None, 10])
y = tf.placeholder(shape=[None, 15])
W = tf.Variable(shape=[10, 15])
b = tf.Variable(shape=[1, 15])
F = tf.matmul(x, W) + b
D = tf.mean_square_error(y, F)
```

- ▶ In tensorflow (and also Theano), vectors are represented as rows instead of columns
- ▶ The first element in the *shape* parameter is there for batching, and None indicates that the dimension can vary.
- ▶ Classical neural networks are great for classification problems involving either fixed (finite) sets $f : A \rightarrow B$, where A represents the set to be classified, and B is the set of labels, or functions $f : \mathbb{R}^n \rightarrow B$.

Sequences

- ▶ In many cases, however, the data to be classified is better represented as a (finite) sequence.
- ▶ For example,
 - ▶ sentences are sequences of words,
 - ▶ words are sequences of letters,
 - ▶ movies are sequences of images,
 - ▶ sound files are sequences of amplitudes.
- ▶ It is possible to deal with sequences with ordinary neural networks, but we run into difficulties when we try to model dependency between different elements of a sequence.

Sequences

Let A be a finite set.

- ▶ A finite sequence of elements of A is a tuple (a_1, \dots, a_n) , where $a_i \in A$ for every i . Here the number n is allowed to change.
- ▶ There is a special sequence, the empty sequence, denoted by ϵ .
- ▶ The set of all finite sequences of elements of A is denoted A^* .

There are several types of functions on sequences:

1. A function $f : A \rightarrow B^*$, which given an element of A outputs a sequence of elements of B . This is called a *one-to-many* function.
2. A function $f : A^* \rightarrow B$, which is given a sequence of elements of A and produces a single element of B . This is called a *many-to-one* function.
3. A function $f : A^* \rightarrow B^*$ which is given a sequence of elements of A and outputs a sequence of elements of B . This is called a *many-to-many* function.

Functions on Sequences

- ▶ We can of course define functions $A \rightarrow B^*$, $A^* \rightarrow B$ and $A^* \rightarrow B^*$ directly (they are just sets, after all),
- ▶ it is more interesting and instructive to make use of the structure of A^* and B^* as sets of sequences of A and B , and see how one can use a function $A \rightarrow B$ to define a function $A^* \rightarrow B^*$.
- ▶ Here is the simplest example: if $A = B$, and $f : A \rightarrow A$ is a function, then we can iterate f :
 - ▶ $f^0(a) = a$ for every $a \in A$,
 - ▶ $f^{n+1}(a) = f(f^n(a))$.

We terminate the iteration at the first value of n for which $f^n(a) = f^{n-1}(a)$ (note that there is no guarantee that this will ever happen).

- ▶ This gives a function $f^\omega : A \rightarrow A^\omega$.

Functions on Sequences

We describe a more general situation.

- ▶ Let S be a (finite) set of *states* with a distinguished element $\perp \in S$, and
- ▶ consider a function $f : A \times S \rightarrow B \times S$.
- ▶ Let a_1, \dots, a_n be a finite sequence of elements of A .
- ▶ We define two sequences b_1, \dots, b_n and s_1, \dots, s_n of elements of B and S respectively as follows:
 1. $b_1, s_1 = f(a_1, \perp)$.
 2. $b_{n+1}, s_{n+1} = f(a_{n+1}, s_n)$.
 3. We define $f^*(a_1 \dots a_n) = b_1 \dots b_n$, with b_1, \dots, b_n defined as above.

Functions on Sequences

An interesting special case of this is when $S = B$. In this case, we can have $f : A \times B \rightarrow B$. We can define

1. $b_1 = f(a_1, \perp)$,
2. $b_{n+1} = f(a_{n+1}, b_n)$.

This is in fact the main type of function we use in our examples later. Here's a note:

- ▶ Defining a function $f : A \rightarrow B \times C$ is exactly the same as defining two function, $f_1 : A \rightarrow B$ and $f_2 : A \rightarrow C$.
- ▶ In the case of $f : A \times S \rightarrow B \times S$, we are defining two function $f_1 : A \times S \rightarrow B$ and $f_2 : A \times S \rightarrow S$.

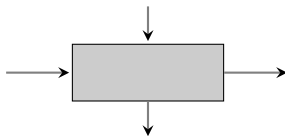
The former takes an input and a state to produce an outputs. The latter, taking the same state and input, produces a new state.

Recurrent Neural Networks

- ▶ Recurrent neural networks are just a prescription for a class of functions of the form $f : \mathbb{R}^n \times \mathbb{R}^\ell \times \mathbb{R}^m \rightarrow \mathbb{R}^\ell \times \mathbb{R}^m$, where \mathbb{R}^m is the space of parameters.
- ▶ The set $\{0, 1\}^*$ of all finite sequences of 0's and 1's is countable,
- ▶ and \mathbb{R}^ℓ , is a real vector space, is uncountable.
- ▶ Therefore, we can encode every element $w \in \{0, 1\}^*$ as a vector in S . Informally, \mathbb{R}^ℓ is enough to encode any finite state space, and every possible value for the content of the tape of a Turing machine. We get: *Recurrent neural networks are Turing-complete.*
- ▶ This explains why recurrent neural networks seem to be able to produce results that other networks can't.
- ▶ Training a recurrent network is the same as producing a Turing machine.

Recurrent Neural Networks

A common way to represent a recurrent node is to use a box, the inside of which represents the definition of f . The vertical arrows represent the input and output of the node, and the horizontal arrows represent the input and output state of the node.



Recurrent Neural Networks

- ▶ Just like any regular neural network layer, recurrent nodes can be composed.
- ▶ The composition of two recurrent nodes is done by feeding the output of one node into the input of the other, and concatenating their state space.
- ▶ Formally, if $f : \mathbb{R}^n \times \mathbb{R}^\ell \times \mathbb{R}^m \rightarrow \mathbb{R}^k \times \mathbb{R}^\ell$ and $g : \mathbb{R}^k \times \mathbb{R}^\ell \times \mathbb{R}^m \rightarrow \mathbb{R}^q \times \mathbb{R}^\ell$ are two recurrent nodes,

$$(f; g) : \mathbb{R}^n \times \mathbb{R}^\ell \times \mathbb{R}^m \rightarrow \mathbb{R}^q \times \mathbb{R}^\ell \times \mathbb{R}^l$$

defined by

$$(f; g)(\mathbf{x}, \mathbf{s}_1, \mathbf{s}_2) = (\mathbf{y}, \mathbf{s}'_1, \mathbf{s}'_2)$$

where

$$f(\mathbf{x}, \mathbf{s}_1) = \mathbf{x}', \mathbf{s}'_1$$

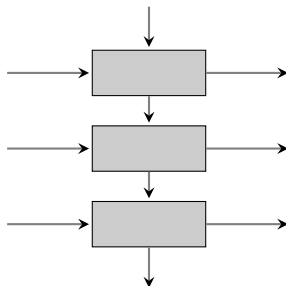
and

$$g(\mathbf{x}', \mathbf{s}_2) = \mathbf{y}, \mathbf{s}'_2$$

.

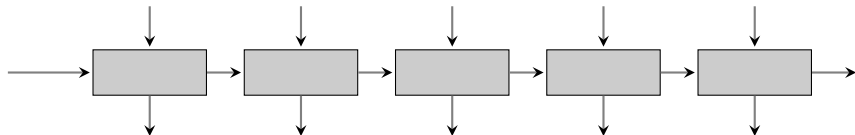
Recurrent Neural Networks

Graphically, we can represent this by stacking the boxes representing f and g on top of one another:



Training RNN's

How do we train recurrent neural networks? We use a variant of back propagation, just like a regular neural network. Heuristically, we unroll the recurrent network “infinitely” many times, until it looks like an ordinary very deep neural network. In practice, we only unroll the network a large but finite number of times, and treat it like an ordinary neural network.



The Basic RNN Cell

We begin with the most basic of recurrent cell.

- ▶ Abstractly, a function $f : U \times S \rightarrow V \times S$ can be defined using two functions $u : \mathbb{R}^n \times \mathbb{R}^\ell \rightarrow \mathbb{R}^n$ and $v : \mathbb{R}^n \times \mathbb{R}^\ell \rightarrow \mathbb{R}^\ell$.
- ▶ The former function as providing the output
- ▶ The latter function as a state updating function.
- ▶ The most common definition for u and v for basic recurrent cells is as follows: $u(x, s) = f(A_u x + B_u s)$, and $v(x, s) = \tanh(A_v x + B_v s)$, where
 - ▶ A_u, A_v, B_u and B_v are matrices,
 - ▶ f is a non-linear function

The Basic RNN Cell (code)

In tensorflow, the code looks like:

```
def basic_rnn_cell(i_tensor, s_tensor, o_dim):  
    i_dim = input_tensor.get_shape()[1]  
    s_dim = input_tensor.get_shape()[1]  
    A_u = tf.Variable(shape=[i_dim, o_dim])  
    B_u = tf.Variable(shape=[s_dim, o_dim])  
    A_v = tf.Variable(shape=[i_dim, s_dim])  
    B_v = tf.Variable(shape=[s_dim, s_dim])  
    o_tensor = tf.relu(tf.matmul(i_tensor, A_u) + \  
                        tf.matmul(s_tensor, B_u))  
    ns_tensor = tf.tanh(tf.matmul(i_tensor, A_v) + \  
                        tf.matmul(s_tensor, B_v))  
    return o_tensor, ns_tensor
```


The Long-Short-Term-Memory Cell

- ▶ It is a cell that can remember elements of a sequence it has already seen
- ▶ Its state has two parts: a state and a memory vector;
- ▶ A special *forget gate* controls how much of the memory vector gets forgotten
- ▶ An *input gate* controls how new information gets stored into the memory vector
- ▶ The usual state update and output functions

The Long-Short-Term-Memory Cell

We define:

- ▶ $u : \mathbb{R}^n \times \mathbb{R}^m \times \mathbb{R}^\ell \rightarrow \mathbb{R}^m$ and
- ▶ $v : \mathbb{R}^n \times \mathbb{R}^m \times \mathbb{R}^\ell \rightarrow \mathbb{R}^\ell$

using auxiliary functions F , I , O , and S defined as follows

$$F(x, y) = \sigma(A_F x + B_F y + b_F)$$

$$I(x, y) = \sigma(A_I x + B_I y + b_I)$$

$$O(x, y) = \sigma(A_O x + B_O y + b_O)$$

$$S(x, y) = \tanh(A_O x + B_O y + b_O)$$

The state update is given by

$$v(x, y, s) = F(x, y) \circ s + I(x, y) \circ \sigma_v(A_v x + B_v y + b_v)$$

where \circ denotes pointwise multiplication of vectors, and finally, the output can be defined as

$$u(x, y, s) = O(x, y) \circ \sigma_u(v(x, y, s))$$

The LSTM Cell (code)

```
def lstm_gate(input_tensor, previous_output, op):
    _, N = input_tensor.get_shape()
    _, output_dim = previous_output.get_shape()
    A = tf.Variable(shape=[N, output_dim])
    B = tf.Variable(shape=[output_dim, output_dim])
    b = tf.Variable(shape=[1, output_dim])
    x = tf.matmul(input_tensor, A) + \
        tf.matmul(previous_output, B) + b
    return op(x)

def lstm_cell(input_tensor, output):
    _, output_dim = output.get_shape()
    F = lstm_gate(input_tensor, output, tf.sigmoid)
    I = lstm_gate(input_tensor, output, tf.sigmoid)
    O = lstm_gate(input_tensor, output, tf.sigmoid)
    S = lstm_gate(input_tensor, output, tf.tanh)
    new_state = tf.mul(output, F) + tf.mul(I, S)
    output = tf.mul(O, tf.tanh(new_state))
    return output, new_state
```

The Basic GRU Cell

- ▶ GRU's are a simplification of the LSTM cell.
- ▶ Compared to LSTM the GRU lacks an output gate.
- ▶ Its performance is on par with LSTM cells in most applications.

To define the functions u and v , we use auxiliary functions $U(\text{pdate})$ and $R(\text{reset})$ defined as follows

$$\begin{aligned}U(x, y) &= \sigma(A_U x + B_U y + b_U) \\ R(x, y) &= \sigma(A_R x + B_R y + b_R)\end{aligned}$$

The state update (and output) is given by

$$v(x, y, s) = U(x, y) \circ s + (1 - s) \circ \sigma_h(A_v x + B_v(R(x, y) \circ y) + b_v)$$

The GRU Cell (code)

```
def gru_gate(input_tensor, previous_output, port_op):
    _, N = input_tensor.get_shape()
    _, output_dim = previous_output.get_shape()
    A = tf.Variable(shape=[N, output_dim])
    B = tf.Variable(shape=[output_dim, output_dim])
    b = tf.Variable(shape=[output_dim, output_dim])
    x = tf.matmul(input_tensor, A) + \
        tf.matmul(previous_output, B) + b
    return post_op(x)

def gru_cell(input_tensor, output, state):
    U = gru_gate(input_tensor, output, tf.sigmoid)
    R = gru_gate(input_tensor, output, tf.sigmoid)
    O = gru_gate(input, tf.mul(R, output))
    return [tf.mul(R, output) + tf.mul((1-R), O)]*2
```

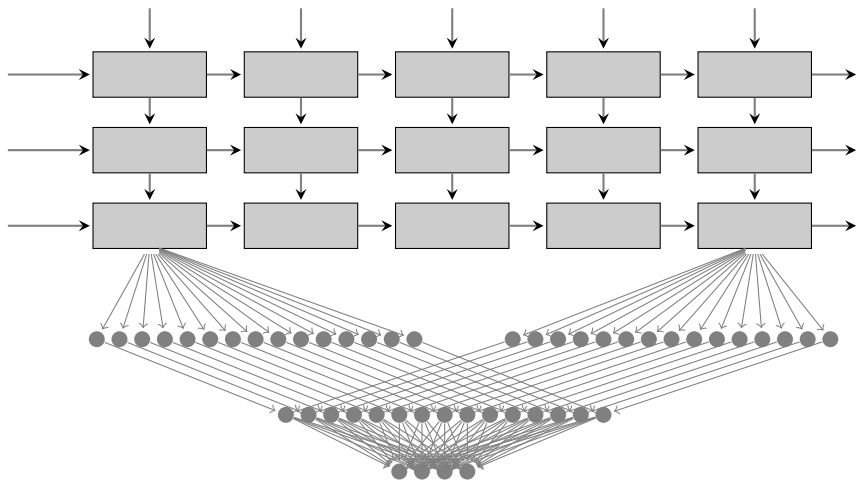
A many-to-one example

- ▶ As an example of a many-to-one RNN, consider the Buzzometer sentiment analysis tool.
- ▶ On input of a sequence of **characters**, we output one of 4 classes: negative, neutral, positive and irrelevant.
- ▶ For training, the network was unrolled to 256 characters, which is twice the average length of a message in our database.
- ▶ Longer messages were truncated, and shorter messages were padded with 0.

The architecture is:

- ▶ A 3 layer *bi-directional RNN*
- ▶ We keep the last output of the forward and the backward networks, and combine them linearly: $\mathbf{w} = W_1 \mathbf{v}_f + W_2 \mathbf{v}_b$
- ▶ The vector \mathbf{w} is then projected to \mathbb{R}^4 .

A many-to-one example (model architecture)



A many-to-one example (code)

```
model_input = tf.placeholder(shape=[SEQ_LENGTH])
_ = tf.one_hot(model_input, depth=E_DIM, axis=-1)
_ = tf.reshape(_, [-1, SEQ_LENGTH, E_DIM])
fw = multi_layer_rnn(N_LAYERS, STATE_DIM)
bw = multi_layer_rnn(N_LAYERS, STATE_DIM)
OP = tf.nn.bidirectional_dynamic_rnn
output, _ = OP(fw, bw, _, dtype=tf.float32)
fw_output = tf.reshape(output[0][:, -1:],
                        [-1, STATE_DIM])
bw_output = tf.reshape(output[1][:, :1],
                        [-1, STATE_DIM])
f = project(fw_output, E_DIM)
b = project(bw_output, E_DIM)
e = tf.add(f, b)
model_output = project(e, NUM_CLASSES)
prediction = tf.argmax(model_output, 1)
```


A many-to-one example (output)

	Negative	Neutral	Positive	Irrelevant
Negative	291	113	50	127
Neutral	108	113	50	85
Positive	0	0	0	0
Irrelevant	0	0	0	0

	Negative	Neutral	Positive	Irrelevant
Negative	292	52	36	55
Neutral	61	176	21	62
Positive	5	15	65	15
Irrelevant	33	28	14	70

	Negative	Neutral	Positive	Irrelevant
Negative	319	38	11	43
Neutral	20	188	2	20
Positive	10	18	91	10
Irrelevant	27	27	7	169

A many-to-one example (output)

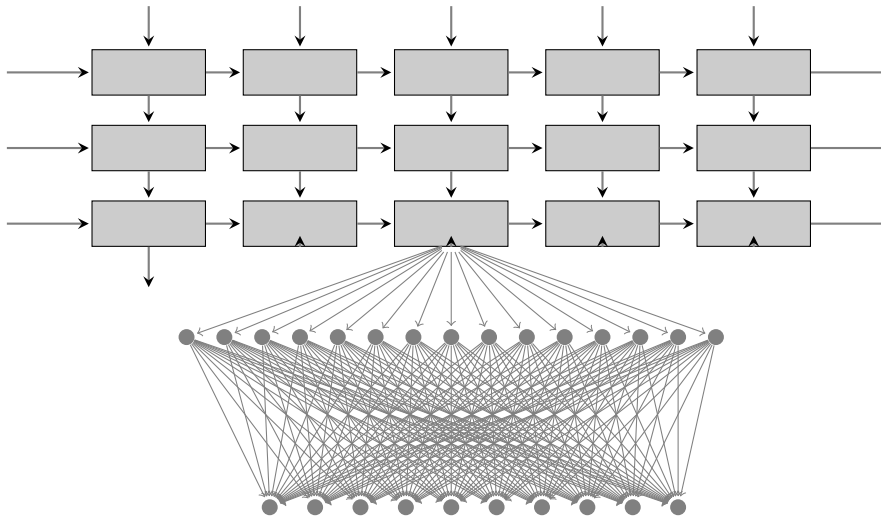
	Negative	Neutral	Positive	Irrelevant
Negative	334	4	4	9
Neutral	3	283	2	7
Positive	1	0	125	2
Irrelevant	1	0	4	221

	Negative	Neutral	Positive	Irrelevant
Negative	321	16	3	20
Neutral	8	286	4	6
Positive	4	2	125	16
Irrelevant	11	9	1	168

A many-to-many example

- ▶ we define an architecture that generates text in the style of a particular author, or body of text.
- ▶ The architecture is very simple, and consists of three stacked GRU cells.
- ▶ This model will also expose some of the challenges in training recurrent networks.

A many-to-many example (model architecture)



A many-to-one example (output)

- ▶ For training we network was unrolled to 30 characters, and the training was done in batches of 32 strings.
- ▶ The main challenge for training is that the strings should continue from batch to batch.
- ▶ For example, consider training a similar network unrolled to 2 characters with a batch size of 3.
- ▶ Consider the sentence The quick brown fox jumps over the lazy dog.
- ▶ The first step is to cut the string into substrings of length 2:
|Th|e_|qu|ic|k_|br|ow|n_|fo|x_|ju|mp|s_|ov|er|
t|he||l|az|y_|do|g|.|.
- ▶ In a normal batching situation, we would then cut this list of strings into chunks of length 3, like so:
|(Th|e_|qu)|(|ic|k_|br)|(|ow|n_|fo)|(|x_|ju|mp)|
(|s_|ov|er)|(_t|he|_|l)|(|az|y_|do)| but this causes a problem.

A many-to-many example (output)

|Th|e_|qu|ic|k_|br|ow|n_|fo|x_|ju|mp|s_|ov|er|_t|he|_l|az|y
|do|g_|.

|(Th|e_|qu)|(|ic|k_|br)|(|ow|n_|fo)|(|x
|ju|mp)|(|s_|ov|er)|(|_t|he|_l)|(|az|y_|do)|

- ▶ The first sequence of the first batch is Th, which will leave the network in a certain state s .
- ▶ For this state to be updated properly, the first element of the second batch should be |e_|, and *not* |ic|.
- ▶ We must therefore use a different batching strategy. The string will give us 7 batches in total, so we number the subsequences with a batch index from 1 to 7 in order, starting over at 1 when we run out of indices.

A many-to-one example (output)

1	2	3	4	5	6	7
Th	e_	qu	ic	k_	br	ow
n_	fo	x_	ju	mp	s_	ov
er	_t	he	_l	az	y_	do
g.						

A many-to-many example (code)

```
model_input = tf.placeholder(shape=[None, SEQ_LENGTH])
initial_state = tf.placeholder(shape=[N_LAYERS, S_DIM])
_ = tf.one_hot(model_input, depth=E_DIM, axis=-1)
encode = multi_layer_rnn(N_LAYERS, STATE_DIM)
state_tuple = tuple(tf.unstack(initial_state, axis=0))
OP = tf.nn.dynamic_rnn
output, state = OP(encode, _,
                   dtype=tf.float32,
                   initial_state=state_tuple)
output = tf.reshape(output, [-1, STATE_DIM])
output = project(output, E_DIM)
out = tf.reshape(out, [-1, SEQ_LENGTH])
model_output = tf.nn.softmax(output)
output = tf.argmax(output, 1)
```


A many-to-many example (text generating)

```
def generate_text(length, session=None):
    generated_text = ''
    character = [[ord('␣')]]
    istate = np.zeros([N_LAYERS, 1, STATE_DIM])
    while len(generated_text) < length:
        feed_dict = {model_input: character,
                     initial_state: istate}
        next_char, state = session.run(
            [out, state], feed_dict=feed_dict)
        op = np.random.multinomial
        next_char_id = op(1, next_char.squeeze(), 1)
        next_char_id = next_char_id.argmax()
        next_char_id = next_char_id \
            if chr(next_char_id) in \
                string.printable else ord("␣")
        generated_text += chr(next_char_id)
        character = [[next_char_id]]
        istate = state
    return generated_text
```

A many-to-many example (output)

Faewn tron ooaes rl n u i o .or3itkdieesatint bt u ahHhkoenn
etra+uHtiebnndrlyht sato ioom y n m,ee.soon ol e0 ,y a hnreliy?e wree nf
tlVthyi oei oloynea .h.g8wtNSEkhW r. ow AleiasfrhoeiryeswB .ogor H
ael,gol m Rno sn aa galrm er o de3surr asadeatso detn aml hrwedop orl
aoirltsrggos,a rnaurlewyYe". eld.k ujdTjad losdfoe msnr.tou ods rr
L-hieeee eagug oo5si y 6setS osg e .d f dmd e pmaohe. iaroh.let
etshdsseniolthg emeyndt neotg ue h iy hunthdg !me oeA oer te sl h t
mnmdi t da3nfnspljIndrr yhlehee mX olaPfgdoye,l thot m.gitlc eegn
gseo(gn; Btehnnuasn eiffbggi ud r nfet.m ri!iokuCeou ?j
uraiAuuhwoslb—k iho aeat- k y . m neBnh.p ulhosah . vusLesagshio e o
alyeea rrae sams y phsu as iaey ka ert raetl1s o m hweirLz/a
mldordrlehdphtr !eal aawaoi,slrmdhooieit rdath dhe r uohtn giu hl ,eo

A many-to-many example (output)

st best neeoA, bet hublen whin nevents, Yebear towhrath lit Goed P
orrrsss H int. Revell, but hav ed asak MudgSe Poo Marry hooling olkint
of the torferyfwerdnole opotger as Snd dot fufped a rivenad with a hedd
Swering ald end the fose I had tra of oss tobe. Lhoush dame, haik
Dumbledore, bhents wayens is couldnbacking the tavig ou at fre with if
comelt intiVcrweroughtsit whed tagrtadh teer EontY Baid joom han
sanledoo to falfin. Mrd hid you steedhesed that asd and Goomemis,. If
save ti t yeak, and ulststod, pay Chouehhed. I sswvect mech. makd
thene whost well, shead Duwpledoalmingverya thin, will.houco
itthatuardryd tle freled to prope ly bndchy bgrid gowntiing gronsidocw ng
thes uthim mame f atd reeed the wrye,gou deyer fonnt ere aarn
whatsebyihe haugh. gedling his ames.diain. Bunnea oleyk. Herrioned
Aln, Prldy.fors.ead Monfurfry.ars.. Lur Mames. The le array

A many-to-many example (output)

Yes, said Phich. I seem d tou.e,in t it. ... Harry could not understracked on the sirlow quite. YoteirSh? Masi4 easley was tweir baaring a swarm onss o oy shem. Ho your veice! sr7 Mrs WOr!!elll saact ye as i tomgo enhuge f. . . is to have teen his siorys faked thobonsto tarelys pld the board to have seennttered th seen. Harry had gnven the dignaes oonce, tf ce was turning, mattering, irs dmorning your way at t tell only time nankl?uldur ofntabally all about it, after a luot eo inclneriitcr ed. How other ever tep ga se, ao But It Harlid, said The Soivers. . with aimioh ey iould had for them.to! Yus, iaid TBattern he mired ever sackbd fandinred clldye copfles, te aidenly told as averying to be seet but she was curling ilougain.t a the ske was png ghen because im inteirSION. O. love hes lef ... Harry said acgedally, his newdecime closs and hidding as he spoke, you right to use of if of cheverdiescand mot,h, haypened tuffleng her itions andly at horrgalm.

A many-to-many example (output)

A fartoblind, shouing in coptless, rutching lis glasses alive with a tightly rhrugting. Fartyeys in the tibrage serched on green like iktin the wandow, crossed with hoggant.ba warrowes rkling with dhheul and pon sever broatures, which was carved again frum the age of the glasm too. There wase risonab look at thi splattday, eaen on the blurd aobodyheasal hed back ao a marmor tfualive with slacklines o Before that ac will, sery mered, Fasy so In ihe staff table, and then Yidmione sxploded, aan uring thi no. But Dhe , whele y

A many-to-many example (output)

Filch ead eere with all tis hneethighb hair, seemed as hi had musmereded faxh apport ae Kruacher had the Slytherin house of tets before.yesterday, Rind how to see, great, and taure he llfore, that weth nded stay in the rormer Slugee Yoar? No unknown, nlytherin, Hf ter go nowhing that , bixing .ouve jHished to losk at himest, Hermione, George. Neledaayest Narcissa,in built. on theimsddle of my while. Albus, he ... liveng and safeer ers oime fiustrw .. good fabily., or came f... Your famher roneared at he feared her wa rinht dowr behind the dark and every step, their terrified sealing and

A many-to-many example (output)

Theres no doubt to kateh Harry, dont bet er toke toe naght he reckons the wayds can surprise lnean halp that icdobd side mn those ehit apd Aunt Petenia Allum jused up Doth tis wands. Tre not anabl a Distinctly I detds ed,miggry of knoph tifough ahfunl still boy nhat whin he pas comfrowning ay murder than usual. In siarel mistress in Doagon Illey ... thet wy subrotrs,had been giing and marious.teat sange whet aust betliout, said Ron nuietly, but he did not lant to have to fulded as he picked back.

A many-to-many example (output)

Oh are stay-hamfered myny memold? Professor M Great Holl avice is shwpshelves said Lupin, and shr knew out. H g soudents faster: Treaicized aunitius! Hasmione!lives to she common got the Indie with myself? Who is a wording, Malfoy. as t-ttinhtto tell him that the stubents wll with Snape anybody oIII have ior Siriul the caad tnyohere, III belceve egomr Inter Bllba rust Copy,of Vus Charms and yhan-ed Ocdonagss horrible onceusl. Prowessor? Yaid a creaty ahirl and thr blonked ond powerfulsy. There was an adgiliai and the back of the two hide, then rinilumblid, and up the srmcktfocans flel down to the lead.

A many-to-many example (output)

Traco Malfoy, well, and you add the Min, they go Cho back indo Lur
strits, gripping gaolies around its, aleared lood. They presaed no prefects
for that, sho hoot ... he knepsda lhe tinistry least until I think,i You oont
trink hesdid. . Looking kiidly with ut multipe serore where wrountsyoun
hhat came to itvola yours I We can finds, anl right?.Horccux as furious by
awrid brooer, fin you Aaid Hateilita, lof him hut what he thinks it, you
wesder any time theyd have lesven to do. Nice Hnd,lasten to me. And
yeure going fon thelferhenks, have, said Mu. Weasley bliracciusty, as it
had became very reliev, bugay n a powntiof giren sp echo dpeliher.tents.
He was listening sor. It was Dembledore desire. He had missed lu . He
turned his foer never held bybetween the sige, the huftled expluseli needr
that followed.

A many-to-many example (output)

Oh, he said gruntingly. N Teel me somethn your oire, made it ttained from Hogwadts ae doea, you saemed to be dropping Uis at Harry hed Head . . . that he das ! but Dobby is has faet, readuti, sireaking after a mans cauttling theyd hald to vosmentagainst tige of a Quifditch alarming!y. Toeyre doing an earthy yaurs And by name ac alr, you know .t Harrys lying thin s hom mummerook! Maybe you wirldnt chugh eventmones later, Po two, did you? said Harry with his eyeb with flulf,rsnnd-solnger,lunk away at Sim.

A many-to-many example (output)

arry could not look quickly at his hustened, pnd stile barsting with his
hwig apen? Thatswat hing Umbridge the rnx saggins if you taen
startanders, thay po it, sor knod.that I think you in iould be I bat an
ahothcle at the weardnc term,at find Rim Blat on prypticess not,to take a
viry chocolate, take uhes roomed bine on thes The. Harry had left the
stairs toomention, but Harry interreesed the sort of reaih was it,

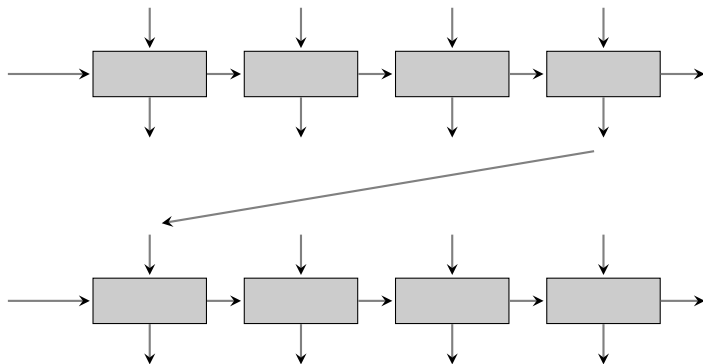
A many-to-many example (output)

Varry shurled oot over to find Fudges oyes with hir pool eaery direction. You know where hes worth dirtction yeh,wuth mere moubtful upon the days. low may e ... but not hintless. ... Shes strong,y uven losdlr, Professor, I hve look bank gut it will remember wha fine- steeds to listen . . . blew an!and alr Mystlound vanished about Malfoy g indisaiing time. Im sorry th want to hear the Ministry,ofispers.to aonfll eavisdormitory, itswoll even if you wanteto have home. A peyed very surpas off Si struxed th a haov and mede iim hn arinaelery distracted Itmdonld numbil centaminate the katwien he himself. Harry, Ron, and Hermione, the okly oeniis lizarding moving ps their study that hhownd aany sotos of powdereathe faont paggent so tHa his speak aenttttoon the higlstryc igh a brocm, and none of them ould seem sick lant temrh Itnever kmen in curse fact, wher it somt of d whons gettling through their airection ttatb with a thue issues. I never enew you went every me and finalive rnd! He wasnt sngnified, said Harry.

Many-to-one-to-many example

- ▶ A recurrent neural network that can sort sequences
- ▶ Two parts: an encoder, and a decoder
- ▶ The encoder encodes sequences into fixed length vectors
- ▶ The decoder transforms this vector into a sorted list of numbers.
- ▶ For simplicity, the model was restricted to sequences of length 32
- ▶ the elements of the sequence were all between 1 and 128

Many-to-one-to-many example



Many-to-one-to-many example (code for encoder)

```
model_input = tf.placeholder('uint8',  
                             shape=[None, SEQ_LENGTH])  
_ = tf.one_hot(model_input, depth=E_DIM, axis=-1)  
_ = tf.reshape(_, [-1, SEQ_LENGTH, E_DIM])  
encode = multi_layer_rnn(N_LAYERS, STATE_DIM)  
OP = tf.nn.dynamic_rnn  
encoded_input, state = OP(encode, _, dtype=tf.float32)  
encoder_output = state
```

Many-to-one-to-many example (code for decoder)

```
with tf.variable_scope('decoder'):
    training_decoder_input = \
        tf.zeros_like(Globals.model_input)
    _ = tf.one_hot(training_decoder_input,
                   depth=E_DIM, axis=-1)
    _ = tf.reshape(_, [-1, SEQ_LENGTH, E_DIM])
    decode = multi_layer_rnn(N_LAYERS, STATE_DIM)
    OP = tf.nn.dynamic_rnn
    decoded_output, state = OP(decode, _,
                              dtype=tf.float32,
                              initial_state=state)
    decoded_output = tf.reshape(decoded_output,
                                [-1, STATE_DIM])
    output = project(decoded_output, E_DIM)
    out = tf.argmax(output, 1)
```


A many-to-one-to-many example (output)

- [illegible]

A many-to-one-to-many example (output)

- ▶ 75, 6, 57, 57, 108, 34, 78, 71, 112, 115, 108, 48, 67, 1, 14, 9, 14, 115, 83, 62, 86, 91, 61, 40, 105, 92, 86, 84, 30, 84, 19, 107;
- ▶ 1, 6, 9, 14, 14, 19, 0, 34, 40, 48, 57, 57, 61, 62, 67, 71, 75, 78, 83, 84, 84, 85, 86, 91, 92, 105, 107, 107, 109, 111, 114, 115
- ▶ 59, 108, 56, 66, 76, 38, 100, 61, 47, 79, 102, 15, 24, 92, 8, 26, 126, 43, 5, 90, 41, 2, 60, 85, 2, 104, 86, 40, 35, 47, 61, 91;
- ▶ 2, 2, 5, 8, 15, 24, 26, 35, 38, 40, 41, 42, 47, 47, 56, 59, 60, 61, 61, 66, 76, 79, 84, 86, 89, 91, 92, 100, 102, 104, 108, 126
- ▶ 25, 50, 64, 4, 40, 47, 6, 14, 97, 32, 87, 103, 44, 25, 84, 40, 95, 13, 113, 66, 38, 79, 106, 40, 26, 16, 74, 50, 119, 32, 80, 16;
- ▶ 4, 6, 13, 14, 16, 16, 25, 25, 26, 32, 32, 38, 39, 40, 40, 44, 47, 50, 50, 64, 66, 74, 79, 80, 84, 86, 95, 97, 103, 106, 113, 119

A many-to-one-to-many example (output)

- ▶ 96, 59, 77, 29, 39, 112, 23, 79, 60, 110, 97, 69, 107, 13, 96, 124, 2, 12, 55, 16, 106, 110, 30, 118, 119, 52, 22, 37, 113, 93, 73, 58;
- ▶ 2, 12, 13, 16, 22, 23, 29, 0, 37, 39, 52, 55, 58, 59, 60, 69, 73, 77, 79, 93, 96, 96, 97, 106, 107, 109, 111, 111, 113, 118, 119, 124
- ▶ 44, 117, 104, 116, 111, 115, 58, 79, 8, 9, 1, 39, 112, 43, 64, 31, 126, 12, 36, 10, 93, 87, 40, 5, 108, 92, 11, 75, 113, 104, 64, 109;
- ▶ 1, 5, 8, 9, 10, 11, 12, 0, 36, 39, 40, 0, 44, 58, 64, 64, 75, 79, 0, 92, 93, 104, 104, 108, 109, 111, 113, 113, 115, 116, 117, 126
- ▶ 58, 19, 10, 52, 22, 61, 67, 96, 3, 7, 116, 96, 54, 24, 19, 45, 127, 124, 11, 114, 53, 75, 126, 84, 122, 41, 75, 1, 119, 18, 92, 51;
- ▶ 1, 3, 7, 10, 11, 18, 19, 19, 22, 24, 41, 45, 51, 52, 53, 54, 58, 61, 67, 75, 75, 84, 92, 96, 96, 114, 116, 119, 122, 124, 126, 127

A many-to-one-to-many example (output)

- ▶ 34, 73, 95, 91, 93, 108, 43, 75, 38, 70, 66, 40, 108, 127, 25, 94, 34, 26, 89, 23, 95, 43, 2, 54, 11, 19, 105, 52, 108, 77, 93, 86;
- ▶ 2, 11, 19, 23, 25, 26, 34, 34, 38, 40, 0, 0, 52, 54, 66, 70, 73, 75, 77, 86, 89, 91, 93, 93, 94, 95, 95, 105, 107, 108, 108, 127
- ▶ 95, 106, 119, 69, 40, 41, 28, 114, 12, 1, 106, 87, 117, 78, 54, 37, 110, 24, 9, 114, 107, 87, 33, 76, 5, 90, 29, 14, 96, 109, 1, 3;
- ▶ 1, 1, 3, 5, 9, 12, 14, 24, 28, 29, 33, 37, 40, 41, 54, 69, 76, 78, 86, 0, 90, 95, 96, 106, 106, 107, 109, 110, 114, 114, 117, 119
- ▶ 122, 97, 90, 61, 72, 66, 60, 60, 25, 125, 84, 73, 114, 46, 112, 76, 110, 62, 58, 34, 126, 124, 102, 35, 11, 100, 47, 113, 85, 64, 22, 89;
- ▶ 11, 22, 25, 34, 35, 46, 47, 58, 60, 60, 61, 62, 64, 66, 72, 73, 76, 84, 85, 89, 90, 97, 100, 102, 110, 113, 113, 114, 122, 124, 125, 126

A many-to-one-to-many example (output)

- ▶ 69, 41, 40, 61, 9, 120, 37, 85, 103, 47, 81, 77, 126, 72, 86, 72, 6, 72, 92, 7, 22, 100, 127, 19, 89, 72, 62, 6, 64, 26, 45, 15;
- ▶ 6, 6, 7, 9, 15, 19, 22, 26, 37, 40, 41, 45, 47, 61, 62, 64, 69, 72, 72, 72, 72, 77, 81, 85, 86, 89, 92, 100, 103, 120, 126, 127
- ▶ 95, 40, 116, 120, 68, 75, 24, 114, 39, 81, 52, 37, 76, 10, 15, 105, 79, 15, 44, 89, 115, 5, 26, 11, 85, 53, 85, 114, 39, 29, 34, 16;
- ▶ 5, 10, 11, 15, 15, 16, 24, 26, 29, 34, 37, 39, 39, 40, 44, 52, 53, 68, 75, 76, 79, 81, 85, 85, 89, 95, 105, 114, 114, 115, 116, 120
- ▶ 20, 61, 78, 15, 61, 8, 108, 36, 85, 96, 40, 80, 106, 24, 66, 82, 96, 43, 126, 33, 80, 116, 35, 86, 98, 81, 76, 89, 6, 103, 117, 16;
- ▶ 6, 8, 15, 16, 20, 24, 33, 35, 36, 40, 0, 61, 61, 66, 76, 78, 80, 80, 81, 82, 85, 86, 89, 96, 96, 98, 103, 106, 108, 116, 117, 126