

A* Algorithm | A* Algorithm Example in AI

📁 Artificial Intelligence

A* Algorithm-

- A* Algorithm is one of the best and popular techniques used for path finding and graph traversals.
- A lot of games and web-based maps use this algorithm for finding the shortest path efficiently.
- It is essentially a best first search algorithm.

Working-

A* Algorithm works as-

- It maintains a tree of paths originating at the start node.
- It extends those paths one edge at a time.
- It continues until its termination criterion is satisfied.

A* Algorithm extends the path that minimizes the following function-

$$f(n) = g(n) + h(n)$$

Here,

- 'n' is the last node on the path
- $g(n)$ is the cost of the path from start node to node 'n'
- $h(n)$ is a heuristic function that estimates cost of the cheapest path from node 'n' to the goal node

Algorithm-

- The implementation of A* Algorithm involves maintaining two lists- OPEN and CLOSED.
- OPEN contains those nodes that have been evaluated by the heuristic function but have not been expanded into successors yet.
- CLOSED contains those nodes that have already been visited.

Step-01:

- Define a list OPEN.
- Initially, OPEN consists solely of a single node, the start node S.

Step-02:

If the list is empty, return failure and exit.

Step-03:

- Remove node n with the smallest value of $f(n)$ from OPEN and move it to list CLOSED.
- If node n is a goal state, return success and exit.

Step-04:

Expand node n .

Step-05:

- If any successor to n is the goal node, return success and the solution by tracing the path from goal node to S.
- Otherwise, go to Step-06.

Step-06:

For each successor node,

- Apply the evaluation function f to the node.
- If the node has not been in either list, add it to OPEN.

Step-07:

Go back to Step-02.

PRACTICE PROBLEMS BASED ON A* ALGORITHM-

Problem-01:

Given an initial state of a 8-puzzle problem and final state to be reached-

2	8	3
1	6	4
7		5

Initial State

1	2	3
8		4
7	6	5

Final State

Find the most cost-effective path to reach the final state from initial state using A* Algorithm.

Consider $g(n)$ = Depth of node and $h(n)$ = Number of misplaced tiles.

Solution-

- A* Algorithm maintains a tree of paths originating at the initial state.
- It extends those paths one edge at a time.
- It continues until final state is reached.

Initial State

2	8	3
1	6	4
7		5

g = 0
h = 4
f = 0+4 = 4

2	8	3
1	6	4
	7	5

g = 1
h = 5
f = 1+5 = 6

2	8	3
1		4
7	6	5

g = 1
h = 3
f = 1+3 = 4

2	8	3
1	6	4
7	5	

g = 1
h = 5
f = 1+5 = 6

2	8	3
	1	4
7	6	5

g = 2
h = 3
f = 2+3 = 5

2		3
1	8	4
7	6	5

g = 2
h = 3
f = 2+3 = 5

2	8	3
1	4	
7	6	5

g = 2
h = 4
f = 2+4 = 6

	8	3
2	1	4
7	6	5

g = 3
h = 3
f = 3+3 = 6

2	8	3
7	1	4
	6	5

g = 3
h = 4
f = 3+4 = 7

	2	3
1	8	4
7	6	5

g = 3
h = 2
f = 3+2 = 5

2	3	
1	8	4
7	6	5

g = 3
h = 4
f = 3+4 = 7

1	2	3
	8	4
7	6	5

g = 4
h = 1
f = 4+1 = 5

1	2	3
8		4
7	6	5

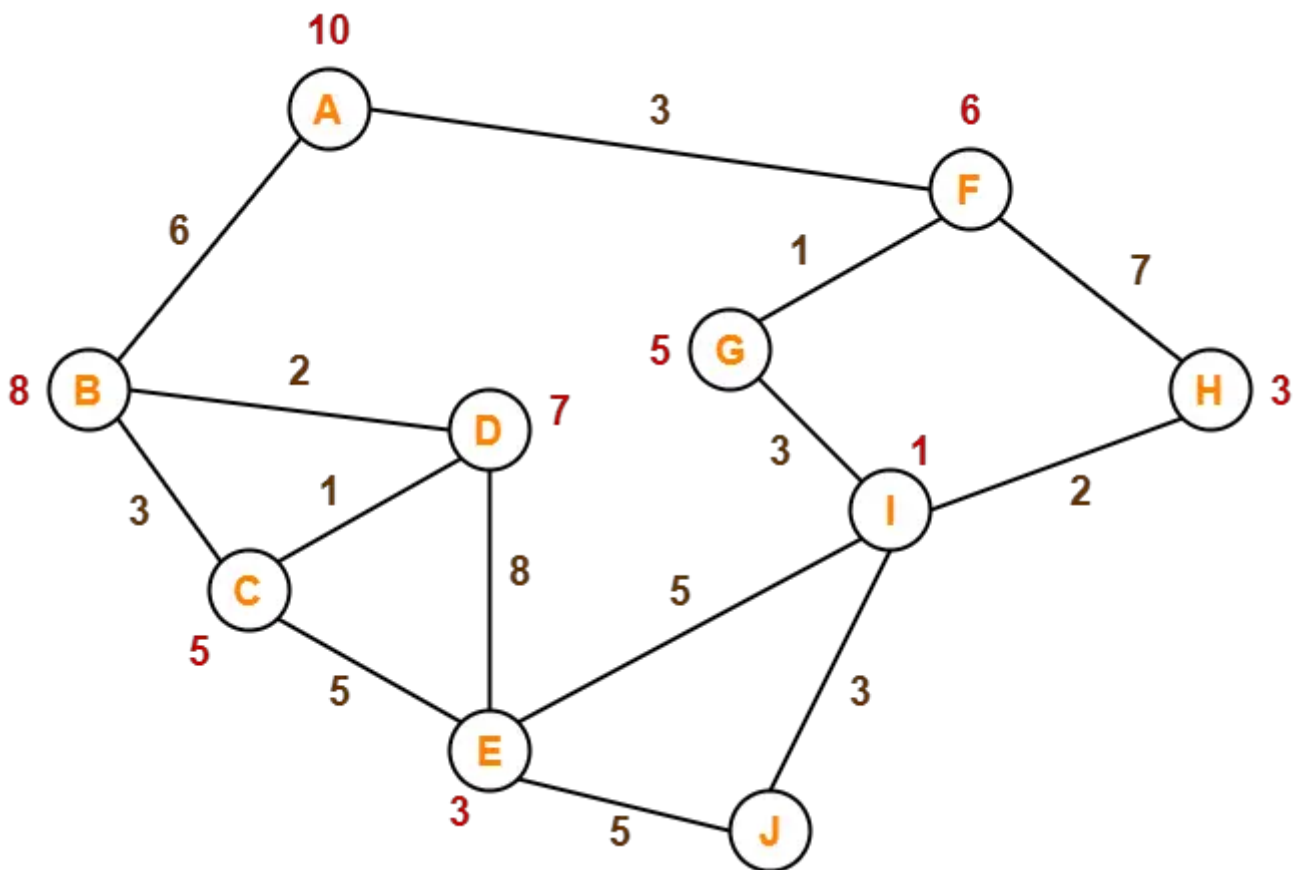
g = 5
h = 0
f = 5+0 = 5

1	2	3
7	8	4
	6	5

g = 5
h = 2
f = 5+2 = 7

Final State

Problem-02:



The numbers written on edges represent the distance between the nodes.

The numbers written on nodes represent the heuristic value.

Find the most cost-effective path to reach from start state A to final state J using A* Algorithm.

Solution-

Step-01:

- We start with node A.
- Node B and Node F can be reached from node A.

A* Algorithm calculates $f(B)$ and $f(F)$.

- $f(B) = 6 + 8 = 14$
- $f(F) = 3 + 6 = 9$

Path- A \rightarrow F

Step-02:

Node G and Node H can be reached from node F.

A* Algorithm calculates $f(G)$ and $f(H)$.

Since $f(G) < f(H)$, so it decides to go to node G.

Path- $A \rightarrow F \rightarrow G$

Step-03:

Node I can be reached from node G.

A* Algorithm calculates $f(I)$.

$$f(I) = (3+1+3) + 1 = 8$$

It decides to go to node I.

Path- $A \rightarrow F \rightarrow G \rightarrow I$

Step-04:

A* Algorithm calculates $f(E)$, $f(H)$ and $f(J)$.

- $f(E) = (3+1+3+5) + 3 = 15$
- $f(H) = (3+1+3+2) + 3 = 12$
- $f(J) = (3+1+3+3) + 0 = 10$

Since $f(J)$ is least, so it decides to go to node J.

Path- $A \rightarrow F \rightarrow G \rightarrow I \rightarrow J$

This is the required shortest path from node A to node J.

