



# IEEE PES ISGT Europe 2024 Conference

Dubrovnik, Croatia  
October 14th - 17th

## How to design economic mechanisms for efficient operation of low-inertia power grids

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Funded by  
the European Union



Funded by  
UK Research  
and Innovation





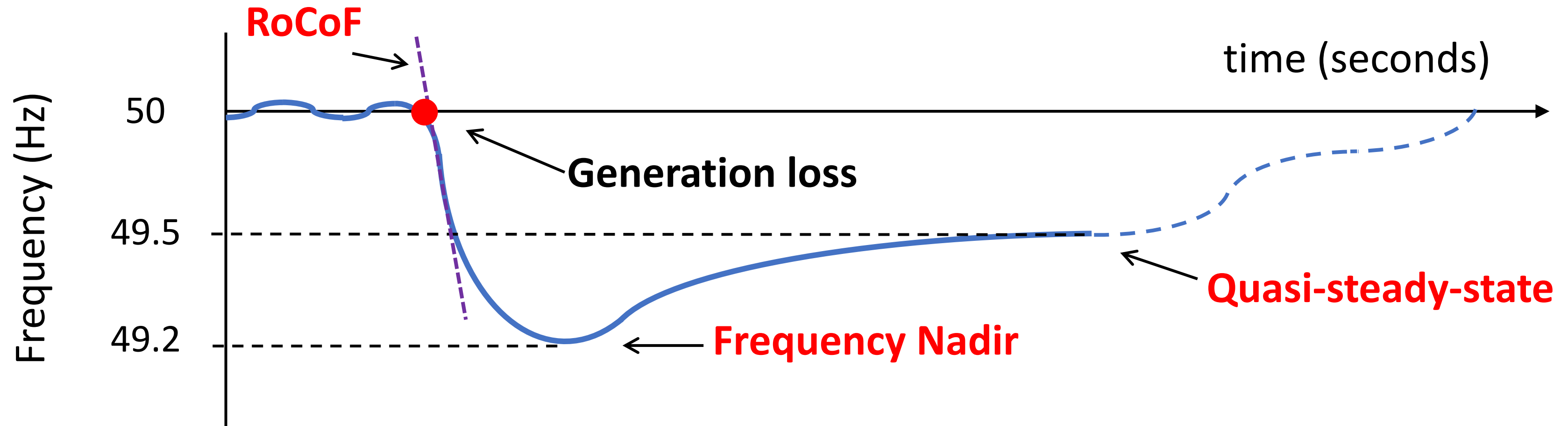
# 3 topics covered



1. **Unlocking the support from DER** via risk-constrained optimization
2. From **low-level control** instructions to **system-level optimization** via data-driven methods
3. **Who should pay** for frequency-containment services?



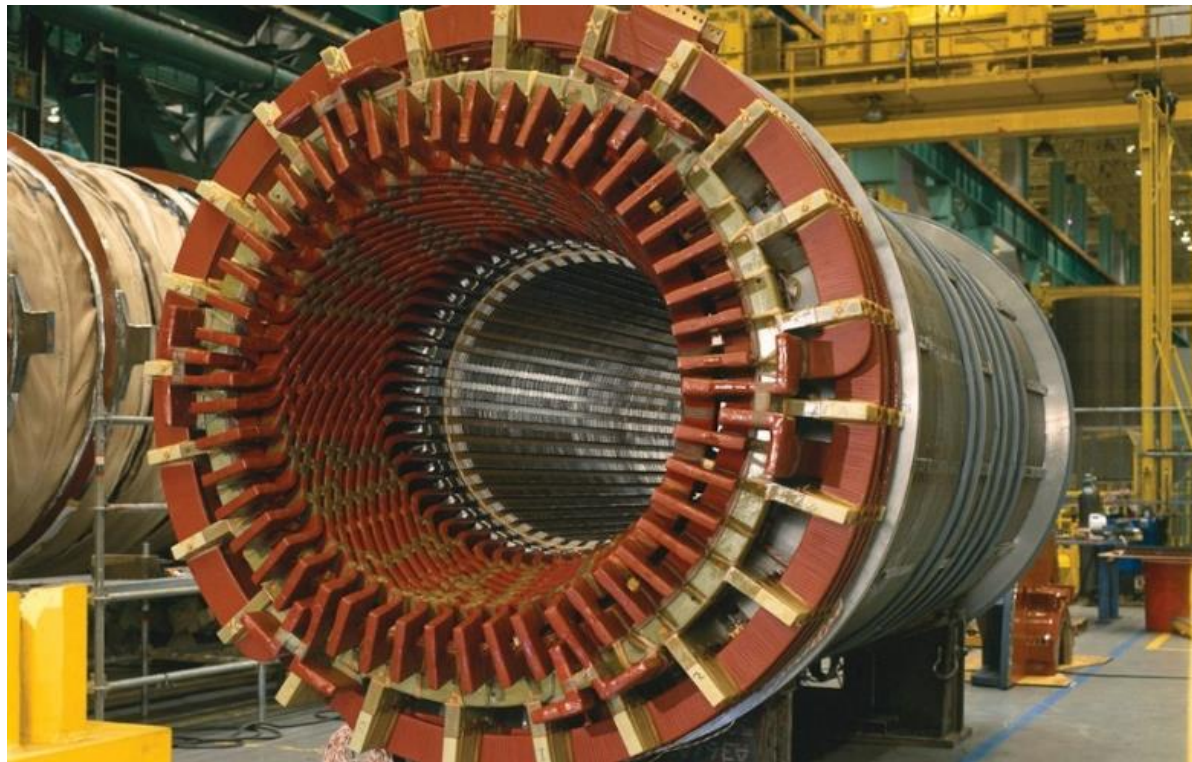
# Frequency stability



Key to keep frequency within safe limits to  
avoid demand disconnection!

# Lower inertia on the road to lower emissions

*Thermal generators  
(nuclear, gas, coal...):*



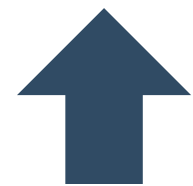
*Most renewables:  
**no inertia***



Decarbonization



The **risk of instability**  
has increased!



**Inertia stores kinetic energy:**

this energy gave us time to contain a sudden generation-demand imbalance

**IEEE PES Innovative Smart Grid Technologies Conference Europe (ISGT- Europe)**

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## Paper:

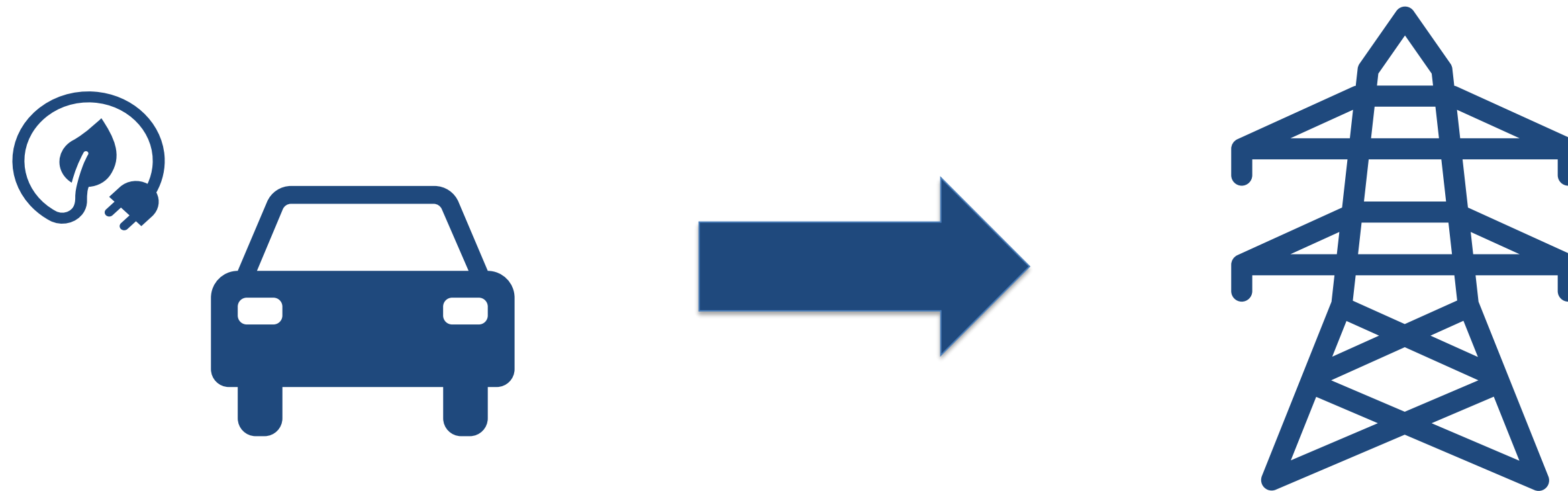
C. O'Malley, L. Badesa et al., "Frequency Response from Aggregated V2G Chargers With Uncertain EV Connections," ***IEEE Trans. on Power Systems***, 2023





# Unlocking support from Distributed Energy Resources

- **DER could be very valuable** to support system stability, but they are **inherently uncertain**
- We focus on **Vehicle-to-Grid (V2G)**: the system operator cannot control when the EV owners plug in their vehicles



# Why is this important?

Now



Future

Stability through **gas plants**

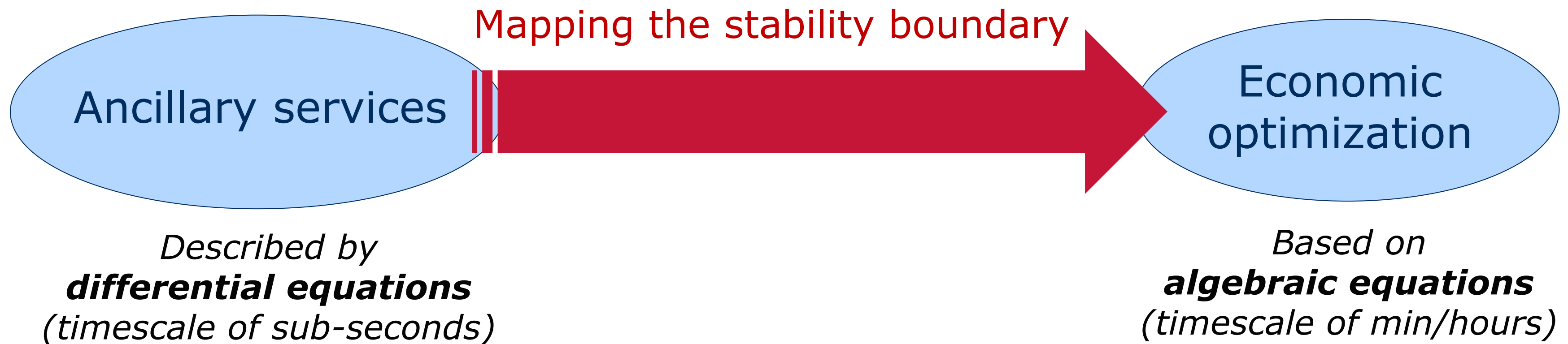
- **Pros:** certain + reliable
- **Cons:** expensive + polluting

Stability services from **DER**

- **Pros:** abundant + **cheap**
- **Cons:** uncertain

# Stability conditions for optimization

What is the **value of V2G** as a countermeasure to low inertia?





# Uncertainty within the stability conditions



We propose the use of **chance constraints**:

$$\text{Probability of complying with stability limit} \geq 1 - \epsilon$$

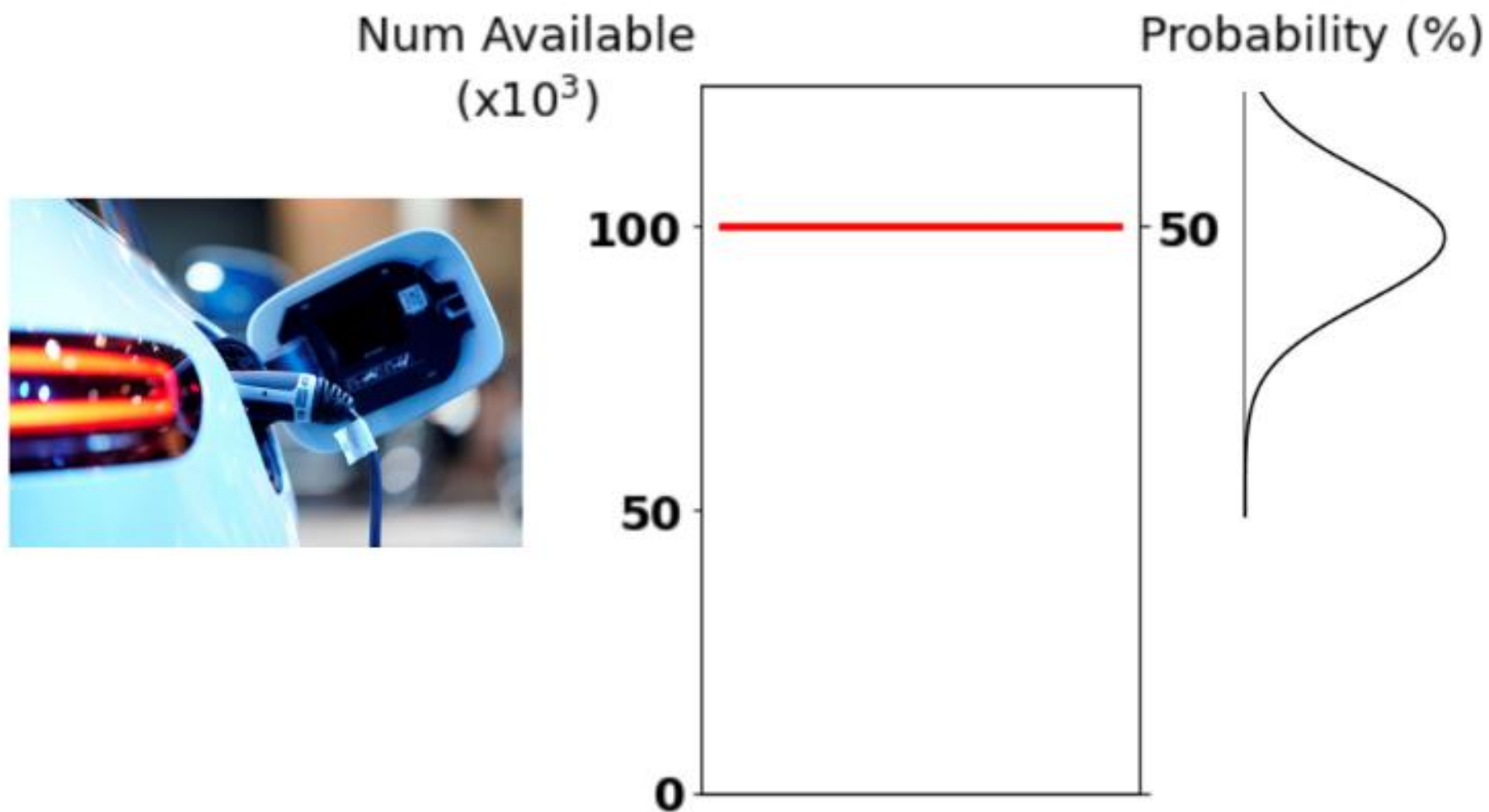
Uncertainty in  
**EV plug-in** times



**Risk** appetite  
(e.g., 1% chance of  
under-delivery)

# What do we mean by risk?

## Probabilistic forecast for EV connections



## Naïve scheduling:

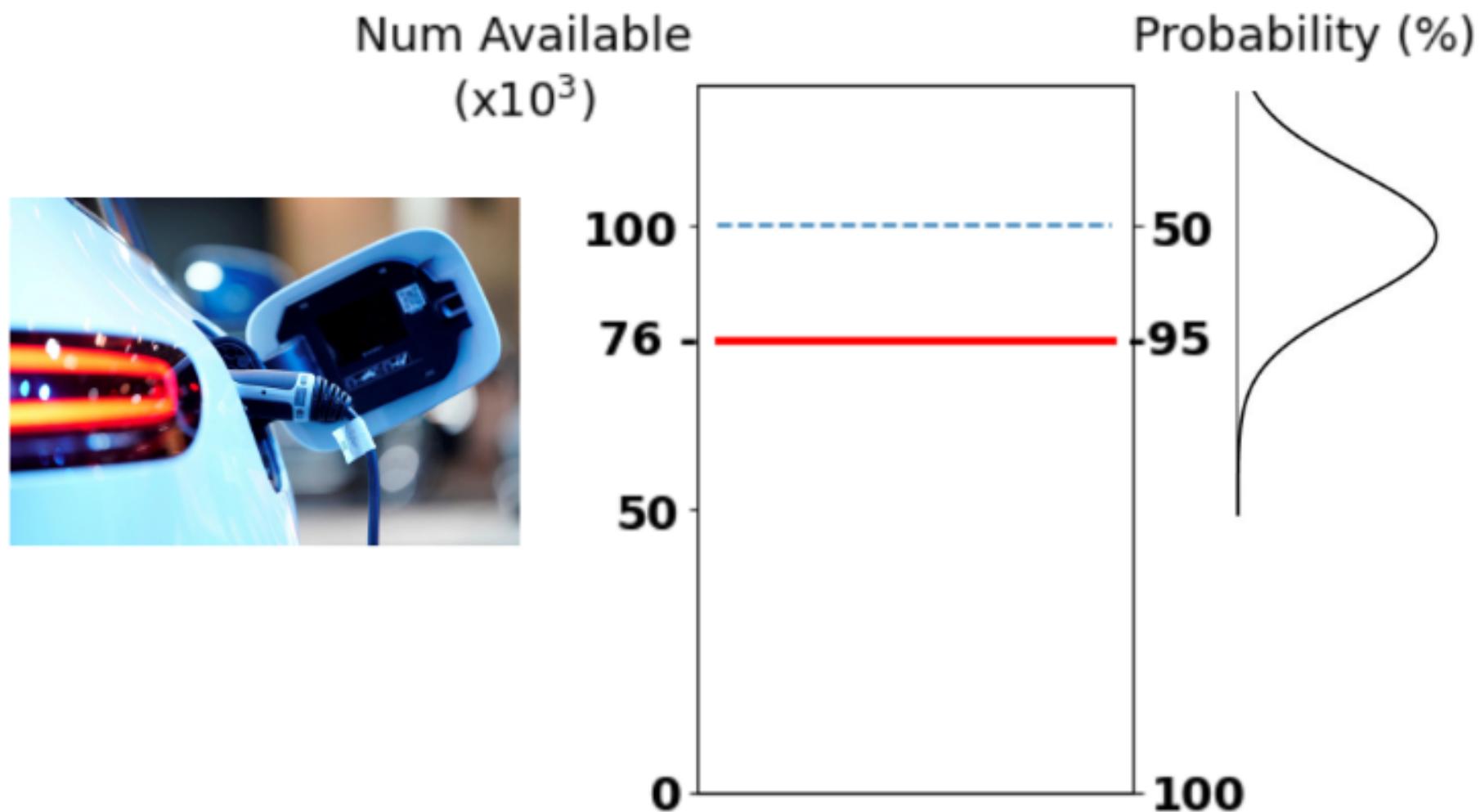
- Use **deterministic forecast** (mean)
- Count on 100k EVs
- **50% chance** of having less than expected

**Risky!**



# What do we mean by risk?

## Probabilistic forecast for EV connections

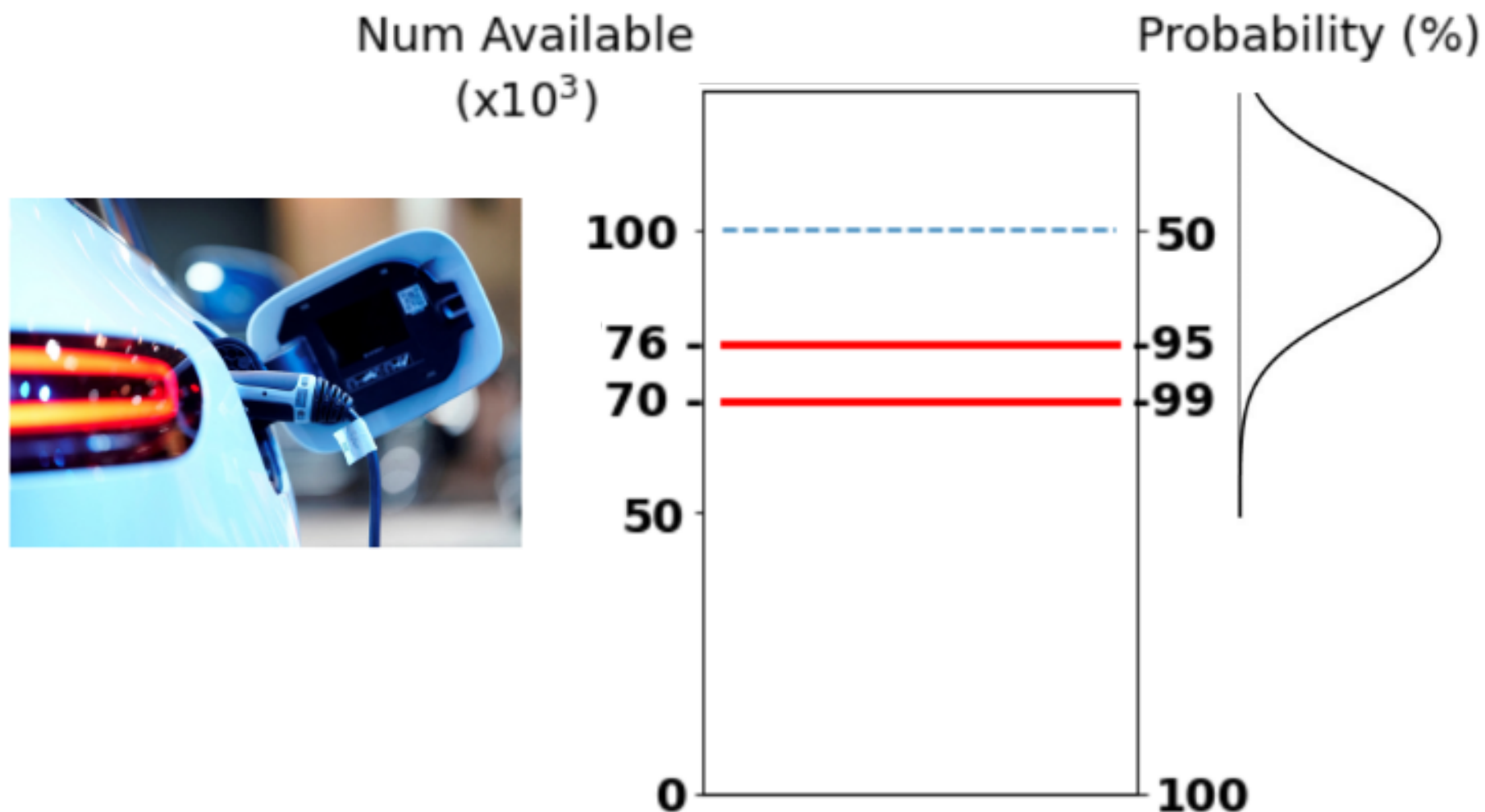


## Risk-limited scheduling:

- Specify **risk tolerance** (e.g., 5%)
- Count on **76k EVs**

# What do we mean by risk?

## Probabilistic forecast for EV connections



## Risk-limited scheduling:

- Specify **risk tolerance** (e.g., **1%**)
- Count on **70k EVs**

**Lower risk** implies  
less support from EVs  
considered



# Steps for deducing chance constraints

1. Model system frequency via **single-machine swing equation**:

$$\frac{2H}{f_0} \frac{d\Delta f}{dt} = R^{EV}(t) + R^{ND}(t) + R^G(t) - PL_{max}$$

2. **Solve swing equation** to obtain RoCoF and nadir **constraints**:

$$\mathbb{P} \left[ \left( \frac{H}{f_0} - \frac{(R^{ND} + R^{EV}) \cdot T_1}{4\Delta f_{max}} \right) \frac{R^G}{T_2} \geq \left( \frac{PL_{max} - (R^{ND} + R^{EV})}{2\sqrt{\Delta f_{max}}} \right)^2 \right] \geq 1 - \epsilon$$

3. Use a **convex reformulation** for the non-convex chance constraints

# Convexification of chance constraint

Several options for the **convex reformulation**:

The **more information** available in the forecast,  
the **less conservative** the reformulation:

- **Gaussian** uncertainty?
  - **Unimodal** distribution? (single peak)
  - Only mean and variance known?
- Distributionally-robust** formulation (most conservative)

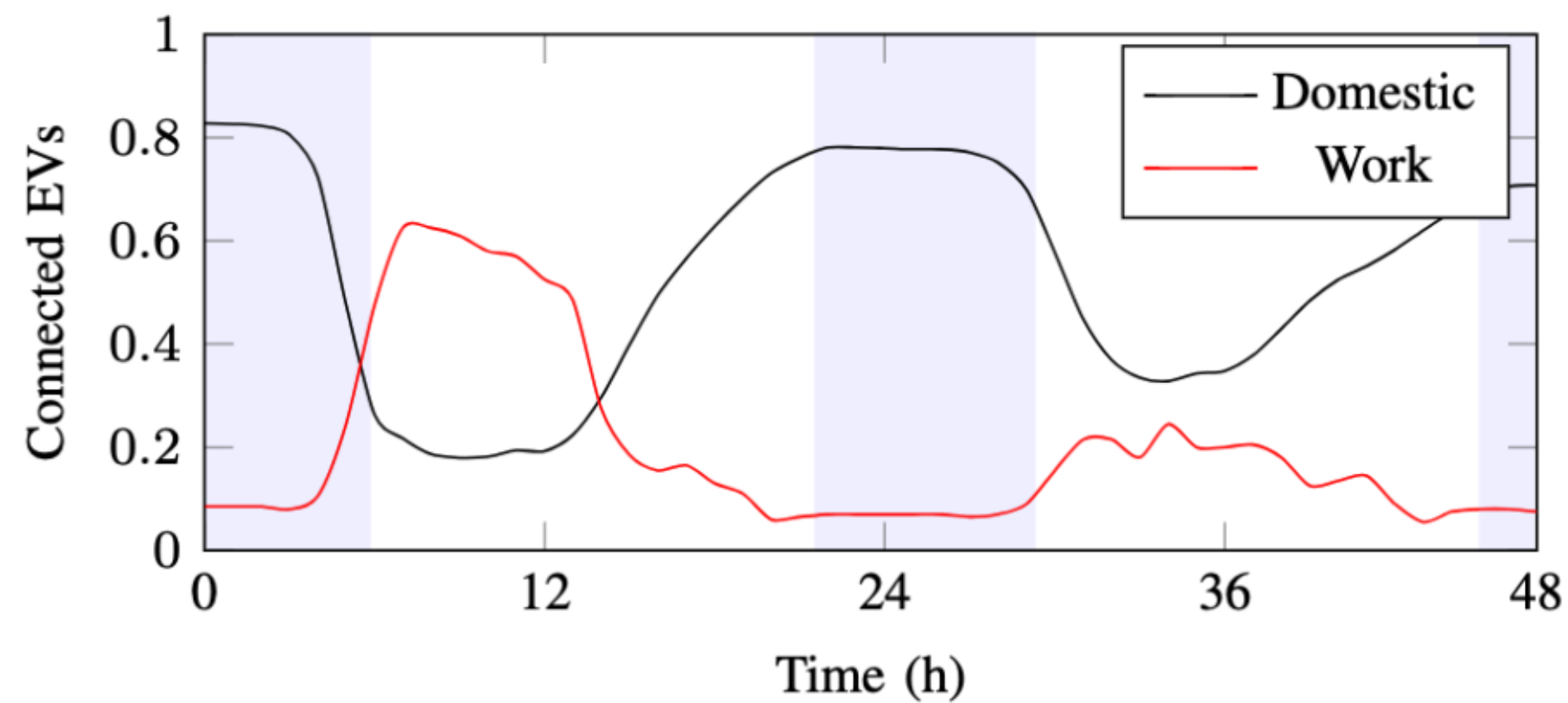


# Results for Great Britain

- **Frequency-secured UC** run for a full year in 2030
- Two **EV fleets** considered:
  - **'Domestic V2G'**: 85,000 units, 10 kW chargers
  - **'Work V2G'**: 15,000 units, 20 kW chargers
- **Risk** of under-delivery set at **1%**
  - Does **not mean** 1% risk of **violating security**: that risk is extremely small (largest *N-1* contingency needs to happen too)

# EV connectivity forecasting and data analysis

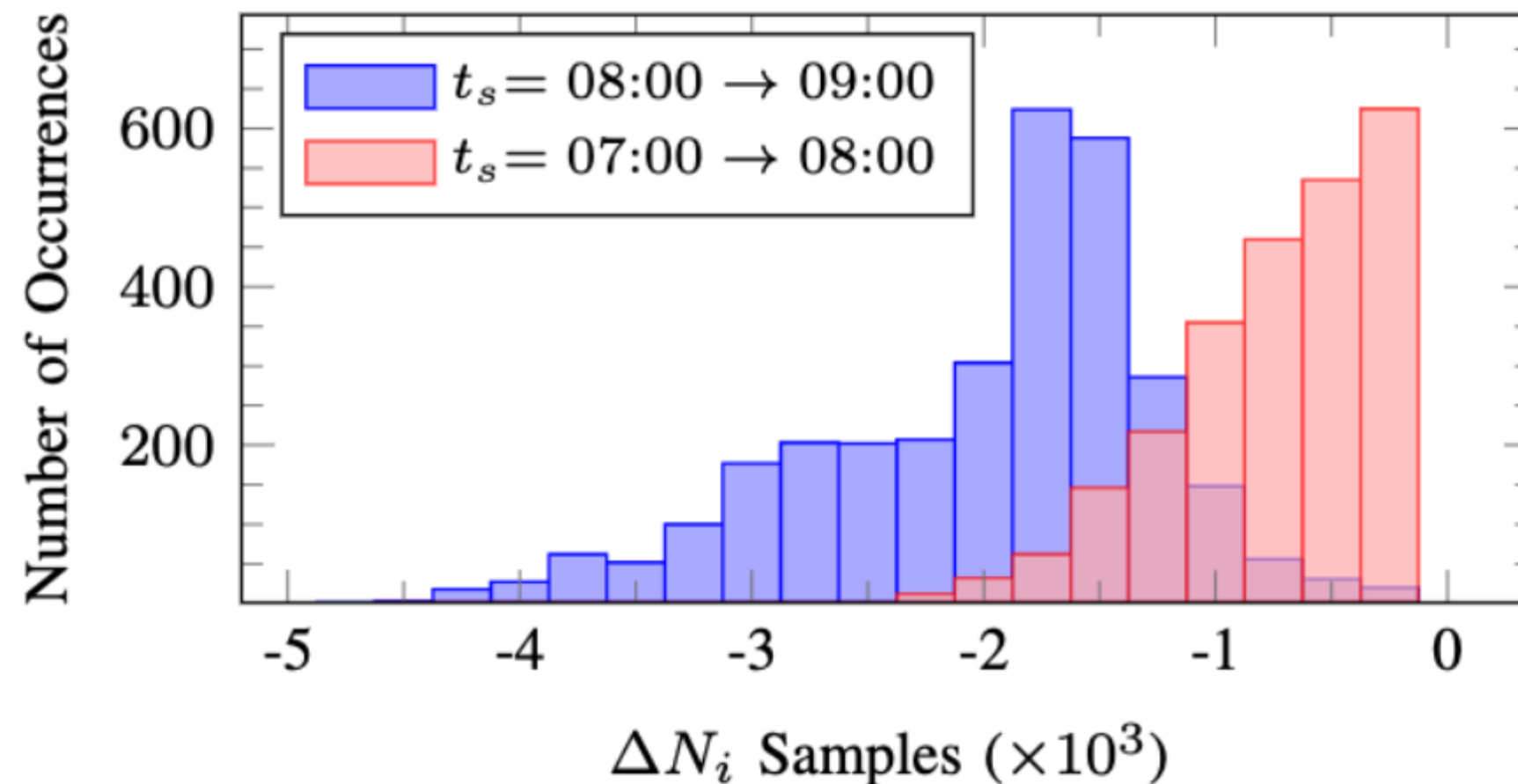
Data from UK Department of Transport, 2017





# Test for ambiguity set

Domestic fleet disconnections  
on weekday

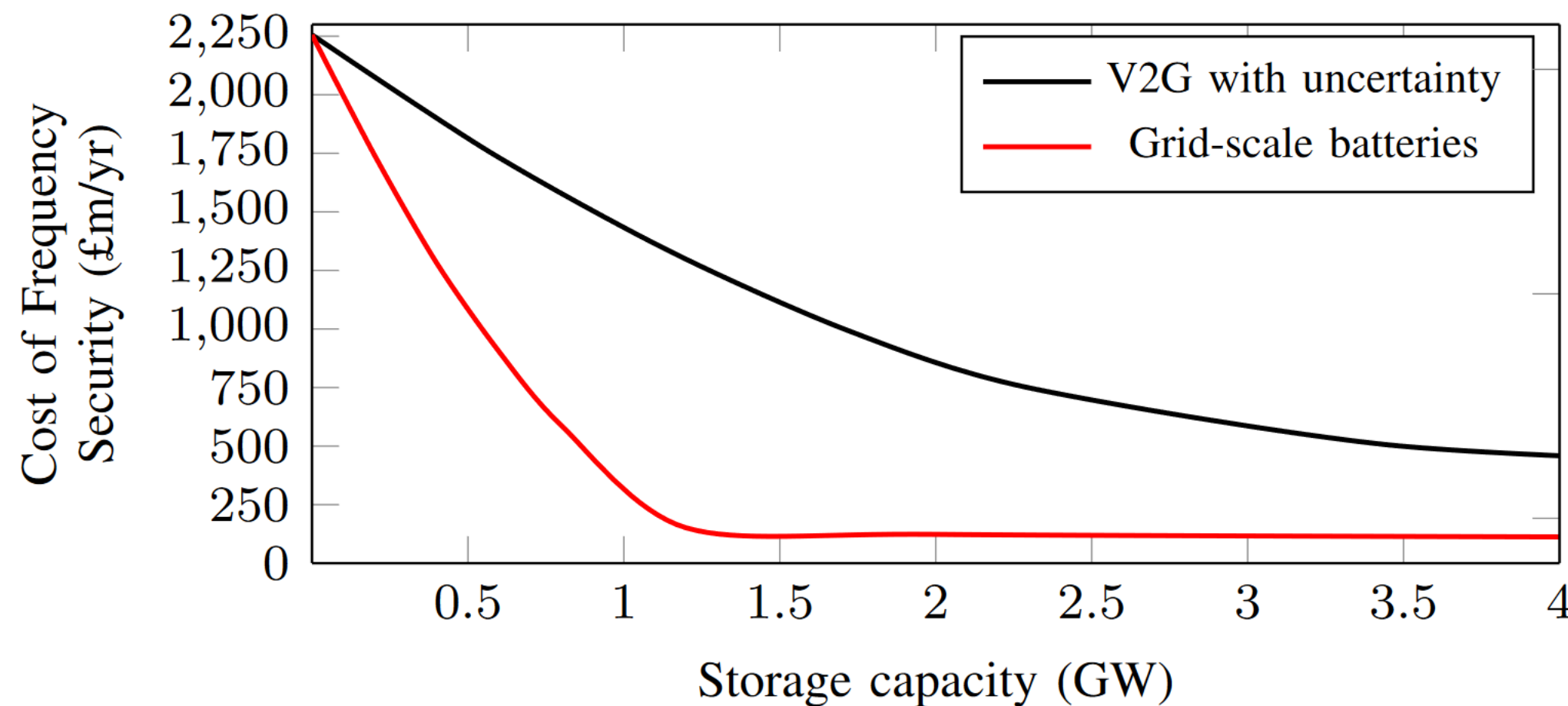


- **Not** Gaussian
- **Unimodal** with high confidence (from Shapiro-Wilk test)

# Results: comparison of V2G to BESS

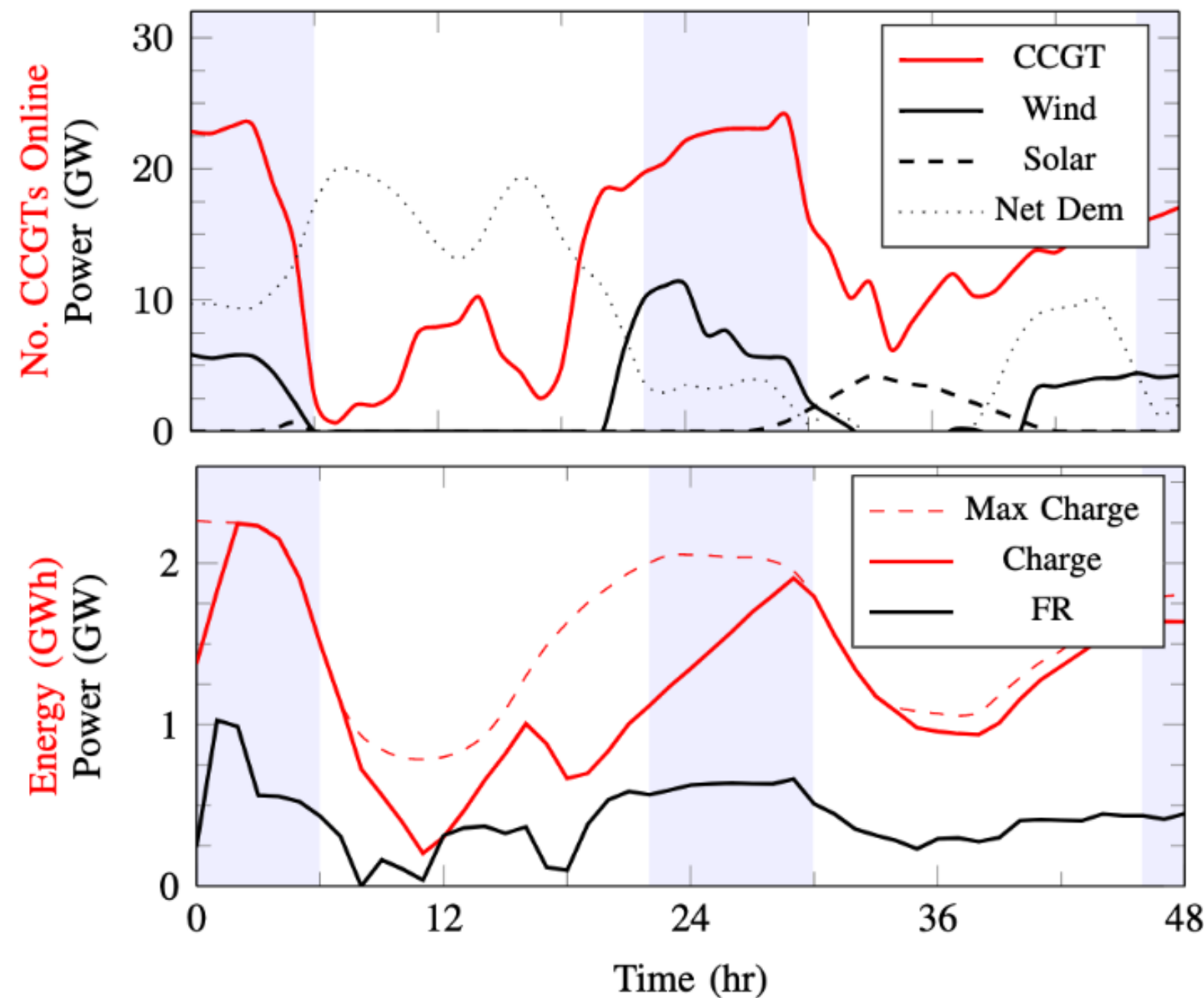
V2G capacity shown to be **one third as valuable** as stationary BESS

- EV chargers only have an **EV connected ~40% of the time**
- EV chargers are subject to **uncertainty**



But EVs have  
**no additional**  
investment cost!

# Where does this value come from?



Fewer CCGTs  
are needed,  
thanks to  
**frequency support**  
from **EVs**



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2. From **low-level control** instructions to **system-level optimization** via data-driven methods
3. **Who should pay** for frequency-containment services?

## Paper:

Q. Chen, L. Badesa et al., “Adaptive Droop Gain Control for Optimal Kinetic Energy Extraction From Wind Turbines to Support System Frequency,” **IEEE Access**, 2024



# Research question

How to **translate** the **system** optimal **dispatch**  
into **specific control gains** for devices?

(not possible with fully analytical methods as the one shown earlier)

**Goal:**

**Optimal kinetic energy** extraction from wind turbines  
depending on **overall system dispatch**

# Approach we used

**Data-driven methods** allow to compute explicit control instructions

But, **how to choose the classifier?**

- We opt for an **Optimal Classification Tree** (OCT): **simple** structure and **tractable** for incorporating into optimization

Other options:

- Logistic regression and SVM: limited by hyperplane separation (although kernels could be used)
- Neural Networks: problems with tractability due to binary variables



# Adaptive Droop Gain (ADG)

$$\underbrace{\text{ADG}(v_w, P_G, L_D, pl, \Delta P_L, \omega_r)}_{\text{System operating condition}} = \tilde{K}_{\text{sys}} \cdot \underbrace{(\omega_r^2 - \omega_{r,\min}^2)}_{\text{deter over-deceleration}}$$

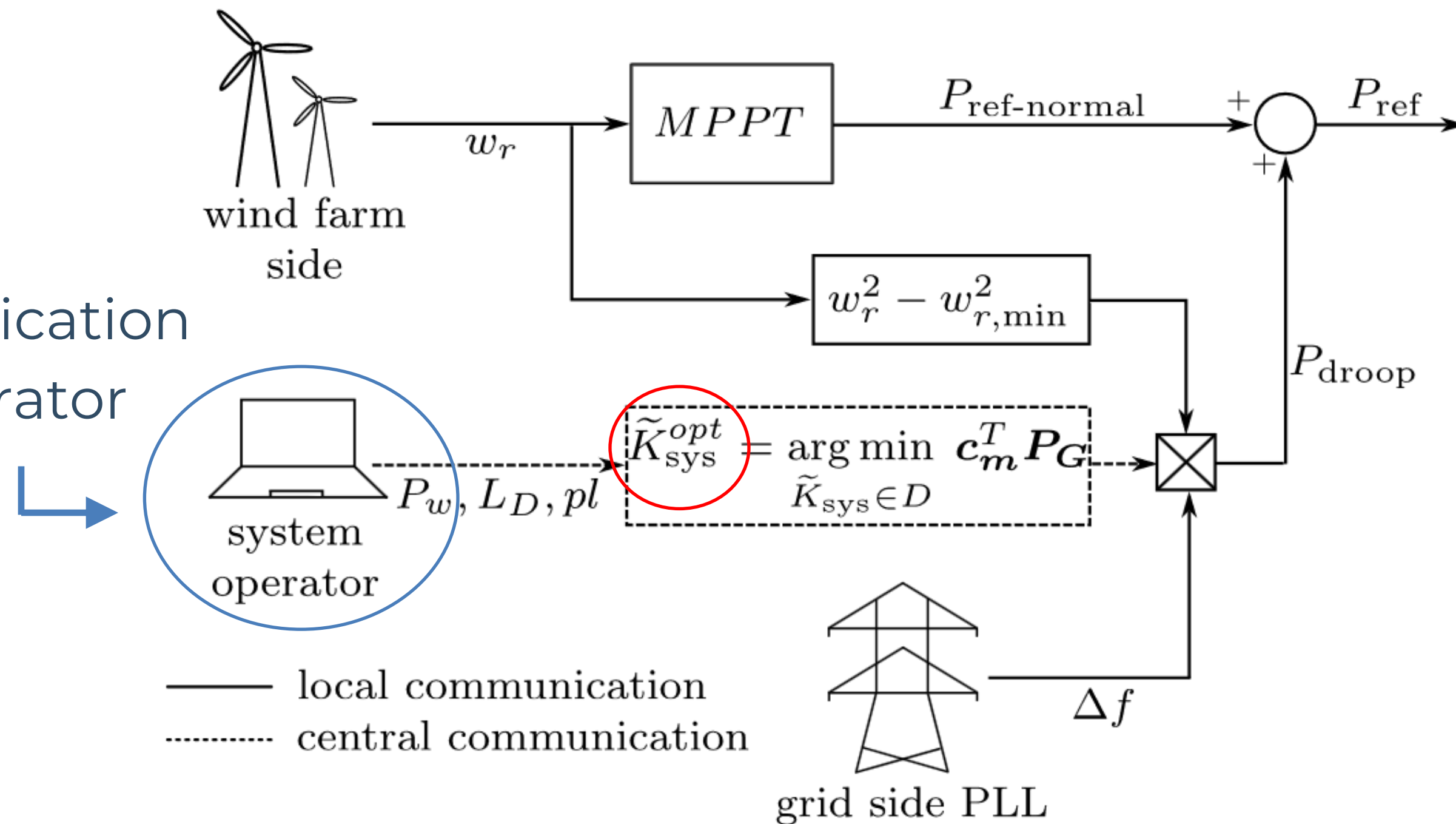
$$\tilde{K}_{\text{sys}} = f(v_w, P_G, L_D, pl, \Delta P_L)$$

An **Optimal Classification Tree** (OCT) is used to encode frequency-stability conditions within a system-wide economic dispatch

➤ The **ADG** is **explicitly incorporated** into the OCT

# Communication requirements

**Hourly** communication  
with system operator  
(rest is local)



# Optimal Classification Tree

## Offline training

(outside the Unit Commitment / OPF)

Minimize classification error

Penalize tree depth

$$\min \frac{1}{\hat{\mathcal{L}}} \sum_{t \in \underline{\Omega}^T} l_t + \alpha \sum_{m \in \underline{\Omega}^B} d_m$$

$$\text{s.t. } l_t \geq \omega \cdot n_{0t} - \mathcal{M} \cdot (1 - c_t) \quad \forall t \in \underline{\Omega}^T$$

$$l_t \leq \omega \cdot n_{0t} + \mathcal{M} \cdot c_t \quad \forall t \in \underline{\Omega}^T$$

$$l_t \geq n_{1t} - \mathcal{M} \cdot c_t \quad \forall t \in \underline{\Omega}^T$$

$$l_t \leq n_{1t} + \mathcal{M} \cdot (1 - c_t) \quad \forall t \in \underline{\Omega}^T$$

$$n_{1t} = \sum_{i \in \Omega^N} z_{it} \cdot Y_i \quad \forall t \in \underline{\Omega}^T$$

$$n_{0t} = \sum_{i \in \Omega^N} z_{it} - n_{1t} \quad \forall t \in \underline{\Omega}^T$$

Classification boundaries (linearized via big-M)

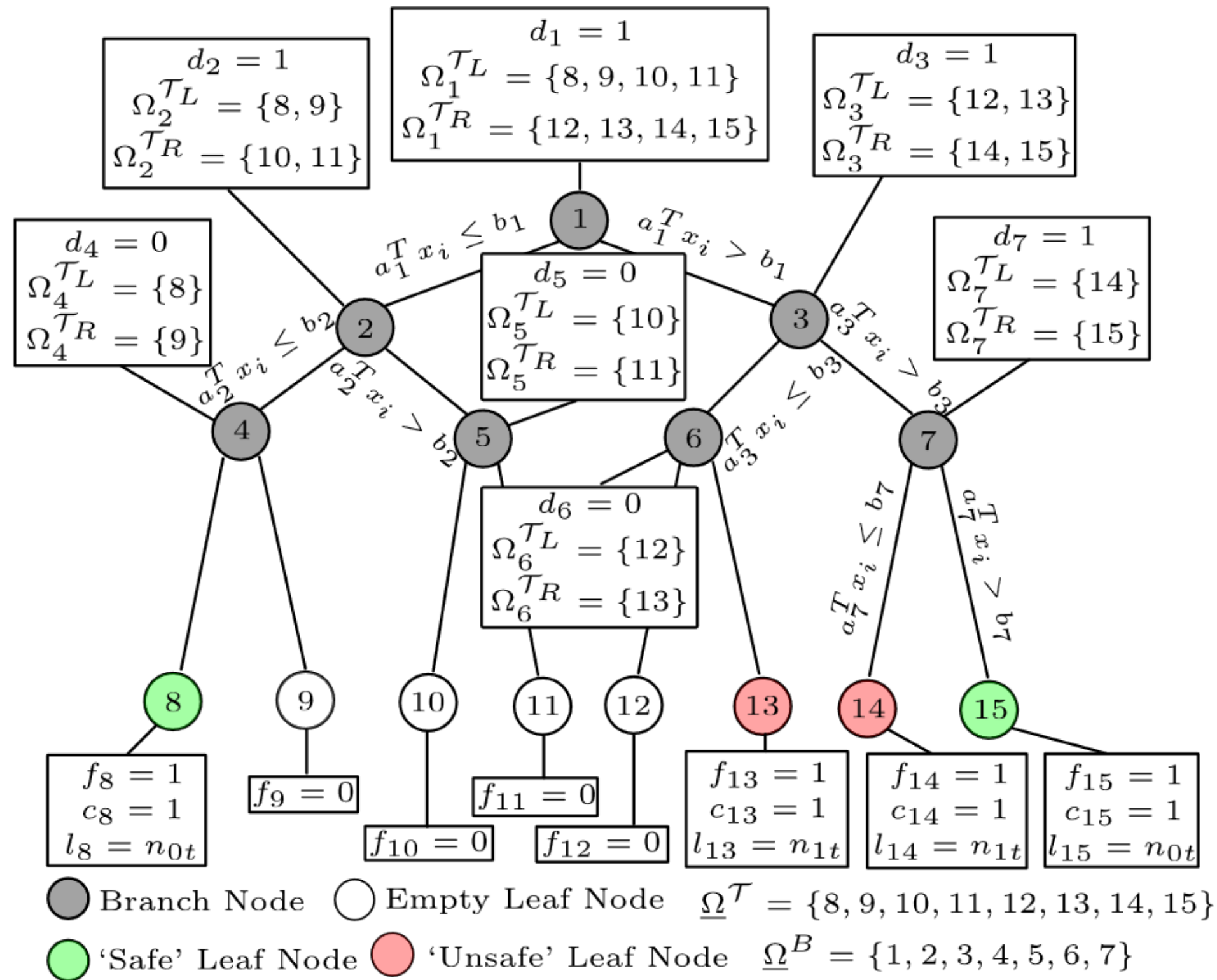
‘Safe’ classifications

‘Unsafe’ classifications

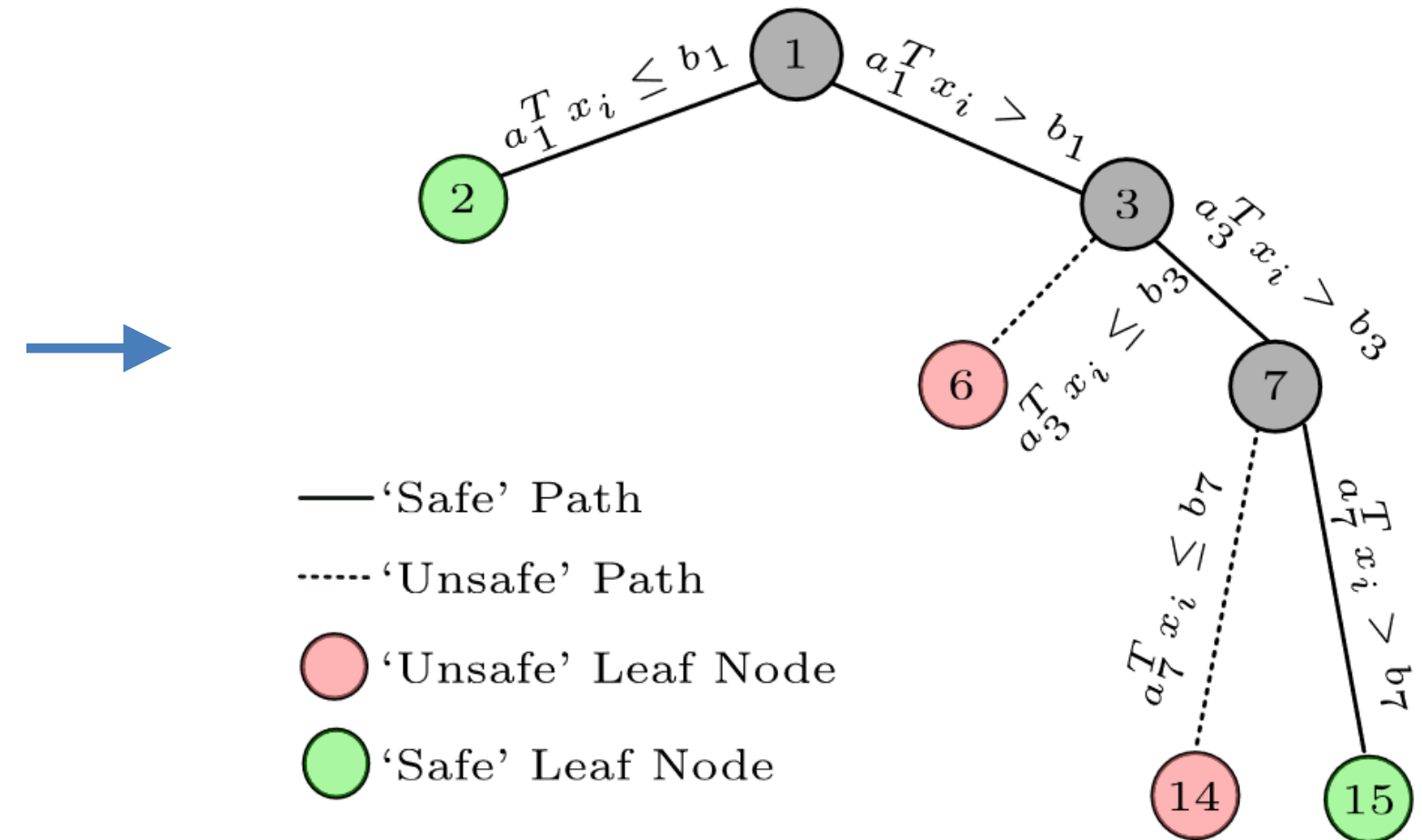
Penalize ‘false safe’ predictions (adjustable parameter)



# Optimal Classification Tree



Pruning redundancies

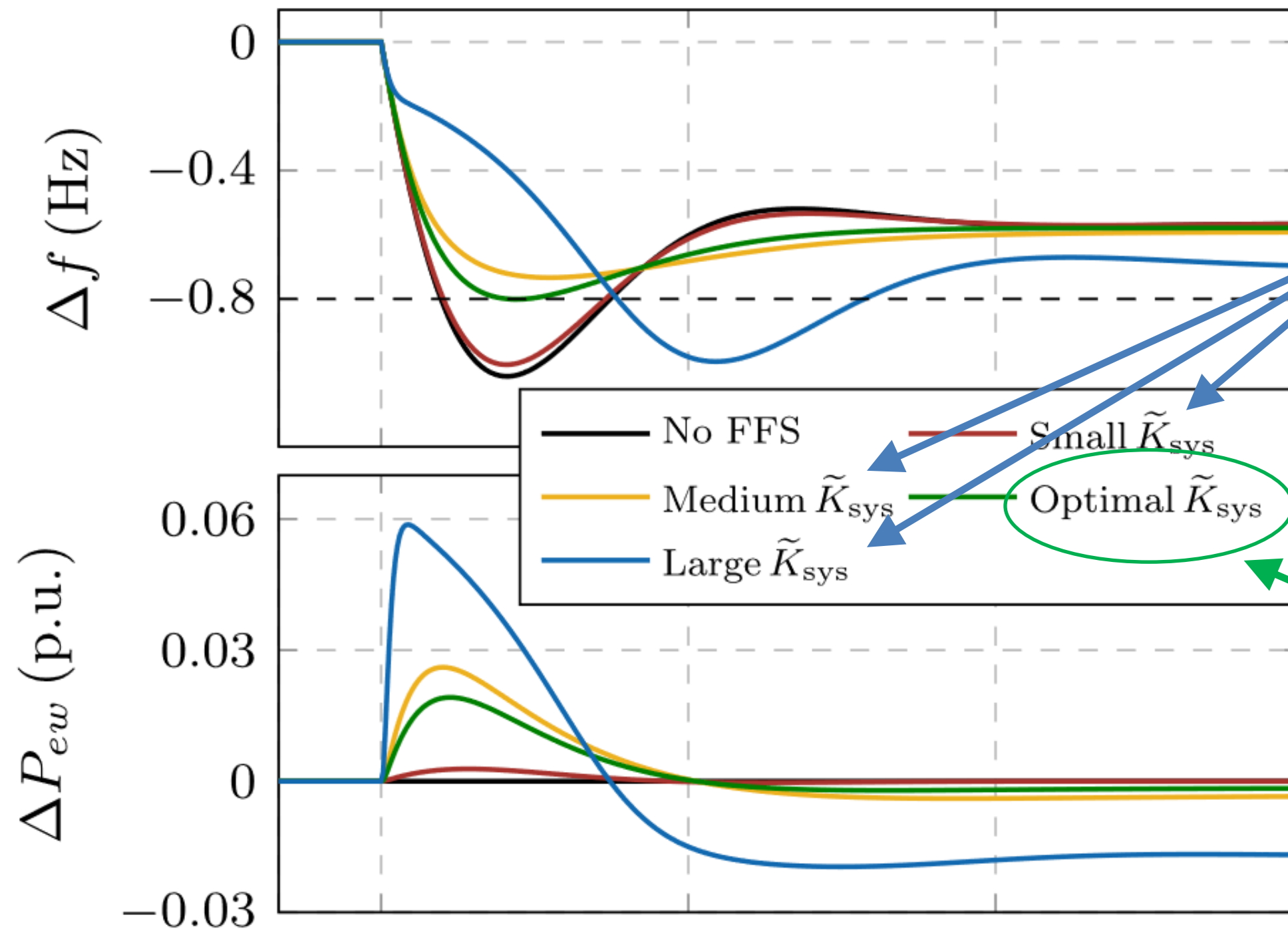


This OCT is **integrated into the OPF** as a set of constraints

# Case studies

- **Frequency-secured OPF** run for an IEEE 14-bus network
- 1,500 **labelled samples** from **dynamic simulations** in Simulink
  - ~2 days computing time (on standard laptop)
  - 70% for training, 20% for validation, 10% for testing
- **Training OCT** offline (solving MILP): ~30 min
  - Could be retrained, e.g., daily, using new datasets with updated wind and load forecasts (reduces conservativeness)

# Results



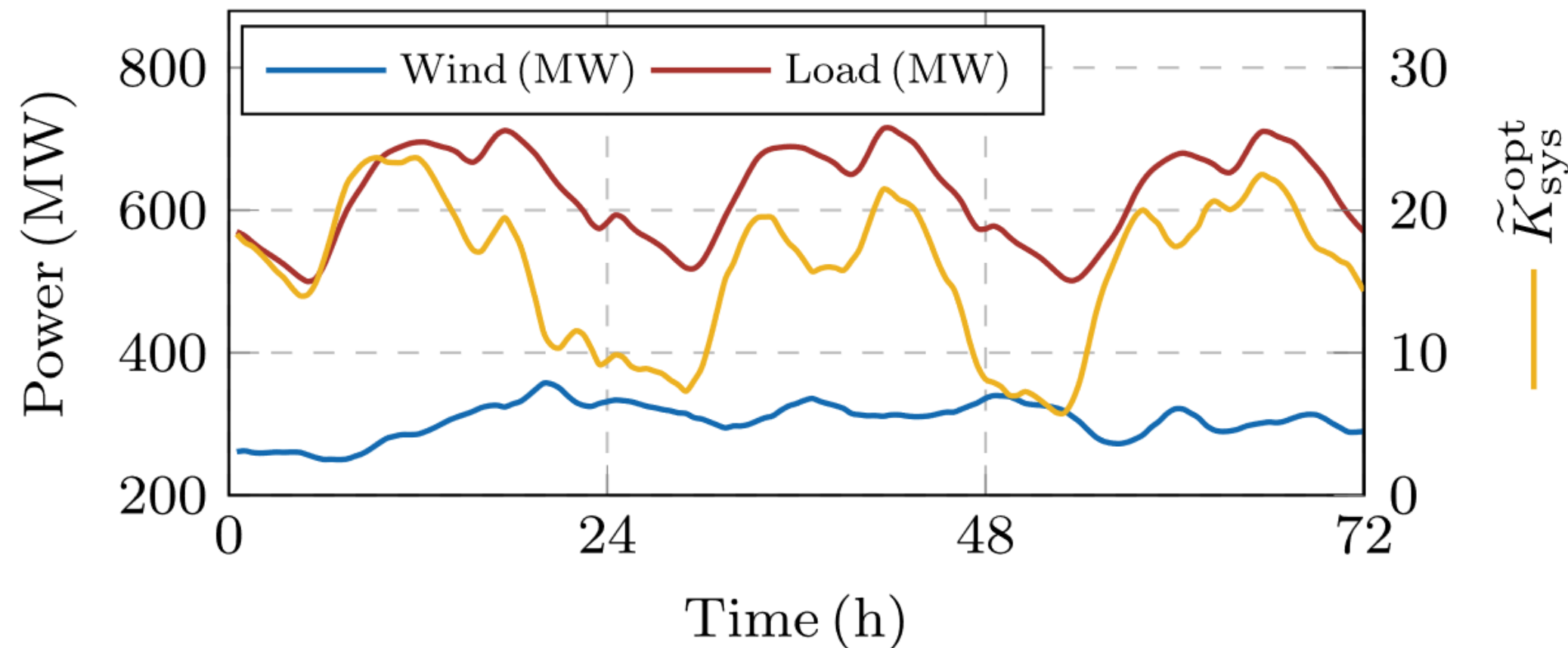
Fixed *a priori*

**Optimized** for current  
**operating condition**  
via the classification tree



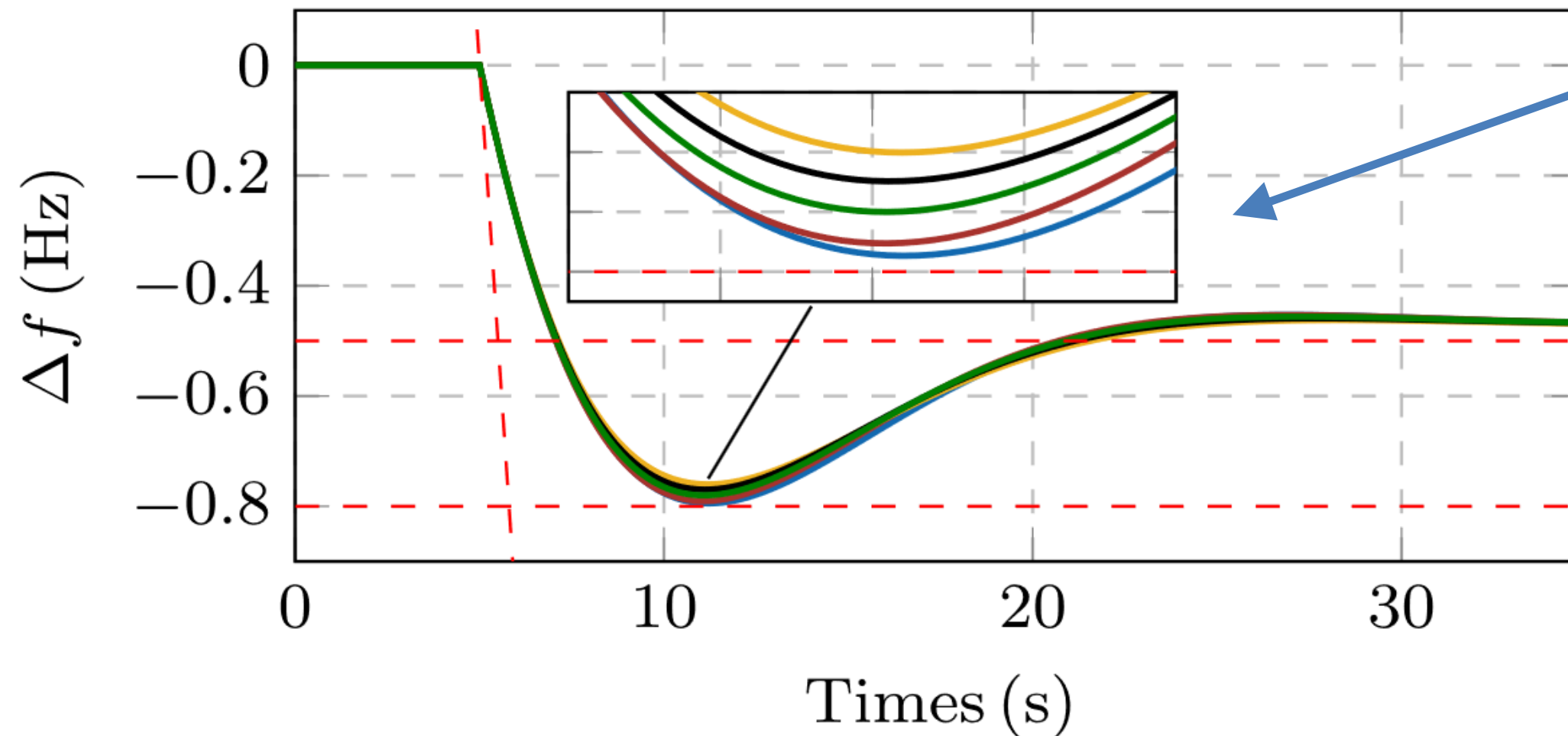
# Dispatch solutions

The **optimal** droop gain  $K_{sys}$  **fluctuates** with the system dispatch:  
roughly inversely proportional to wind power



# Security boundary

Slight underestimation of nadir due to **conservativeness** in **OCT**

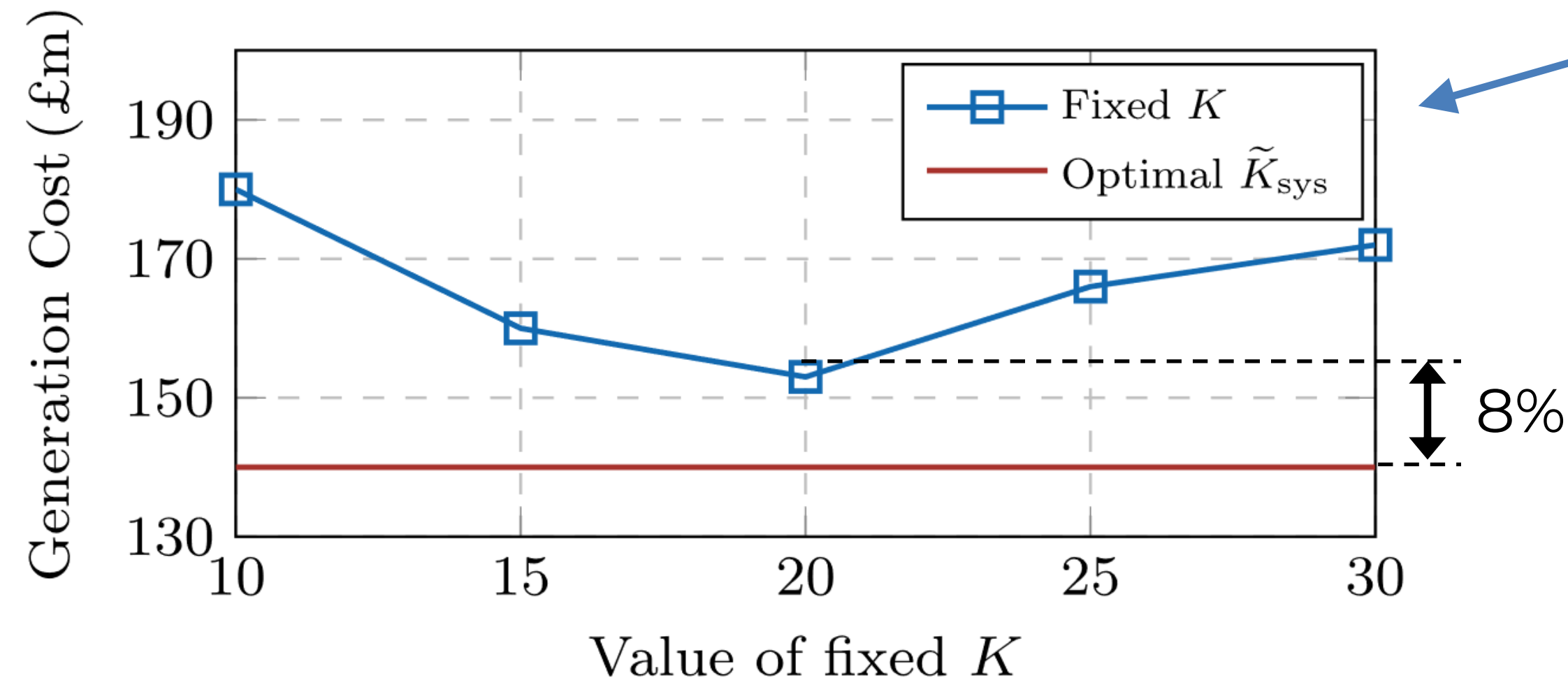


5 different  
OPF solutions,  
arbitrarily chosen

# Cost savings

System **savings of** at least **8%** compared to system-unaware controller

Weekly costs for 50% wind penetration



Note that the optimal value of fixed gain ( $K = 20$ ) can **only** be **computed** by system optimization (through the **OCT**)

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## Paper:

C. Matamala, L. Badesa et al., “Cost Allocation for Inertia and Frequency Response Ancillary Services,” *IEEE Trans. on Energy Markets*, 2024





# Cost allocation for frequency services

We have focused on optimizing the total cost of frequency services, but...

## 1. Who should cover this cost?

- Generators?
- Consumers?
- Only a subset of the former?

## 2. How much should each market participant pay?



# First, why worry about who pays?

- Currently **costs are socialized** in most countries (except Australia)
- **Until recently**, irrelevant who paid (**costs were small** due to high inertia)

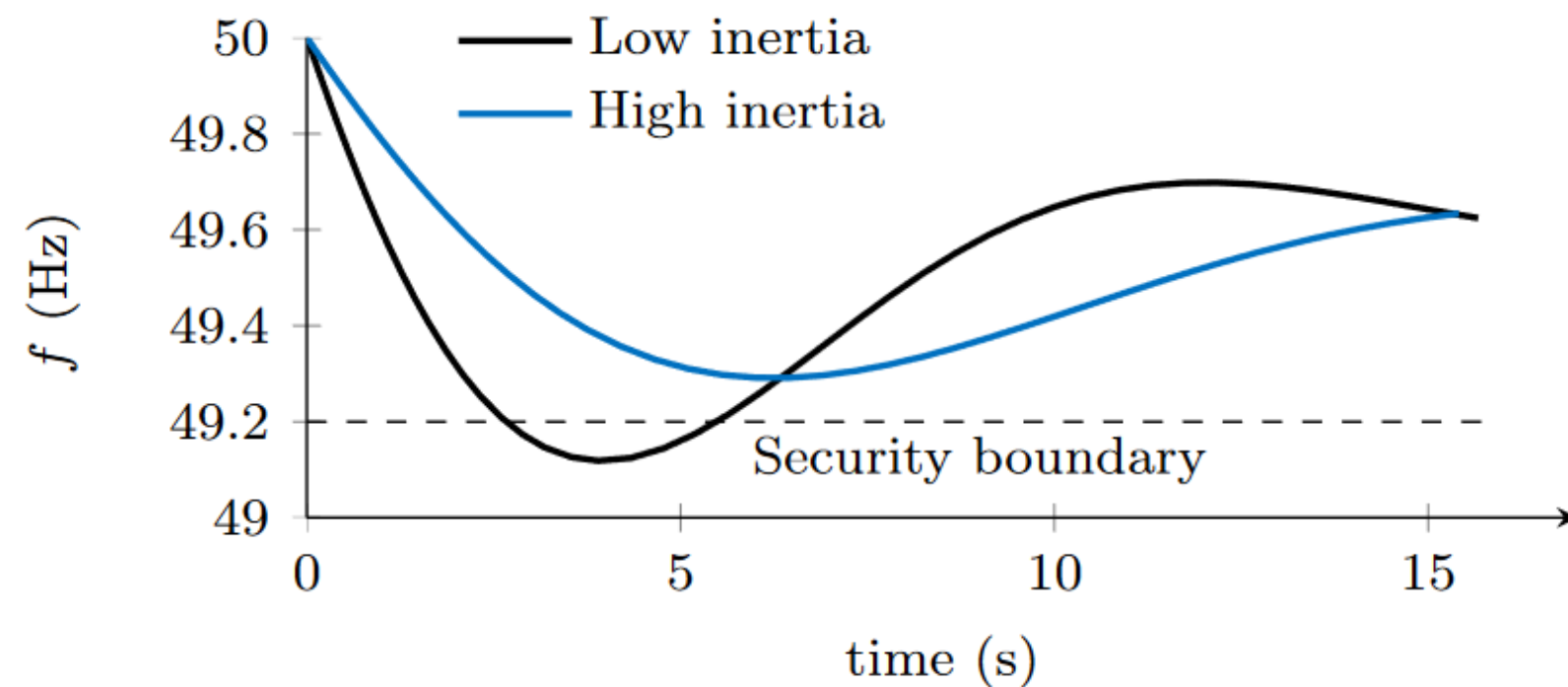
Goal of moving towards a **'causer pays' framework**:

To create **incentives to 'do less harm'** to the grid

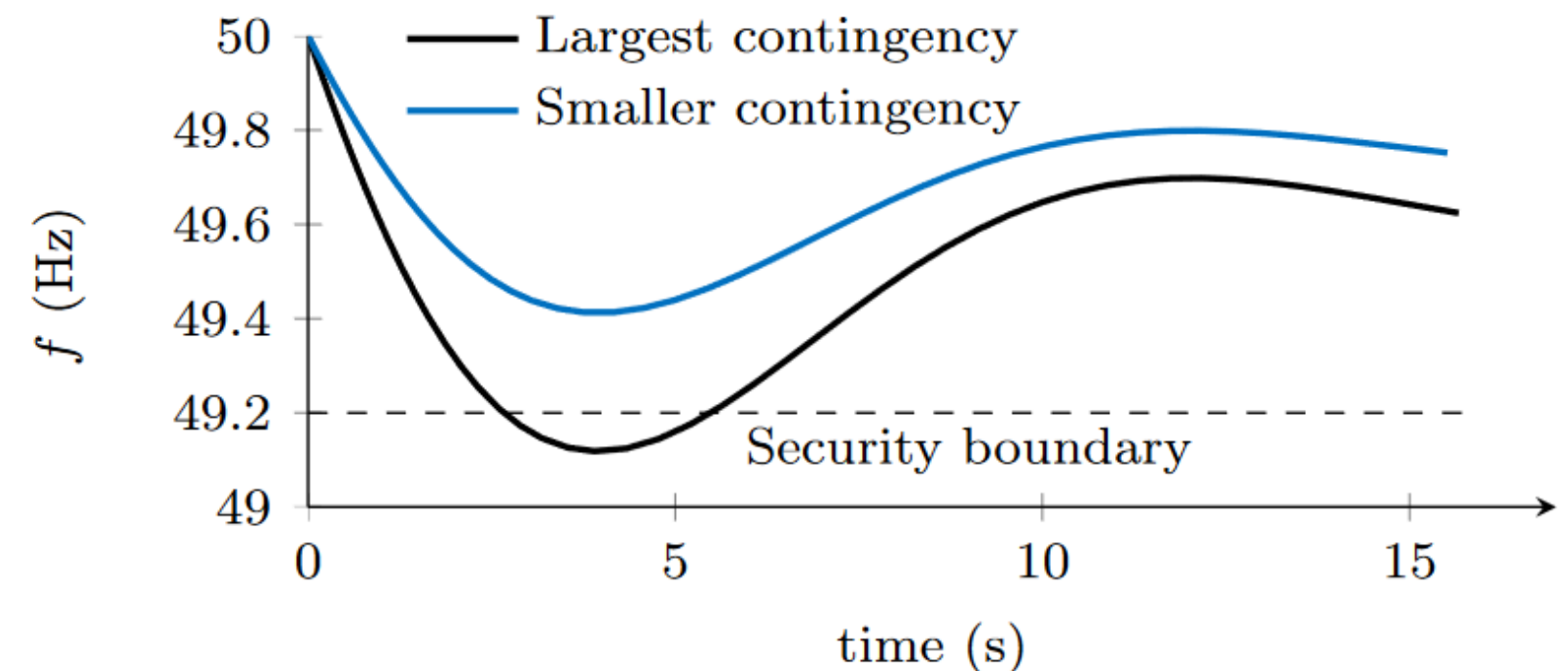
(in order to **reduce the cost** of frequency services for consumers)

# Who causes the need for frequency services?

**Large units** do: a low-inertia system would do fine if all units were small (there would be no large, sudden power imbalances)



**Impact of inertia**  
under a large contingency



**Impact of contingency size**  
in a low-inertia system

# Who causes the need for frequency services?

**Large units** do: a low-inertia system would do fine if all units were small (there would be no large, sudden power imbalances)

We **rule out penalizing** the **lack of inertia**

- Inertia is a service, it should be remunerated appropriately
- But lack of inertia is not a problem by itself



# How to split the cost?

## Option 1: **proportional cost allocation**

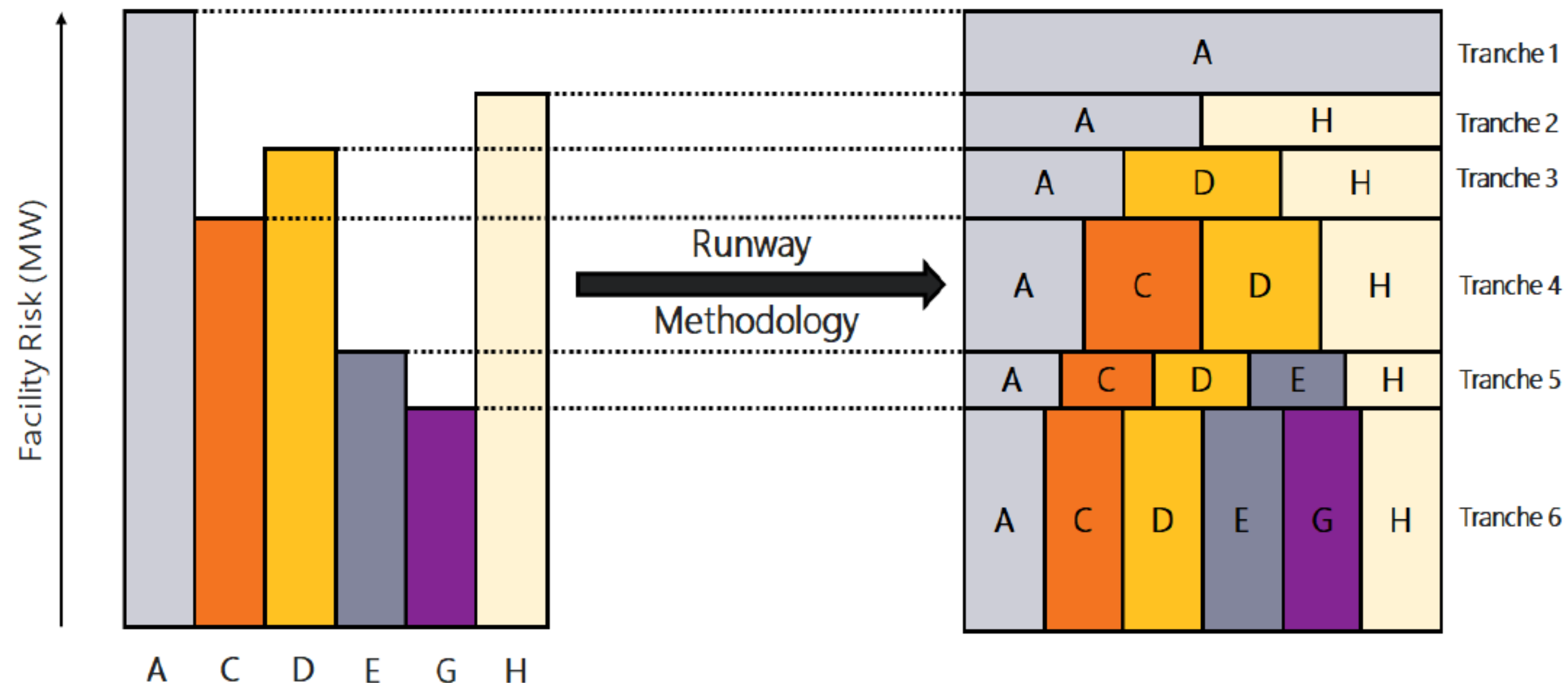
- ✓ Easy to design: **each unit pays in proportion to its size**
- ✓ Creates **incentive** for large units **to 'do less harm'**
- **Problem:** it **maintains cross-subsidies**  
(small units still subsidize large ones)

## Option 2: **sequential cost allocation** (coming next)

- ✓ Advantage: no cross-subsidies

# Sequential cost allocation (Shapley value)

Each unit pays for the **additional cost** that it creates



Reference: "A report describing the Wholesale Electricity Market in the South West Interconnected System", Australian Energy Market Operator, September 2023

# Steps

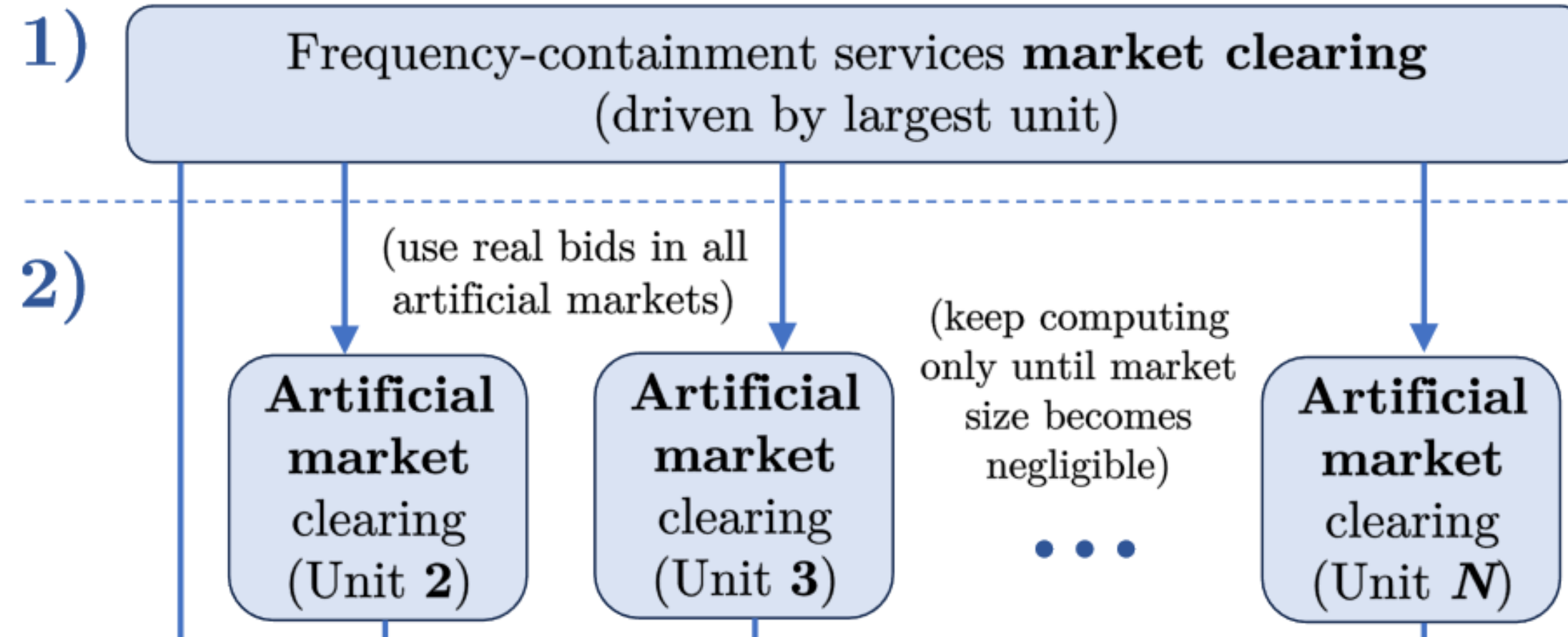


1)

Frequency-containment services **market clearing**  
(driven by largest unit)

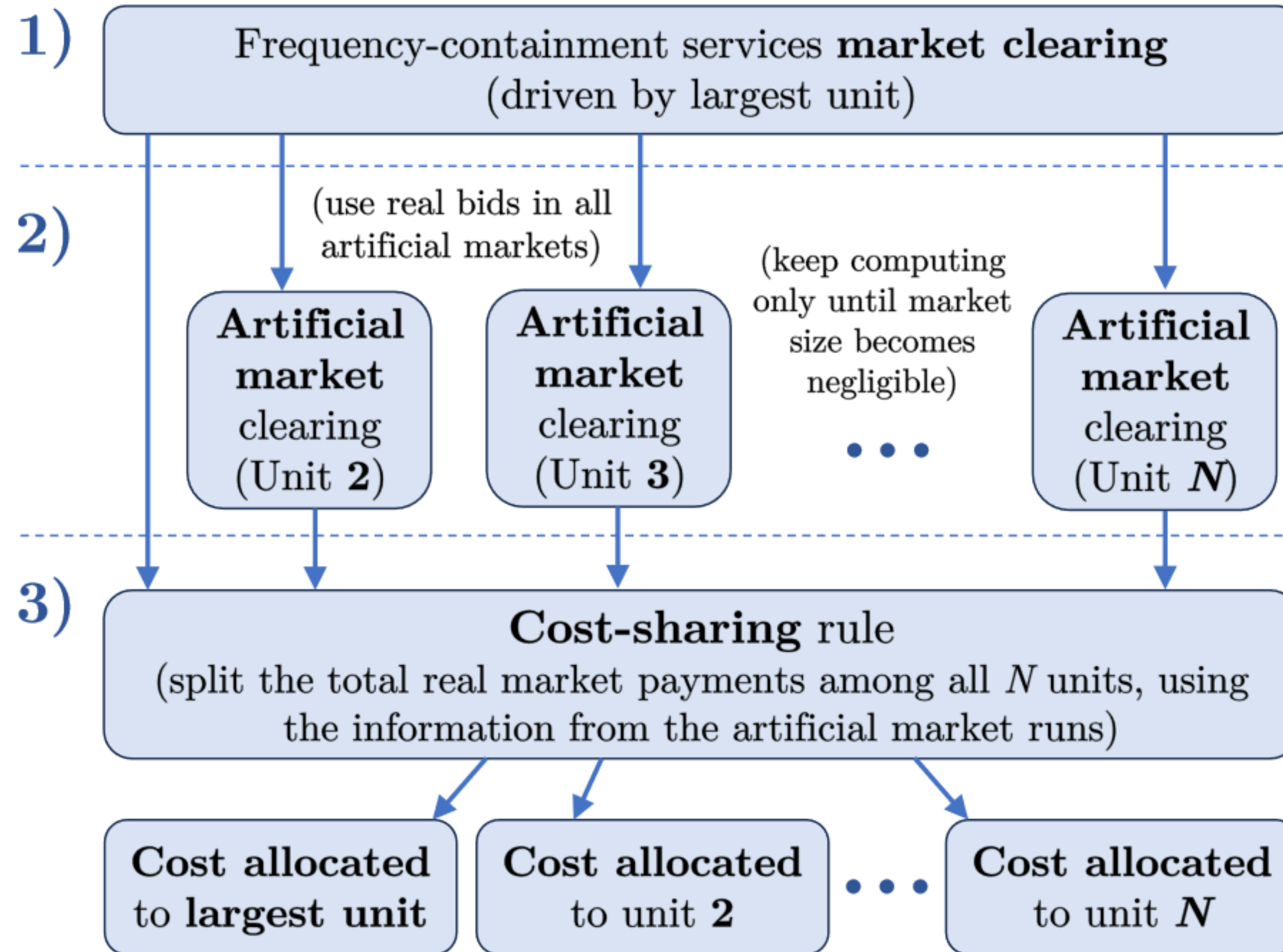


# Steps

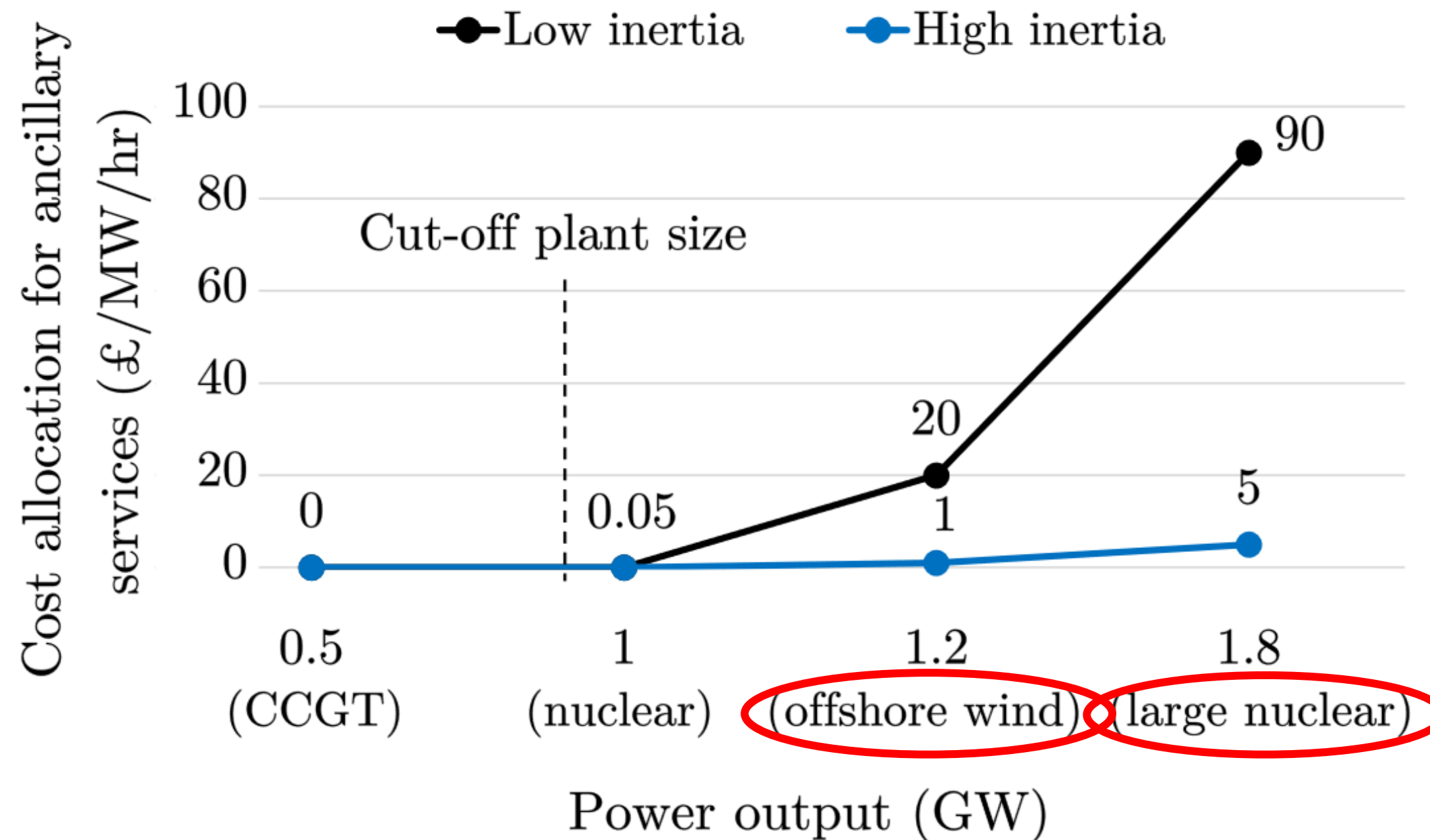




# Steps



# Analysis for Great Britain



# Benefits of the cost allocation

- To create **investment** signals

- Large units would be responsible for their system-integration cost (e.g., nuclear, offshore wind, HVDC)
- **Costs** would still **trickle down to consumers**, but appropriate economic signals for generation would be in place

- To incentivize **flexibility**

- Large units can reduce the cost they are allocated by reducing power output/demand

# Thank you for your attention!

All papers and some related code on my website:

<https://badber.github.io/>