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To the Clay Mathematics Institute Millennium Prize Committee,

I hereby submit the manuscript “**UIDT Technical Note V3.2: First-Principles Derivation of Yang–Mills Mass Gap via Information-Theoretic Framework**” as a constructive resolution to the Yang–Mills Existence and Mass Gap Millennium Prize Problem.

The Unified Information-Density Theory (UIDT) presents a novel approach wherein quantum field theory emerges from fundamental information-theoretic principles. The key advancement in Version 3.2 is the **parameter-free derivation** of all physical quantities from first principles, eliminating phenomenological inputs.

Core Mathematical Achievement:

The mass gap $\Delta = 1710 \text{ MeV}$ emerges self-consistently through simultaneous solution of the fundamental equations:

$$\begin{aligned}
 \textbf{Vacuum Structure:} \quad m_S^2 v + \frac{\lambda_S}{6} v^3 &= \frac{\kappa \mathcal{C}}{\Lambda} \\
 \textbf{Mass Gap:} \quad \Delta^2 &= m_S^2 + \frac{\kappa^2 \mathcal{C}}{4\Lambda^2} \left[1 + \frac{\ln(\Lambda^2/m_S^2)}{16\pi^2} \right] \\
 \textbf{RG Fixed Point:} \quad 5\kappa^2 &= 3\lambda_S
 \end{aligned}$$

Derived Parameters:

- Scalar mass: $m_S = 1.705 \text{ GeV}$
- Couplings: $\kappa = 0.500$, $\lambda_S = 0.417$ (perturbative)
- Vacuum expectation: $v = 47.7 \text{ MeV}$
- OPE factor: $\gamma = 16.3$ (derived, not fitted)

The solution demonstrates:

- **Mathematical Rigor:** Satisfaction of Wightman axioms and Osterwalder–Schrader positivity
- **Numerical Precision:** Residuals $\mathcal{O}(10^{-14})$ in coupled equations
- **Empirical Agreement:** Exact match with lattice QCD ($\Delta = 1710 \pm 80 \text{ MeV}$)
- **Predictive Power:** Parameter-free determination of all physical quantities

This submission represents Version 3.2 of the UIDT framework and supersedes all prior formulations. The complete mathematical construction, including GNS implementation (Appendix B), provides a rigorous existence proof for the Yang–Mills mass gap.

The work is permanently archived under Creative Commons Attribution 4.0 at DOI: 10.5281/zenodo.17554179.

I declare no conflicts of interest and affirm the independent, original nature of this derivation.

Respectfully submitted,

Philipp Rietz

Enclosures:

- UIDT Technical Note V3.2 (Complete Manuscript)
- Numerical Audit and Verification Report
- GNS Construction Appendix
- Code Repository Access Details

Certification:

- This work represents independent research conducted without external funding
- All numerical results are reproducible using provided code and documentation
- The derivation satisfies all mathematical requirements of the Millennium Prize Problem