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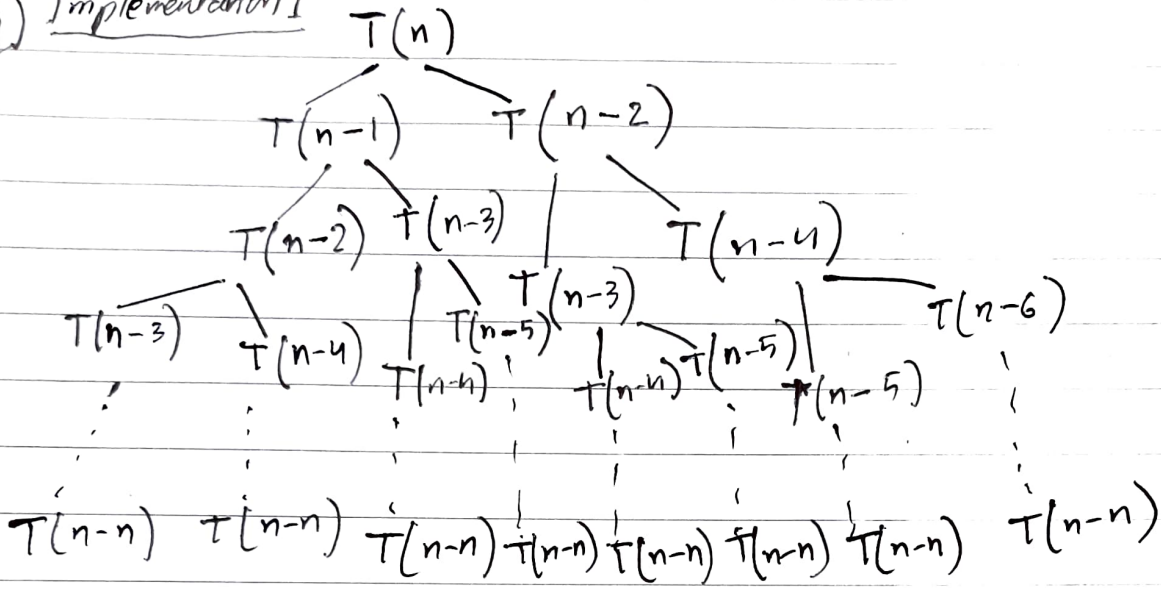
Section: 4

TASK 2

(2) Implementation 1



node = n | height = n
height = log n | node = 2^n

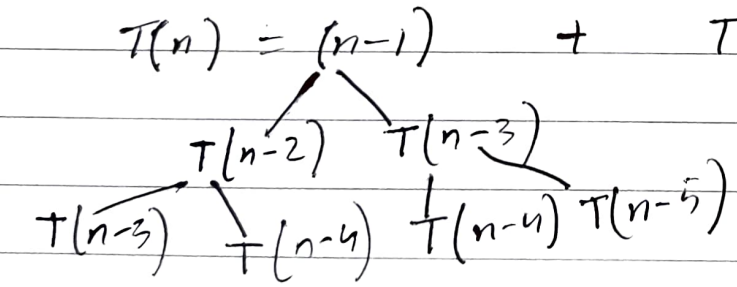
node	height
n	log n
2^n	$2^{\log_2 n}$
2^n	n

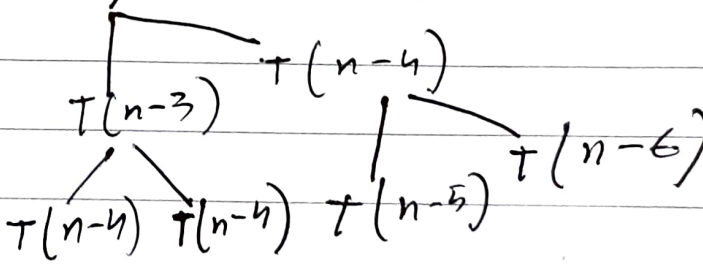
Time complexity: $O(2^n)$

Implementation-2

```
def fibonacci_2(n)
    fibonacci_array = [0,1]
    if n<0:
        print("Invalid input!")          } O(1)
    elif n<=2:
        return fibonacci_array[n-1]      } O(1)
    else:
        for i in range(2,n):             } O(n)
            fibonacci_array.append(fibonacci_array[i-1]+
                                   fibonacci_array[i-2])
        return fibonacci_array[-1]

n = int(input("Enter a number: "))
nth_fib = fibonacci_2(n)
print("The %d-th fibonacci number is %d" % (n, nth_fib))
```





function runs two times here

$$T(n) = 2n$$
$$= O(n)$$

TASK 4

(4)

```
for i=0 to n-1        } O(n)
    for j=0 to n-1    } O(n)
        for k=0 to n-1
            C[i,j] += A[i,k] * B[k,j]   } O(n)
        end for
    end for
end for
```

∴ Time complexity $= O(n^3)$

TASK 5

(5)

1. $T(n) = T(n/2) + (n-1)$

$a=1$, $b=2$, $c=1$, $k=1$

$b^k = 2^1 = 2$

$b^k > a$

Time complexity $= O(n^k)$

$= O(n)$

2. $T(n) = T(n-1) + n-1$

$T(n-1) = T(n-2) + (n-1) - 1$

$T(n) = (T(n-2) + (n-1) - 1) + n - 1$

$T(n) = T(n-2) + n - 2 + n - 1$

$T(n-2) = T(n-3) + (n-2) - 1$

$T(n) = T(n-3) + (n-3) + (n-2) + (n-1)$

$T(n) = T(n-k) + (n-k) + (n-(k-1)) + n-(k-2)$
$+ \cdots\cdots + (n-3) + (n-2) + (n-1)$

let $n-k = 1$

$n = k+1$

$T(n) = T(1) + (k+1) - k + (k+1-k+1) +$
$(k-1-k+2) + \cdots (n-2) + (n-1)$

$= 0 + 1 + 2 + 3 + \cdots\cdots (n-2) + (n-1)$

$= \frac{n(n-1)}{2}$

$= O(n^2)$

3. $T(n) = T(n/3) + 2T(n/3) + n$

$T(n) = 3T(n/3) + n$

$a = 3, b = 3, c = 1, k = 1$

$b^k = 3^1 = 3 = a$

$b^k = a$

Time complexity $= O(n^k \log n)$

$= O(n \log n)$

4. $T(n) = 2T(n/2) + n^2$

$a = 2, b = 2, c = 1, k = 2$

$b^k = 2^2 = 4$

$b^k > 0$

Time complexity $= O(n^k)$

$= O(n^2)$ (proved)