US Open Men 2013 Analysis

April 16, 2017

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1 Summary

- Predicting the results of sporting matches is complicated business. Factors that cannot be captured by data such as crowd enthusiasm, home field advantage, and rivalries do exist and have an impact on the outcome.
- We began our analysis of the 2013 US Men's Open with 42 variables broken into one response variables, 18 un-useful variables, 1 un-useful categorical variable and 23 possible covariates. Breaking the data 70/30 into training and testing data, we developed a prediction model utilizing 22 covariates to predict the Final Games Won for Player 1. This model had an R^2 of 88.15% and an Adjusted R^2 of 84.62%—there was someone work to be done in slimming the number of predictor variables.
- Through Partial F Testing, we eliminated 17 variables from our model to be left with BCP.1(break points created by player 1), BPW.1(break points won by player 1), TPW.1(total points won by player 1), TPW.2(total points won by player 2).
- Due to the nature of our data, we assumed early on that multicollinearity would be an issue. We found, using Variance Inflation Factors (VIF), that TPW.1 and TPW.2 were correlated. Outside of the data, this makes sense as the more points player one wins, the more points player two will no win. Also, both final points for the players will increase due to the nature of a tennis game. To adjust for this multicollinearity, we removed TPW.1 from the model.
- Our final model, FNL1= 6.722e-01 BPC.1 + 1.892e-01 TPW.2, suggests that As the number of break points created by player 1 increases by 1, the final number of games won by player 1 XXXXXX As the number of break points won by player 1 increases by 1, the final number of games won by player 1 XXXXXX As player 2's total number of points increases by 1, the final number of games won by player 1 XXXXXX
- After our model was built, we applied our testing data to the model..

2 Business Understanding

This is a public, multivariate dataset concerning the US Men's Tennis Open in 2013. Our data is sourced from UCI Machine Learning Repository (Jauhari, Morankar, Fokoue)

(https://archive.ics.uci.edu/ml/datasets/Tennis+Major+Tournament+Match+Statistics).

It has 42 variables in all. Each observation represents a singles tennis match.

In tennis, a match is composed of two to three sets. To win a match, a player must win two sets. A set is composed of at least six games. To win a set, one must win at least six games, with a two game advantage over the games won by the opposing player. The scoring of games in tennis is a little odd. The score begins 0-0 or "love." After the first point is scored, the score is "love"-15. The scoring continues sequentially, "love" (0 points), 15(2 points), 30(3 points), 40(4 points). The game must be won by two points. If the score is 40-40, that is called 40-all or "deuce," the one player must score an additional two points consecutively to win the game.

The response variable which we will be attempting to predict will by FNL.1 (the final number of games won by player 1). In predicting this variable, some other variables become obsolete such as Result and STX.Y. Four other variables that we will not include in our analysis are WNR.X and UFE.X as no data populates those fields. Below is the complete list of variables and their uses.

2.1 Variables in the data set

Use	Variable	Type	Description
None	Player 1		Name of player 1
None	Player 2		Name of player 2
None	Result	Ordinal $(0/1)$	Referenced on player 1. If player 1 wins- result=1 (FNL.1>FNL.2)
Covariate	FSP.1	Real Number	First serve percentage for player 1
Covariate	FSW.1	Real Number	First serve won by player 1
Covariate	SSP.1	Real Number	Second serve percentage for player 1
Covariate	SSW.1	Real Number	Second serve won by player 1
Covariate	ACE.1	Numeric-Integer	Aces won by player 1
Covariate	DBF.1	Numeric-Integer	Double faults committed by player 1
None	WNR.1	Numeric	Winners earned by player 1
None	UFE.1	Numeric	Unforced errors committed by player 1
Covariate	BPC.1	Numeric	Break points created by player 1
Covariate	BPW.1	Numeric	Break points won by player 1
Covariate	NPA.1	Numeric	Net points attempted by player 1
Covariate	NPW.1	Numeric	Net points won by player 1
Covariate	TPW.1	Numeric	Total points won by player 1
None	ST1.1	Numeric-Integer	Set 1 Result for player 1
None	ST2.1	Numeric-Integer	Set 2 Result for player 1
None	ST3.1	Numeric-Integer	Set 3 Result for player 1
None	ST4.1	Numeric-Integer	Set 4 Result for player 1
None	ST5.1	Numeric-Integer	Set 5 Result for player 1
Response	FNL.1	Numeric-Integer	Final number of games won by player 1
Covariate	FSP.1	Real Number	First serve percentage for player 2
Covariate	FSW.2	Real Number	First serve won by player 2
Covariate	SSP.2	Real Number	Second servce percentage for player 2
Covariate	SSW.2	Real Number	Second serve won by player 2
Covariate	ACE.2	Numeric-Integer	Aces won by player 2
Covariate	DBF.2	Numeric-Integer	Double faults committed by player 2
None	WNR.2	Numeric	Winners earned by player 2
None	UFE.2	Numeric	Unforced errors committed by player 2
Covariate	BPC.2	Numeric	Break points created by player 2
Covariate	BPW.2	Numeric	Break points won by player 2
Covariate	NPA.2	Numeric	Net points attempted by player 2
Covariate	NPW.2	Numeric	Net points won by player 2
Covariate	TPW.2	Numeric	Total points won by player 2
None	ST2.1	Numeric-Integer	Set 1 Result for player 2
None	ST2.2	Numeric-Integer	Set 2 Result for player 2
None	ST2.3	Numeric-Integer	Set 3 Result for player 2
None	ST2.4	Numeric-Integer	Set 4 Result for player 2
None	ST2.5	Numeric-Integer	Set 5 Result for player 2
None	FNL.2	Numeric-Integer	Final number of games won by player 2
Covariate	Round	Numeric-Integer	Round of the tournament at which the game is played

3 Data Understanding

- $\bullet\,$ We will use ${\tt dim}$ function to get the dimensions of the data
- \bullet str function to get the variable information
- head function to read first few observations
- summary function to get a summary of the data set

3.1 Data set summary

```
usopen <- read.csv("USOpen-men-2013.csv")
dim(usopen)
## [1] 126
str(usopen)
                   126 obs. of 42 variables:
## 'data.frame':
   $ Player1: Factor w/ 81 levels "Adrian Mannarino",..: 65 74 37 7 26 47 10 60 24 54 ...
   $ Player2: Factor w/ 79 levels "Adrian Mannarino",..: 52 2 30 17 23 9 18 35 5 6 ...
   $ Round : int 1 1 1 1 1 1 1 1 1 ...
## $ Result : int 1 1 0 0 1 0 0 0 0 1 ...
## $ FNL1
            : int 3 3 2 1 3 1 2 1 2 3 ...
##
   $ FNL2
            : int 0033133230...
##
   $ FSP.1 : int 63 61 55 52 58 59 53 51 58 51 ...
## $ FSW.1 : int 45 44 61 41 54 68 59 39 68 35 ...
## $ SSP.1 : int 37 39 45 48 42 41 47 49 42 49 ...
##
   $ SSW.1 : int 16 19 32 19 30 37 44 24 31 27 ...
##
   $ ACE.1 : int 7 3 11 13 21 20 8 17 15 4 ...
## $ DBF.1 : int 7 2 13 8 3 11 8 6 8 5 ...
## $ WNR.1 : logi NA NA NA NA NA NA ...
   $ UFE.1 : logi NA NA NA NA NA NA ...
## $ BPC.1 : int 5 4 5 2 5 1 10 0 5 9 ...
## $ BPW.1 : int 16 13 13 9 16 1 18 1 22 11 ...
##
   $ NPA.1 : int 18 NA NA NA NA 30 NA 5 NA NA ...
##
   $ NPW.1 : int 25 NA NA NA NA 42 NA 10 NA NA ...
## $ TPW.1 : int 106 99 149 97 148 133 183 82 159 117 ...
## $ ST1.1 : int 6 6 6 5 6 7 6 3 6 6 ...
## $ ST2.1 : int
                  6 6 3 6 6 2 3 7 3 7 ...
   $ ST3.1 : int 6 6 6 3 6 6 7 3 6 7 ...
## $ ST4.1 : int NA NA 6 0 6 6 7 NA 6 NA ...
## $ ST5.1 : int NA NA 1 NA NA 4 NA 4 NA ...
##
   $ FSP.2 : int
                  59 56 55 55 61 71 59 55 49 49 ...
##
   $ FSW.2 : int 37 37 66 52 63 72 65 42 58 35 ...
## $ SSP.2 : int 41 44 45 45 39 29 41 45 51 51 ...
## $ SSW.2 : int 17 15 27 27 30 26 38 28 43 20 ...
   $ ACE.2 : int 6 18 10 16 8 6 2 12 10 4 ...
## $ DBF.2 : int 4 8 9 3 2 1 7 2 12 3 ...
## $ WNR.2 : logi NA NA NA NA NA NA ...
##
   $ UFE.2 : logi NA NA NA NA NA NA ...
##
   $ BPC.2 : int 1 0 5 6 0 3 11 2 4 7 ...
## $ BPW.2 : int 3 1 15 9 3 11 26 9 14 12 ...
## $ NPA.2 : int 30 NA NA NA NA 30 NA 10 NA NA ...
## $ NPW.2 : int 40 NA NA NA NA 48 NA 10 NA NA ...
   $ TPW.2 : int 83 71 149 121 123 151 187 104 160 103 ...
## $ ST1.2 : int 3 3 7 7 7 6 7 6 3 4 ...
## $ ST2.2 : int
                  4 3 6 4 2 6 6 6 6 6 ...
##
   $ ST3.2
           : int
                   2 4 2 6 3 7 6 6 1 5 ...
   $ ST4.2 : int NA NA 2 6 3 7 5 NA 7 NA ...
   $ ST5.2 : int NA NA 6 NA NA 6 NA 6 NA 6 NA ...
head(usopen)
```

```
##
                  Plaver1
                                   Player2 Round Result FNL1 FNL2 FSP.1 FSW.1
## 1
        Richard Gasquet Michael Russell
                                                 1
                                                         1
                                                              3
                                                                    0
                                                                          63
                                                                                45
## 2
         Stephane Robert Albano Olivetti
                                                              3
                                                                    0
                                                                          61
                                                                                 44
## 3 Jan-Lennard Struff Guillaume Rufin
                                                         0
                                                              2
                                                                    3
                                                                          55
                                                                                 61
                                                 1
                                                         0
                                                              1
                                                                    3
                                                                          52
## 4
            Aljaz Bedene Dmitry Tursunov
                                                 1
                                                                                41
## 5
         Feliciano Lopez
                            Florent Serra
                                                 1
                                                         1
                                                              3
                                                                    1
                                                                          58
                                                                                54
     Kenny De Schepper
                            Bradley Klahn
                                                 1
                                                         0
                                                                    3
                                                                          59
     SSP.1 SSW.1 ACE.1 DBF.1 WNR.1 UFE.1 BPC.1 BPW.1 NPA.1 NPW.1 TPW.1 ST1.1
##
## 1
         37
               16
                       7
                              7
                                   NA
                                          NA
                                                  5
                                                        16
                                                              18
                                                                           106
## 2
         39
               19
                       3
                              2
                                   NA
                                          NA
                                                  4
                                                        13
                                                              NA
                                                                     NA
                                                                            99
                                                                                    6
## 3
                      11
         45
               32
                             13
                                   NA
                                          NA
                                                  5
                                                        13
                                                              NA
                                                                     NA
                                                                           149
                                                                                    6
## 4
         48
               19
                      13
                              8
                                   NA
                                          NA
                                                  2
                                                         9
                                                              NA
                                                                     NA
                                                                            97
                                                                                    5
## 5
         42
               30
                      21
                              3
                                   NA
                                          NA
                                                  5
                                                        16
                                                              NA
                                                                     NA
                                                                           148
                                                                                    6
## 6
         41
               37
                      20
                                   NA
                                          NA
                                                              30
                                                                     42
                                                                           133
                                                                                    7
                             11
                                                  1
                                                         1
##
     ST2.1 ST3.1 ST4.1 ST5.1 FSP.2 FSW.2 SSP.2 SSW.2 ACE.2 DBF.2 WNR.2 UFE.2
## 1
                                          37
         6
                6
                      NA
                             NA
                                   59
                                                 41
                                                        17
                                                               6
                                                                      4
                                                                            NA
                                                                                   NA
## 2
         6
                6
                      NA
                             NA
                                   56
                                          37
                                                 44
                                                        15
                                                              18
                                                                      8
                                                                            NA
                                                                                   NA
## 3
          3
                6
                                   55
                                          66
                                                 45
                                                        27
                                                              10
                                                                            NA
                                                                                   NA
                       6
                             1
## 4
         6
                3
                       0
                            NA
                                   55
                                          52
                                                 45
                                                        27
                                                              16
                                                                      3
                                                                            NA
                                                                                   NA
## 5
         6
                6
                       6
                            NA
                                   61
                                          63
                                                 39
                                                        30
                                                               8
                                                                      2
                                                                            NA
                                                                                   NA
## 6
          2
                6
                       6
                             NA
                                   71
                                          72
                                                 29
                                                        26
                                                               6
                                                                      1
                                                                            NA
                                                                                  NA
     BPC.2 BPW.2 NPA.2 NPW.2 TPW.2 ST1.2 ST2.2 ST3.2 ST4.2 ST5.2
##
## 1
          1
                3
                             40
                                   83
                                           3
                                                  4
                                                         2
                      30
                                                              NA
                                                                     NA
## 2
                                                  3
         0
                1
                      NA
                             NA
                                   71
                                           3
                                                         4
                                                              NA
                                                                     NA
## 3
          5
               15
                      NA
                            NA
                                  149
                                           7
                                                         2
                                                               2
                                                                      6
                                                  6
## 4
          6
                9
                      NA
                            NA
                                  121
                                           7
                                                  4
                                                         6
                                                               6
                                                                     NA
## 5
          0
                3
                      NA
                            NA
                                  123
                                           7
                                                  2
                                                         3
                                                               3
                                                                     NA
## 6
          3
               11
                      30
                             48
                                  151
                                           6
                                                  6
                                                         7
                                                               7
                                                                     NA
```

summary(usopen)

##	P	Player1	Player2	Round	Result
##	Novak Djokovic	: 6 Rafae	el Nadal : 7 M	Min. :1	Min. :0.0000
##	Richard Gasquet	: 6 David	d Ferrer : 5	lst Qu.:1	1st Qu.:0.0000
##	Andy Murray	: 5 Mikha	ail Youzhny: 4 M	Median :1	Median :0.0000
##	Roger Federer	: 4 Milos	s Raonic : 4 M	Mean :1	Mean :0.4683
##	Stanislas Wawri	nka: 4 Tomas	s Berdych : 4	3rd Qu.:1	3rd Qu.:1.0000
##	Tommy Robredo	: 4 Denis	s Istomin : 3 N	Max. :1	Max. :1.0000
##	(Other)	:97 (Othe	er) :99		
##	FNL1	FNL2	FSP.1	FSW	.1
##	Min. :0.000	Min. :0.000) Min. :38.00	Min.	:14.00
##	1st Qu.:1.000	1st Qu.:1.000	1st Qu.:53.00	1st Qu.	:38.00
##	Median :2.000	Median:3.000	Median :59.00	Median	:47.00
##	Mean :1.841	Mean :1.881	Mean :58.65	Mean	:47.44
##	3rd Qu.:3.000	3rd Qu.:3.000	3rd Qu.:63.00	3rd Qu.	:57.00
##	Max. :3.000	Max. :3.000	Max. :75.00	Max.	:87.00
##					
##	SSP.1	SSW.1	ACE.1	DBI	F.1
##	Min. :25.00	Min. : 8.00			: 0.000
##	1st Qu.:37.00	1st Qu.:17.00) 1st Qu.: 5.000) 1st Qu	.: 3.000
##	Median :41.00	Median :23.00	Median : 8.000) Median	: 5.000
##	Mean :41.35	Mean :23.38	8 Mean : 8.508	8 Mean	: 4.952
##	3rd Qu.:47.00	3rd Qu.:29.00	3rd Qu.:11.000) 3rd Qu	.: 7.000
##	Max. :62.00	Max. :45.00	Max. :29.000	Max.	:14.000
##					

```
BPC.1
                                                        BPW.1
##
    WNR.1
                    UFE.1
##
   Mode:logical
                   Mode:logical
                                  Min.
                                        : 0.000
                                                         : 0.00
                                                   Min.
   NA's:126
##
                   NA's:126
                                  1st Qu.: 2.000
                                                    1st Qu.: 7.00
##
                                  Median : 5.000
                                                   Median :10.50
##
                                  Mean : 4.198
                                                    Mean :10.26
##
                                  3rd Qu.: 6.000
                                                    3rd Qu.:14.00
##
                                  Max.
                                        :10.000
                                                    Max. :23.00
##
##
        NPA.1
                        NPW.1
                                        TPW.1
                                                         ST1.1
##
          : 4.00
                         : 4.00
                                                           :0.000
   Min.
                    Min.
                                    Min. : 38.0
                                                     Min.
   1st Qu.:12.00
                    1st Qu.:19.75
                                    1st Qu.: 91.0
                                                     1st Qu.:4.000
                                    Median :111.5
                                                     Median :6.000
##
   Median :17.00
                    Median :25.50
   Mean :18.28
                    Mean
                           :27.86
                                    Mean :112.9
                                                     Mean
                                                            :4.968
   3rd Qu.:25.00
                                                     3rd Qu.:6.000
##
                    3rd Qu.:36.25
                                    3rd Qu.:137.0
##
   Max.
           :39.00
                    Max.
                           :63.00
                                    Max.
                                           :195.0
                                                     Max.
                                                            :7.000
##
   NA's
           :38
                    NA's
                           :38
##
        ST2.1
                        ST3.1
                                        ST4.1
                                                         ST5.1
##
   Min.
           :1.000
                    Min.
                           :0.000
                                    Min.
                                           :0.000
                                                     Min.
                                                            :0.00
##
   1st Qu.:3.000
                    1st Qu.:3.000
                                    1st Qu.:3.000
                                                     1st Qu.:4.00
##
   Median :6.000
                    Median :6.000
                                    Median :6.000
                                                     Median:4.00
##
   Mean
           :4.889
                    Mean
                           :4.696
                                    Mean
                                           :4.821
                                                     Mean
                                                           :4.52
##
    3rd Qu.:6.000
                    3rd Qu.:6.000
                                    3rd Qu.:6.000
                                                     3rd Qu.:6.00
           :7.000
                           :7.000
                                           :7.000
##
   Max.
                    Max.
                                    Max.
                                                     Max.
                                                           :7.00
##
                    NA's
                           :1
                                    NA's
                                           :59
                                                     NA's
                                                           :101
##
        FSP.2
                        FSW.2
                                        SSP.2
                                                         SSW.2
   Min.
          :44.00
                    Min.
                           :10.00
                                    Min.
                                           :16.00
                                                     Min.
                                                           : 2.00
##
   1st Qu.:55.00
                    1st Qu.:34.25
                                    1st Qu.:37.00
                                                     1st Qu.:16.00
   Median :58.00
                    Median :45.50
                                    Median :42.00
                                                     Median :23.00
                           :46.94
##
          :58.92
   Mean
                    Mean
                                    Mean
                                           :41.08
                                                     Mean
                                                           :23.13
                                                     3rd Qu.:28.00
   3rd Qu.:63.00
                    3rd Qu.:59.50
                                    3rd Qu.:45.00
##
   Max.
           :84.00
                    Max.
                           :90.00
                                    Max.
                                           :56.00
                                                     Max.
                                                           :48.00
##
##
        ACE.2
                         DBF.2
                                       WNR.2
                                                       UFE.2
   Min.
         : 0.000
                     Min.
                            : 0.000
##
                                      Mode:logical
                                                      Mode:logical
   1st Qu.: 4.250
##
                     1st Qu.: 3.000
                                      NA's:126
                                                      NA's:126
##
   Median: 8.000
                     Median: 4.000
   Mean : 9.262
                     Mean : 4.595
##
   3rd Qu.:11.000
                     3rd Qu.: 6.000
##
   Max.
         :39.000
                     Max.
                           :15.000
##
##
       BPC.2
                         BPW.2
                                         NPA.2
                                                          NPW.2
                                     Min. : 4.00
##
   Min. : 0.000
                     Min. : 0.00
                                                      Min.
                                                           : 6.00
   1st Qu.: 2.000
                     1st Qu.: 7.00
                                     1st Qu.:12.00
                                                      1st Qu.:19.00
##
   Median : 4.000
                     Median :10.00
                                     Median :18.50
                                                      Median :27.50
         : 4.087
                                           :19.84
                                                            :31.17
   Mean
                     Mean
                           :10.25
                                     Mean
                                                      Mean
   3rd Qu.: 6.000
                                     3rd Qu.:26.00
                                                      3rd Qu.:41.00
##
                     3rd Qu.:13.75
   Max. :11.000
##
                     Max.
                            :26.00
                                     Max.
                                             :48.00
                                                      Max.
                                                             :81.00
##
                                     NA's
                                             :38
                                                      NA's
                                                             :38
##
        TPW.2
                         ST1.2
                                         ST2.2
                                                          ST3.2
##
   Min.
          : 45.00
                     Min.
                            :0.000
                                     Min.
                                             :0.000
                                                      Min.
                                                             :0.000
##
   1st Qu.: 87.25
                     1st Qu.:3.250
                                     1st Qu.:3.000
                                                      1st Qu.:3.000
##
                     Median :6.000
                                                      Median :6.000
  Median :114.00
                                     Median :6.000
##
   Mean :113.18
                     Mean :5.016
                                     Mean :4.516
                                                      Mean :4.616
   3rd Qu.:137.00
                     3rd Qu.:6.000
                                     3rd Qu.:6.000
##
                                                      3rd Qu.:6.000
```

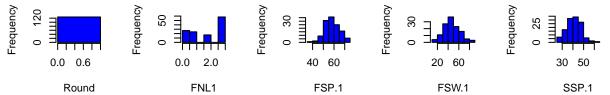
```
##
    Max.
            :207.00
                      Max.
                              :7.000
                                        Max.
                                               :7.000
                                                         Max.
                                                                 :7.000
##
                                                         NA's
                                                                 :1
##
        ST4.2
                          ST5.2
##
    Min.
            :0.000
                     Min.
                             :1.00
##
    1st Qu.:4.000
                     1st Qu.:5.00
##
    Median :6.000
                     Median:6.00
    Mean
           :5.015
                            :5.32
                     Mean
##
    3rd Qu.:6.000
                     3rd Qu.:6.00
##
    Max.
            :7.000
                     Max.
                             :7.00
##
   NA's
            :59
                     NA's
                             :101
```

- Summary statistics
 - There are 126 observations with 42 variables
 - We read first few observations from the data set
 - WNR.1, WNR.2, UFE.2 and UFE.1 variables have no data
 - There are missing observations for ST4.1, ST5.1, NPA.2, NPW.2, ST3.2, ST4.2 and ST5.2 variables
- We use hist function to plot the histograms
- We use plot function to plot the density function
- As the variables are larger in number we avoid scatter plots at this moment

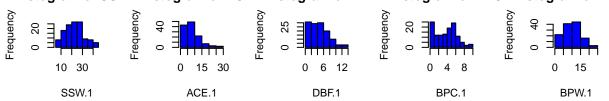
3.2 Plots

```
#Histograms
par(mfrow=c(3,5))
hist(Round, col="blue",xlab="Round")
hist(FNL1, col="blue",xlab="FNL1")
hist(FSP.1, col="blue",xlab="FSP.1")
hist(FSW.1, col="blue",xlab="FSW.1")
hist(SSP.1, col="blue",xlab="SSP.1")
hist(SSW.1, col="blue",xlab="SSW.1")
hist(ACE.1, col="blue",xlab="ACE.1")
hist(DBF.1, col="blue",xlab="DBF.1")
hist(BPC.1, col="blue",xlab="BPC.1")
hist(BPW.1, col="blue",xlab="BPW.1")
hist(NPA.1, col="blue",xlab="NPA.1")
hist(NPW.1, col="blue",xlab="NPW.1")
hist(TPW.1, col="blue",xlab="TPW.1")
hist(FSP.2, col="blue",xlab="FSP.2")
hist(FSW.2, col="blue",xlab="FSW.2")
```

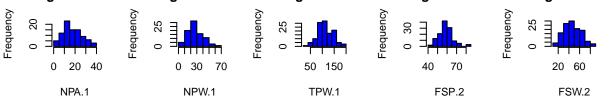
Histogram of Roul Histogram of FNL Histogram of FSP Histogram of FSW Histogram of SSP



Histogram of SSW Histogram of ACE Histogram of DBF Histogram of BPC Histogram of BPW

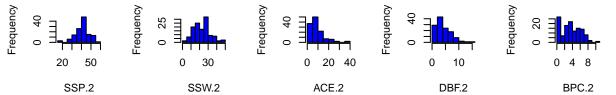


Histogram of NPA Histogram of NPW Histogram of TPW Histogram of FSP Histogram of FSW

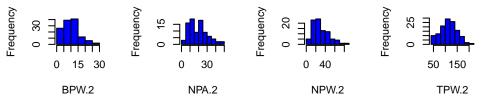


```
par(mfrow=c(3,5))
hist(SSP.2, col="blue",xlab="SSP.2")
hist(SSW.2, col="blue",xlab="SSW.2")
hist(ACE.2, col="blue",xlab="ACE.2")
hist(DBF.2, col="blue",xlab="DBF.2")
hist(BPC.2, col="blue",xlab="BPC.2")
hist(BPW.2, col="blue",xlab="BPW.2")
hist(NPA.2, col="blue",xlab="NPA.2")
hist(NPW.2, col="blue",xlab="NPW.2")
hist(TPW.2, col="blue",xlab="TPW.2")
#Density Plot
par(mfrow=c(3,5))
```

Histogram of SSP Histogram of SSW Histogram of ACE Histogram of DBF Histogram of BPC

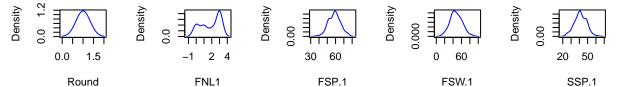


Histogram of BPW Histogram of NPA Histogram of NPW Histogram of TPW

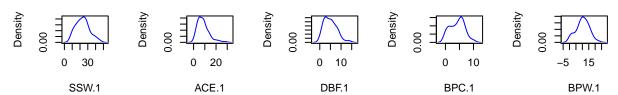


```
plot(density(Round), col="blue",xlab="Round")
plot(density(FNL1), col="blue",xlab="FNL1")
plot(density(FSP.1), col="blue",xlab="FSP.1")
plot(density(FSW.1), col="blue",xlab="FSW.1")
plot(density(SSP.1), col="blue",xlab="SSP.1")
plot(density(SSW.1), col="blue",xlab="SSW.1")
plot(density(ACE.1), col="blue",xlab="ACE.1")
plot(density(DBF.1), col="blue",xlab="DBF.1")
plot(density(BPC.1), col="blue",xlab="BPC.1")
plot(density(BPW.1), col="blue",xlab="BPW.1")
plot(density(NPA.1,na.rm=T), col="blue",xlab="NPA.1")
plot(density(NPW.1,na.rm=T), col="blue",xlab="NPW.1")
plot(density(TPW.1), col="blue",xlab="TPW.1")
plot(density(FSP.2), col="blue",xlab="FSP.2")
plot(density(FSW.2), col="blue",xlab="FSW.2")
```

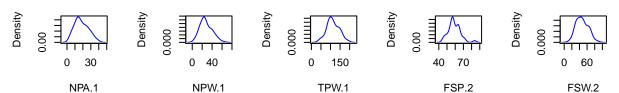
ensity.default(x = Rdensity.default(x = Flensity.default(x = Flensity.



ensity.default(x = Slensity.default(x = Alensity.default(x = Blensity.default(x = B

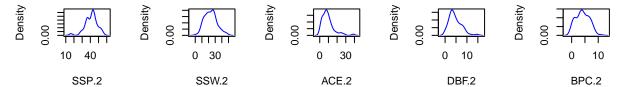


y.default(x = NPA.1, y.default(x = NPW.1, ensity.default(x = Tlensity.default(x = Flensity.default(x = Flensity.

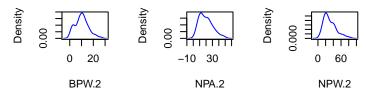


```
par(mfrow=c(3,5))
plot(density(SSP.2), col="blue",xlab="SSP.2")
plot(density(SSW.2), col="blue",xlab="SSW.2")
plot(density(ACE.2), col="blue",xlab="ACE.2")
plot(density(DBF.2), col="blue",xlab="DBF.2")
plot(density(BPC.2), col="blue",xlab="BPC.2")
plot(density(BPW.2), col="blue",xlab="BPW.2")
plot(density(NPA.2,na.rm=T), col="blue",xlab="NPA.2")
plot(density(NPW.2,na.rm=T), col="blue",xlab="NPW.2")
```

lensity.default(x = S-ensity.default(x = S-ensity.default(x = A-ensity.default(x = B-ensity.default(x =



ensity.default(x = Bly.default(x = NPA.2, y.default(x = NPW.2,



• Most of the data is numeric with little or no cleaning required. We can replace the missing values with zero (or mean value) to simplify the data modeling process.

4 Data Preparation

- We will not consider the variable Round as it is a constant and is not impacting the response or regressor variables as evident from the scatter plots
- We have chosen the response variable as FNL1 Final number of games won by player 1
- Covariates for consideration FSP.1, FSW.1, SSP.1, SSW.1, ACE.1, DBF.1, BPC.1, BPW.1, NPA.1, NPW.1, TPW.1, FSP.2, FSW.2, SSP.2, SSW.2, ACE.2, DBF.2, BPC.2, BPW.2, NPA.2, NPW.2, TPW 2
- We observe NA values in NPA and NPW variables and replace them with 0

```
usopen$NPA.1[is.na(usopen$NPA.1)] <- 0
usopen$NPW.1[is.na(usopen$NPW.1)] <- 0
usopen$NPW.2[is.na(usopen$NPW.2)] <- 0
usopen$NPA.2[is.na(usopen$NPA.2)] <- 0</pre>
```

• Rest of the data looks pretty clean

5 Modeling

- We will utilize multiple linear regression method for this model.
- Based on the correlation matrix and partial f tests we will decide on the final list of covariates and final number of observations

5.1 Correlation martix for selected covariates

```
cor(usopen[, c( "FSP.1", "FSW.1", "SSP.1", "SSW.1", "ACE.1", "DBF.1", "BPC.1", "BPW.1",
    "NPA.1", "NPW.1", "TPW.1", "FSP.2", "FSW.2", "SSP.2", "SSW.2", "ACE.2", "DBF.2", "BPC.2",
    "BPW.2", "NPA.2", "NPW.2", "TPW.2"
)])
```

- We observe high correlation between NPA.1 and NPW.1, TPW.1 and FSW.1,NPA.2 and NPW.2, FSW.2 and TPW.2
- Other combinations of variables are also correlated
- There is a good probability that we may experience multicollinearity in our model
- We split the data set into testing (30%) and training data (70%)

5.2 Data split

```
# setting the seed to make the partition reproductible
set.seed(999)
index <-
    sample(seq_len(nrow(usopen)), size = floor(0.70 * nrow(usopen)))
usopen_train <- usopen[index,]
usopen_test <- usopen[-index,]</pre>
```

- We now create model based on training data
- summary function is used to get the model details

5.3 Model details

data = usopen_train)

##

```
model_usopen <-
lm(
    FNL1 ~ FSP.1 + FSW.1 + SSP.1 + SSW.1 + ACE.1 + DBF.1 + BPC.1 + BPW.1 + NPA.1 +
        NPW.1 + TPW.1 + FSP.2 + FSW.2 + SSP.2 + SSW.2 + ACE.2 + DBF.2 + BPC.2 +
        BPW.2 + NPA.2 + NPW.2 + TPW.2,
        data = usopen_train
)
summary(model_usopen)

##
## Call:
## lm(formula = FNL1 ~ FSP.1 + FSW.1 + SSP.1 + SSW.1 + ACE.1 + DBF.1 +
## BPC.1 + BPW.1 + NPA.1 + NPW.1 + TPW.1 + FSP.2 + FSW.2 + SSP.2 +
## SSW.2 + ACE.2 + DBF.2 + BPC.2 + BPW.2 + NPA.2 + NPW.2 + TPW.2,</pre>
```

```
##
## Residuals:
##
        Min
                   1Q
                        Median
                                      30
   -0.97603 -0.30841
                       0.03371
                                0.33374
                                          1.05906
##
##
  Coefficients: (2 not defined because of singularities)
##
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.262626
                            1.376240
                                       -0.917
                                               0.36220
## FSP.1
                 0.002551
                            0.015872
                                        0.161
                                               0.87280
                -0.002686
## FSW.1
                            0.018716
                                       -0.144
                                               0.88630
## SSP.1
                       NA
                                   NA
                                           NA
                                                     NA
## SSW.1
                 0.007278
                            0.025829
                                        0.282
                                               0.77899
## ACE.1
                 0.005061
                            0.013210
                                        0.383
                                               0.70284
## DBF.1
                 0.024640
                            0.025376
                                        0.971
                                               0.33504
## BPC.1
                            0.063603
                 0.116067
                                        1.825
                                               0.07248
## BPW.1
                -0.049449
                            0.026547
                                       -1.863
                                               0.06689
## NPA.1
                -0.019090
                            0.030332
                                       -0.629
                                               0.53125
## NPW.1
                 0.007268
                            0.020210
                                        0.360
                                               0.72028
## TPW.1
                 0.061255
                            0.014343
                                        4.271 6.29e-05
## FSP.2
                 0.024471
                            0.015574
                                        1.571
                                               0.12083
## FSW.2
                -0.009003
                            0.020432
                                       -0.441
                                               0.66090
## SSP.2
                       NA
                                   NA
                                           NA
                                                     NA
## SSW.2
                 0.027966
                            0.023308
                                        1.200
                                               0.23443
                            0.010839
## ACE.2
                 0.021018
                                        1.939
                                               0.05671
## DBF.2
                -0.004163
                            0.029013
                                       -0.143
                                               0.88633
## BPC.2
                0.086542
                            0.073086
                                        1.184
                                               0.24055
## BPW.2
                -0.025209
                            0.026448
                                       -0.953
                                               0.34393
## NPA.2
                0.041423
                            0.025749
                                        1.609
                                               0.11238
## NPW.2
                -0.023605
                            0.017060
                                       -1.384
                                               0.17105
## TPW.2
                -0.053608
                            0.016279
                                       -3.293
                                               0.00158 **
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  Residual standard error: 0.4957 on 67 degrees of freedom
  Multiple R-squared: 0.8815, Adjusted R-squared: 0.8462
## F-statistic: 24.93 on 20 and 67 DF, p-value: < 2.2e-16
```

- The null hypothesis is $H_0: \beta_1 = \beta_2 = ... = \beta_p = 0$
- That is, there is not a single predictor which can be considered statistically significant
- The alternate hypothesis is H_a : At least one β_i is not zero
- That is, there is at least predictor which can explain the change in resultant variable
- We reject null hypothesis when the p value is < 0.05
- From the model summary we observe that there are only 2 statistically significant variables (null hypothesis is rejected for these)
 - TPW.1
 - TPW.2
- The F-statistic is 24.93 and the corresponding p-value is significantly lower than 0.05 so we can conclude to reject that null hypothesis that no predictor variable explains the variability in the response variable
- The R^2 value is 0.8815
- The model explains 88.15% of the variability in FNL1

5.4 Partial F tests

• We now do a partial f-test for the variables FSP.1, FSW.1, SSP.1, SSW.1, ACE.1, DBF.1, NPA.1, NPW.1, FSP.2, FSW.2, SSP.2, SSW.2, ACE.2, DBF.2, NPA.2, NPW.2 and BPC.2

```
model_usopen_p <-
  lm(FNL1 ~ BPC.1 + BPW.1 + TPW.1 + BPW.2 + TPW.2,
     data = usopen_train)
anova(model_usopen, model_usopen_p)
## Analysis of Variance Table
## Model 1: FNL1 ~ FSP.1 + FSW.1 + SSP.1 + SSW.1 + ACE.1 + DBF.1 + BPC.1 +
       BPW.1 + NPA.1 + NPW.1 + TPW.1 + FSP.2 + FSW.2 + SSP.2 + SSW.2 +
       ACE.2 + DBF.2 + BPC.2 + BPW.2 + NPA.2 + NPW.2 + TPW.2
##
## Model 2: FNL1 ~ BPC.1 + BPW.1 + TPW.1 + BPW.2 + TPW.2
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
         67 16.465
## 2
         82 20.008 -15
                         -3.5425 0.961 0.5046
```

- We observe that p value is > 0.05 and therefore all these variables are not statistically significant
- We can now exclude these variables from our analysis
- We summarize our current model

```
summary(model usopen p)
##
## lm(formula = FNL1 ~ BPC.1 + BPW.1 + TPW.1 + BPW.2 + TPW.2, data = usopen_train)
## Residuals:
       Min
                 1Q
                      Median
                                    3Q
                                            Max
## -0.94966 -0.29081 0.04009 0.31831 1.20486
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.409225
                          0.201126
                                     2.035 0.04512 *
## BPC.1
               0.163649
                          0.043440
                                    3.767 0.00031 ***
## BPW.1
              -0.055868
                          0.017387 -3.213 0.00188 **
## TPW.1
               0.048078
                          0.005446
                                     8.828 1.58e-13 ***
## BPW.2
               -0.024529
                          0.015967
                                    -1.536 0.12834
              -0.034274
## TPW.2
                          0.005362 -6.392 9.40e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.494 on 82 degrees of freedom
## Multiple R-squared: 0.856, Adjusted R-squared: 0.8473
## F-statistic: 97.53 on 5 and 82 DF, p-value: < 2.2e-16
```

• We run another partial f-test for the variable BPW.2

Analysis of Variance Table

```
##
## Model 1: FNL1 ~ BPC.1 + BPW.1 + TPW.1 + BPW.2 + TPW.2
## Model 2: FNL1 ~ BPC.1 + BPW.1 + TPW.1 + TPW.2
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 82 20.008
## 2 83 20.584 -1 -0.57582 2.3599 0.1283
```

- We again get a p-value > 0.05
- Hence BPW.2 is also not statistically significant
- We summarize our current model

```
summary(model_usopen_p_2)
##
## Call:
## lm(formula = FNL1 ~ BPC.1 + BPW.1 + TPW.1 + TPW.2, data = usopen_train)
##
## Residuals:
##
       Min
                  1Q
                      Median
                                   3Q
                                           Max
## -1.04081 -0.40456 0.08174 0.36555 1.07170
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.397609
                          0.202623
                                    1.962 0.053078 .
## BPC.1
               0.132087
                          0.038586
                                     3.423 0.000964 ***
## BPW.1
               -0.053149
                          0.017437 -3.048 0.003090 **
## TPW.1
               0.053237
                          0.004322 12.317 < 2e-16 ***
## TPW.2
              -0.040555
                          0.003496 -11.599 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.498 on 83 degrees of freedom
## Multiple R-squared: 0.8519, Adjusted R-squared: 0.8448
## F-statistic: 119.4 on 4 and 83 DF, p-value: < 2.2e-16
```

5.5 Standardize the covariate coefficients

• We now standardize the regression coefficients using unit normal scaling

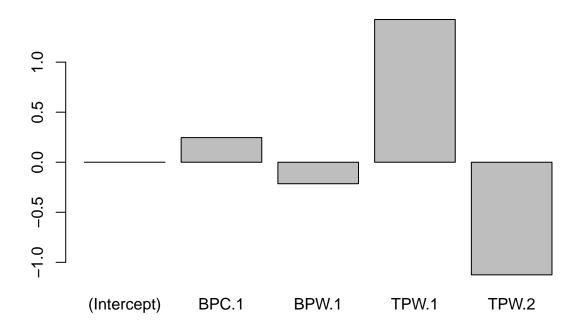
• We now create the new model using standardized values

```
## Call:
## lm(formula = FNL1 ~ BPC.1 + BPW.1 + TPW.1 + TPW.2, data = usopen_train_standard)
##
## Residuals:
## Min 1Q Median 3Q Max
```

```
## -0.82346 -0.32007 0.06467 0.28921 0.84790
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.475e-16 4.200e-02
                                      0.000 1.000000
## BPC.1
               2.462e-01 7.192e-02
                                      3.423 0.000964 ***
## BPW.1
              -2.148e-01 7.047e-02 -3.048 0.003090 **
## TPW.1
               1.426e+00 1.158e-01 12.317
                                             < 2e-16 ***
## TPW.2
              -1.125e+00 9.700e-02 -11.599 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.394 on 83 degrees of freedom
## Multiple R-squared: 0.8519, Adjusted R-squared: 0.8448
## F-statistic: 119.4 on 4 and 83 DF, p-value: < 2.2e-16
```

• To better visualize the coefficients we plot the barplot

barplot(model_usopen_std\$coefficients)



• We observe that the most statistically significant variables are TPW.1 and TPW.2

5.6 Multicollinearity checks

- We check our model for multicolllinearity
- We will the vif function from car library to examine multicollinearity

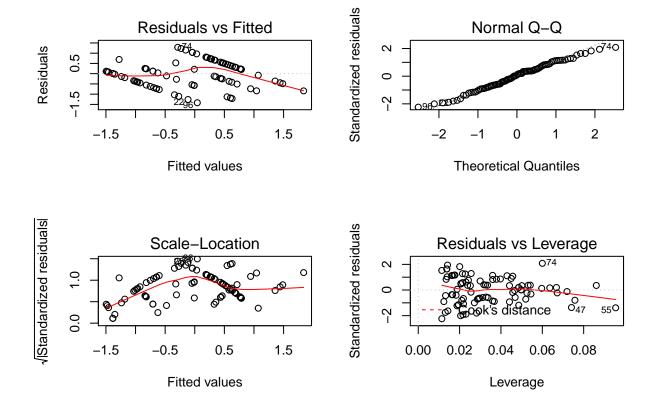
```
library(car)
vif(model_usopen_std)
                        TPW.1
                                 TPW.2
##
      BPC.1
               BPW.1
## 2.899012 2.782959 7.514762 5.273466
  • We observe that there is multicollinearity in our model (as was expected)
  • We find the colleration matrix of the variables
cor(usopen_train_standard[, c("FNL1", "BPC.1", "BPW.1", "TPW.1", "TPW.2")])
##
                FNL1
                           BPC.1
                                     BPW.1
                                                TPW.1
                                                            TPW.2
## FNL1
          1.00000000 0.75807021 0.5302779 0.4943759 -0.06581077
## BPC.1 0.75807021 1.00000000 0.6804967 0.4540390 -0.00928395
## BPW.1 0.53027788 0.68049669 1.0000000 0.6824489 0.35180657
## TPW.1 0.49437585 0.45403905 0.6824489 1.0000000 0.79731644
## TPW.2 -0.06581077 -0.00928395 0.3518066 0.7973164 1.00000000
  • Since TPW.1 and TPW.2 are highly correlated, we keep only TPW.1 and recreate the model
model_usopen_std_2 <-
  lm(FNL1 \sim BPC.1 + BPW.1 + TPW.1,
     data = usopen_train_standard)
summary(model_usopen_std_2)
##
## Call:
## lm(formula = FNL1 ~ BPC.1 + BPW.1 + TPW.1, data = usopen_train_standard)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                             Max
## -1.32305 -0.46140 -0.00508 0.45556
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
               7.619e-17 6.759e-02
                                       0.000 1.00000
## (Intercept)
## BPC.1
                7.449e-01 9.279e-02
                                       8.028 5.34e-12 ***
## BPW.1
               -1.557e-01 1.131e-01
                                      -1.377 0.17229
## TPW.1
                2.624e-01 9.302e-02
                                       2.821 0.00597 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6341 on 84 degrees of freedom
## Multiple R-squared: 0.6118, Adjusted R-squared: 0.598
## F-statistic: 44.14 on 3 and 84 DF, p-value: < 2.2e-16
  • We now calculate the VIF to check for multicollinearity
library(car)
vif(model_usopen_std_2)
      BPC.1
               BPW.1
                        TPW.1
## 1.863158 2.768419 1.872437
```

- There is no multicolinearity on this model
- As there is one statistically insignificant variable in this model, we run partial F test again for the variable BPW.1

```
model_usopen_std_2p <-
  lm(FNL1 \sim BPC.1 +
                      TPW.1,
     data = usopen_train_standard)
summary(model_usopen_std_2p)
##
## Call:
## lm(formula = FNL1 ~ BPC.1 + TPW.1, data = usopen_train_standard)
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -1.41846 -0.44510 0.05935 0.48807
                                        1.28546
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.064e-16 6.795e-02
                                       0.000
                                               1.0000
## BPC.1
               6.722e-01 7.670e-02
                                       8.764 1.62e-13 ***
## TPW.1
               1.892e-01 7.670e-02
                                       2.467
                                               0.0156 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6374 on 85 degrees of freedom
## Multiple R-squared: 0.6031, Adjusted R-squared: 0.5937
## F-statistic: 64.58 on 2 and 85 DF, p-value: < 2.2e-16
library(car)
vif(model_usopen_std_2p)
      BPC.1
##
               TPW.1
## 1.259686 1.259686
  • This model does not have multicollinearity
anova(model_usopen_std_2, model_usopen_std_2p)
## Analysis of Variance Table
##
## Model 1: FNL1 ~ BPC.1 + BPW.1 + TPW.1
## Model 2: FNL1 ~ BPC.1 + TPW.1
     Res.Df
##
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
         84 33.770
## 2
         85 34.532 -1 -0.76185 1.895 0.1723
  • Using anova function we arrive to the conclusion that the vairable BPW.1 is not statistically significant
```

• We now do the residual plots

```
par(mfrow = c(2, 2))
plot(model_usopen_std_2p)
```



6 Evaluation

• We calculate the mean square error for the models created

```
t <- predict(model_usopen_std, usopen_test)
mean((t - usopen_test[, c("FNL1")]) ** 2)

## [1] 1852.487

t <- predict(model_usopen_std_2, usopen_test)
mean((t - usopen_test[, c("FNL1")]) ** 2)

## [1] 969.4526

t <- predict(model_usopen_std_2p, usopen_test)
mean((t - usopen_test[, c("FNL1")]) ** 2)</pre>
```

- ## [1] 564.1643
 - We observe that as we proceeded to refine our model the MSE kept on decreasing
 - And we have the least MSE in our final model