

Strategies for factoring.

① look for the greatest common factor

② Try grouping terms together

③ identify special cases - $x^2 + bx + c$
 $ax^2 + bx + c$
 $x^2 - y^2$

(2) ④ simplify if possible.

$$9 - (2x+1)^2 = (3 + 2x+1)(3 - 2x-1) \\ = (4 + 2x)(2 - 2x)$$

$$\begin{aligned} & 24x^4 - 16x^3 - 81x + 54 \\ & 8x^3(3x-2) - (27)(3x-2) \\ (h) & = (3x-2)(8x^3 - 27) \\ & = (3x-2)(2x-3)(4x^2 + 6x + 9) \end{aligned}$$

$$\begin{aligned} & 12x^3y - 30x^2y - 18xy \\ & = 3xy(4x^2 - 10x - 6) \\ (p) & = 6xy(2x^2 - 5x - 3) \\ & = 6xy(2x^2 - 6x + 1x - 3) \\ & = 6xy(2x(x-3) + (x-3)) \\ & = 6xy(x-3)(2x+1) \end{aligned}$$

$m+n = -5$
 $mn = -6$
 $m = -6, n = 1$

$$128x^4 - 8y^2x^2$$

$$\begin{aligned} (a) &= 8x^2(16x^2 - y^2) \\ &= 8x^2(4x - y)(4x + y) \end{aligned}$$

$$\begin{aligned} (m) &= (5x + 7)^2 - 16 \\ &= (5x + 7 + 4)(5x + 7 - 4) \\ &= (5x + 11)(5x + 3) \end{aligned}$$

$$\begin{aligned} (f) &= y^2x - 3y^2 - 4x + 12 \\ &= y^2(x - 3) - 4(x - 3) \\ &= (x - 3)(y^2 - 4) \\ &= (x - 3)(y + 2)(y - 2) \end{aligned}$$

$$(n) \quad x^4 - x^2 - 20 = (x^2 + 4)(x^2 - 5) = (x^2 + 4)(x + 5)(x - 5).$$

$$\begin{aligned} (g) \quad 8x^4(x - 4) - 27x(x - 4) &= x(x - 4)(8x^3 - 27) \\ &= x(x - 4)(2x - 3)(4x^2 + 6x + 9) \end{aligned}$$

$$\begin{aligned} (t) \quad x^6 - 64 &= (x^2 - 4)(x^4 + 16x^2 + 16) \\ &= (x + 2)(x - 2)(x^4 + 16x^2 + 16) \end{aligned}$$

$$\begin{aligned} (r) \quad (x + 1)^2 - (x + 1) - 6 &= (x + 1 - 3)(x + 1 + 3) \\ &= (x - 2)(x + 4) \end{aligned}$$

Simplify $\frac{x^2+3x}{x^2+5x}$

$$\frac{x^2+3x}{x^2+5x} = \frac{x(x+3)}{x(x+5)} \quad \text{find gcf}$$

$$= \frac{\cancel{x}(x+3)}{\cancel{x}(x+5)} \quad \text{cancel out common factors}$$

$$= \frac{x+3}{x+5}$$

Steps to simplify

① Factor numerator and denominator

② Cancel common factors

③ Simplify.

Note $\frac{x+3}{x+5}$ the x's cannot be canceled as they are not common factors

Ex/1 Simplify $\frac{x^2-9}{x^2+5x+6}$

$$= \frac{(x+3)(x-3)}{(x+2)(x+3)} \quad \text{① factor}$$

$$= \frac{\cancel{(x+3)}(x-3)}{(x+2)\cancel{(x+3)}} \quad \text{② cancel common factors}$$

$$= \frac{x-3}{x+2} \quad \text{③ simplify}$$

$$\text{Ex/2} \quad \frac{x^4+8x^2+7}{3x^5-3x} = \frac{(x^2+1)(x^2+7)}{3x(x^4-1)} = \frac{(x^2+1)(x^2+7)}{3x(x^2-1)(x^2+1)} \quad \text{①}$$

$$= \frac{\cancel{(x^2+1)}(x^2+7)}{3x(x^2-1)\cancel{(x^2+1)}} \quad \text{②}$$

$$= \frac{x^2+7}{3x(x^2-1)} \quad \text{③}$$

Simplify $\frac{5x^2 + 20xy + 20y^2}{x^2 - xy - 6y^2} = \frac{5(x^2 + 4yx + 4y^2)}{(x-3y)(x+2y)}$

$$= \frac{5(x+2y)(x+2y)}{(x-3y)(x+2y)}$$

$$= \frac{5(x+2y)\cancel{(x+2y)}}{(x-3y)\cancel{(x+2y)}}$$

$$= \frac{5(x+2y)}{(x-3y)}$$

Least common multiple (LCM)

$$3z^3 - 6z^2 - 9z \quad 7z^4 + 21z^3 + 14z^2$$

$$= 3z(z^2 - 2z - 3) \quad 7z^2(z^2 + 3z + 2)$$

$$= 3z(z+1)(z-3) \quad 7z^2(z+1)(z+2)$$

4	6
8	12
12	18
16	24
⋮	

4	6
2	2
2	3

LCM(4, 6) = 2 · 2 · 3

$$\text{LCM} \rightarrow 3 \cdot z^2 \cdot (z+1)(z-3) \cdot 7(z+2)$$

$$= 21z^2(z+1)(z-3)(z+2)$$

Ex $\frac{a-2}{a+2} - \frac{(a-3)}{a^2+4a+4} \quad (a+2) \quad a^2+4a+4$

$$(a+2)(a+2)$$

$$= \frac{(a-2)(a+2)}{(a+2)(a+2)} - \frac{a-3}{(a+2)(a+2)}$$

$$= \frac{a^2 - 4 - a + 3}{(a+2)(a+2)} = \frac{a^2 - a - 1}{(a+2)(a+2)}$$

LCM $\rightarrow (a+2)(a+2)$

$$\frac{2p+6}{p+5} \div \frac{10}{4p+20} = \frac{2p+6}{p+5} \times \frac{4p+20}{10}$$

$$= \frac{(2p+6)(4p+20)}{(p+5)(10)}$$

$$= \frac{2(p+3) \cdot 4 \cdot \cancel{(p+5)}}{(\cancel{p+5}) \cdot (2 \cdot 5)}$$

$$= \frac{4(p+3)}{5}$$

$$\frac{a^2-4}{a^2-1} \cdot \frac{a+1}{a+2} = \frac{(a^2-4)(a+1)}{(a^2-1)(a+2)}$$

$$= \frac{(a+2)(a-2)(a+1)}{(a-1)(a+1)(a+2)}$$

$$= \frac{a-2}{a-1}$$

$$\text{Ex// } \frac{3x^2y}{2ab} \cdot \frac{14a^2b}{18xy^2} = \frac{\overset{1}{\cancel{3}}x^{\overset{2}{\cancel{2}}}y^{\overset{1}{\cancel{1}}} \cdot \overset{7}{\cancel{14}}a^{\overset{2}{\cancel{2}}}b^{\overset{1}{\cancel{1}}}}{\overset{2}{\cancel{18}}x^{\overset{1}{\cancel{1}}}y^{\overset{2}{\cancel{2}}} \cdot \overset{6}{\cancel{6}}ab} \\ = \frac{7xa}{6y}$$

$$\text{Ex// } \frac{2x^2-3x-20}{2x^2-7x-30} \div \frac{2x^2-5x-12}{4x^2+12x+9} \cdot \frac{x^2-36}{4x^2-9} \\ = \frac{(x-4)(2x+5)}{(2x+5)(x-6)} \times \frac{4x^2+12x+9}{2x^2-5x-12} \cdot \frac{x^2-36}{4x^2-9} \\ = \frac{(x-4)(2x+5)}{(2x+5)(x-6)} \cdot \frac{(2x+3)(2x+3)}{(x-4)(2x+3)} \cdot \frac{(x+6)(x-6)}{(2x+3)(2x-3)} \\ = \frac{\cancel{(x-4)}\cancel{(2x+5)}\cancel{(2x+3)}\cancel{(2x+3)}(x+6)\cancel{(x-6)}}{\cancel{(2x+5)}\cancel{(x-6)}\cancel{(x-4)}\cancel{(2x+3)}\cancel{(2x+3)}(2x-3)} \\ = \frac{x+6}{2x-3}$$

$$m+n=12 \quad nm=6 \\ nm=36 \\ 4x^2+6x+6x+9 \\ 2x(2x+3)+3(2x+3) \\ m+n=-5 \quad -8 \quad 3 \\ nm=-24 \\ 2x^2-8x+3x-12 \\ = 2x(x-4)+3(x-4)$$