

Section 5:

# **Types and Programming Languages**

CS 164 @ UC Berkeley, Spring 2024

# Reminders

WA 2 is due on Friday, Feb 23

PA2 is released, and is due on March 18 at 11:59 PST.

Start early!!

Reminder to take care of yourselves, and to prioritize your health! WAs are worth 5% of your grade so don't stress too much about them!

# Free Variables

Variables which are not defined in a given expression

```
def f() -> int:  
    return x + y
```

```
def f(x : int, y : int) -> int:  
    return g(x + y)
```

# Type Environments

Map free variables to their types

<code>x : int = 24</code>	<code>{x : int}</code>
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<code>def f(y : int) -&gt; bool:</code>	
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<code>    z : int = 0</code>	<code>{??}</code>
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<code>    return y &gt; z</code>	
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<code>f(x)</code>	<code>{??}</code>
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# Type Environments and Functions

Entries for functions contain argument and return types, as well as types for local variables:

```
x : int = 24
```

```
{x : int}
```

```
def f(y : int) -> bool:
```

```
{x : int,
```

```
    z : int = 0
```

```
    f : {int -> bool
```

```
    return y > z
```

```
    y : int,
```

```
f(x)
```

```
    z : int }}
```

# Type Inference Rules

Hypotheses above the bar imply the conclusion below the bar

“ $O \vdash \dots v : T$ ” is read as

“Under the scope with type environment  $O$ ,  $v$  can be proven to have type  $T$ ”

$$\frac{\begin{array}{c} O \vdash e_1 : \text{int} \\ O \vdash e_2 : \text{int} \end{array}}{O \vdash e_1 + e_2 : \text{int}} \quad [\text{add}]$$

# Type Inference Tree Proofs

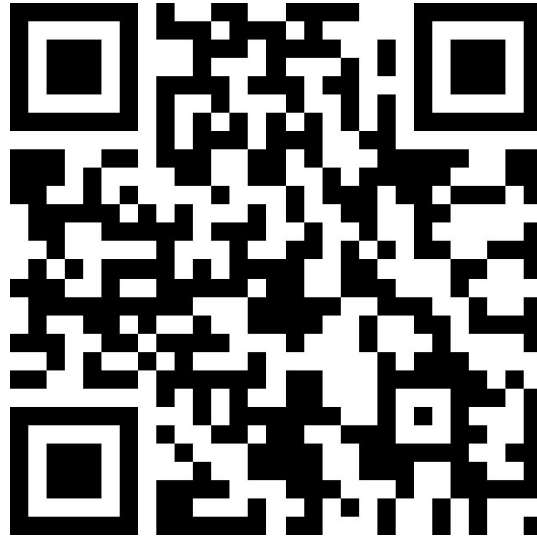
Full expression at root of tree

Each subtree proves the hypotheses needed to satisfy rule

Each subtree proves the type of a subexpression of the full expression

(Somewhat) akin to top-down parsing

$$\frac{\frac{\vdash \text{False} : \text{bool}}{\vdash \text{not False} : \text{bool}} \quad \frac{\vdash 1 : \text{int} \quad \frac{\vdash 2 : \text{int} \quad \vdash 3 : \text{int}}{\vdash 2 * 3 : \text{int}}}{\vdash 1 + 2 * 3 : \text{int}}}{\vdash \text{while not False} : 1 + 2 * 3}$$



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