## Assignment 1 CSCE 4323: Formal Languages and Computability Fall 2018

## Exercises from the book

The following exercises can be found in Chapter 1 of the Sipser book, 2nd edition. Solutions should be provided as code for each in a text document following the format for a DFA on the web site http://web.cs.ucdavis.edu/~doty/automata/. A template file "CSCE4323-F18-HW-template.txt" can be found on the course site on Blackboard.

- 1.4 Each of the following languages is the intersection of two simpler languages. In each part, construct DFAs for the simpler languages, then combine them using the construction discussed in footnote 3 (page 46) to give the definition of a DFA for the language given. In all parts  $\Sigma = \{a, b\}$ .
  - a.  $\{w|w \text{ has at least three } a$ 's and at least two b's  $\}$
  - c.  $\{w|w \text{ has an even number of } a$ 's and one or two two b's  $\}$
  - f.  $\{w|w \text{ has an odd number of } a$ 's and ends with a  $b\}$
- 1.5 Each of the following is the complement of a simpler language. In each part, construct a DFA for the simpler language, then use it to give the definition of a DNA for the language given. In all parts  $\Sigma = \{a, b\}$ .
  - d.  $\{w|w \text{ is any string not in } a^*b^*\}$
  - f.  $\{w|w \text{ is any string not in } a^* \cup b^*\}$
  - g.  $\{w|w \text{ is any string that doesn't contain exactly two } a's \}$
- 1.6 Give definitions of DFAs recognizing the following languages. In all parts, the alphabet is  $\{0,1\}$ .
  - f.  $\{w|w \text{ doesn't contain the substring } 110\}$
  - i.  $\{w | \text{ every odd position of } w \text{ is a } 1\}$
  - j.  $\{w|w \text{ contains at least two 0s and at most one 1}\}$
  - m. The empty set