

Module 3

STACKS and QUEUES

Introduction to Stacks

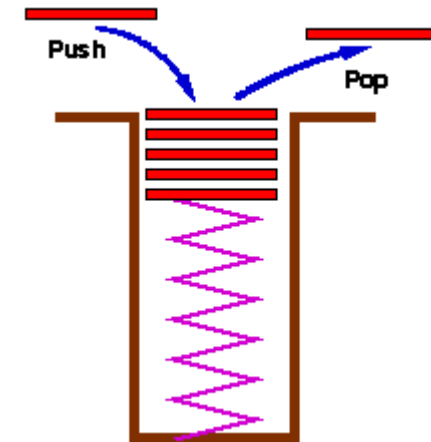
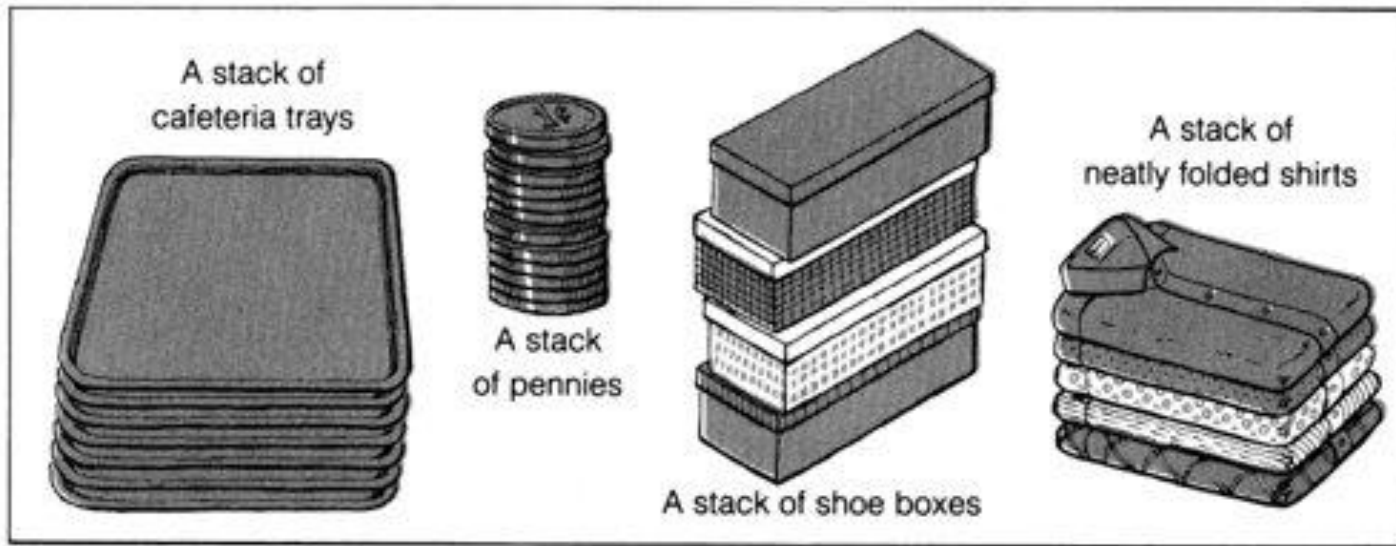
What is a Stack?

- A linear data structure that follows the Last In, First Out (LIFO) principle.
- The last element added is the first one to be removed.

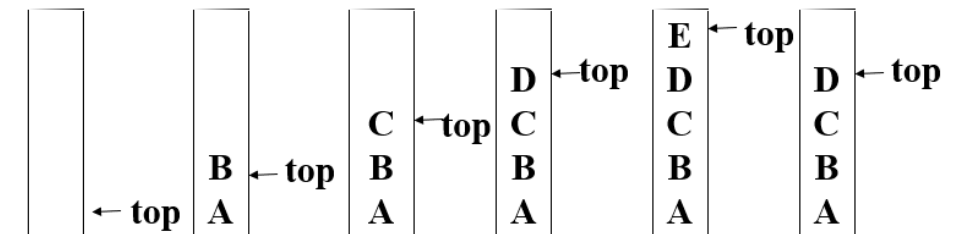
Key Operations

- Push: Add an element to the top of the stack.
- Pop: Remove the top element from the stack.
- Peek/Top: View the top element without removing it.
- isEmpty: Check if the stack is empty.

EXAMPLE AND ILLUSTRATION



Stack: A Last-In-First-Out (LIFO) list



Stack ADT Operations

- **CreateS(max-stack-size)** – Create empty stack.
- **IsFull(stack, max-stack-size)** – TRUE if full.
- **Add(stack, item)** – Push to top.
- **IsEmpty(stack)** – TRUE if empty.
- **Delete(stack)** – Pop from top.
- **Error Handling**: `stack-full()` and `stack-empty()` functions.

Stacks in Program Execution: Function Calls and Stack Frames

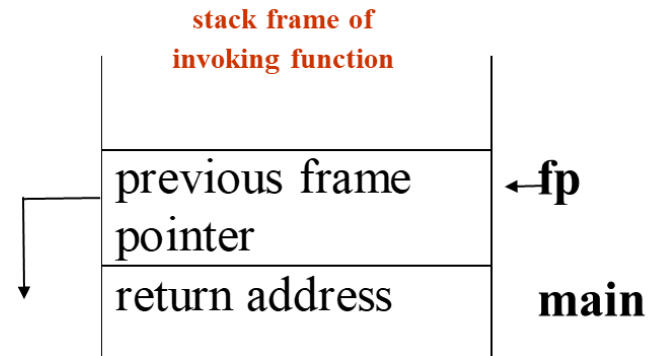
- **Stacks** are integral to program execution.
- **Essential** for managing **function/procedure calls and returns**.
- **Stack frame** enables **recursive calls** without special handling.
- **Function Call** → *Push* a new stack frame.
- **Function Return** → *Pop* the top stack frame.
- **Stack Frame Contents:**
 - Function arguments.
 - Return address (location to resume after call).
 - Local variables (non-static).

Activation Records (Stack Frames) in Function Calls

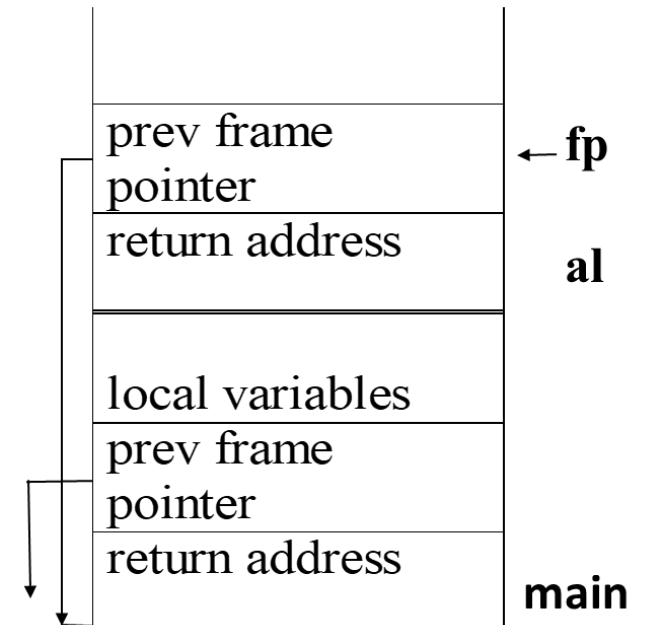
- When a function is invoked, the program creates an **activation record** (also called a **stack frame**) and places it **on top of the system stack**.
- **Initially**, the activation record contains:
- A **pointer to the previous stack frame** (points to the invoking function's frame).
- The **return address** (location to continue execution after the function returns).
- The **previous frame pointer** links back to the stack frame of the invoking function, maintaining the call chain.

Stack Frame of Function call

fp: a pointer to current stack frame



system stack before a1 is invoked
(a)



system stack after a1 has been invoked
(b)

System stack after function call a1

Stack Implementation Methods

Array Implementation

- Uses a fixed-size array to store stack elements.
- Simple to implement but has limited capacity.
- `top` variable tracks the current top position.

Linked List Implementation

- Uses dynamically allocated nodes linked together.
- Stack can grow or shrink at runtime (no fixed size limit).
- `top` pointer references the top node in the list.

Implementation of Stack (Array-based)

- Use **1D array** \rightarrow `stack[MAX-STACK-SIZE]`.
- `top` variable tracks top index.
- Initially `top = -1` (empty).
- **Push Operation**: Increment `top` \rightarrow store item.
- **Pop Operation**: Retrieve item at `top` \rightarrow decrement `top`.
- **Checks**:
 - `IsEmpty` \rightarrow `top == -1`.
 - `IsFull` \rightarrow `top == MAX-STACK-SIZE - 1`

Implementation of Stack (Array-based)

- #define MAX 5
- int stack[MAX], top = -1;
- **// Push operation**
- void push(int item) {
- if (top == MAX - 1)
- printf("Stack Overflow!\n");
- else
- stack[++top] = item;
- printf("%d pushed to stack.\n", value); }
- **// Pop operation**
- void pop() {
- if (top == -1)
- printf("Stack Underflow!\n");
- else
- printf("Popped: %d\n", stack[top--]);
- }

Implementation of Stack (Array-based)

- **// Peek function**

- void peek() {
- if (top == -1) {
- printf("Stack is empty!\n");
- } else {
- printf("Top element is: %d\n", stack[top]);
- }
- }

- **// isEmpty function**

- void isEmpty() {
- if (top == -1) {
- printf("Stack is empty.\n");
- } else {
- printf("Stack is not empty.\n");
- }
- }

Implementation of Stack (Array-based)

- **// Display stack**
- void display() {
- if (top == -1)
- printf("Stack is Empty\n");
- else {
- printf("Stack: ");
- for (int i = top; i >= 0; i--)
- printf("%d ", stack[i]);
- printf("\n"); } }
- **int main() {**
- int choice, item;
- do {
- printf("\n1.Push 2.Pop 3.Display 4.Exit\n");
- printf("Enter choice: ");
- scanf("%d", &choice);
- switch (choice) {
- case 1: printf("Enter item: ");
- scanf("%d", &item);
- push(item);
- break;

Implementation of Stack (Linked List-based)

- **// Node structure**

- struct Node {
- int data;
- struct Node* next;};
- struct Node* top = NULL;

- **// Push operation**

- void push(int value) {
- struct Node* newNode = (structNode*)malloc(sizeof(struct Node));
- if (!newNode) {
- printf("Stack Overflow!\n");
- return; }
- newNode->data = value;
- newNode->next = top;
- top = newNode;
- printf("%d pushed to stack\n", value);}

Implementation of Stack (Linked List-based)

- **// Pop operation**

- void pop() {
- if (top == NULL) {
- printf("Stack Underflow!\n");
- return; }
- struct Node* temp = top;
- printf("%d popped from stack\n", top->data);
- top = top->next;
- free(temp); }

- **// Peek operation**

- void peek() {
- if (top == NULL) {
- printf("Stack is empty\n");
- return; }
- printf("Top element: %d\n", top->data);}
- // isEmpty operation
- int isEmpty() {
- return (top == NULL); }

Implementation of Stack (Linked List-based)

- **// Display stack**

- void display() {
- struct Node* temp = top;
- if (temp == NULL) {
- printf("Stack is empty\n");
- return; }
- printf("Stack elements: ");
- while (temp != NULL) {
- printf("%d ", temp->data);
- temp = temp->next; }
- printf("\n"); }

- **// Main function**

- int main() {
- int choice, value;
- while (1) {
- printf("\n1. Push\n2. Pop\n3. Peek\n4. isEmpty\n5. Display\n6. Exit\n");
- printf("Enter your choice: ");
- scanf("%d", &choice);
- switch (choice) {
- case 1:.....

Evaluation of Expressions – infix, postfix, prefix and conversions

Applications of Stack

- Balancing Symbols (e.g., parentheses matching)
- Duplicate Parentheses
- Expression Conversion & Evaluation
 - Converting infix to prefix/postfix
 - Evaluating postfix expressions
 - Evaluating prefix expressions

Balancing the parentheses

Ensure that every opening symbol ($($, $\{$, $[$) has a matching closing symbol $($, $\}$, $]$), and they are properly nested.

BALANCED EXPRESSION	UNBALANCED EXPRESSION
$(a + b)$	$(a + b$
$[(c - d) * e]$	$[(c - d * e]$
$\{ () \} []$	$\{ [()] \}$

Checking Balanced Parentheses using Stack

- **Step 1:** Create an empty stack.
- **Step 2:** Scan expression from left to right.
- **Step 3:**
 - If symbol is **opening** (, {, [, push it onto the stack.
 - If symbol is **closing**), },]):
 - If stack is empty → Not balanced.
 - Else pop from stack and check if it matches the opening symbol.
- **Step 4:** After scan, if stack is empty → Balanced, else → Not balanced.

Implementation

- `#define MAX 100`
- `struct stack {`
- `char stck[MAX];`
- `int top;} s;`
- **// Push function**
- `void push(char item) {`
- `if (s.top == MAX - 1) return 0;{`
- `printf("Stack is Full\n");`
- `} else {`
- `s.top++;`
- `s.stck[s.top] = item; return 1;`
- `} }`

Implementation

- **// Pop function**

- void pop() {
- if (s.top == -1) {
- printf("Stack is Empty\n");
- } else {
- s.top--;
- } }

- **// Function to check matching pairs**

- int checkPair(char val1, char val2) {
- return ((val1 == '(' && val2 == ')') ||
- (val1 == '[' && val2 == ']') ||
- (val1 == '{' && val2 == '}'));
- }

Implementation

- **// Function to check if expression is balanced**
- `int checkBalanced(char expr[], int len) {`
- `for (int i = 0; i < len; i++) {`
- `if (expr[i] == '(' || expr[i] == '[' || expr[i] == '{') {`
- `push(expr[i]);`
- `} else if (expr[i] == ')' || expr[i] == ']' || expr[i] == '}') {`
- `if (s.top == -1)`
- `return 0;`
- `else if (checkPair(s.stck[s.top], expr[i])) {`
- `pop();`
- `} else {`
- `return 0;`
- `} } }`
- `return (s.top == -1); }`

Implementation

- **// Main function**
- `int main() {`
- `char exp[MAX];`
- `printf("Enter an expression: ");`
- `fgets(exp, MAX, stdin);`
- `exp[strcspn(exp, "\n")] = '\0';`
- `int len = strlen(exp);`
- `s.top = -1;`
- `if (checkBalanced(exp, len))`
- `printf("Balanced");`
- `else`
- `printf("Not Balanced");`
- `return 0;`
- `}`

Duplicate Parentheses

- An expression has *duplicate parentheses* if an extra pair of brackets surrounds a valid subexpression unnecessarily.
- In other words, if an expression is enclosed by multiple balanced parentheses without need.
- **Examples**
 - $((a+b)) \rightarrow$ **Duplicate exists** \rightarrow **Return True**
 - $(a+(b+c)) \rightarrow$ **No duplicate** \rightarrow **Return False**
- Duplicate parentheses reduce readability and do not change meaning of the expression.

Detect Duplicate Parentheses

1. Initialize an empty stack.
2. For each character `ch` in the expression:
 - a) If `ch` is an operand or operator → Continue.
 - b) If `ch` is an opening parenthesis '(' → Push it onto the stack.
 - c) If `ch` is a closing parenthesis ')':
 - i. If the top of the stack is '(' →
 - Duplicate found → Return True.
 - ii. Else → Pop elements until '(' is found.
 - (This ensures valid matching of parentheses.)

Detect Duplicate Parentheses

3. After scanning all characters:

- a) If the stack is not empty → Unmatched parentheses → Return True.
- b) Else → Return False (No duplicate parentheses).

Implementation

- #define MAX_SIZE 100
- bool isDuplicate(char s[]) {
- char Stack[MAX_SIZE];
- int top = -1;
- int n = strlen(s);
- for (int i = 0; i < n; i++) {
- if (s[i] == '(') {
- // Case 1: Empty brackets ()
- if (top != -1 && Stack[top] == '(') {
- return 1; // Duplicate }
- int elementsInside = 0;
- // Pop until '(' is found
- while (top != -1 && Stack[top] != '(') {
- elementsInside++;
- top--; }
- // Pop the '(' also
- if (top != -1) {
- top--; }

Implementation

- // If no valid content inside ()
- if (elementsInside < 1){
- return true;
- } }
- else {
- // Push character onto stack
- Stack[++top] = s[i];
- } }
- // If unmatched parentheses remain
- while (top != -1){
- if (Stack[top] == '('){
- return true;
- }
- top--;
- }
- return false;
- }

Implementation

- `int main() {`
- `char s[MAX_SIZE] = "(((a+(b)))+(c+d)))";`
- `if (isDuplicate(s)) {`
- `printf("Expression contains duplicate parenthesis.\n");`
- `} else {`
- `printf("Expression does not contain duplicate parenthesis.\n");`
- `}`
- `return 0; }`

Expression Conversion & Evaluation

Infix, postfix and prefix expressions

- **Infix:** *operand1 operator operand2* - Ex: $A+B$
- **Prefix:** *operator operand1 operand2* - Ex: $+AB$
- **Postfix:** *operand1 operand2 operator* - Ex: $AB+$

PRECEDENCE AND ASSOCIATIVITY

Token	Operator	Precedence ¹	Associativity
() [] -> .	function call array element struct or union member	17	left-to-right
-- ++	increment, decrement ²	16	left-to-right
-- ++ ! ~ - + & * sizeof	decrement, increment ³ logical not one's complement unary minus or plus address or indirection size (in bytes)	15	right-to-left
(type)	type cast	14	right-to-left
* / %	multiplicative	13	left-to-right
+ -	binary add or subtract	12	left-to-right
<< >>	shift	11	left-to-right
> >= < <=	relational	10	left-to-right
== !=	equality	9	left-to-right
&	bitwise and	8	left-to-right
^	bitwise exclusive or	7	left-to-right
	bitwise or	6	left-to-right
&&	logical and	5	left-to-right
	logical or	4	left-to-right
?:	conditional	3	right-to-left
= += -= /= *= %= <<= >>= &= ^= =	assignment	2	right-to-left
,	comma	1	left-to-right

Problems with Infix

- Hard to parse (ambiguous without rules).
- Requires precedence rules.
- Needs parentheses for clarity.
- Example: $(A + B) * C$ vs. $A + (B * C)$.

Alternative Notations

- **Prefix (Polish Notation):** Operator before operands $\rightarrow +AB$.
- **Postfix (Reverse Polish Notation):** Operator after operands $\rightarrow AB+$.
- Advantage: No parentheses, no precedence/associativity issues.

Infix, postfix and prefix expressions

Infix Notation	Prefix Notation	Postfix Notation
$A + B$	$+ AB$	$AB +$
$(A - C) + B$	$+ - ACB$	$AC - B +$
$A + (B * C)$	$+ A * BC$	$ABC * +$
$(A+B)/(C-D)$	$/ + AB - CD$	$AB + CD - /$
$(A + (B * C))/(C - (D * B))$	$/ + A * BC - C * DB$	$ABC * + CDB * - /$

Conversion of **Infix to Postfix** Expression

- **Operands** → Send directly to output.
- **Left parenthesis (** → Push onto stack.
- **Right parenthesis)** → Pop & output until (is found.
- **Operators**
 - If stack empty / top is (→ Push operator.
 - If incoming operator has **higher precedence** → Push it.
 - If **lower precedence** → Pop & output until condition satisfied.
 - If **same precedence** →
 - **Left** → **Right associativity** → Pop & output top, then push new one.
 - **Right** → **Left associativity** → Push new one.
 - **End of expression** → Pop all operators from stack to output.

INFIX to POSTFIX- Simple expression

Token	Stack			Top	Output
	[0]	[1]	[2]		
<i>a</i>				-1	<i>a</i>
<i>+</i>	<i>+</i>			0	<i>a</i>
<i>b</i>	<i>+</i>			0	<i>ab</i>
<i>*</i>	<i>+</i>	<i>*</i>		1	<i>ab</i>
<i>c</i>	<i>+</i>	<i>*</i>		1	<i>abc</i>
<i>eos</i>				-1	<i>abc*+</i>

INFIX to POSTFIX- Parenthesized expression

Token	Stack			Top	Output
	[0]	[1]	[2]		
<i>a</i>				-1	<i>a</i>
<i>*</i>	*			0	<i>a</i>
<i>(</i>	*	(1	<i>a</i>
<i>b</i>	*	(1	<i>ab</i>
<i>+</i>	*	(+	2	<i>ab</i>
<i>c</i>	*	(+	2	<i>abc</i>
<i>)</i>	*			0	<i>abc +</i>
<i>*</i>	*			0	<i>abc +*</i>
<i>d</i>	*			0	<i>abc +*d</i>
<i>eos</i>	*			0	<i>abc +*d*</i>

Implementation

- `#define MAX_SIZE 100`
- **// Function prototypes**
- `int IsOperator(char c);`
- `int IsOperand(char c);`
- `int precedence(char op);`
- `int hasHigherOrEqualPrecedence(char op1, char op2);`
- `void convert(char infix[], char postfix[]);`

Implementation

- // Main function
- int main() {
- char infix[MAX_SIZE], postfix[MAX_SIZE];
- int ch;
- do {
- printf("Enter an infix expression: ");
- fgets(infix, MAX_SIZE, stdin);
- infix[strcspn(infix, "\n")] = '\0';
- convert(infix, postfix);
- printf("\nInfix : %s", infix);
- printf("\nPostfix : %s", postfix);
- printf("\n\nDo you want to enter another expression? (1/0): ");
- scanf("%d", &ch);
- getchar(); // clear newline from buffer
- } while (ch == 1);
- return 0;
- }

Implementation

- `// Check if character is operator`
- `int IsOperator(char c) {`
- `return (c == '+' || c == '-' || c == '*' || c == '/' || c == '^'); }`
- `// Check if character is operand (A-Z, a-z, 0-9)`
- `int IsOperand(char c) {`
- `return ((c >= 'A' && c <= 'Z') ||`
- `(c >= 'a' && c <= 'z') ||`
- `(c >= '0' && c <= '9'));`
- `}`
- `// Return precedence value`
- `int precedence(char op) {`
- `if (op == '+' || op == '-') return 1;`
- `if (op == '*' || op == '/') return 2;`
- `if (op == '^') return 3;`
- `return 0;`

Implementation

- `// Check precedence & associativity`
- `int hasHigherOrEqualPrecedence(char op1, char op2) {`
- `int p1 = precedence(op1);`
- `int p2 = precedence(op2);`
- `if (p1 == p2) {`
- `if (op1 == '^') // '^' is right-associative`
- `return 0;`
- `return 1; // others are left-associative }`
- `return (p1 > p2); }`

Implementation

- `// Convert infix to postfix`
- `void convert(char infix[], char postfix[]) {`
- `char stack[MAX_SIZE];`
- `int top = -1, i = 0, j = 0;`
- `char ch;`
- `// Add '(' to stack and ')' to infix (sentinel`
 `trick)`
- `stack[++top] = '(';`
- `strcat(infix, " ");`
- `while ((ch = infix[i++]) != '\0') {`
- `if (ch == ' ')`
- `continue; // ignore spaces`
- `else if (ch == '(')`
- `stack[++top] = ch;`
- `else if (IsOperand(ch))`
- `postfix[j++] = ch;`

Implementation

- `else if (IsOperator(ch)) {`
- `while (top != -1 &&`
 `hasHigherOrEqualPrecedence(stack[top], ch))`
- `postfix[j++] = stack[top--];`
- `stack[++top] = ch; }`
- `else if (ch == ')') {`
- `while (top != -1 && stack[top] != '(')`
- `postfix[j++] = stack[top--];`
- `top--; // remove '('}}`
- `postfix[j] = '\0';`
- `}`

Practice Infix to Postfix in stack

- $((A*(B+D)/E)-F*(G+H/K))$
- $(K+L- M*N+(O^P)*W/U/V *T+Q)$

Evaluation of Postfix Expression (using Stack)

1. Initialize an empty stack
2. For each symbol X in the postfix expression:
 - a) If X is an operand → Push X onto stack
 - b) If X is an operator:
 - i. Pop the top two operands from stack
 - ii. Apply the operator (second popped op <operator> first popped op)
 - iii. Push the result back onto stack
3. After scanning the expression:
 - The value left in the stack is the final result

EVALUATION OF POSTFIX EXPRESSION: $23*5+$

Step	Symbol	Action	Stack
1	2	Push	2
2	3	Push	2 3
3	*	Pop 3 & 2 $\rightarrow 2*3=6 \rightarrow$ Push 6	6
4	5	Push	6 5
5	+	Pop 5 & 6 $\rightarrow 6+5=11$ \rightarrow Push 11	11

EVALUATION OF POSTFIX EXPRESSION

Evaluate the postfix
expression **3 8 + 9 8 / -**

3 8	<div> <div>8</div> <div>3</div> </div>
+	$3 + 8 = 11$ <div>11</div>
9 8	<div> <div>8</div> <div>9</div> <div>11</div> </div>
/	$9/8 = 1.125$ <div> <div>1.125</div> <div>11</div> </div>
-	$11 - 1.125 = 9.875$ <div>9.875</div>

Conversion of **Infix to Prefix** Expression

- 1. Reverse the given infix expression - While reversing, replace '(' with ')' and ')' with '('.
- 2. Initialize an empty stack for operators.
- Initialize an empty string for the output (prefix).
- 3. Scan the reversed infix expression from left to right:
 - a) If the symbol is an operand → Append it to output.
 - b) If the symbol is '(' → Push it onto stack.
 - c) If the symbol is ')' →
 - Pop from stack and append to output until '(' is found.
 - Discard the '('.

Conversion of **Infix to Prefix** Expression

- d) If the symbol is an operator:
 - i. If stack is empty \rightarrow Push operator.
 - ii. If operator has higher precedence than top of stack \rightarrow Push operator.
 - iii. If operator has same precedence \rightarrow
 - - Push operator (for left-associative ops).
 - - Special case: If operator is '^' (right-associative), pop stack top and then push '^'.
 - iv. If operator has lower precedence than top of stack \rightarrow
 - Pop from stack to output until condition is satisfied,
 - then push the operator.

Conversion of **Infix to Prefix** Expression

- 4. After scanning the expression:
 - Pop and append all remaining operators from stack to output.
- 5. Reverse the output string.
- This final string is the Prefix expression.

Verification

- **Reverse infix first** (with brackets swapped)
- **Operands** → **output directly**
- **Operator handling** (higher → push, equal → depends on associativity, lower → pop until safe)
- **Parentheses handling** () pushed, (pops until) is found)
- **End** → **pop remaining operators**
- **Final reverse output**

Implementation

- `#define MAX_SIZE 100`
- `int IsOperator(char c);`
- `int IsOperand(char c);`
- `int Precedence(char c);`
- `int isRightAssociative(char c);`
- `void ReverseString(char str[]);`
- `void ReverseAndSwap(char str[]);`
- `void Convert(char infix[], char prefix[]);`
- `int main() {`
- `char infix[MAX_SIZE], prefix[MAX_SIZE];`
- `int ch;`
- `do { printf("Enter an infix expression: ");`
- `scanf("%s", infix);`
- `Convert(infix, prefix);`
- `printf("\nInfix Expression: %s", infix);`
- `printf("\nPrefix Expression: %s\n", prefix);`

Implementation

- `printf("\nDo you want to enter another (1/0)? ");`
- `scanf("%d", &ch);`
- `} while (ch == 1);`
- `return 0; }`
- `int IsOperator(char c){`
- `return (c == '+' || c == '-' || c == '*' || c == '/' || c == '^);`
- `}`

- `int IsOperand(char c){`
- `return ((c >= 'A' && c <= 'Z') ||`
- `(c >= 'a' && c <= 'z') ||`
- `(c >= '0' && c <= '9'));` `}`
- `int Precedence(char c){`
- `if (c == '+' || c == '-') return 1;`
- `if (c == '*' || c == '/') return 2;`
- `if (c == '^') return 3;`
- `return 0; }`

Implementation

- `// Right associativity check (only ^ is right-associative)`
- `int isRightAssociative(char c)`
- `{`
- `if (c == '^') return 1;`
- `return 0;`
- `}`
- `void ReverseString(char str[]) {`
- `int i, j;`
- `char temp;`
- `for (i = 0, j = strlen(str) - 1; i < j; i++, j--) {`
- `temp = str[i];`
- `str[i] = str[j];`
- `str[j] = temp;`
- `} }`

Implementation

- `// Reverse + swap brackets`
- `void ReverseAndSwap(char str[]) {`
- `ReverseString(str);`
- `for (int i = 0; str[i] != '\0'; i++) {`
- `if (str[i] == '(') str[i] = ')';`
- `else if (str[i] == ')') str[i] = '(';`
- `}`
- `}`
- `// ----- Conversion Function -----`
- `void Convert(char infix[], char prefix[]) {`
- `char stack[MAX_SIZE];`
- `int top = -1;`
- `int i = 0, j = 0;`
- `char ch;`
- `// Step 1: Reverse infix and swap brackets`
- `ReverseAndSwap(infix);`

Implementation

- // Step 2: Scan the reversed infix
- while ((ch = infix[i++]) != '\0') {
- if (ch == ' ') continue;
- if (IsOperand(ch)) {
- prefix[j++] = ch;
- } else if (ch == '(') {
- stack[++top] = ch; }
- else if (ch == ')') {
- while (top != -1 && stack[top] != '(') {
- prefix[j++] = stack[top--]; }
- top--; // discard '(' }
- else if (IsOperator(ch)) {
- while (top != -1 && IsOperator(stack[top])
- && (Precedence(stack[top]) > Precedence(ch)
- || (Precedence(stack[top]) ==
- Precedence(ch) && isRightAssociative(ch))))
- {
- prefix[j++] = stack[top--];
- }
- stack[++top] = ch; } }

Implementation

- // Step 3: Pop remaining operators
- while (top != -1) {
- prefix[j++] = stack[top--];
- }
- prefix[j] = '\0';
- // Step 4: Reverse result
- ReverseString(prefix);
- }
- **Practice step by step**
- **A+B-C*D+(E^F)*G/H/I*J+K**

Evaluation of Prefix Expression

- 1. Initialize an empty stack.
- 2. Scan the prefix expression from **right to left**:
 - a) If the symbol is an operand → Push it onto stack.
 - b) If the symbol is an operator:
 - i. Pop the top two operands from the stack.
 - ii. Apply the operator as:
$$\text{result} = (\text{first popped operand}) <\text{operator}> (\text{second popped operand})$$
 - iii. Push the result back onto the stack.
- 3. After scanning all symbols:
 - The value left in the stack is the final result.

Prefix Evaluation:

EVALUATION OF PREFIX EXPRESSION

INPUT : **/+33-+47*+123**

Symbol	Stack	Action
3	3	Push 3 into stack.
2	3,2	Push 2 into stack.
1	3,2,1	Push 1 into stack.
+	3,3	Pop 1 and 2 from stack and push 1+2=3 into stack.
*	9	Pop 3 and 3 from stack and push 3*3=9 into stack.
7	9,7	Push 7 into stack.
4	9,7,4	Push 4 into stack.
+	9,11	Pop 7 and 4 from stack and push 7*4=11 into stack.
-	2	Pop 9 and 11 from stack and push 11-9=2 into stack.
3	2,3	Push 3 into stack.
3	2,3,3	Push 3 into stack.
+	2,6	Pop 3 and 3 from stack and push 3+3=6 into stack.
/	3	Pop 2 and 6 from stack and push 2/6=3 into stack.

**Find the
mistake**

Implementation

- `#define MAX 100`
- ----- Stack Definition -----
- `typedef struct {`
- `int data[MAX];`
- `int top;`
- `} Stack`
- ----- Stack Functions -----
- `void Push(Stack *s, int value) {`
- `if (s->top == MAX - 1) {`
- `printf("Stack Overflow\n");`
- `exit(1); }`
- `s->data[++(s->top)] = value; }`
- `int Pop(Stack *s) {`
- `if (s->top == -1) {`
- `printf("Stack Underflow\n");`
- `exit(1); }`
- `return s->data[(s->top)--]; }`

Implementation

- // ----- Prefix Evaluation -----
- int EvaluatePrefix(char expression[]) {
- Stack stack;
- stack.top = -1;
- int i, op1, op2, result;
- // Scan expression from right to left
- for (i = strlen(expression) - 1; i >= 0; i--)
- {
- char ch = expression[i];
- if (ch == ' ')
- continue;
- if (isdigit(ch)) {
- Push(&stack, ch - '0'); // convert char
- digit to int
- }
- else {
- op1 = Pop(&stack);
- op2 = Pop(&stack);

Implementation

- switch (ch) {
 - case '+': result = op1 + op2; break;
 - case '-': result = op1 - op2; break;
 - case '*': result = op1 * op2; break;
 - case '/': result = op1 / op2; break;
 - case '%': result = op1 % op2; break;
 - default:
 - printf("Invalid operator: %c\n", ch);
 - return -1; } }
 - Push(&stack, result);
 - return Pop(&stack); // Final result
 - }

Implementation

- // ----- Main Function -----
- `int main() {`
- `char expr[MAX];`
- `printf("Enter a prefix expression: ");`
- `scanf("%[^\n]s", expr);`
- `int result = EvaluatePrefix(expr);`
- `printf("Result = %d\n", result);`
- `return 0; }`
- **Practice**
- CONVERT INFIX TO POSTFIX USING STACK
- $a * b + c / d - (e + f) * g / (h - i) + j * k$
- APPLY VALUES AND EVALUATE THE PREFIX FOR THE SAME EXPRESSION