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1. Tentukan deret Taylor dan maclueron dari:

a. $f(x) = \frac{1}{1+x}$

b. $f(x) = \ln(1+x)$

2. Tentukan deret Taylor dan maclueron dari:

a. $f(x) = \sin x$

b. $f(x) = \cos x$

jawab

1.a $f(x) = \frac{1}{1+x}$

deret taylor

$$1 + \frac{\frac{d}{dx}\left(\frac{1}{1+x}\right)(0)}{1!}x + \frac{\frac{d^2}{dx^2}\left(\frac{1}{1+x}\right)(0)}{2!}x^2 + \frac{\frac{d^3}{dx^3}\left(\frac{1}{1+x}\right)(0)}{3!}x^3 + \dots$$

deret maclaurin

$$1 + \frac{\frac{d}{dx}\left(\frac{1}{1+x}\right)(0)}{1!}x + \frac{\frac{d^2}{dx^2}\left(\frac{1}{1+x}\right)(0)}{2!}x^2 + \frac{\frac{d^3}{dx^3}\left(\frac{1}{1+x}\right)(0)}{3!}x^3 + \dots$$

1.b. $f(x) = \ln(1+x)$

deret taylor

$$f(0) = 0 + \frac{\frac{d}{dx}(\ln(1+x))(0)}{1!}x + \frac{\frac{d^2}{dx^2}(\ln(1+x))(0)}{2!}x^2 + \frac{\frac{d^3}{dx^3}(\ln(1+x))(0)}{3!}x^3 + \dots$$

deret maclaurin

$$f(0) = 0 + \frac{\frac{d}{dx}(\ln(1+x))(0)}{1!}x + \frac{\frac{d^2}{dx^2}(\ln(1+x))(0)}{2!}x^2 + \frac{\frac{d^3}{dx^3}(\ln(1+x))(0)}{3!}x^3 + \dots$$

2.a. $f(x) = \sin x$

$f(x) = \sin(x)$ dimana $x_0 = 0$

$$f(x) = \sin(x) = \sin(0)h \cos(0) - \frac{h^2}{2}\sin(0) - \frac{h^3}{6}\cos(0)$$

$$f(x) = \sin(x) = x - \frac{x^3}{6} + \frac{x^5}{120} - \dots$$

2.b. $f(x) = \cos x$

$$\cos x = 1 - \frac{1}{2!}x^2 + \frac{1}{4!}x^4 - \frac{1}{6!}x^6 + \frac{1}{8!}x^8 + \dots$$