# Update Estimation and Scheduling for Over-the-Air Federated Learning with Energy Harvesting Devices

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June 12, 2025





# What is Federated Learning (FL)?

### Federated Learning

- A machine learning approach where:
  - Data remains decentralized
  - Devices collaboratively train a shared global model

### **Key Components**

- Mobile Users (MUs)
- Parameter Server (PS)

#### Process



Figure 1: Illustration of a standard FL.

- PS sends the global model to users.
- ② Users compute local updates.
- **3** Updates are aggregated by the PS.
- 4 Repeat until convergence.

# Why Federated Learning (FL)?

Introduction

#### Traditional ML

- Centralized data sharing:
  - Requires high resources
  - Compromises privacy

## Collaborative model training without sharing local data

- Advantages:
  - Preserves privacy
  - Reduces latency
  - Improves learning quality

### Why Over-the-Air (OTA) FL?

### Challenge in FL

 Key bottleneck: Communication bandwidth.

#### Solution: OTA FL

- Leverages superposition property of wireless MAC
- Saves bandwidth by avoiding separate transmissions for each user.

$$\Delta \boldsymbol{\theta}(t) = \frac{1}{M} \sum_{m=1}^{M} \Delta \boldsymbol{\theta}_m(t). \tag{1}$$

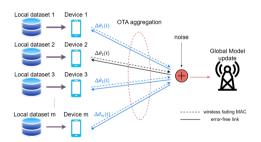


Figure 2: Illustration of OTA FL.

# Challenges in OTA FL

### Energy Harvesting (EH) Devices

- Uneven and stochastic participation in learning.
- Existing studies focus on optimizing energy usage via:
  - Transceiver optimization, receive beamforming design.
- Bernoulli energy arrival process:
  - The m-th user receives unit energy with probability  $p_e^m(t)$ ,

$$E_{m}(t) = \begin{cases} 1 \text{ with probability } p_{e}^{m}(t), \\ 0 \text{ with probability } 1 - p_{e}^{m}(t). \end{cases}$$
 (2)

• Unit-sized battery at the users.

# Challenges in OTA FL

#### Non-i.i.d. Data Distribution

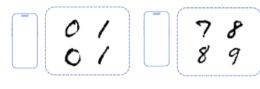


Figure 3: Illustration of non-i.i.d data.

#### Non-i.i.d. Data

- Data heterogeneity impacts:
  - Model convergence <sup>2</sup>.
  - Accuracy due to bias in updates.
- Existing works tackle this with:
  - Clustered Sampling <sup>3</sup>
  - Diverse User Selection <sup>4</sup>

• In contrast, our OTA FL setup uses noisy aggregated updates.

These studies rely on separate transmission of user updates.

<sup>&</sup>lt;sup>2</sup> X. Li et al., "On the convergence of FedAvg on non-iid data," arXiv preprint, arXiv:1907.02189, 2019.

<sup>&</sup>lt;sup>3</sup> Y. Fraboni et al., "Clustered sampling for client selection in federated learning," ICML, 2021.

 $<sup>^4\,</sup>$  R. Balakrishnan et al., "Diverse client selection for federated learning via submodular maximization," ICLR, 2022.

### Contributions

Introduction

#### Diverse User Selection for FL with EH Devices

- 1. Entropy-Based Scheduling:
  - For known data distributions.
  - Ensures a **balanced representation** of data labels.
- 2. LSE-Based Scheduling:
  - For unknown data distributions.
  - Estimates user updates from aggregated signals at the PS.
  - Clusters users based on estimated representations to enhance diversity and eliminate redundant information.

### FL Setup

- M: number of MUs
- K: number of receive antennas
- **Objective:**

$$F(\boldsymbol{\theta}) = \sum_{m=1}^{M} \frac{|B_m|}{B} F_m(\boldsymbol{\theta}), \tag{3}$$

where:

- $F_m(\theta)$ : Local loss function.
- $F_m(\boldsymbol{\theta}) = \frac{1}{|B_m|} \sum_{\boldsymbol{u} \in P} f(\boldsymbol{\theta}, \boldsymbol{u})$

Selected users S(t) perform  $\tau$  iterations of local SGD:

$$\boldsymbol{\theta}_{m}^{i+1}(t) = \boldsymbol{\theta}_{m}^{i}(t) - \eta_{m}^{i}(t) \nabla F_{m}(\boldsymbol{\theta}_{m}^{i}(t), \xi_{m}^{i}(t)),$$

$$\tag{4}$$

The *m*-th user computes the model update as:

$$\Delta \boldsymbol{\theta}_{m}(t) = \boldsymbol{\theta}_{m}^{\tau}(t) - \boldsymbol{\theta}_{m}^{1}(t). \tag{5}$$

These updates are transmitted back to the PS for aggregation as:

$$\Delta \boldsymbol{\theta}_{PS}(t) = \frac{1}{|S(t)|} \sum_{m \in S(t)} \Delta \theta_m(t). \tag{6}$$

# **OTA FL Setup**

- Using **over-the-air** transmission over a fading MAC via **superposition** of signals
- The received signal at the *k*-th antenna of the PS at iteration *t* is:

$$\mathbf{y}_{PS,k}(t) = \sum_{m \in S(t)} \mathbf{h}_{m,k}(t) \circ \mathbf{x}_m(t) + \mathbf{z}_{PS,k}(t), \quad (7)$$

#### where:

- $h_{m,k}(t)$ : i.i.d. channel gain from user m to antenna k with  $h_{m,k}^n(t) \sim CN(0, \sigma_k^2)$ .
- $x_m(t)$ : Signal transmitted by user m.
- $z_{PS} k(t)$ : i.i.d. circularly symmetric AWGN with  $z_{DS,k}^n(t) \sim CN(0,\sigma_z^2)$ .

• The PS aligns and combines signals from K antennas to mitigate fading effects.

$$\mathbf{y}_{PS}(t) = \frac{1}{K} \sum_{k=1}^{K} \left( \sum_{m \in S(t)} \mathbf{h}_{m,k}(t) \right)^* \circ \mathbf{y}_{PS,k}(t), \tag{8}$$

with:

exact information on the sum of the channel gains

## **OTA FL Setup**

 The n-th symbol of (8) can be partition into three signals<sup>5</sup>

$$y_{PS}^{n}(t) = \underbrace{\sum_{m \in S(t)} \left( \frac{1}{K} \sum_{k=1}^{K} |h_{m,k}^{n}(t)|^{2} \right) \Delta \theta_{m}^{n,cx}(t)}_{y_{PS}^{n,sig}(t) \text{ (signal term)}}$$

$$+ \underbrace{\frac{1}{K} \sum_{m \in S(t)} \sum_{m' \in S(t)} \sum_{k=1}^{K} (h_{m,k}^{n}(t))^{*} h_{m',k}^{n}(t) \Delta \theta_{m'}^{n,cx}(t)}_{y_{PS}^{n,int}(t) \text{ (interference term)}}$$

$$+ \underbrace{\frac{1}{K} \sum_{m \in S(t)} \sum_{k=1}^{K} (h_{m,k}^{n}(t))^{*} z_{PS,k}^{n}(t)}_{y_{PS}^{n,noise}(t) \text{ (noise term)}}$$
(9)

 Recovery of noisy aggregated updates as

$$\Delta \hat{\boldsymbol{\theta}}_{PS}^{n}(t) = \frac{1}{|S(t)|\sigma_{h}^{2}} \operatorname{Re}\{y_{PS}^{n}(t)\},\tag{10a}$$

$$\Delta \hat{\boldsymbol{\theta}}_{PS}^{n+N}(t) = \frac{1}{|S(t)|\sigma_h^2} \operatorname{Im}\{y_{PS}^n(t)\},\tag{10b}$$

to update the global model, as

$$\boldsymbol{\theta}_{PS}(t+1) = \boldsymbol{\theta}_{PS}(t) + \Delta \hat{\boldsymbol{\theta}}_{PS}(t). \quad (11)$$

<sup>5</sup> M. M. Amiri et al., "Blind Federated Edge Learning," IEEE Trans. Wireless Commun., vol. 20, no. 8, pp. 5129-5143, Aug. 2021.

## Convergence Analysis

#### Convergence Rate:

· We have

$$\mathbb{E}\left[\|\boldsymbol{\theta}(t) - \boldsymbol{\theta}^*\|_2^2\right] \le \left(\prod_{i=0}^{t-1} A(i)\right) \|\boldsymbol{\theta}(0) - \boldsymbol{\theta}^*\|_2^2 + \sum_{j=0}^{t-1} B(j) \prod_{i=j+1}^{t-1} A(i),$$
(12)

with

$$\begin{split} A(i) &\triangleq 1 - \mu \eta(i) \left( \tau - \eta(i)(\tau - 1) \right), \\ B(i) &\triangleq \frac{\eta^2(i)\tau^2 G^2}{K} + \frac{\sigma_z^2 N}{\alpha_i^2 K |S(i)| \sigma_h^2} \\ &+ \left( 1 + \mu (1 - \eta(i)) \right) \eta^2(i) G^2 \frac{\tau(\tau - 1)(2\tau - 1)}{6} + \eta^2(i)(\tau^2 + \tau - 1) G^2 + 2\eta(i)(\tau - 1) \Gamma \\ &+ \left( \eta^2(t)\tau(\tau - 1) LG + \eta(t)\tau \epsilon \right)^2 + \left( \eta^2(t)\tau(\tau - 1) LG + \eta(t)\tau \epsilon \right) c, \end{split}$$

• with  $\epsilon$  being the gradient approximation error and defined as

$$\epsilon \triangleq \left\| \frac{1}{M} \sum_{m=1}^{M} \nabla F_m(\theta_m(t)) - \frac{1}{|S(t)|} \sum_{m \in S(t)} \nabla F_m(\theta_m(t)) \right\|_2. \tag{13}$$

# User Scheduling Strategies: Entropy-Based

#### We propose diverse user selection to handle:

- · Data heterogeneity
- · Stochastic participation

### **Entropy-Based Scheduling:**

 Goal: Achieve a uniform representation of data across users.

### Methodology:

 Compute the Shannon entropy of label distributions for all available subsets

$$\mathbf{L} = \begin{bmatrix} l_{1,0} & l_{1,1} & \cdots & l_{1,N_c-1} \\ l_{2,0} & l_{2,1} & \cdots & l_{2,N_c-1} \\ \vdots & \vdots & \ddots & \vdots \\ l_{M,0} & l_{M,1} & \cdots & l_{M,N_c-1} \end{bmatrix}.$$

 Select users with the highest combined entropy to ensure diversity

# User Scheduling Strategies: LSE-Based

### LSE-Based Scheduling:

 Goal: Estimate the representative user updates at the PS.

#### **Estimation Phase**

- Active users transmit their updates without scheduling
- PS stores global updates to create user representations
- Groups users into clusters using cosine similarities
- Selects equal users from each cluster for unbiased training

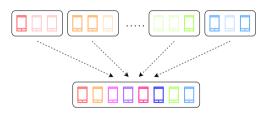


Figure 4: Illustration of clusters and diverse scheduling.

# User Scheduling Strategies: LSE-Based

• Define a matrix  $\hat{\Theta}_{PS}$ , where each row corresponds to the **global model updates** 

$$\hat{\mathbf{\Theta}}_{PS,j} = \mathbf{A}_j \mathbf{\Theta}_j + \mathbf{N'}_j$$

$$\hat{\boldsymbol{\Theta}}_{PS,j} = \boldsymbol{A}_{j} \begin{bmatrix} \Delta \boldsymbol{\theta}_{j,1} \\ \vdots \\ \Delta \boldsymbol{\theta}_{j,M} \end{bmatrix}_{M \times 2N} + \begin{bmatrix} N'_{j,1} \\ \vdots \\ N'_{j,2N} \end{bmatrix}^{T} . \quad (14)$$

where:

- $A_i$ : binary **participation vector** of size M.
- $\Theta_j$ : matrix with each row representing the **local model updates** from users.
- *N'*<sub>j</sub>: **effective noise** from MAC fading, AWGN, and combining errors.

• We also define  $\Theta_{rep} \in \mathbb{R}^{M \times 2N}$  as

$$\hat{\boldsymbol{\Theta}}_{PS,j} = \boldsymbol{A}_{j}(\boldsymbol{\Theta}_{rep} + \boldsymbol{\Theta}_{d,j}) + \boldsymbol{N}'_{j}, \tag{15}$$

where 
$$\Theta_{d,j} \triangleq \Theta_{rep} - \Theta_j$$
 and  $N_j^* \triangleq A_j \Theta_{d,j} + N_j'$ .

• Combining  $\hat{\mathbf{\Theta}}_{PS,j}$  across T iterations

$$\hat{\mathbf{\Theta}}_{PS} = A\mathbf{\Theta}_{rep} + N^*, \tag{16}$$

- Solve for  $\Theta_{rep}$  using Least-Squares Estimation.
- Using  $\Theta_{rep}$ , the PS:
  - Captures the **data characteristics** of users.
  - Groups users based on cosine similarity of representations.

- MNIST & FMNIST: Single-layer neural network with 2N=7850.
- **CIFAR-10**: Convolutional Neural Network (CNN) with 2N=797,962.
- SGD with a learning rate of 0.05 and a scheduler,  $\tau = 5$  and mini-batch size  $|\xi_m(t)| = 100$  for MNIST and FMNIST, and  $\tau = 3$  and  $|\xi_m(t)| = 128$  for CIFAR-10.

- Non-i.i.d. Data Scenarios
  - 1 or 2 classes per user
  - $p_m \sim \text{Dir}_{N_c}(\beta)$  with  $\beta \in \{0.1, 0.2\}$
- Wireless Setup
  - K = 200, M = [20 100] users
  - Noise variance:  $\sigma_h^2 = 1$ , and  $\sigma_z^2 = 0.1$ .

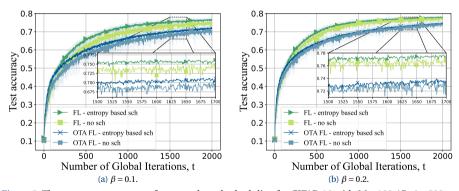


Figure 5: The mean test accuracy of entropy-based scheduling for CIFAR-10 with M=100,  $|B_m|=500$  and  $p_e^m(t)=0.1$ ,  $\forall m,t$ .

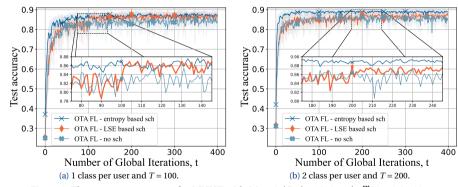


Figure 6: The mean test accuracy for MNIST with M = 40,  $|B_m| = 1250$  and  $p_e^m(t) = 0.25$ ,  $\forall m, t$ .

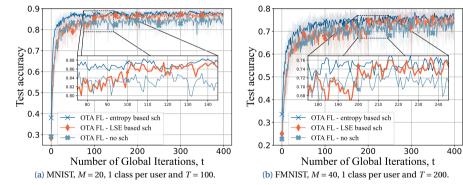


Figure 7: The mean test accuracy for MNIST and FMNIST.

### Conclusions

- We analyze the convergence rate for the OTA FL with EH devices and demonstrate the effect of user scheduling.
- Entropy-based scheduling approach yields higher and more stable accuracy levels.
- LSE-based scheduling can estimate user representations at the PS.
- Scheduling diverse users preserves privacy, eliminates redundant update transfers, and improves learning performance.

#### Future Directions

- Investigate the effect of estimation strategies under varying scenarios and energy constraints
- Implement clustered federated learning for the user clusters derived from our estimation.

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June 12, 2025

# Thank You!

Questions?

#### Acknowledgments

This work is supported by TUBITAK (Grant 221N366) under the CHIST-ERA SONATA project. Furkan Bagci is also supported by Türk Telekom within the 5G & Beyond Graduate Programme. Mohammad Kazemi acknowledges support from UKRI (Grant 101103430) under the Horizon Europe Guarantee.



