# MadDiff

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# Part I Introduction

## Introduction

Welcome to the documentation of MadDiff.jl

#### Note

This documentation page is under construction.

#### Note

This documentation is also available in PDF format.

## What is MadDiff?

MadDiff.jl is a simple algebraic modeling/differentiation package. MadDiff.jl constructs first and second derivative functions off-line (i.e., prior to calling the optimization solver) by applying operator overloading-based automatic differentiation on functions. The exact derivative functions can be obtained as results.

# **Bug reports and support**

Please report issues and feature requests via the Github issue tracker.

# Part II

**Quick Start** 

## **Getting Started**

#### 4.1 Automatic Differentiation

MadDiff provides a flexible user-interface for evaluating first/second-order derivatives of nonlinear expressions. In the following example, using MadDiff, we will create a function, gradient, and Hessian evaluator of the following function:

$$f(x) = x_1^2 + e^{(x_2^{p_1})/2} + \log(x_2 x_3 + p_2),$$

where  $\boldsymbol{x}$  is the variable vector, and  $\boldsymbol{p}$  is the parameter vector.

We first import MadDiff.

using MadDiff

First, we create a Source of Variable's.

```
x = Variable()
```

x

The Base.getindex! function is extended so that x[i] for any i creates an expression for  $x_i$ . For example,

x[2]

x[2]

We can do a similar thing for Parameter's.

```
p = Parameter()
p[1]
```

p[1]

Now, we create the nonlienar expression expression.

```
 | expr = x[1]^2 + exp(x[2]^p[1])/2 + log(x[2]^*x[3]+p[2]) 
 | x[1]^2 + exp(x[2]^p[1])/2 + log(x[2]^*x[3] + p[2])
```

The function evaluator of the above expression can be created by using MadDiff.function\_evaluator as follows:

```
| f = function_evaluator(expr)
| #316 (generic function with 2 methods)
```

Now for a given variable and parameter values, the function can be evaluated as follows.

0.8651562596580804

The gradient evaluator can be created as follows:

```
y0 = similar(x0)
g = gradient_evaluator(expr)
g(y0,x0,p0)
y0

3-element Vector{Float64}:
0.0
1.8420127083438709
0.4
```

The Hessian evaluator can be created as follows:

Note that only lower-triangular entries are evaluated.

The evaluator can be constructed in a sparse format:

```
sh,ij = sparse_hessian_evaluator(expr);
z1 = zeros(length(ij))
sh(z1,x0,p0)
z1
```

```
4-element Vector{Float64}:
2.0
0.4860381250316117
0.319999999999995
-0.16000000000000003
```

The sparse coordinates are:

|ij

```
4-element Vector{Tuple{Int64, Int64}}:
(1, 1)
(2, 2)
(3, 2)
(3, 3)
```

#### 4.2 Nonlinear Programming

#### **Built-in API**

MadDiff provides a built-in API for creating nonlinear prgogramming models and allows solving the created models using NLP solvers (in particular, those that are interfaced with NLPModels, such as NLPModelsIpopt and MadNLP). We now use MadDiff's bulit-in API to model the following nonlinear program:

$$\begin{split} \min_{\{x_i\}_{i=0}^N} \sum_{i=2}^N 100 (x_{i-1}^2 - x_i)^2 + (x_{i-1} - 1)^2 \\ \text{s.t.} 3x_{i+1}^3 + 2x_{i+2} - 5 + \sin(x_{i+1} - x_{i+2}) \sin(x_{i+1} + x_{i+2}) + 4x_{i+1} - x_i e^{x_i - x_{i+1}} - 3 = 0 \end{split}$$

We model the problem with:

```
N = 10000
| 10000
First, we create a MadDiffModel.
| m = MadDiffModel()
| MadDiffModel{Float64} (not instantiated).
```

The objective can be set as follows:

The variables can be created as follows:

```
objective(m, sum(100(x[i-1]^2-x[i])^2+(x[i-1]-1)^2 for i=2:N));
```

x = [variable(m; start = mod(i,2)==1 ? -1.2 : 1.) for i=1:N];

The constraints can be set as follows:

The important last step is instantiating the model. This step must be taken before calling optimizers.

instantiate!(m)

```
MadDiffModel{Float64} (instantiated).
 Problem name: Generic
 All variables:
                     10000 All constraints:
                     10000
                               free: ..... 0
      free:
      lower: ..... 0
                                lower: ..... 0
                               upper: .... 0
      upper: ..... 0
                               low/upp: ..... 0
     low/upp: ..... 0
      fixed: ..... 0
                                fixed: 9998
     infeas: ..... 0
                               infeas: ..... 0
       nnzh: ( 99.96% sparsity) 19999
                               linear: ..... 0
                             nonlinear:
                                nnzj: (99.97% sparsity) 29994
 Counters:
       obj: ..... 0
                                grad: ..... 0
   cons: ..... 0
    cons_lin: .... 0
                              cons_nln: ..... 0
   jcon: ..... 0
      jgrad: .... 0
                                 jac: ..... 0
  jac lin: ..... 0
     jac_nln: .... 0
                                jprod: ..... 0
  jprod_lin: ..... 0
    jprod_nln: .... 0
                               jtprod: ..... 0
  jtprod_lin: ..... 0
   jtprod_nln: .... 0
                                hess: ..... 0
   hprod: ..... 0
      jhess: ..... 0
                               ihprod: ..... 0
```

To solve the problem with Ipopt,

```
using NLPModelsIpopt
ipopt(m);
```

This is Ipopt version 3.14.4, running with linear solver MUMPS 5.4.1.

```
Number of nonzeros in equality constraint Jacobian...:
                                                       29994
Number of nonzeros in inequality constraint Jacobian.:
                                                          0
Number of nonzeros in Lagrangian Hessian.....
                                                       19999
                                                       10000
Total number of variables.....:
                   variables with only lower bounds:
                                                          O
                                                          0
               variables with lower and upper bounds:
                   variables with only upper bounds:
                                                          0
Total number of equality constraints....:
                                                        9998
Total number of inequality constraints....:
                                                          0
       inequality constraints with only lower bounds:
                                                          0
  inequality constraints with lower and upper bounds:
                                                          0
       inequality constraints with only upper bounds:
                                                          0
                   inf pr inf du lg(mu) ||d|| lg(rg) alpha du alpha pr ls
       objective
  0 2.5405160e+06 2.48e+01 2.73e+01 -1.0 0.00e+00 - 0.00e+00 0.00e+00
  1 1.3512419e+06 1.49e+01 8.27e+01 -1.0 2.20e+00
                                                    - 1.00e+00 1.00e+00f 1
  2 1.5156131e+05 4.28e+00 1.36e+02 -1.0 1.43e+00 - 1.00e+00 1.00e+00f 1
  3 6.6755024e+01 3.09e-01 2.18e+01 -1.0 5.63e-01 - 1.00e+00 1.00e+00f 1
  4 \quad 6.2338933e + 00 \quad 1.73e - 02 \quad 8.47e - 01 \quad -1.0 \quad 2.10e - 01 \quad - \quad 1.00e + 00 \quad 1.00e + 00h \quad 1
  5 6.2324586e+00 1.15e-05 8.16e-04 -1.7 3.35e-03 - 1.00e+00 1.00e+00h 1
  6 6.2324586e+00 8.36e-12 7.97e-10 -5.7 2.00e-06 - 1.00e+00 1.00e+00h 1
Number of Iterations....: 6
                                 (scaled)
                                                         (unscaled)
Objective..... 7.8692659500479645e-01
                                                   6.2324586324379885e+00
Dual infeasibility....: 7.9743417331632266e-10
                                                   6.3156786526652763e-09
Constraint violation...: 8.3555384833289281e-12
                                                   8.3555384833289281e-12
Variable bound violation: 0.0000000000000000e+00
                                                   0.0000000000000000e+00
Complementarity.....: 0.00000000000000000e+00
                                                   Overall NLP error.....: 7.9743417331632266e-10
                                                   6.3156786526652763e-09
Number of objective function evaluations
                                                  = 7
Number of objective gradient evaluations
                                                  = 7
Number of equality constraint evaluations
                                                  = 7
Number of inequality constraint evaluations
                                                  = 0
Number of equality constraint Jacobian evaluations = 7
Number of inequality constraint Jacobian evaluations = 0
Number of Lagrangian Hessian evaluations
                                                 = 6
Total seconds in IPOPT
                                                  = 1.549
```

#### MadDiff as a AD backend of JuMP

EXIT: Optimal Solution Found.

MadDiff can be used as an automatic differentiation backend of JuMP. The problem above can be modeled in JuMP and solved with Ipopt along with MadDiff

```
using JuMP, Ipopt

m = JuMP.Model(Ipopt.Optimizer)
```

```
@variable(m, x[i=1:N], start=mod(i,2)==1 ? -1.2 : 1.)
@NLobjective(m, Min, sum(100(x[i-1]^2-x[i])^2+(x[i-1]-1)^2 for i=2:N))
@NLconstraint(m, [i=1:N-2],
\Rightarrow 3x[i+1]^3+2*x[i+2]-5+\sin(x[i+1]-x[i+2])\sin(x[i+1]+x[i+2])+4x[i+1]-x[i]\exp(x[i]-x[i+1])-3 == 0
optimize!(m; differentiation_backend = MadDiffAD())
This is Ipopt version 3.14.4, running with linear solver MUMPS 5.4.1.
Number of nonzeros in equality constraint Jacobian...:
                                                      29994
Number of nonzeros in inequality constraint Jacobian.:
                                                         0
Number of nonzeros in Lagrangian Hessian....:
                                                      19999
Total number of variables....:
                                                      10000
                   variables with only lower bounds:
                                                         0
                                                         0
              variables with lower and upper bounds:
                   variables with only upper bounds:
                                                         0
Total number of equality constraints.....
                                                      9998
Total number of inequality constraints....:
                                                         0
                                                         0
       inequality constraints with only lower bounds:
  inequality constraints with lower and upper bounds:
                                                         0
       inequality constraints with only upper bounds:
                 inf_pr inf_du lg(mu) ||d|| lg(rg) alpha_du alpha_pr ls
iter
       objective
  0 2.5405160e+06 2.48e+01 2.73e+01 -1.0 0.00e+00 - 0.00e+00 0.00e+00
  1 1.3512419e+06 1.49e+01 8.27e+01 -1.0 2.20e+00
                                                   - 1.00e+00 1.00e+00f 1
  2 1.5156131e+05 4.28e+00 1.36e+02 -1.0 1.43e+00
                                                  - 1.00e+00 1.00e+00f 1
                                                  - 1.00e+00 1.00e+00f 1
  3 6.6755024e+01 3.09e-01 2.18e+01 -1.0 5.63e-01
                                                 - 1.00e+00 1.00e+00h 1
  4 6.2338933e+00 1.73e-02 8.47e-01 -1.0 2.10e-01
  5 6.2324586e+00 1.15e-05 8.16e-04 -1.7 3.35e-03 - 1.00e+00 1.00e+00h 1
  6 6.2324586e+00 8.36e-12 7.97e-10 -5.7 2.00e-06 - 1.00e+00 1.00e+00h 1
Number of Iterations....: 6
                                (scaled)
                                                        (unscaled)
Objective..... 7.8692659500479645e-01
                                                  6.2324586324379885e+00
Dual infeasibility.....: 7.9743417331632266e-10
                                                  6.3156786526652763e-09
Constraint violation...: 8.3555384833289281e-12
                                                  8.3555384833289281e-12
0.0000000000000000e+00
Complementarity.....: 0.0000000000000000e+00
                                                  0.0000000000000000e+00
Overall NLP error.....: 7.9743417331632266e-10
                                                  6.3156786526652763e-09
Number of objective function evaluations
                                                 = 7
Number of objective gradient evaluations
                                                 = 7
                                                 = 7
Number of equality constraint evaluations
Number of inequality constraint evaluations
                                                = 0
Number of equality constraint Jacobian evaluations = 7
Number of inequality constraint Jacobian evaluations = 0
Number of Lagrangian Hessian evaluations
                                                = 6
Total seconds in IPOPT
                                                 = 1.581
EXIT: Optimal Solution Found.
```

## Part III

# **How it Works**

## **How it Works**

This page was generated using Literate.jl.

## Part IV

## **API Manual**

#### **MadDiffCore**

#### 6.1 MadDiffCore

```
MadDiffCore.MadDiffCore - Module.
   MadDiffCore
   Core algorithm for MadDiff.
MadDiffCore.AbstractExpression - Type.
   | AbstractExpression{T <: AbstractFloat}
   Abstract type for expression, gradient, hessian, entry, and field evaluators.
    source
MadDiffCore.Constant - Type.
   Constant{T <: AbstractFloat} <: Expression{T}</pre>
   Expression for constants.
   Constant(x::T) where T <: AbstractFloat</pre>
   Returns a Constant with value x.
   Example
    julia> e = Constant(1.)
    julia> non_caching_eval(e, [1.,2.,3.])
    1.0
    source
MadDiffCore.Constant - Method.
   Constant{T}(x::R) where {T <: AbstractFloat, R <: Real}
   Returns a Constant\{T,R\} whose value is x.
    source
```

```
MadDiffCore.Entry - Type.
   Entry{T <: AbstractFloat}</pre>
   Abstract type for entry evaluators.
    source
MadDiffCore.Expression - Type.
   Expression{T <: AbstractFloat}</pre>
   Abstract type for expression evaluators.
    source
MadDiffCore.Expression1 - Type.
   | Expression1{T <: AbstractFloat, F <: Function ,E <: Expression{T}} <: Expression{T}
   Expression for univariate function
    source
MadDiffCore.Expression2 - Type.
   | Expression2{T <: AbstractFloat, F <: Function, E1, E2} <: Expression{T}
   Expression for bivariate function
    source
MadDiffCore.ExpressionIfElse - Type.
   ExpressionIfElse{T,E0 <: Expression{T}, E1, E2} <: Expression{T}</pre>
   Expression for ifelse
    source
MadDiffCore.ExpressionSum - Type.
   | ExpressionSum{T <: AbstractFloat, E <: Expression{T}, I} <: Expression{T}
   Expression for a summation of Expressions
   source
MadDiffCore.Field - Type.
   | Field{T <: AbstractFloat}
   Abstract type for field evaluators.
   source
MadDiffCore.Gradient - Type.
   Gradient{T <: AbstractFloat}</pre>
```

Abstract type for gradient evaluators.

```
source
MadDiffCore.Gradient - Method.
   Gradient(e :: Expression{T}) where T
   Returns the Gradient of an absraction e.
   source
MadDiffCore.Gradient0 - Type.
   | GradientO{T <: AbstractFloat} <: Gradient{T}
   Gradient of Variable.
   source
MadDiffCore.Gradient1 - Type.
   | Gradient1{T <: AbstractFloat, F, D1 <: Gradient} <: Gradient{T}
   Gradient of Expression1.
   source
MadDiffCore.Gradient2 - Type.
   | Gradient2{T <: AbstractFloat, F,D1 <: Gradient,D2 <: Gradient} <: Gradient{T}
   Gradient of Expression2.
   source
MadDiffCore.Gradient2F1 - Type.
   Gradient2F1{T <: AbstractFloat, F, D1 <: Gradient, R<: Real} <: Gradient{T}
   Gradient of Expression2 whose first argument is <: Real.
   source
MadDiffCore.Gradient2F2 - Type.
   | Gradient2F2{T <: AbstractFloat, F,D1 <: Gradient, R<: Real} <: Gradient{T}
   Gradient of Expression2 whose second argument is <: Real.
    source
MadDiffCore.GradientIfElse - Type.
   GradientIfElse{T, G1, G2} <: Gradient{T}</pre>
   Gradient of ExpressionIfElse
    source
MadDiffCore.GradientNull - Type.
```

```
GradientNull{T <: AbstractFloat} <: Gradient{T}</pre>
   Gradient of Parameter or Constant.
    source
MadDiffCore.GradientSum - Type.
   GradientSum{T <: AbstractFloat,D <: Gradient{T},I} <: Gradient{T}
   Gradient of ExpressionSum.
   source
MadDiffCore.Hessian - Type.
   Hessian{T <: AbstractFloat}</pre>
   Abstract type for hessian evaluators.
    source
MadDiffCore.Hessian02 - Type.
   | Hessian02{T,H11,H12,H21,H22} <: Hessian{T}
   Hessian of '
    source
MadDiffCore.Hessian11 - Type.
   | Hessian11{T,F,H1,H11} <: Hessian{T}
   Hessian of Expression1
   source
MadDiffCore.Hessian11F1 - Type.
   Hessian11F1{T,F,H1,H11,R} <: Hessian{T}</pre>
   Hessian of Expression2 whose first argument is <: Real.
   source
MadDiffCore.Hessian11F2 - Type.
   Hessian11F2{T,F,H1,H11,R} <: Hessian{T}</pre>
   Hessian of Expression2 whose second argument is <: Real.
    source
MadDiffCore.HessianNull - Type.
   | HessianNull{T} <: Hessian{T} end
   Hessian of linear expressions (e.g., Variable, Expression2{T, typeof(*), Int64, Variable{T}} where T)
    source
```

```
MadDiffCore.Parameter - Type.
   Parameter{T <: AbstractFloat} <: Expression{T}</pre>
   Expression for parameters.
   source
MadDiffCore.Parameter - Method.
   Parameter(n::Int)
   Returns a Parameter{Float64} whose index is n
   Example
    julia> e = Parameter(3)
    julia> non_caching_eval(e, [1.,2.,3.], [4.,5.,6.])
    6.0
   source
MadDiffCore.Parameter - Method.
   Parameter{T}(n::Int) where T <: AbstractFloat
   Returns a Parameter\{T\} whose index is n.
    source
MadDiffCore.Variable - Type.
   Variable{T <: AbstractFloat} <: Expression{T}</pre>
   Expression for variables.
   source
MadDiffCore.Variable - Method.
   Variable(n::Int)
   Returns a Variable{Float64} whose index is n
   Example
    julia> e = Variable(2)
    julia> non_caching_eval(e, [1.,2.,3.])
    2.0
    source
MadDiffCore.Variable - Method.
   | Variable{T}(n::Int) where T <: AbstractFloat
   Returns a Variable\{T\} whose index is n.
    source
```

#### **MadDiffModels**

#### 7.1 MadDiffModels

MadDiffModels.MadDiffModels - Module.

```
MadDiffModels
```

MadDiffModels is a submodule of MadDiff. MadDiffModels allows modeling nonlinear optimization problem of the following form:

```
minimize: f(x)

subject to: xl \le x \le xu

gl \le g(x) \le gu,
```

#### where:

- $x \in R^n$  is the decision variable.
- f : R^n -> R is the objective function
- g : R^n -> R^m is the constraint mapping.

The model is constructed as an NLPModel (see https://github.com/JuliaSmoothOptimizers/NLPModels.jl), and can be solved with various NLP solvers such as:

- MadNLP (https://github.com/MadNLP/MadNLP.jl)
- Ipopt (https://github.com/JuliaSmoothOptimizers/NLPModelsIpopt.jl)
- Knitro (https://github.com/JuliaSmoothOptimizers/NLPModelsKnitro.jl)

source

```
MadDiffModels.Constraint - Type.
```

```
Constraint
```

A constraint index of MadDiffModel.

source

```
MadDiffModels.MadDiffModel - Type.
```

```
| MadDiffModel{T <: Real}
```

**Example** 

```
A mathematical model of a nonlinaer program.
    source
MadDiffModels.MadDiffModel - Method.
    | MadDiffModel()
    Creates an empty MadDiffModel{Float64}.
    Example m = MadDiffModel(linear_solver = "ma27")
    source
MadDiffModels.MadDiffModel - Method.
    |MadDiffModel{T}()
    Creates an empty MadDiffModel{T}.
    Example m = MadDiffModel{Float32}()
    source
MadDiffModels.ModelComponent - Type.
   ModelComponent
    A model component (eitehr a variable or a parameter) of MadDiffModel.
    source
MadDiffModels.constraint - Method.
   constraint(m::MadDiffModel, e::MadDiffCore.Expression; lb=0., ub=0.)
    Adds a constraint to MadDiffModel. Example "' m = MadDiffModel()
    x = [variable(m) \text{ for } i=1:3] \text{ constraint}(m, x[1]^2 + 2*sin(x[2]) - exp(x[3]) >= 0) \text{ constraint}(m, x[1]^4 + 2*sin(x[2]) - exp(x[3]) >= 0)
    x[2]^4 x[3]^4; lb = 0.1, ub = 1.)
    source
MadDiffModels.dual - Method.
   dual(c::Constraint)
    Retrun the dual of constraint c.
    source
MadDiffModels.instantiate! - Method.
   instantiate!(m::MadDiffModel; sparse = true)
    Instantiates the model m. The model must be instantiated before solving.
```

```
using MadDiff, NLPModelsIpopt
    m = MadDiffModel()
    x = [variable(m) for i=1:3]
    objective(m, x[1]^2 + x[2]^2 + \sin(x[3]))
    constraint(m, 3x[2]^2 \ll 1.)
    instantiate!(m)
    ipopt(m)
   source
MadDiffModels.lower_bound - Method.
   |lower_bound(c::Constraint)
   Retrun the lower bound of constraint c.
    source
MadDiffModels.lower_bound - Method.
   lower_bound(x::ModelComponent{V}) where V <: MadDiffCore.Variable</pre>
   Retrun the lower bound of variable x.
    source
MadDiffModels.objective - Method.
   objective(m::MadDiffModel, e::MadDiffCore.Expression
   Sets the objective function for MadDiffModel. Only minimization is supported. Example
    m = MadDiffModel()
    x = [variable(m) for i=1:3]
    objective(m, x[1]^2 + x[2] + sin(x[3]))
   source
MadDiffModels.parameter - Method.
   parameter(m::MadDiffModel{T}, val)
   Creates a parameter for MadDiffModel with value val. Example
    m = MadDiffModel()
    p = parameter(m, 0.5)
   source
MadDiffModels.set_lower_bound - Method.
   set_lower_bound(c::Constraint,val)
```

```
Set the lower bound of constraint c to val.
    source
MadDiffModels.set_lower_bound - Method.
    | set_lower_bound(x::ModelComponent{V},val) where V <: MadDiffCore.Variable
    Set the lower bound of variable 'x' to val.
    source
MadDiffModels.set_upper_bound - Method.
   set_upper_bound(c::Constraint,val)
    Set the upper bound of constraint c to val.
    source
MadDiffModels.set_upper_bound - Method.
   \begin{tabular}{ll} | set\_upper\_bound(x::ModelComponent\{V\},val) & where V <: MadDiffCore.Variable \\ \end{tabular}
    Set the upper bound of variable 'x' to val.
    source
MadDiffModels.setvalue - Method.
   | setvalue(p::ModelComponent{P},val) where P <: MadDiffCore.Parameter
    Set the value of parameter 'p' to val.
    source
MadDiffModels.setvalue - Method.
   | setvalue(x::ModelComponent{V},val) where V <: MadDiffCore.Variable
    Set the value of variable 'x' to val.
    source
MadDiffModels.upper_bound - Method.
   upper_bound(c::Constraint)
    Retrun the upper bound of constraint c.
    source
MadDiffModels.upper_bound - Method.
   upper_bound(x::ModelComponent{V}) where V <: MadDiffCore.Variable</pre>
    Retrun the upper bound of variable x.
    source
MadDiffModels.value - Method.
```

```
value(p::ModelComponent{P}) where P <: MadDiffCore.Parameter</pre>
   Return the value of parameter p.
   source
MadDiffModels.value - Method.
   Return the value of variable x.
   source
MadDiffModels.variable - Method.
   variable(m::MadDiffModel{T}; lb=-Inf, ub=Inf, start=0.)
   Creates a variable for MadDiffModel.
   Example
   m = MadDiffModel()
   x = variable(m; lb = -1, ub = 1, start = 0.5)
   source
NLPModels.cons! - Method.
   | NLPModels.cons!(m::MadDiffModel,x::AbstractVector,y::AbstractVector)
   Evaluate the constraints of m at x and store the result in the vector y.
   source
NLPModels.get_ifix - Function.
   get_ifix(m::MadDiffModel)
   Return the value ifix from MadDiffModel.
   source
NLPModels.get_ifree - Function.
   get_ifree(m::MadDiffModel)
   Return the value ifree from MadDiffModel.
   source
NLPModels.get_iinf - Function.
   get_iinf(m::MadDiffModel)
   Return the value iinf from MadDiffModel.
   source
NLPModels.get_ilow - Function.
```

```
get_ilow(m::MadDiffModel)
   Return the value ilow from MadDiffModel.
    source
NLPModels.get_irng - Function.
   get_irng(m::MadDiffModel)
   Return the value irng from MadDiffModel.
   source
NLPModels.get_islp - Function.
   get_islp(m::MadDiffModel)
   Return the value islp from MadDiffModel.
    source
NLPModels.get_iupp - Function.
   get_iupp(m::MadDiffModel)
   Return the value iupp from MadDiffModel.
    source
NLPModels.get_jfix - Function.
   get_jfix(m::MadDiffModel)
   Return the value jfix from MadDiffModel.
   source
NLPModels.get jfree - Function.
   get_jfree(m::MadDiffModel)
   Return the value jfree from MadDiffModel.
   source
NLPModels.get_jinf - Function.
   get_jinf(m::MadDiffModel)
   Return the value jinf from MadDiffModel.
    source
NLPModels.get_jlow - Function.
   get_jlow(m::MadDiffModel)
   Return the value jlow from MadDiffModel.
    source
```

```
NLPModels.get_jrng - Function.
   get_jrng(m::MadDiffModel)
   Return the value jrng from MadDiffModel.
    source
NLPModels.get_jupp - Function.
   get_jupp(m::MadDiffModel)
   Return the value jupp from MadDiffModel.
    source
NLPModels.get_lcon - Function.
   get_lcon(m::MadDiffModel)
   Return the value Icon from MadDiffModel.
    source
NLPModels.get_lin - Function.
   get_lin(m::MadDiffModel)
   Return the value lin from MadDiffModel.
    source
NLPModels.get_lin_nnzj - Function.
   get_lin_nnzj(m::MadDiffModel)
   Return the value lin_nnzj from MadDiffModel.
    source
NLPModels.get_lvar - Function.
   get_lvar(m::MadDiffModel)
   Return the value Ivar from MadDiffModel.
   source
NLPModels.get minimize - Function.
   | get_minimize(m::MadDiffModel)
   Return the value minimize from MadDiffModel.
   source
NLPModels.get_name - Function.
   get_name(m::MadDiffModel)
```

```
Return the value name from MadDiffModel.
   source
NLPModels.get_ncon - Function.
   get_ncon(m::MadDiffModel)
   Return the value ncon from MadDiffModel.
   source
NLPModels.get_nlin - Function.
   get_nlin(m::MadDiffModel)
   Return the value nlin from MadDiffModel.
   source
NLPModels.get_nln - Function.
   get_nln(m::MadDiffModel)
   Return the value nln from MadDiffModel.
   source
NLPModels.get_nln_nnzj - Function.
   get_nln_nnzj(m::MadDiffModel)
   Return the value nln_nnzj from MadDiffModel.
   source
NLPModels.get nlvb - Function.
   get_nlvb(m::MadDiffModel)
   Return the value nlvb from MadDiffModel.
   source
NLPModels.get_nlvc - Function.
   get_nlvc(m::MadDiffModel)
   Return the value nlvc from MadDiffModel.
    source
NLPModels.get_nlvo - Function.
   get_nlvo(m::MadDiffModel)
   Return the value nlvo from MadDiffModel.
    source
NLPModels.get_nnln - Function.
```

```
get_nnln(m::MadDiffModel)
   Return the value nnln from MadDiffModel.
    source
NLPModels.get_nnzh - Function.
   get_nnzh(m::MadDiffModel)
   Return the value nnzh from MadDiffModel.
   source
NLPModels.get_nnzj - Function.
   get_nnzj(m::MadDiffModel)
   Return the value nnzj from MadDiffModel.
    source
NLPModels.get_nnzo - Function.
   get_nnzo(m::MadDiffModel)
   Return the value nnzo from MadDiffModel.
    source
NLPModels.get_nvar - Function.
   get_nvar(m::MadDiffModel)
   Return the value nvar from MadDiffModel.
   source
NLPModels.get ucon - Function.
   get_ucon(m::MadDiffModel)
   Return the value ucon from MadDiffModel.
   source
NLPModels.get_uvar - Function.
   get_uvar(m::MadDiffModel)
   Return the value uvar from MadDiffModel.
    source
NLPModels.get_x0 - Function.
   get_x0(m::MadDiffModel)
   Return the value x0 from MadDiffModel.
    source
```

```
NLPModels.get_y0 - Function.
   get_y0(m::MadDiffModel)
   Return the value y0 from MadDiffModel.
    source
NLPModels.grad! - Method.
    NLPModels.grad!(m::MadDiffModel,x::AbstractVector,y::AbstractVector)
   Evaluate the gradient of m at x and store the result in the vector y.
    source
NLPModels.hess_coord! - Method.
    NLPModels.hess coord!(m::MadDiffModel,x::AbstractVector,lag::AbstractVector,z::AbstractVector;
    \hookrightarrow obj_weight = 1.0)
   Evaluate the Lagrangian Hessian of m at primal x, dual lag, and objective weight obj_weight and store
   the result in the vector zin sparse coordinate format.
    source
NLPModels.hess_structure! - Method.
   | NLPModels.hess_structure!(m::MadDiffModel,I::AbstractVector{T},J::AbstractVector{T})
   Evaluate the structure of the Lagrangian Hessian and store the result in I and J in sparse coordinate format.
    source
NLPModels.jac coord! - Method.
   | NLPModels.jac_coord!(m::MadDiffModel,x::AbstractVector,J::AbstractVector)
   Evaluate the constraints Jacobian of m at x and store the result in the vector J in sparse coordinate format.
    source
NLPModels.jac structure! - Method.
   NLPModels.jac_structure!(m::MadDiffModel,I::AbstractVector{T},J::AbstractVector{T})
   Evaluate the structure of the constraints Jacobian and store the result in I and J in sparse coordinate
   format.
    source
NLPModels.obj - Method.
   NLPModels.obj(m::MadDiffModel,x::AbstractVector)
   Return the objective value of m at x.
    source
```

#### **MadDiffMOI**

#### 8.1 MadDiffMOI

```
MadDiffM0I.MadDiffM0I - Module.
   |MadDiffM0I
   MadDiffM0I is a submodule of MadDiff. MadDifM0I allows solving nonlinear optimization problems speci-
   fied by MathOptInterface (https://github.com/jump-dev/JuMP.jl/tree/od/moi-nonlinear).
   source
MadDiffCore.Expression - Method.
   Expression(ex::MOI.Nonlinear.Expression; subex = nothing)
   Create a MadDiff.Expression from MOI.Expression.
    source
MadDiffCore.SparseNLPCore - Method.
   | MadDiffCore.SparseNLPCore(nlp_data::MOI.Nonlinear.Model)
   Create MadDiffCore.SparseNLPCore from MOI.Nonlinear.Model.
    source
MadDiffMOI.MadDiffAD - Type.
   | MadDiffAD() <: MOI.Nonlinear.AbstractAutomaticDifferentiation
   A differentiation backend for MathOptInterface based on MadDiff
    source
MadDiffMOI.MadDiffEvaluator - Type.
   | MadDiffEvaluator <: MOI.AbstractNLPEvaluator
   A type for callbacks for MathOptInterface's nonlinear model.
MathOptInterface.NLPBlockData - Method.
```

```
MOI.NLPBlockData(evaluator::MadDiffEvaluator)
   Create MOI.NLPBlockData from MadDiffEvaluator
    source
MathOptInterface.Nonlinear.Evaluator - Method.
   MOI.Nonlinear.Evaluator(model::MOI.Nonlinear.Model, ::MadDiffAD, ::Vector(MOI.VariableIndex))
   Create a MOI.Nonlinear.Evaluator from MOI.Nonlinear.Model using MadDiff's AD capability.
    source
MathOptInterface.eval_constraint - Method.
   | MOI.eval_constraint(evaluator::MadDiffEvaluator, g, x)
    Evaluate the gradient of evaluator at x and store the result in the vector g.
    source
MathOptInterface.eval_constraint_jacobian - Method.
   MOI.eval_constraint_jacobian(evaluator::MadDiffEvaluator, J, x)
   Evaluate the constraints Jacobian of evaluator at x and store the result in the vector J in sparse coordinate
   format.
    source
MathOptInterface.eval_hessian_lagrangian - Method.
   | MOI.eval_hessian_lagrangian(evaluator::MadDiffEvaluator, H, x, σ, μ)
   Evaluate the Lagrangian Hessian of evaluator at primal x, dual \mu, and objective weight \sigma and store the
   result in the vector H in sparse coordinate format.
    source
MathOptInterface.eval objective - Method.
   MOI.eval_objective(evaluator::MadDiffEvaluator, x)
    Return the objective value of evaluator at x.
    source
MathOptInterface.eval_objective_gradient - Method.
   | MOI.eval_objective_gradient(evaluator::MadDiffEvaluator, g, x)
   Evaluate the constraints of evaluator at x and store the result in the vector g.
    source
MathOptInterface.hessian_lagrangian_structure - Method.
   MOI.hessian_lagrangian_structure(evaluator::MadDiffEvaluator)
```

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Return the structure of the Lagrangian Hessian in  $Vector{Tuple{Int,Int}}$  format.

source

 ${\tt MathOptInterface.jacobian\_structure-Method}.$ 

| MOI.jacobian\_structure(evaluator::MadDiffEvaluator)

Return the structure of the constraints Jacobian in  $Vector{Tuple{Int,Int}}$  format.

source