

**PROBLEM 1:** Suppose relation  $R(A, B, C)$  has the tuples:

A	B	C
3	2	1
4	2	3
4	5	6
2	5	3
1	2	6

and relation  $S(A, B, C)$  has the tuples:

A	B	C
2	5	3
2	5	4
4	2	3
3	2	1

Compute  $(R - S) \cup (S - R)$ , often called the “symmetric difference” of  $R$  and  $S$ . List all the tuples in the result relation.

**SOLUTION:** Relation  $(R - S) \cup (S - R)$  has tuples:

A	B	C
4	5	6
1	2	6
2	5	4

**PROBLEM 2:** Suppose relation  $R(A, B)$  has the tuples:

A	B
1	2
3	4
5	6

and relation  $S(B, C, D)$  has the tuples:

B	C	D
2	4	6
8	6	8
7	5	9

Compute  $R \bowtie_{R.A < S.C \wedge R.B < S.D} S$  and list all the result tuples.

**SOLUTION:** Relation  $R \bowtie_{R.A < S.C} S$  has tuples:

R.A	R.B	S.B	S.C	S.D
1	2	2	4	6
1	2	8	6	8
1	2	7	5	9
3	4	2	4	6
3	4	8	6	8
3	4	7	5	9
5	6	8	6	8

Relation  $R \bowtie_{R.B < S.D} S$  has tuples:

R.A	R.B	S.B	S.C	S.D
1	2	2	4	6
1	2	8	6	8
1	2	7	5	9
3	4	2	4	6
3	4	8	6	8
3	4	7	5	9
5	6	8	6	8
5	6	7	5	9

Relation  $R \bowtie_{R.A < S.C \wedge R.B < S.D} S$  has tuples:

R.A	R.B	S.B	S.C	S.D
1	2	2	4	6
1	2	8	6	8
1	2	7	5	9
3	4	2	4	6
3	4	8	6	8
3	4	7	5	9
5	6	8	6	8

**PROBLEM 3:** Assume the following database for this problem. The relations represent information on bank branches:

**Customer**(customer – name, street, city)

**Branch**(branch – name, city)

**Account**(customer – name, branch – name, account – number)

The **Customer** relation has the customer names and their addresses.

Write a relational-algebra expression for each of the following queries:

- Find names of all customers who have an account in 'Region12' branch.
- Find names of all customers who have an account in a branch NOT located in the same city as the one they live in.
- Find the branches that do not have any accounts.
- Find names of customers who do not have any accounts in the 'Region12' branch.
- Find names of customers who have accounts in all the branches located in 'Los Angeles'.
- Find names of customers who have only one account.

**SOLUTIONS:**

- $\pi_{customer - name}(\sigma_{branch - name = 'Region12'}(Account))$
- $\pi_{customer - name}(\sigma_{A.city <> B.city \wedge A.branch - name = B.branch - name}(\rho_B(Branch) \times \rho_A(Customer \bowtie Account)))$
- $\pi_{branch - name}(Branch) - \pi_{branch - name}(Account)$
- $\pi_{customer - name}(Customer) - \pi_{customer - name}(\sigma_{branch - name = 'Region12'}(Account))$
- $\pi_{customer - name}(Customer) - \pi_{customer - name}(\pi_{customer - name}(Customer) \times \pi_{branch - name}(\sigma_{city = 'Los Angeles'}(Branch)) - \pi_{customer - name, branch - name}(Account))$
- $\pi_{customer - name}(Customer) - \pi_{A.customer - name}(\sigma_{(A.branch - name <> B.branch - name \vee A.account - number <> B.account - number) \wedge A.customer - name = B.customer - name}(\rho_A(Account) \times \rho_B(Account)))$

**PROBLEM 4:** The relation **Student**(**sid**, **GPA**) captures the student-GPA information, where **sid** is the id of a student and **GPA** is the student's GPA. Write a relational algebra that finds the ids of the students with the lowest GPA.

**SOLUTION:**

$$\pi_{sid}(Student) - \pi_{A.sid}(\sigma_{A.sid <> B.sid \wedge A.GPA > B.GPA}(\rho_A(Student) \times \rho_B(Student)))$$