# Supervised learning: Regression 1

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#### Introduction

In this practical, you will learn how to perform regression analysis, how to plot with confidence and prediction intervals, how to calculate MSE, perform train-test splits, and write a function for cross validation.

Just like in the practical at the end of chapter 3 of the ISLR book, we will use the Boston dataset, which is in the MASS package that comes with R.

```
library(ISLR)
library(MASS)
library(tidyverse)
```

## Regression in $\ensuremath{\mathbb{R}}$

Regression is performed through the lm() function. It requires two arguments: a formula and data. A formula is a specific type of object that can be constructed like so:

```
some_formula <- outcome ~ predictor_1 + predictor_2</pre>
```

You can read it as "the outcome variable is a function of predictors 1 and 2". As with other objects, you can check its class and even convert it to other classes, such as a character vector:

```
class(some_formula)
## [1] "formula"
```

### as.character(some formula)

You can estimate a linear model using lm() by specifying the outcome variable and the predictors in a formula and by inputting the dataset these variables should be taken from.

1. Create a linear model object called  $lm_ses$  using the formula  $medv \sim lstat$  and the Boston dataset

You have now trained a regression model with medv (housing value) as the outcome/dependent variable and lstat (socio-economic status) as the predictor / independent variable.

Remember that a regression estimates  $\beta_0$  (the intercept) and  $\beta_1$  (the slope) in the following equation:

$$\boldsymbol{y} = \beta_0 + \beta_1 \cdot \boldsymbol{x}_1 + \boldsymbol{\epsilon}$$

- 2. Use the function coef() to extract the intercept and slope from the  $lm_ses$  object. Interpret the slope coefficient.
- 3. Use summary() to get a summary of the  $lm_ses$  object. What do you see? You can use the help file ?summary.lm.

We now have a model object 1m ses that represents the formula

$$\mathsf{medv}_i = 34.55 - 0.95 * \mathsf{lstat}_i + \epsilon_i$$

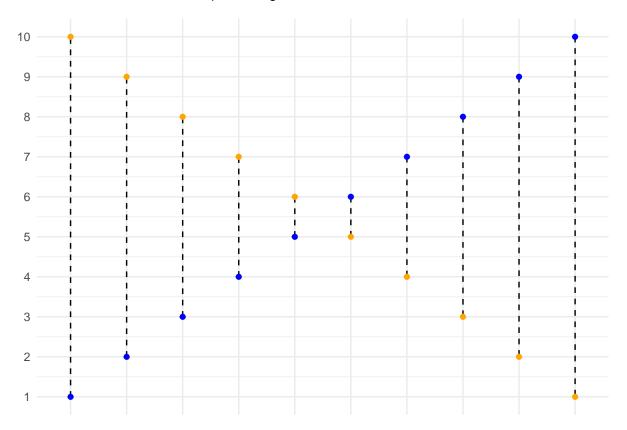
With this object, we can predict a new medv value by inputting its lstat value. The predict() method enables us to do this for the lstat values in the original dataset.

4. Save the predicted y values to a variable called y\_pred

11. The interval argument can be used to generate confidence or prediction intervals. Create a new object called y_pred_95 using predict() (again with the pred_dat data) with the interval argument set to "confidence". What is in this object?
12. Create a data frame with 4 columns: medv, lstat, lower, and upper.
13. Add a geom_ribbon() to the plot with the data frame you just made. The ribbon geom requires three aesthetics: x (lstat, already mapped), ymin (lower), and ymax (upper). Add the ribbon below the geom_line() and the geom_points() of before to make sure those remain visible. Give it a nice colour and clean up the plot, too!
14. Explain in your own words what the ribbon represents.
15. Do the same thing, but now with the prediction interval instead of the confidence interval.
Mean square error
16. Write a function called mse() that takes in two vectors: true y values and predicted y values, and which outputs the mean square error.
Start like so:
<pre>mse &lt;- function(y_true, y_pred) {     # your function here }</pre>
Wikipedia may help for the formula.
17. Make sure your mse() function works correctly by running the following code.

## [1] 33

You have now calculated the mean squared length of the dashed lines below.



18. Calculate the mean square error of the  $lm_ses$  model. Use the medv column as  $y_true$  and use the predict() method to generate  $y_pred$ .

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Prop

You have calculated the mean squared length of the dashed lines in the plot below

## Train-validation-test split

Now we will use the sample() function to randomly select observations from the Boston dataset to go into a training, test, and validation set. The training set will be used to fit our model, the validation set will be used to calculate the out-of sample prediction error during model building, and the test set will be used to estimate the true out-of-sample MSE.

- 19. The Boston dataset has 506 observations. Use c() and rep() to create a vector with 253 times the word "train", 152 times the word "validation", and 101 times the word "test". Call this vector splits.
- 20. Use the function sample() to randomly order this vector and add it to the Boston dataset using mutate(). Assign the newly created dataset to a variable called boston\_master.

21.		() to create a training, validation, and test set fro stasets boston_train, boston_valid, and bost	<del>-</del>
We w	ill set aside the bost	on_test dataset for now.	
22.		ession model called $model_1$ using the training due in the first $lm()$ exercise. Use $summary()$ to ch	
23.	Calculate the MSE	with this object. Save this value as model_1_mse	_train.
24.		MSE on the validation set and assign it to variable lata argument in predict().	emodel_1_mse_valid.
This is	s the estimated out-o	f-sample mean squared error.	
25.	Create a second n train and validatio	nodel model_2 which includes age and tax as pn MSE.	redictors. Calculate the
26.	Compare model 1 choose and why?	and model 2 in terms of their training and validation	n MSE. Which would you
27.	Calculate the test number tell you?	MSE for the model of your choice in the previous q	uestion. What does this

### Programming exercise: cross-validation

This is an advanced exercise. Some components we have seen before in this and previous practicals, but some things will be completely new. Try to complete it by yourself, but don't worry if you get stuck. If you don't know about for loops in R, read up on those before you start the exercise.

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- · R help files
- Internet search & stack exchange
- · Your peers
- · The answer, which shows one solution

You may also just read the	answer an	id try to und	erstand wha	t happens	in each	step

