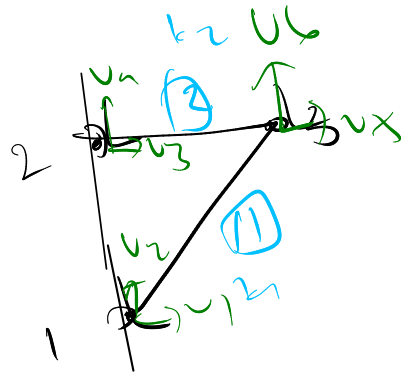


Finite Element



$$F = K d \Rightarrow [K] \{u\} = \{F\}$$

$$[K] \{u\} = \{F\}$$

matrix
stiffness
global

$$[6 \times 6]$$

$$2 \times 2$$

nodal
displacement

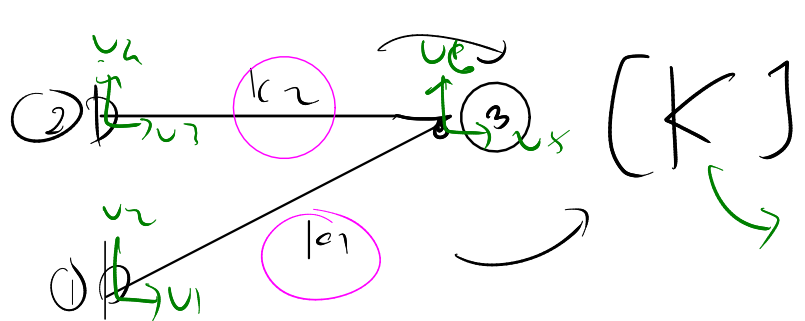
$$\begin{Bmatrix} u_1 \\ v_1 \end{Bmatrix}$$

$$(2, 1)$$

vector
global

$$\begin{Bmatrix} f_1 \\ f_2 \\ f_3 \end{Bmatrix}$$

$$(2, 1)$$



$$[K]$$

$$= \begin{bmatrix} u_1 & u_2 & u_3 & u_4 & u_5 & u_6 \\ k_1 \checkmark & \checkmark & & & \checkmark & \checkmark \\ \checkmark & \checkmark & & & \checkmark & \checkmark \\ & & \checkmark & \checkmark & \checkmark & \checkmark \\ & & \checkmark & \checkmark & \checkmark & \checkmark \\ \checkmark & \checkmark & \checkmark & \checkmark & \checkmark & \checkmark \\ \checkmark & \checkmark & \checkmark & \checkmark & \checkmark & \checkmark \end{bmatrix}$$

$$u = k_1$$

$$\checkmark = k^{(2)}$$

$$K^{(1)} = \begin{bmatrix} & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \end{bmatrix}$$

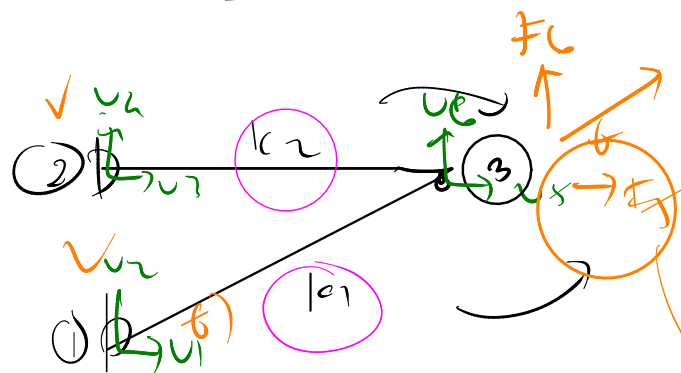
$$K^{(2)} = \begin{bmatrix} u_3 & u_4 & u_5 & u_6 \\ & & & \\ & & & \\ & & & \\ & & & \end{bmatrix}$$

$$[K] = \begin{bmatrix} k_1/2 & k_1/2 & 0 & 0 & -k_1/2 & -k_1/2 \\ k_1/2 & k_1/2 & 0 & 0 & -k_1/2 & -k_1/2 \\ 0 & 0 & k_2 & 0 & -k_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ -k_1/2 & -k_1/2 & -k_2 & 0 & k_1/2 + k_2 & k_1/2 \\ -k_1/2 & -k_1/2 & 0 & 0 & k_1/2 & k_1/2 \end{bmatrix}$$

$$[K] = \{u\} = \{F\}$$

Finite Element

E_{dst}
 \downarrow
 $k \rightarrow K, f$



bc

Solve

$$[K] \{u\} = \{F\}$$

element displacement \rightarrow Stress / Strain

$$U = \begin{Bmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \\ u_x \\ u_b \end{Bmatrix}$$

$$\begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ u_x \\ u_b \end{Bmatrix}$$

$$\begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ F_x \\ F_b \end{Bmatrix}$$

$$\begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ F_x \\ 0 \end{Bmatrix}$$

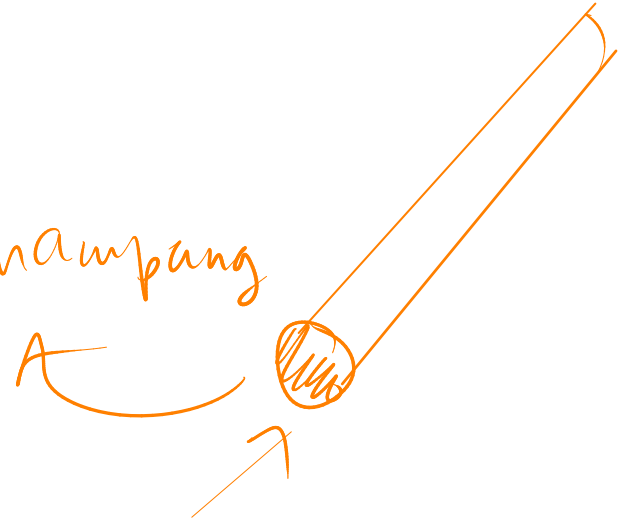
$$\begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ F_b \end{Bmatrix}$$

$$\begin{Bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ F_{cos\theta} \\ F_{sin\theta} \end{Bmatrix}$$

Stress $\Rightarrow \sigma = E \cdot \epsilon$

σ → Stress
 E → Modulus Young / Elasticity
 ϵ → Strain

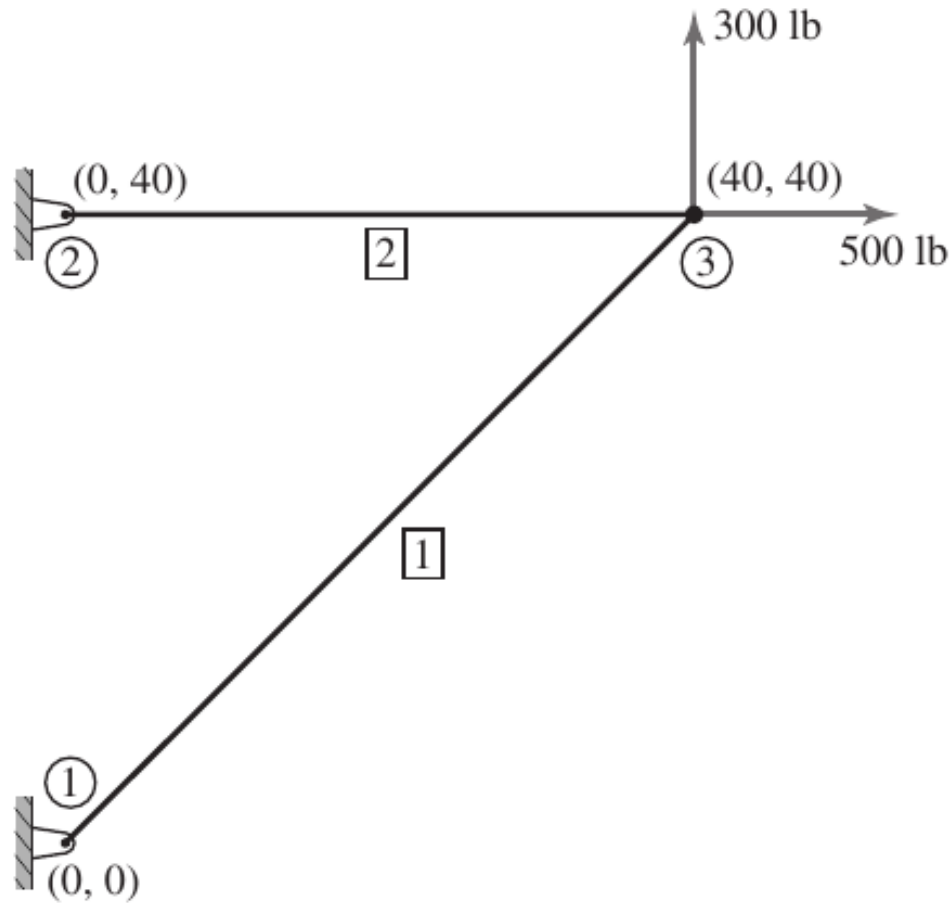
F → Gaya (Normal)
 A → luas penampang



Problem:

$$E_1 = E_2 =$$

$10 \times 10^6 \text{ lb/in}^2$ and cross-sectional areas $A_1 = A_2 = 1.5 \text{ in}^2$



Find:

determine the displacement components of node 3, the reaction force components at nodes 1 and 2, and the element displacements, stresses, and forces

a) u_3 & v_3

b) r_1, r_2, r_3, r_4

c) e_1, e_2

d) σ $\sigma = \frac{F}{A}$

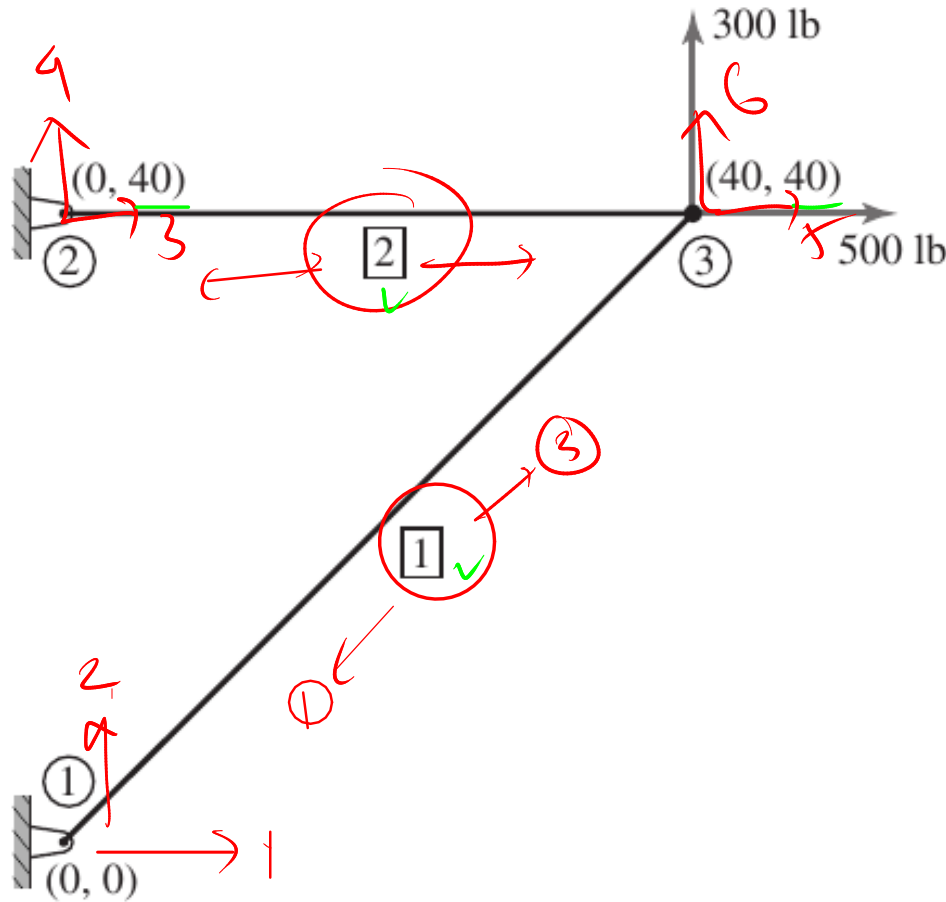
e) f

Solusi komputer FEM

1) Edoof

2) Ditinjau
kapan
tiap n

$e_{x1} = [0, 40]$
 $e_{y1} = [0, 40]$
 $e_{x2} = [0, 40]$
 $e_{y2} = [40, 40]$



② coordinate

↓
③ K, f

$k^{(1)} 4 \times 4$
 $k^{(2)} 4 \times 4$

$K 6 \times 6$

↓ gens

$$\begin{bmatrix} 6 & 6 & 0 & 0 & 0 & 0 \\ 0 & 6 & 0 & 0 & 0 & 0 \\ 0 & 0 & 6 & 0 & 0 & 0 \\ 0 & 0 & 0 & 6 & 0 & 0 \\ 0 & 0 & 0 & 0 & 6 & 0 \\ 0 & 0 & 0 & 0 & 0 & 6 \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} F_1 \\ F_2 \\ F_3 \\ F_4 \\ F_5 \\ F_6 \end{bmatrix}$$

$$\boxed{\sigma = \frac{F}{A}} \quad \varepsilon, \quad \varepsilon = \frac{\sigma}{E}$$

