

1- Please calculate time complexities of the following code snippets using **Sigma  $\Sigma$  (Mathematical)** notations and present the final complexity using bigO notation.

**Note:** You can omit/disregard time complexities that would come from **for** loops. Please only calculate time complexities based on the code lines with **print** command. Final bigO complexity will not change.

**Example:**

```
for (int i = 1; i <= n; i++) {
    print("hi");    //    1
    print("bye");   //    1
}
```

$$\sum_{i=1}^n 2 = 2n$$

a: 

```
for (int i = 1; i <= 5; i++)
    for (int j = 0; j < 2*n; j++)
        print("hi");
```

b: 

```
for (int i = 1; i <= n; i++)
    for (int j = 0; j < n; j++)
        print("hi");
```

c: 

```
for (int i = 1; i <= n; i++) {
    print("1.loop");
    for (int j = i; j <= n; j++)
        print("2.loop");
}
```

d: 

```
for (int i = 1; i <= n; i++) {
    print("1.loop");
    for (int j = 1; j <= i; j++)
        print("2.loop");
}
```

e: 

```
for (int j = 1; j <= n; j*=2)
    print("hi");
```

f: 

```
for (int j = 2; j <= n; j=j^2)
    print("hi");
```

g: 

```
for (int i = 1; i <= n; i += 2)
    for (int j = 1; j <= n; j += 2)
        for (int k = 1; k <= n; k *= 2)
            print("hi");
```

h: 

```
for (int i = 1; i <= n; i += 2)
    for (int j = 1; j <= n; j += 2)
        for (int k = j; k <= n; k++)
            print("hi");
```

i: 

```
for (int i = 1; i <= n; i++)
    for (int j = 1; j <= n; j *= 2)
        for (int k = 1; k <= j; k++)
            print("hi");
```

j: 

```
for (int i = 1; i <= n; i += 2) {
    for (int j = 1; j <= i; j++) {
        for (int k = 1; k <= n; k += 5)
            print("hi");
        for (int k = 1; k <= n; k *= 2)
            print("hi");
    }
}
```

- 2- Please write a **linear** function (in a regular language or pseudocode) that calculates **factorial** ! of a given number, calculate the time complexity of the function and present the final complexity using bigO notation.
- 3- Please write a **recursive** function (in a regular language or pseudocode) that calculates **factorial** ! of a given number, calculate the time complexity of the function and present the final complexity using bigO notation.
- 4- Please write a **linear** function (in a regular language or pseudocode) that calculates **fibonacci** value of a given index number, calculate the time complexity of the function and present the final complexity using bigO notation.
- 5- Please write a **recursive** function (in a regular language or pseudocode) that calculates **fibonacci** value of a given index number, calculate the time complexity of the function and present the final complexity using bigO notation.