

## 2) Deformation Retraction from $\mathbb{R}^n$ to $S^{n-1}$

$\Rightarrow$  Essentially, it is just a normalization. We take  $x \in \mathbb{R}^n$ ,  $\frac{x}{\|x\|} \in S^{n-1}$ . But

we also need a parameter  $t$ .  $\frac{x}{\|x\|}$  won't work as  $t=0$  will be undefined. Hence

$\frac{x}{\|x\| \cdot t + (1-t)}$  is well defined.  $f_0 = x$

$f_t = \frac{x}{\|x\| \cdot t + (1-t)}$  is continuous, as  $f_{it} = \frac{x_i}{\|x\| \cdot t + (1-t)}$

all of its components are continuous