

LECTURE 3

Suppose that (i) f_σ is injective $\forall \sigma \in \Delta$
(ii) $\text{im } f_\sigma \cap \text{im } f_\tau = \text{im } f_{\sigma \cap \tau}$
where im denotes image. Then \star for $\sigma, \tau \in \Delta$
 $|\Delta| = \bigcup_{\sigma \in \Delta} \text{im } (f_\sigma)$

2015

along with
20

000345 • WEEK 01

TUE JAN

$\tau := \{A \cap K\} : A \text{ is an open set in } \mathbb{R}^d \text{ under standard topology } \tau \text{ is the generated topology}$

1	8	15	22	29	M	D
2	9	16	23	30	T	E
3	10	17	24	31	W	C
4	11	18	25		T	2
5	12	19	26		F	0
6	13	20	27		S	1
7	14	21	28		S	4

evaluation of Δ

Example, (1) $\Delta = \{1, 2, 12\}$, Then $V = \{1, 2\}$

Let $f: V \rightarrow \mathbb{R}$ given by $f(1) = 5$ &

$$f(2) = 10$$

$$f_1: X^0 \rightarrow \mathbb{R} = 1 \times f(1) = 5$$

$$\text{Similarly } f_2: X^0 \rightarrow \mathbb{R} = 1 \times f(2) = 10$$

Finally: $f_{12}: X^1 \rightarrow \mathbb{R}$ &

$$f_{12} = \lambda_0 f(1) + \lambda_1 f(2) = x \cdot 5 + 10$$

Verify \odot f_1, f_2, f_{12} . f_1 & f_2 are linearly
independent

take $x, x' \in X$

$$f(x) = f(x')$$

$$\lambda_0 f(1) + \lambda_1 f(2) = \lambda'_0 f(1) + \lambda'_1 f(2)$$

Now, $f(1)$ & $f(2)$ are scalar,

$$(\lambda_0 - \lambda'_0) f(1) = (\lambda'_1 - \lambda_1) f(2)$$

$$\text{im}(f_1) \cap \text{im}(f_2) = \emptyset$$

$$\text{im}(f_1 \cap f_2) = \text{im}(f_1) \cap \text{im}(f_2) = \emptyset$$

$$\text{im}(f_1 \cap f_2) = \emptyset$$

$$\text{Now, } \text{im}(f_1) \cap \text{im}(f_1|_{B_1}) = \{5\}$$

$$\text{Also, } \text{im}(f_1|_{B_1}) = \text{im}(f_1) = \{5\}$$

$$\text{Similarly, } \text{im}(f_2) \cap \text{im}(f_2|_{B_2}) = \text{im}(f_2|_{B_2})$$

Some Notions Of ABSTRACT ALGEBRA