Model-Based RL

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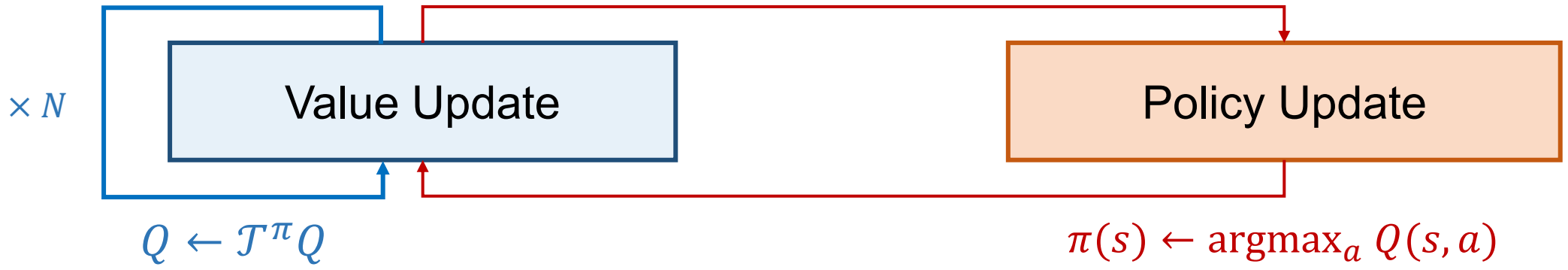
Recap: Model-Free RL



$Q \leftarrow \mathcal{T}^{\pi} Q$ means $Q(s,a) \leftarrow R(s,a) + \gamma \sum_{s',a'} P(s'|s,a)\,\pi(a'|s')Q(s',a')$ for all s, a

Recap: Generalized Policy Iteration with Samples

For $k = 1,\ 2, \ldots$

For $i = 1, 2, \ldots, N$:

Choose action a_i with the current policy

Receive reward $r_i \sim R(s_i, a_i)$ and $s_i' \sim P(\cdot\,|s_i, a_i)$

$s_{i+1} = s_i'$ if episode continues, $s_{i+1} \sim \rho$ if episode ends

Push (s_i, a_i, r_i, s_i') to $\mathcal{B}$

Data collection

Draw (s, a, r, s') from $\mathcal{B}$, and use them to update policy/value

Empty $\mathcal{B}$ if under on-policy training

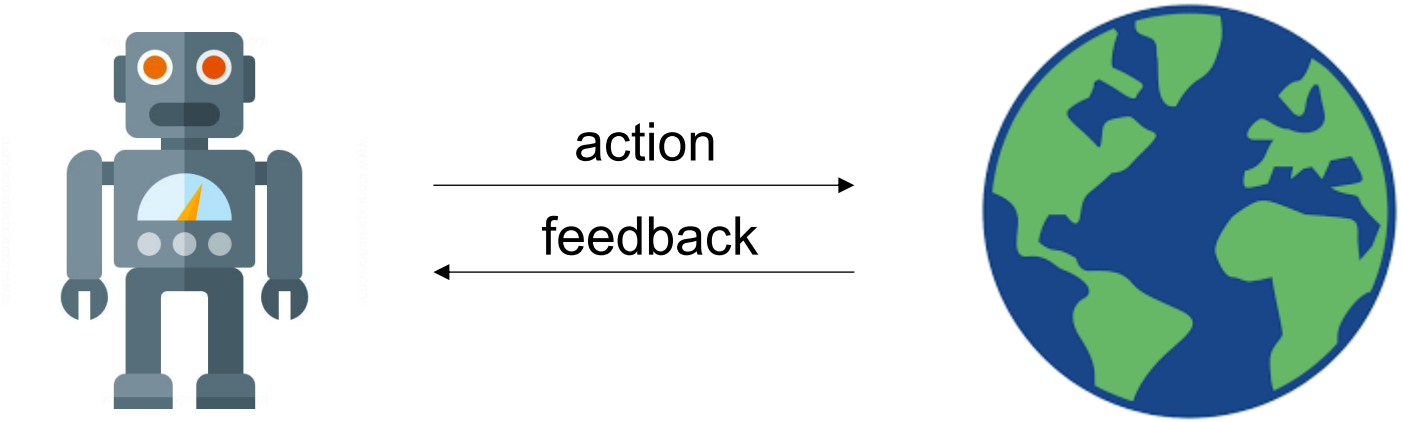
Policy / value update

When Is Model-Based Method Helpful?

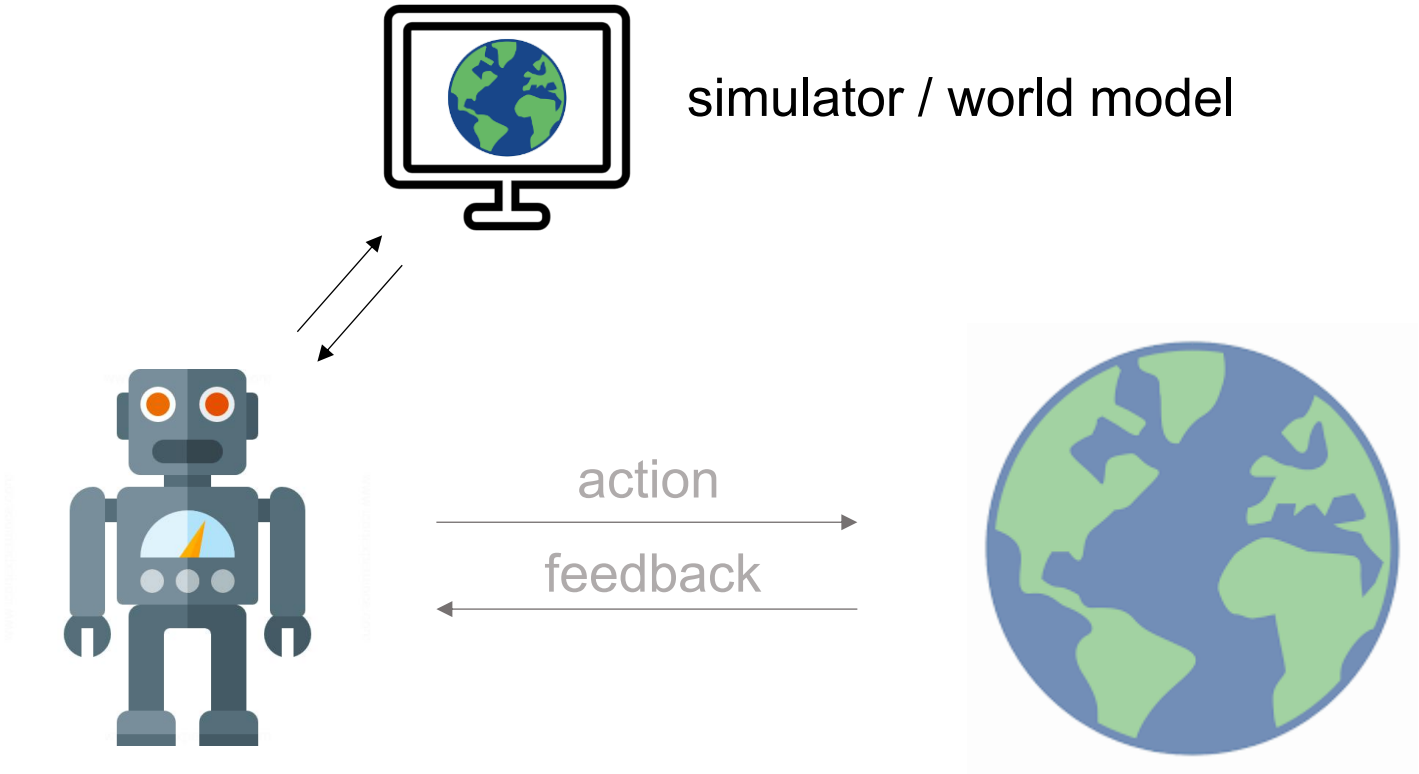
- Model (transition) is easy to learn
  - Deterministic transition could be easier to learn to stochastic one
  - System identification: known parameterized model with unknown parameters

- Model is known
  - The space/action space is too large for full policy/value iteration (Go, Chess)

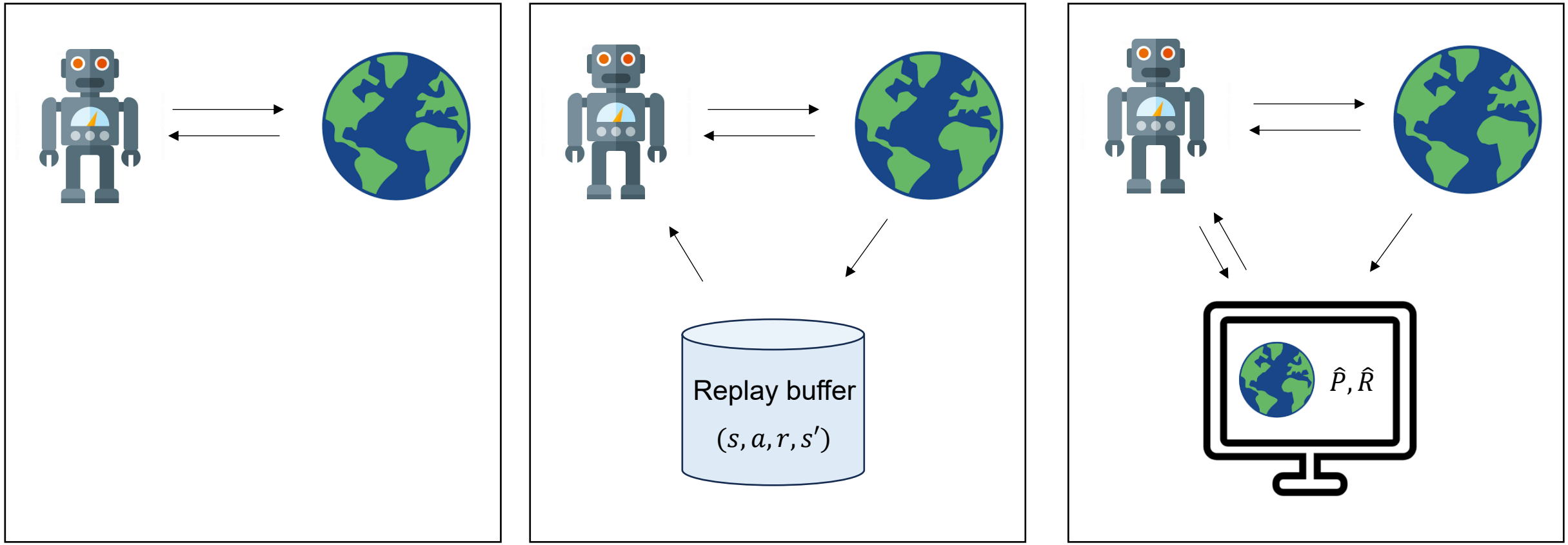
Model-Based RL



Model-Based RL



Comparison between training methods



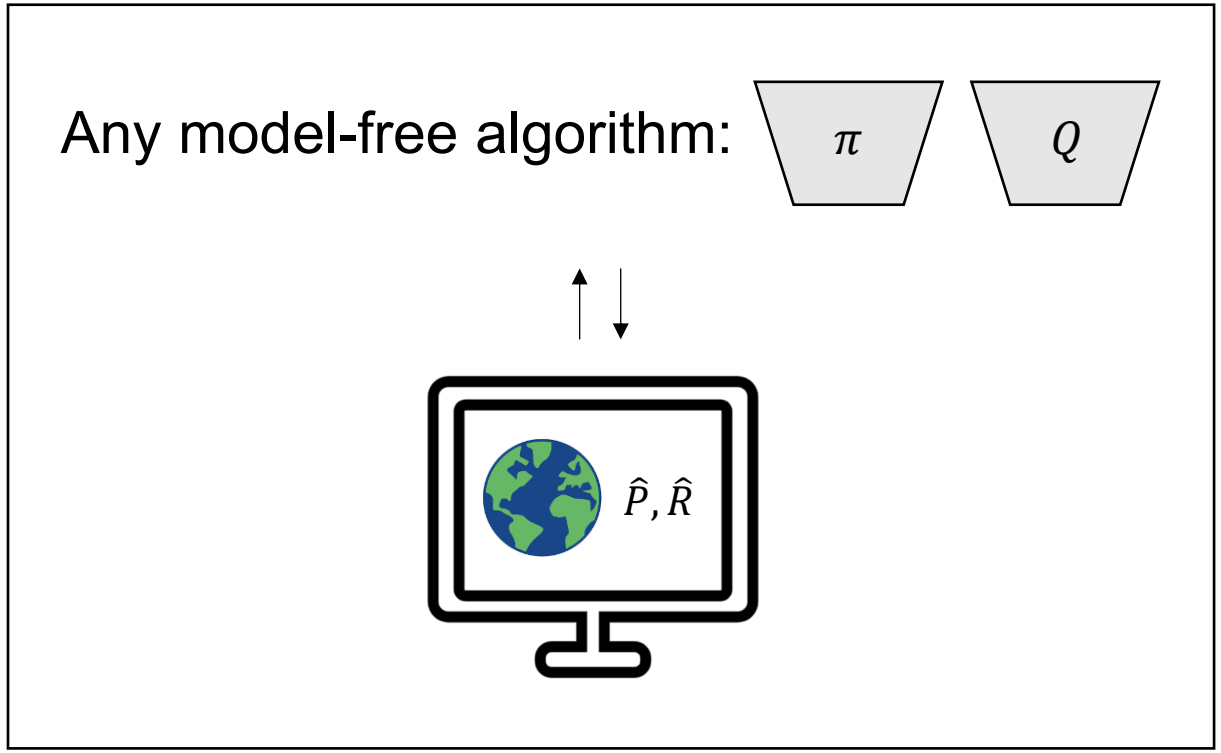
Model-free On-policy

Model-free Off-policy

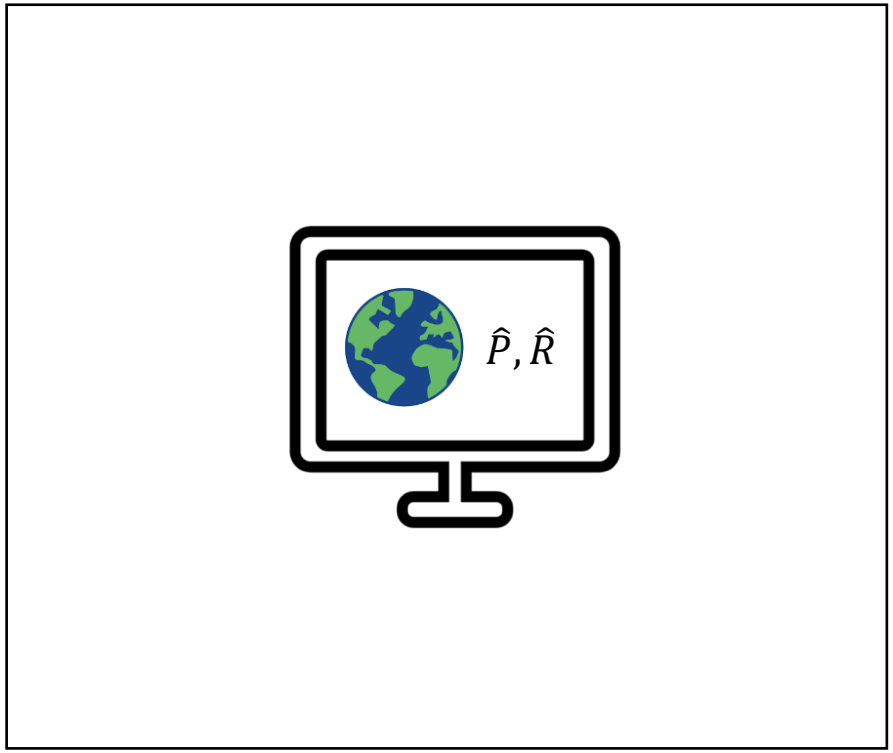
Model-based

Model-Based RL

Two ways to use the simulator / world model / model:



Model-assisted model-free learning



Planning with a model

1. Model-Assisted Model-Free Learning (Dyna-style)

For $k = 1,\ 2, \ldots$

For $i = 1, 2, \ldots, N$:

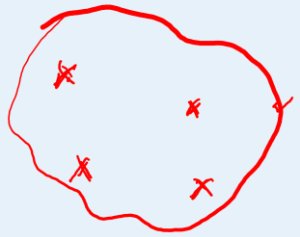
Choose action a_i with the current policy π_k

Receive reward $r_i \sim R(s_i, a_i)$ and $s_i' \sim P(\cdot\,|s_i, a_i)$

$s_{i+1} = s_i'$ if episode continues, $s_{i+1} \sim \rho$ if episode ends

Push (s_i, a_i, r_i, s_i') to $\mathcal{B}$

Data collection



Update model $\hat{P}, \hat{R}$ with data in $\mathcal{B}$

Model update

Repeat several times:

Sample $(s, a) \sim \mathcal{B}$, or sample $s \sim \mathcal{B}$ and $a \sim \pi_k(\cdot\,|s)$ or uniform

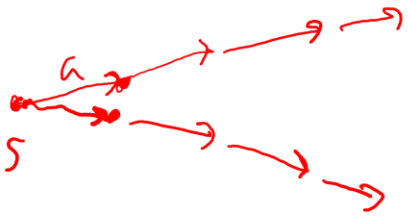
Let $r \sim \hat{R}(s, a)$ and $s' \sim \hat{P}(\cdot\,|s, a)$

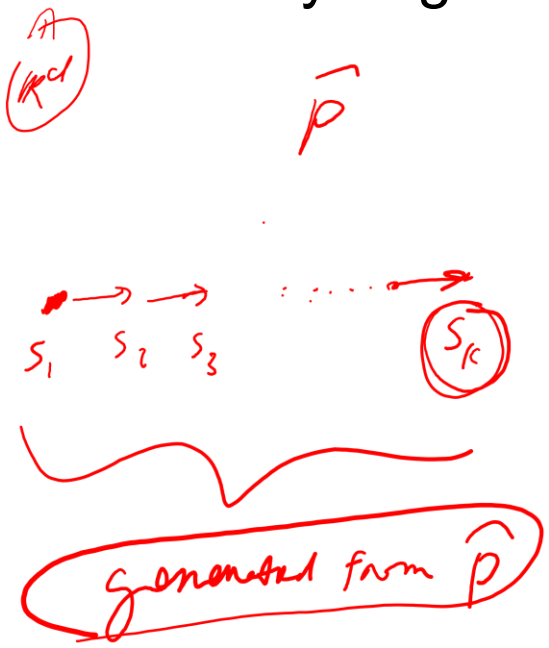
Update policy / value with sample (s, a, r, s')

Policy / value update

1. Model-Assisted Model-Free Learning (Dyna-style)

Why still sample s from the buffer? Why not generate s randomly or generate it from the trained model?





1. Model-Assisted Model-Free Learning (Dyna-style)

Some Dyna-style algorithms:

Gu et al., Continuous deep Q-Learning with model-based acceleration, 2016. (MBA)
Feinberg et al., Model-based value expansion, 2018. (MVE)
Janner et al., When to trust your model: model-based policy optimization. 2019. (MBPO)

The performance of MB-RL is heavily influenced by how to represent and train $\hat{P}$ efficiently, while making it predictive and scalable:

Hafner et al., Mastering Diverse Domains through World Models. 2023. (DreamerV3)

2. Planning with A Model

If we have a model / simulator, how to decide the next action without having a trained policy / value network?

Exact / closed-form solution: finite-state-finite-action, linear system

$$s_{t+1} = A s_t + B a_t + w_t$$

$a_t \in \mathbb{R}^k$, noise

$s_t \in \mathbb{R}^d$

$$\text{loss} = s_t^T Q s_t + a_t^T R a_t$$

2. Planning with A Model

If we have a model / simulator, how to decide the next action without having a trained policy / value network?

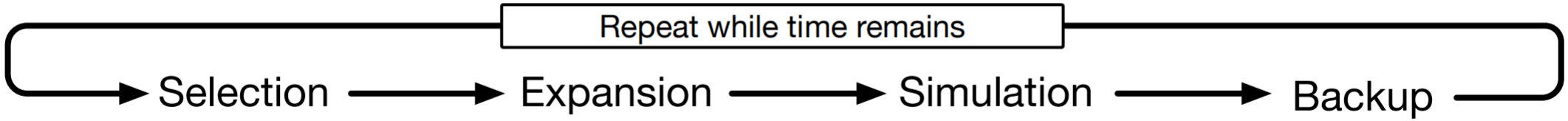
Search (for large state space without structure):

"Create the policy on the fly": decide $\pi(\cdot|s)$ only when reaching s

This is most often used when there is a **default** policy, but we aim to enhance it on the fly.

$\pi : S \times A$

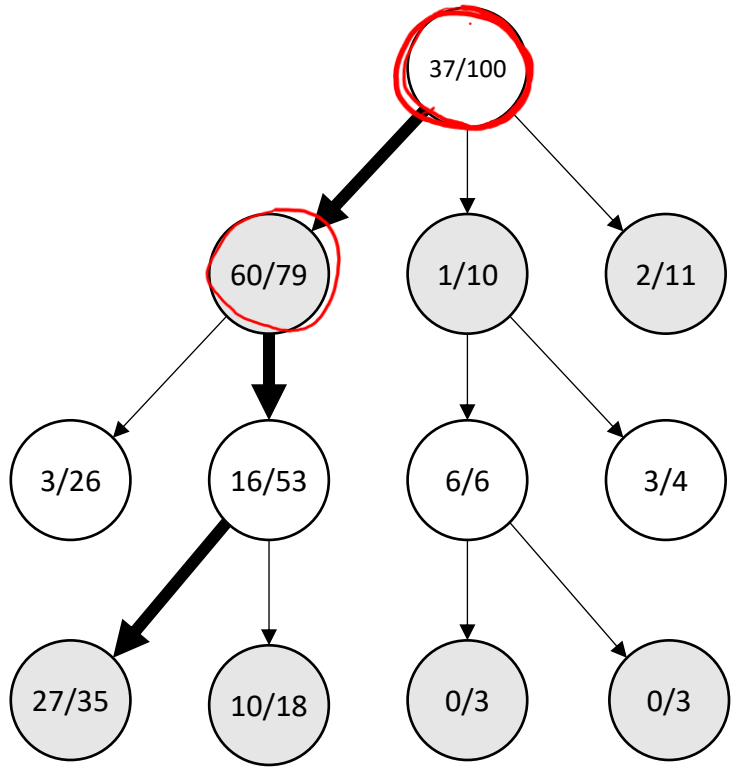
Monte-Carlo Tree Search (MCTS)



Monte-Carlo Tree Search (MCTS)

Selection

- Starting from the root node, execute **tree policy** until reaching a leaf node
- One effective tree policy is given by UCB1, which chooses an action based on



$$\frac{W(n)}{N(n)} + C \times \sqrt{\frac{\log N(\text{parent}(n))}{N(n)}}$$

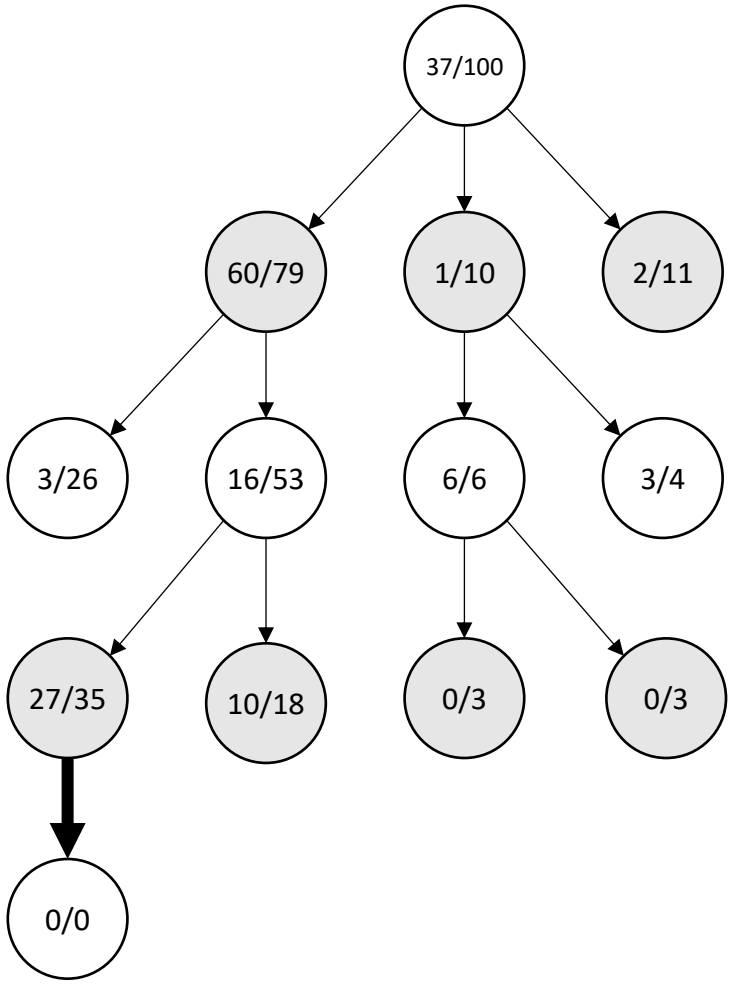
$W(n)$: total #wins of all playouts that went through node n

$N(n)$: total #playouts that went through node n

Monte-Carlo Tree Search (MCTS)

Expand

- On some iterations, grow the search tree from selected leaf nodes by adding one or more child nodes

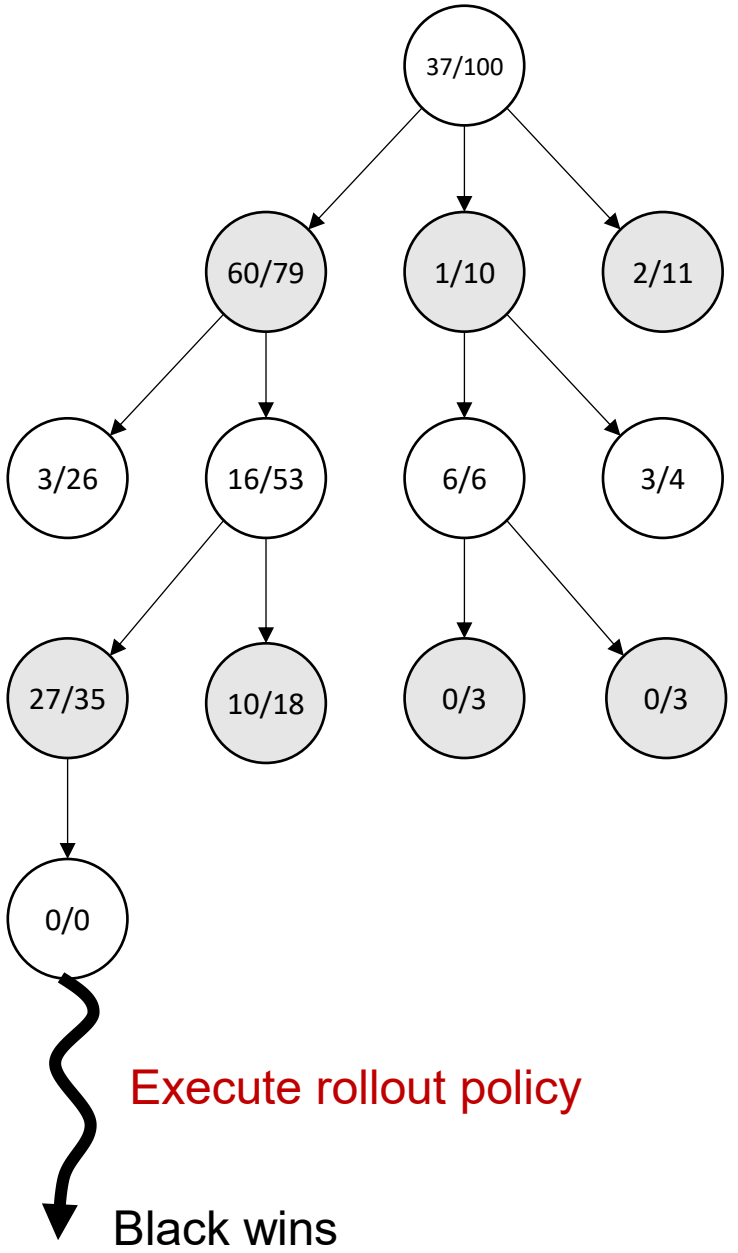


Monte-Carlo Tree Search (MCTS)

Simulation

- From the selected or expanded node (if any), execute the **rollout policy** to the end of the game

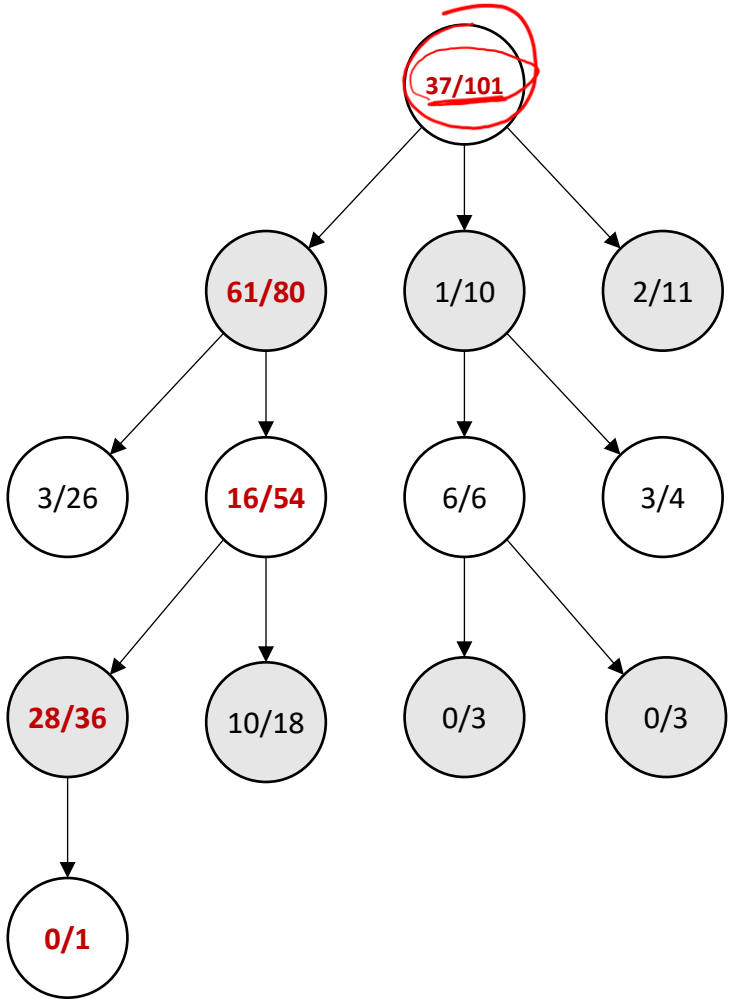
- Rollout policy
  - Could be heuristics, such as “consider capture moves” in chess
  - Could be learned through neural networks by self-play



Monte-Carlo Tree Search (MCTS)

Backup

- Update the #wins and #playouts on nodes along the tree policy



Monte-Carlo Tree Search (MCTS)

Finally,

- Choose the action from the root node that has the largest visit count.
- After the opponent’s move, start the same procedure from the new state (can keep the statistics from the previous state)

2. Planning with A Model

If we have a model / simulator, how to decide the next action without having a trained policy / value network?

Search (for large state space without structure):

"Create the policy on the fly": decide $\pi(\cdot\,|s)$ only when reaching s

This is often used when there is a **default** policy, but we aim to enhance it on the fly.

Plan for multiple steps, but execute only the first step.