

# Homework 4

6501 Reinforcement Learning (Spring 2025)

Submission deadline: 11:59pm, May 8 (**NO LATE SUBMISSION**)

This is the last assignment, but it accounts for 2/5 of the total homework score for the semester. Please start early—this assignment is not only longer but also more challenging than the previous ones. The latex template can be found [here](#).

The task is straightforward: implement DQN and PPO to solve the classic CartPole environment. Download the starter code [here](#). The code structure is similar to HW2, where both value-based and policy-based algorithms share a Python class due to the structural similarity between a  $Q$ -network and a policy network. This allows you to reuse some of your HW2 code. Of course, you're welcome to modify the code structure if you find a better design.

You can definitely find many good implementations of DQN and PPO online, but we encourage you to first complete your own implementation (you can seek help from LLMs). Afterwards, you're encouraged to compare your work with open-source implementations—for example, [stable-baseline3](#). These reference codes often include useful tricks and engineering details that are not often discussed explicitly in textbooks or lectures.

## 1 Environment

We focus on the CartPole environment, which is a game provided by the OpenAI Gym library. A brief introduction is given below, and more information about the environment can be found in [https://www.gymnasium.dev/environments/classic\\_control/cart\\_pole/](https://www.gymnasium.dev/environments/classic_control/cart_pole/).

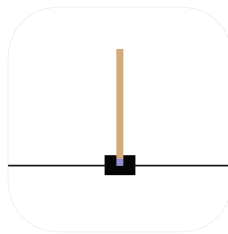


Figure 1: Cart Pole

To get familiar with the environment, you can run the function `generate_videos()` provided in the starter code, which generates a video of the game being played by a random policy. You may adapt this code to generate videos of your trained policy instead.

## 2 Starter Code

The default command-line usage in the starter code is:

```
HW4.py --seed [seed] --algorithm [algorithm] --figure [figure]
```

where `[seed]` specifies the random seed used to control both the algorithm’s and the environment’s randomness. This allows you to debug and compare different algorithms under the same initial conditions. `[algorithm]` indicates the algorithm to use—one of DQN, DDQN, PPO, or RAND. `[figure]` is the filename for saving the output plot (e.g., `output.png`). The starter code automatically saves the figure every 100 episodes.

You will be asked to include this output figure in your homework submission for several questions below.

We have already implemented a random policy that selects actions uniformly at random. To get started, try running:

```
HW4.py --seed 0 --algorithm RAND --figure output_RAND.png
```

## 3 Deep Q-learning

### 3.1 DQN

We will begin by using the standard DQN algorithm to play CartPole. The algorithm is shown in [Algorithm 1](#).

It is common to set  $N = M = 1$  in [Algorithm 1](#), since DQN reuses past data via experience replay and does not need to wait until a large batch of new data is collected before performing an update. The parameters  $N$  and  $M$  are explicitly included to make the structure more comparable to that of PPO.

In the starter code, the exploration rate  $\epsilon$  is time-varying and gradually decays to zero. Its scheduling is controlled by the parameters `EPS_START`, `EPS_END`, and `EPS_DECAY` in the starter code. Recommended hyperparameter values are provided in the starter code.

To reduce your workload, we have implemented the  $\epsilon$ -greedy action selection rule and the replay buffer.

- (a) (10%) Implement [Algorithm 1](#) to play CartPole. Paste the output plot here, which should show both the return per episode and its running average over a window of 100 episodes.

Your score for this part will be computed as:

$$\min \left\{ \frac{\text{maximum running average within 2000 episodes}}{475}, 1 \right\} \times 100\%. \quad (1)$$

That is, if within the first 2000 episodes there exists a window of 100 episodes where the running average return exceeds 475, you will receive full credit. If you do not reach this threshold within 2000 episodes, you may also increase the total number of episodes in your plot, but your score will be scaled by a factor of  $\frac{2000}{\text{total number of episodes used}}$ .

There is no need to average results over multiple random seeds—just choose a seed that yields good performance.

You may try some of the tips listed below, as some people have found them helpful. Note that applying these techniques will cause your implementation to deviate from the original algorithm outlined in [Algorithm 1](#).

- Gradient clipping: Clip the gradient if its magnitude exceeds a threshold (e.g., 0.5).
- Using Huber loss: Replace the squared loss in [Eq. \(2\)](#) with Huber loss (see [this blog](#) for a brief explanation).

- (b) (5%) List the hyperparameters you use in (a):

Hyperparameter	Value
MINIBATCH_SIZE ( $B$ in <a href="#">Algorithm 1</a> )	
LR ( $\alpha$ in <a href="#">Algorithm 1</a> )	
EPS_START	
EPS_END	
EPS_DECAY	
TAU ( $\tau$ in <a href="#">Algorithm 1</a> )	

If you use any trick beyond what is described in [Algorithm 1](#), please briefly describe it here. Also, list any additional hyperparameters you introduced in the table above.

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**Algorithm 1** DQN (with  $\epsilon$ -greedy exploration)

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1 **Parameters:**  $N, M, B, \alpha$  (learning rate),  $\tau$  (target network update rate),  $\epsilon$  (exploration probability).

2 Initialize the replay buffer  $D = \{\}$ .

3 Initialize the online network  $Q_\theta$  with weights  $\theta$

4 Initialize the target network  $Q_{\bar{\theta}}$  with weights  $\bar{\theta} = \theta$

5 Sample  $s_{\text{tmp}} \sim \rho$ , where  $\rho$  is the initial state distribution.

6 **for**  $k = 1, \dots$  **do**

7      $s_1 \leftarrow s_{\text{tmp}}$

8     **for**  $i = 1, 2, \dots, N$  **do**

9         Select action  $a_i = \begin{cases} \operatorname{argmax}_a Q_\theta(s_i, a) & \text{with probability } 1 - \epsilon \\ \text{random action} & \text{with probability } \epsilon \end{cases}$

10         Observe reward  $r_i$  and the next state  $s'_i$ .

11          $D \leftarrow D \cup \{(s_i, a_i, r_i, s'_i)\}$ .

12         If  $s'_i$  is a terminal state, sample  $s_{i+1} \sim \rho$ ; otherwise, set  $s_{i+1} = s'_i$ .

13      $s_{\text{tmp}} \leftarrow s_{N+1}$

14     **for**  $j = 1, \dots, M$  **do**

15         Randomly sample a minibatch  $\mathcal{B} \subset \mathcal{D}$  with size  $|\mathcal{B}| = B$ .

16         Update the online network:

$$\theta \leftarrow \theta - \alpha \nabla_\theta \frac{1}{B} \sum_{(s, a, r, s') \in \mathcal{B}} \left( Q_\theta(s, a) - r - \gamma \max_{a'} Q_{\bar{\theta}}(s', a') \right)^2 \quad (2)$$

17         where  $\max_{a'} Q_{\bar{\theta}}(s', a') \triangleq 0$  if  $s'$  is a terminal state.

18         Update the target network:

$$\bar{\theta} \leftarrow \tau \theta + (1 - \tau) \bar{\theta}.$$

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### 3.2 Double DQN

Now change [Eq. \(2\)](#) in [Algorithm 1](#) to the following:

$$\theta \leftarrow \theta - \alpha \nabla_\theta \frac{1}{B} \sum_{i=1}^B \left( Q_\theta(s_i, a_i) - r_i - \gamma Q_{\bar{\theta}}(s'_i, a'_i) \right)^2 \quad \text{with } a'_i \triangleq \operatorname{argmax}_a Q_\theta(s'_i, a),$$

which yields Double DQN.

(c) (5%) Implement Double DQN to play Cart Pole. Use the same random seed and the same choices of parameters as in (a). Paste the output plot here. The score for this part will be calculated using the same formula as in [Eq. \(1\)](#).

## 4 Proximal Policy Optimization

Next, we will use PPO to play CartPole. The standard PPO algorithm is shown in [Algorithm 2](#).

(d) (15%) Implement PPO to play Cart Pole, and paste the output plot here. Your score for this part will be computed as:

$$\min \left\{ \frac{\text{maximum running average within 6000 episodes}}{475}, 1 \right\} \times 100\%.$$

Note that the allowed number of episodes to reach the desired performance is increased to 6000. As in part (a), you may go beyond 6000 episodes, but your score will be scaled by  $\frac{6000}{\text{number of episodes you use}}$ . Recommended choices of the hyperparameters are provided in the starter code.

As in DQN, there are some practical tips that go beyond [Algorithm 2](#), which many people find helpful:

- **Normalizing the advantage:** Instead of directly using the advantage estimates  $\hat{A}(s_i, a_i)$  returned by GAE, normalize them as follows:

$$A'(s_i, a_i) = \frac{\hat{A}(s_i, a_i) - \mu}{\sigma + 10^{-8}}$$

where  $\mu = \frac{1}{N} \sum_{i=1}^N \hat{A}(s_i, a_i)$  and  $\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (\hat{A}(s_i, a_i) - \mu)^2}$ . The  $10^{-8}$  could be replaced by other small number.

- Gradient clipping.

We highlight the first tip, as we've also observed improvement in performance when using it.

(e) (5%) List the hyperparameters you use in (d):

Hyperparameter	Value
N ( $N$ in <a href="#">Algorithm 2</a> )	
M ( $M$ in <a href="#">Algorithm 2</a> )	
MINIBATCH_SIZE ( $B$ in <a href="#">Algorithm 2</a> )	
LR ( $\alpha$ and $\alpha'$ in <a href="#">Algorithm 2</a> )	List both if you use $\alpha \neq \alpha'$
LAMBDA ( $\lambda$ in <a href="#">Algorithm 2</a> )	
BETA ( $\beta$ in <a href="#">Algorithm 2</a> )	
EPS ( $\epsilon$ in <a href="#">Algorithm 2</a> )	

If you use any trick beyond what is described in [Algorithm 2](#), please briefly describe it here. Also, list any additional hyperparameters you introduced in the table above.

**Remark** [Line 13](#) in [Algorithm 2](#) reuses the advantage estimate  $\hat{A}(s_i, a_i)$  to construct  $\hat{V}(s_i)$ , which is then used to train the state-value function in [Line 20](#). This effectively makes [Line 20](#) a TD( $\lambda$ ) update, using the same  $\lambda$  as in the advantage estimation for the policy update.

However, as we've noted before, these two  $\lambda$  values need not be the same. You may also explore the case where they differ. To do so, just compute a separate advantage estimate  $\hat{A}'(s_i, a_i)$  using a different  $\lambda'$ , and define  $\hat{V}(s_i) = \hat{A}'(s_i, a_i) + V_\phi(s_i)$ .

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**Algorithm 2** PPO

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```
1 Parameters:  $N, M, B, \alpha$  (policy learning rate),  $\alpha'$  (value learning rate),  $\lambda$  (GAE parameter),  $\beta$  (KL penalty coefficient),  
    $\epsilon$  (clipping parameter).  
2 Initialize the policy network  $\pi_\theta$  with weights  $\theta$   
3 Initialize the value network  $V_\phi$  with weights  $\phi$ .  
  
4 Sample  $s_{\text{tmp}} \sim \rho$ , where  $\rho$  is the initial state distribution.  
5 for  $k = 1, \dots$  do  
6    $s_1 \leftarrow s_{\text{tmp}}$   
7   for  $i = 1, 2, \dots, N$  do  
8     Select action  $a_i \sim \pi_\theta(\cdot | s_i)$ .  
9     Observe reward  $r_i$  and the next state  $s'_i$ .  
10    If  $s'_i$  is a terminal state, sample  $s_{i+1} \sim \rho$ ; otherwise, set  $s_{i+1} = s'_i$ .  
11   $s_{\text{tmp}} \leftarrow s_{N+1}$   
12  Compute  $\hat{A}(s_i, a_i)$  for all  $i = 1, \dots, N$  by calling  $\text{GAE}_\lambda(\{s_i, a_i, r_i, s'_i\}_{i=1}^N, V_\phi)$  (Algorithm 3).  
13  Define  $\hat{V}(s_i) = \hat{A}(s_i, a_i) + V_\phi(s_i)$  for all  $i = 1, \dots, N$ .  
14  Define  $\hat{\pi}(a_i | s_i) = \pi_\theta(a_i | s_i)$  for all  $i = 1, \dots, N$ .  
15   $\hat{A}(s_i, a_i), \hat{V}(s_i), \hat{\pi}(a_i | s_i)$  should all be viewed as constant below — call tensor.detach() for them.  
  
16  for  $j = 1, \dots, M$  do  
17    Randomly sample a minibatch  $\mathcal{B} \subset \{(s_i, a_i, r_i, s'_i)\}_{i=1}^N$  with size  $|\mathcal{B}| = B$ .  
18    Update the policy network:  
  
      
$$\theta \leftarrow \theta + \alpha \nabla_\theta \frac{1}{B} \sum_{(s, a, r, s') \in \mathcal{B}} \left( \min \{ \varrho_\theta(s, a) \hat{A}(s, a), \varrho_\theta^{\text{clip}}(s, a) \hat{A}(s, a) \} - \beta (\varrho_\theta(s, a) - 1 - \log \varrho_\theta(s, a)) \right),$$
  
  
    where  $\varrho_\theta(s, a) \triangleq \frac{\pi_\theta(a|s)}{\hat{\pi}(a|s)}$  and  $\varrho_\theta^{\text{clip}}(s, a) \triangleq \max\{1 - \epsilon, \min\{1 + \epsilon, \varrho_\theta(s, a)\}\}$ .  
19    Update the value network:  
  
      
$$\phi \leftarrow \phi - \alpha' \nabla_\phi \frac{1}{B} \sum_{(s, a, r, s') \in \mathcal{B}} \left( V_\phi(s) - \hat{V}(s) \right)^2.$$
  
20
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**Algorithm 3**  $\text{GAE}_\lambda$ 

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**Parameter:**  $\lambda$

**Input:**  $\{(s_i, a_i, r_i, s'_i)\}_{i=1}^N$  and  $V_\phi$ .

Define  $\hat{A}(s_{N+1}, a_{N+1}) \triangleq 0$ .

**for**  $i = N, N-1, \dots, 1$  **do**

**if**  $s'_i$  is a terminal state **then**

$\delta_i \leftarrow r_i - V_\phi(s_i)$

$\hat{A}(s_i, a_i) \leftarrow \delta_i$

**else**

$\delta_i \leftarrow r_i + \gamma V_\phi(s_{i+1}) - V_\phi(s_i)$

$\hat{A}(s_i, a_i) \leftarrow \delta_i + \lambda \gamma \hat{A}(s_{i+1}, a_{i+1})$

**return**  $\{\hat{A}(s_i, a_i)\}_{i=1}^N$ .

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