

Development of the timing system for the  
Bunch-to-Bucket transfer between the FAIR  
accelerators

Institution Name



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# Zusammenfassung

# **Widmung**

# Deklaration

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# Glossary

accuracy	Closeness of agreement between the observed start and the best estimate of the start of the synchronization window, which is the sum of the precision and trueness
Frame loss rate	The ratio of the number of the lost frames to the number of the theoretic received frames of a tested port
Group DDS	DDS module that generates an Reference RF Signal for a group of cavities
jitter	The absolute value of the difference between the latency of two consecutive received frames belonging to the same stream from one Xena port to another Xena port
latency	The time interval between the time of Xena port receiving frame and the time of another Xena port sending frame
precision	Closeness of agreement between the actual start of the synchronization window of different SCUs
Reference RF Signal	Signal generated by the Group DDS and delivered to an individual RF cavity as a reference for the gap signal
Synchronization Reference Signal	Shared reference signal whose frequency is a multiple of the BuTiS T0 100 kHz and whose zero-crossing is aligned with T0 edges
Timing frame	A specified ethernet frame with 110 byte frame length, which contains one or more timing message

## Glossary

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Trigger SCU	Production of the trigger signal for kicker electronics
trueness	Closeness of agreement between the average actual start of the synchronization window of different SCUs and the best estimation start of the synchronization window

# List of Abbreviations

B2B	Bunch to Bucket
B2B source SCU	Bunch-to-Bucket source Scalable Control Unit
B2B target SCU	Bunch-to-Bucket target Scalable Control Unit
BI	Beam Instrumentation
BuTiS	Bunchphase Timing System
CCS	Central Control System
CM	Clock Master
CPU	Central Processing Unit
CR	Collector Ring
DM	Data Master
DSP	Digital Signal Processor
ESR	Experimental Storage Ring
ESR	New Experimental Storage Ring
FAIR	Facility for Antiproton and Ion Research
FEC	Front End Controller
FESA	Front-End software Architecture
FPGA	Field Programmable Gate Array
GMT	General Machine Timing
LLRF	Low-level RF
MM	Management Master

## **List of Abbreviations**

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MPS	Machine Protection System
PAM	Central Processing Unit
PAP	Phase Advance Prediction
PC	Personal Computer
PSM	Phase Shift Module
RESR	Recycled Experimental Storage Ring
RF	Radio Frequency
SCU	Scalable Control Unit
SM	Settings Management
TM	Timing Master
TOF	Time-of-flight
TTL	Transistor–Transistor Logic
VLAN	Virtual Local Area Network
WR	White Rabbit

# List of symbols

$f_{actual}$	Actual rf freqnecy modulation profile
$\alpha_b(\phi_s)$	Bucket area factor
$\phi_s$	Synchronous phase
$\varepsilon$	Adiabaticity parameter
$Q_x$	Horizontal Chromaticity of SIS18
$Q_y$	Vertical chromaticity of SIS18
$\Delta Q_x$	Horizontal chromatic tune shift of SIS18 due to the rf frequency modulation
$\Delta Q_y$	Vertical chromatic tune shift of SIS18 due to the rf frequency modulation
$\gamma_t$	Transition energy
$t_{best}$	Best estimate of alignment of Reference RF Signals of SIS18 and SIS100
$\delta t_{best}$	Uncertainty of the best estimate of alignment of Reference RF Signals of SIS18 and SIS100
$\psi_{h=1}^{SIS100}$	Predicted SIS100 rf phase at h=1
h	Harmonic number of the rf signal
$\psi_{h=1/5}^{SIS18}$	Predicted SIS18 rf phase at h=1/5
$t_\psi$	Time of the rf phase prediction
$\phi_{h=2}^{SIS18}$	RF phase at the cavity frequency h=2 of SIS18
$\phi_{h=10}^{SIS100}$	RF phase at the cavity frequency h=10 of SIS100

## List of symbols

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$\delta t_\psi$	Uncertainty of the predicted phase advance at time domain
$\delta\psi_{h=1}^{SIS100}$	Uncertainty of the predicted SIS100 rf phase at h=1
$\delta\psi_{h=1/5}^{SIS18}$	Uncertainty of the predicted SIS18 rf phase at h=1/5
$\delta\phi_{h=10}^{SIS100}$	Uncertainty of RF phase at the cavity frequency h=10 of SIS100
$\delta\phi_{h=2}^{SIS18}$	Uncertainty of RF phase at the cavity frequency h=2 of SIS18
$T_{phase\_shift}^{upper\_bound}$	Upper bound time of the phase shft process
$\delta T_{phase\_shift}^{upper\_bound}$	Uncertainty of the upper bound time of the phase shft process
$\Delta\phi_{adjustment}$	Phase adjustment of the frequency beating method
$\psi_{s\_alignment}$	RF phase of the cavity frequency at the start of the probable rang of alignment
$\Delta t_{win\_correct}$	Time correction for the start of the probable range of alignment to the best estimate of the start of the synchronization window
G	Bunch gap
L	Distance from the leftmost to the rightmost SIS18 extraction/SIS100 injection kicker unit
D	Sum distance of d and the 2nd crate
d	Distance between two extraction kicker crates of SIS18
$\beta$	
c	Speed of the light
$t_{B2B}$	Start time of the B2B transfer
$\Delta t$	Beating time for the synchronization

## List of symbols

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$\Delta\phi_s(t)$	Change of the synchronous phase
$C_{SIS18}$	Circumference of the designed orbit of SIS18
$C_{SIS100}$	Circumference of the designed orbit of SIS100
$f_{h=1}^{SIS18}$	Revolution frequency of SIS18
$f_{h=1}^{SIS100}$	Revolution frequency of SIS100
$f_{h=2}^{SIS18}$	Caivity frequency of SIS18
$f_{h=10}^{SIS100}$	Caivity frequency of SIS100
$\Delta\phi_{shift}$	Phase shift to be achieved by the phase shift method
$\Delta f_{rf}(t)$	Rf frequency modulation for the phase shift method
T	Period of rf frequency modulation for the phase shift method
$t_0$	Start time of the rf frequency modulation for the phase shift method

# **Chapter 1**

## **Introduction**

**1.1 FAIR project**

**1.2 Beam transfer systems of the FAIR accelerator**

# Chapter 2

## Theoretical background

Transferring bunches of particles from a synchrotron into specified buckets of another synchrotron has several underlying basic principles. In Sec. 2.1, the basic principles for the B2B transfer will be introduced. For FAIR, these principles are realized based on the existing FAIR control system and LLRF system. So these two systems will be introduced in Sec. 2.2.

### 2.1 Introduction of the basic principles for the B2B transfer

The energy of the beam is same before and after the B2B transfer, so the energy of the source synchrotron must first of all match that of the target synchrotron. Principally speaking, every synchrotron has its independent RF system. Then the phase advance between the bunch and the bucket must be precisely controlled before the bunch is ejected. The process of achieving the detailed phase adjustment between two RF systems is termed "RF synchronization". For the correct bucket injection, the filled buckets and the bucket to be filled must be marked. The bunch fast extraction must happen exactly one "time of flight" before the required bucket of the target synchrotron passes the injection region. The injection kicker must kick when the bucket passes the injection region. In this section, all of the B2B basic principles will be explained.

#### 2.1.1 Energy match

The bunch coordinates in the longitudinal phase plane of the source synchrotron, just before transfer, must be accurately controlled, according to the bucket to be filled. The target synchrotron has to center the bucket on the desired orbit<sup>1</sup>, according to the energy of the bunch. This requirement guarantees the energy match between the bunch and bucket. The energy of a beam is determined by the 'magnetic rigidity', which is defined as the following:

$$B(t)\rho_0 = \frac{p(t)}{e} \quad (2.1)$$

where  $p(t)$  is the magnitude of the particle momentum,  $e$  is the charge of the particle,  $B(t)$  is magnetic field, and  $\rho_0$  is the bending radius of a particle immersed in a

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<sup>1</sup>Design orbit or injection orbit

## 2.1. Introduction of the basic principles for the B2B transfer

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magnetic field  $B(t)$ . The ratio of  $p(t)$  to  $e$  describes the 'stiffness' of a beam, it can be considered as a measure of how much angular deflection results when a particle travels through a given magnetic field.

The bunch is transferred from the source to the target synchrotron with the same energy. So the beam has the same momentum and velocity for both synchrotrons. According to eq. 2.1, the magnetic rigidity of two synchrotrons must be matched:

$$B^{src}(t)\rho_0^{src} = \frac{p}{e} = B^{trg}(t)\rho_0^{trg} \quad (2.2)$$

Where the superscript of the symbol denotes the synchrotron, "src" represents the source synchrotron and "trg" the target synchrotron.

Besides, the rf frequency of two synchrotrons must meet the following relation.

$$C^{src}\frac{f_{rf}^{src}(t)}{h^{src}} = \beta c = C^{trg}\frac{f_{rf}^{trg}(t)}{h^{trg}} \quad (2.3)$$

where  $C$  is the circumference of the synchrotron,  $h$  the harmonic number of the rf signal and  $f_{rf}$  denotes the rf frequency at the harmonic number  $h$ ,  $\beta$  the fraction of the particle velocity to the lightspeed.

### 2.1.2 Loop freeze

### 2.1.3 Phase difference between two RF systems

For the RF synchronization between two synchrotrons, the prerequisite is to know the phase difference between two independent RF systems.

### 2.1.4 RF synchronization

There are usually two methods available for the synchronization process. The synchronization is achieved by an azimuthal positioning of the bunch in the source synchrotron or the bucket in the target synchrotron. This is so-called "phase shift method". When two rf frequencies are slightly different, they are beating, perceived as periodic variations in phase difference, whose rate is the difference between the two frequencies. The synchronization is automatically achieved. This is so-called "frequency beating method". Both methods provide a time frame for the B2B transfer, within which a bunch could be transferred into a bucket with the center mismatch at least better than  $1^\circ$ . The time frame is called the synchronization window.

For both methods, the accompanying beam dynamics must be taken into consideration. Of the four variables, the revolution frequency  $f(t)$ ,  $B(t)$ ,  $p(t)$  and the orbit radius  $R(t)$ , only two are independent. This leads to four very useful differential relations. The momentum of particle is given by

$$p(t) = e\rho_0\left[\frac{R(t)}{R_0}\right]^{1/\alpha_p}B(t) \quad (2.4)$$

where  $R_0$  is its nominal value; and  $\alpha_p$ , the momentum compaction factor. From eq. 2.4, the first-order total differential of  $p(t)$  is given as

## 2.1. Introduction of the basic principles for the B2B transfer

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$$dp(t) = \frac{e\rho_0}{\alpha_p(R_0)^{1/\alpha_p}} B(t) R(t)^{1/\alpha_p - 1} dR(t) + e\rho_0 \left[ \frac{R(t)}{R_0} \right]^{1/\alpha_p} B(t) dB(t) \quad (2.5)$$

Dividing both sides of eq. 2.5 by  $p(t)$ , we obtain

$$\frac{dp(t)}{p(t)} = \gamma_t^2 \frac{\Delta R}{R} + \frac{\Delta B}{B} \quad (2.6)$$

Now, for circular accelerators, the following general relation holds

$$f(t) = \frac{v(t)}{2\pi R(t)} \quad (2.7)$$

where  $v(t)$  is its velocity. The total differential of  $f(t)$  is given by

$$df(t) = \frac{1}{2\pi} \left[ \frac{dv(t)}{R(t)} - \frac{v(t)}{R^2(t)} dR(t) \right] \quad (2.8)$$

Dividing both sides of eq. 2.8 by  $f(t)$  yields

$$\frac{df(t)}{f(t)} = \frac{dv(t)}{v(t)} - \frac{dR(t)}{R(t)} \quad (2.9)$$

The fractional change in  $v(t)$  is related to the fractional change in  $p(t)$ :

$$\frac{dp(t)}{p(t)} = \gamma^2(t) \frac{dv(t)}{v(t)} \quad (2.10)$$

where  $\gamma(t)$  is the relativistic factor, which measures the total particle energy,  $E(t)$ , in units of the particle rest energy,  $E_0$ . Solving  $dv(t)/v(t)$  from eq. 2.10 and substituting it into eq. 2.9 yields

$$\frac{df(t)}{f(t)} = \gamma^2(t) \frac{dp(t)}{p(t)} - \frac{dR(t)}{R(t)} \quad (2.11)$$

Replacing  $dp(t)/p(t)$  in eq. 2.11 with eq. 2.6, we have

$$\frac{df(t)}{f(t)} = \gamma^2(t) \frac{dB(t)}{B(t)} + \left[ \frac{\gamma_t^2}{\gamma^2(t)} - 1 \right] \frac{dR(t)}{R(t)} \quad (2.12)$$

where  $\gamma_t$  is the transition gamma, which is related to  $\alpha_p$  as  $\gamma_t = 1/\sqrt{\alpha_p}$ . In the same way, solving  $dR(t)/R(t)$  from eq. 2.6 and substituting it into eq. 2.11, we obtain

$$\frac{df(t)}{f(t)} = \left( \frac{1}{\gamma^2(t)} - \frac{1}{\gamma_t^2} \right) \frac{dp(t)}{p(t)} + \frac{1}{\gamma_t^2} \frac{dB(t)}{B(t)} \quad (2.13)$$

### 2.1.4.1 Phase shift method

Based on the phase difference, the rf system of the source or target or both synchrotrons are modulated away from their nominal value for a period of time and then modulated back so that the phase shift created by the frequency modulation could compensate for the expected phase difference. After the phase shift, the

## 2.1. Introduction of the basic principles for the B2B transfer

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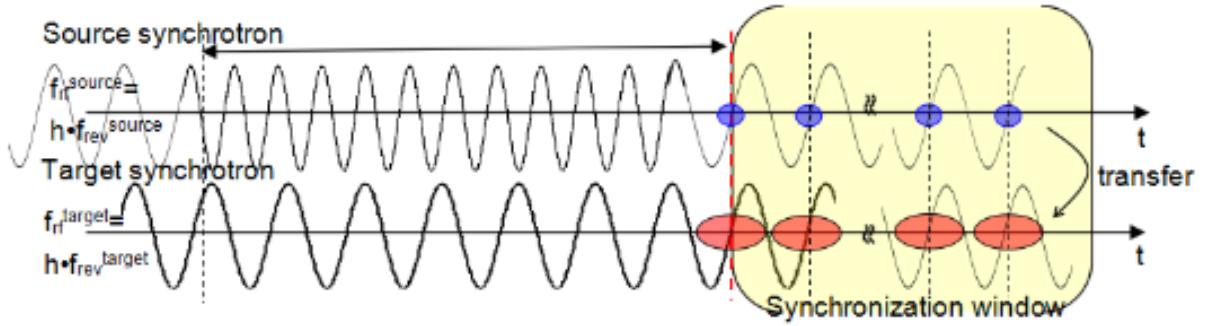


Figure 2.1: The illustration of the phase shift method.

bunches of the source synchrotron are synchronized with random buckets of the target synchrotron. The phase shift process must be performed adiabatically for the longitudinal emittance to be preserved.

Fig. 1 illustrates the phase shift method. The top and bottom RF signals are respectively from the source and target synchrotrons. For the phase shift method two RF signals are of the same frequency. The blue dots show the position of the bunches of the source synchrotron, the red dots correspond to the bucket positions of the target synchrotron. The compensation of the time-of-flight is not drawn here. The red dashed line shows the end of the phase shift process and the beginning of the synchronization window, drawn in yellow. After the phase shift, bunches match with the random buckets.

A particular case of the B2B synchronization occurs, when the target synchrotron is empty, i.e. it did not capture any bunch yet, the phase shift can be done for the target synchrotron without adiabatical consideration (e.g. Phase jump is possible).

Now we analyze the rf frequency modulation of the phase shift from the beam dynamics viewpoint.

- Radial excursion and momentum shift due to rf frequency modulation

For the phase shift method, the magnetic field is not affected by the frequency modulation, so  $\Delta B = 0$ . By substituting  $\Delta B = 0$  into eq. 2.12 and eq. 2.13, we could get respectively the accompanying radial excursion and momentum shift by the frequency modulation.

$$\frac{\Delta f}{f} = \left( \frac{\gamma_t^2}{\gamma^2} - 1 \right) \frac{\Delta R}{R} \quad (2.14)$$

and

$$\frac{\Delta f}{f} = \left( \frac{1}{\gamma^2} - \frac{1}{\gamma_t^2} \right) \frac{\Delta p}{p} \quad (2.15)$$

- Transverse dynamics analysis

The momentum spread  $\Delta p/p \neq 0$  during the phase shift process causes chromaticity drift  $\Delta Q$ .  $Q'$  is the chromaticity.

$$\Delta Q = Q' \frac{\Delta p}{p} \quad (2.16)$$

## 2.1. Introduction of the basic principles for the B2B transfer

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- Shift of synchronous phase

The synchronous phase deviates from  $0^\circ$  during the frequency modulation. From the expression of the particle momentum,  $p(t)$ , given in eq. 2.4, the time derivative of  $p(t)$  can be written as

$$\frac{dp(t)}{dt} = \frac{e\rho_0 B(t)}{\alpha_p R_0^{1/\alpha_p}} R(t)^{1/\alpha_p - 1} \frac{dR(t)}{dt} + e\rho_0 \left(\frac{R(t)}{R_0}\right)^{1/\alpha_p} \frac{dB(t)}{dt} \quad (2.17)$$

Now, the relationship between the rate of change in momentum of a particle,  $dp(t)/dt$ , and the force applied on it,  $F(t)$ , is governed by Newton's second law:

$$\frac{dp(t)}{dt} = F(t) \quad (2.18)$$

$F(t)$  is given by the product of the accelerating electric field,  $E(t)$ , and the charge of particle,  $e$ . Substituting  $dp(t)/dt$  given in eq. 2.17 and  $F(t) = eE(t)$  into eq. 2.18, we have

$$\frac{e\rho_0 B(t)}{\alpha_p R_0^{1/\alpha_p}} R(t)^{1/\alpha_p - 1} \frac{dR(t)}{dt} + e\rho_0 \left(\frac{R(t)}{R_0}\right)^{1/\alpha_p} \frac{dB(t)}{dt} = eE(t) \quad (2.19)$$

From this equation, we obtain the expression of energy gain in one turn,

$$2\pi R_0 \left[ \frac{e\rho_0 B(t)}{\alpha_p R_0^{1/\alpha_p}} R(t)^{1/\alpha_p - 1} \frac{dR(t)}{dt} + e\rho_0 \left(\frac{R(t)}{R_0}\right)^{1/\alpha_p} \frac{dB(t)}{dt} \right] = eV(t) \sin[\phi_{s0}(t) + \Delta\phi_s(t)] \quad (2.20)$$

where  $V(t)$  is the RF accelerating voltage per turn;  $\phi_{s0}$ , the synchronous phase in the operation with no frequency modulation; and  $\Delta\phi_s(t)$ , the change in the synchronous phase originating from the rf frequency modulation.

The magnetic field is not affected by the frequency change, we can assume  $dB(t)/dt = 0$ . Before the synchronization, it is a stationary bucket with the synchronous phase  $0^\circ$ . Then, eq. 2.20 reduce to

$$2\pi R_0 \left[ \frac{e\rho_0 B(t)}{\alpha_p R_0^{1/\alpha_p}} R(t)^{1/\alpha_p - 1} \frac{dR(t)}{dt} \right] = eV(t) \sin[\Delta\phi_s(t)] \quad (2.21)$$

Solving  $\Delta\phi_s(t)$  from eq. 2.21, we have

$$\Delta\phi_s(t) = \sin^{-1} \left[ \frac{2\pi\rho_0 B}{\alpha_p V} \left( \frac{R(t)}{R_0} \right)^{1/\alpha_p - 1} \frac{dR(t)}{dt} \right] \quad (2.22)$$

From eq. 2.22, we know that  $\Delta\phi_s(t)$  is only determined by  $dR(t)/dt$  during the frequency modulation.

- Bucket area factor

At the flattop, the bucket is a stationary bucket with  $\phi_{s0}(t) = 0$ . During the frequency modulation process, the bucket becomes a running bucket with  $\Delta\phi_s(t) \neq 0$ . The ratio of bucket areas of a running bucket to a stationary bucket is bucket area factor  $\alpha_b(\Delta\phi_s)$ . The bucket area factor could be estimated by [5].

$$\alpha_b(\Delta\phi_s) \approx (1 - \sin(\Delta\phi_s))(1 + \sin(\Delta\phi_s)) \quad (2.23)$$

## 2.1. Introduction of the basic principles for the B2B transfer

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- Adiabaticity analysis

$\omega_s(t)$  is the small-amplitude synchrotron frequency given by

$$\omega_s(t) = \left[ -\frac{\eta(t) h \omega_{rev}^2(t) e V(t) \cos \phi_s(t)}{2\pi \beta^2(t) E(t)} \right]^{1/2} \quad (2.24)$$

A process is called “adiabatic” when the RF parameters are changed slowly enough for the longitudinal emittance to be preserved. The condition that the parameters are slowly varying can be expressed by

$$\varepsilon = \frac{1}{\omega_s^2(t)} \left| \frac{d\omega_s(t)}{dt} \right| \ll 1 \quad (2.25)$$

Compared with  $\phi_s(t)$ , all of the other variables change very slowly.  $\phi_s(t) = \phi_{s0}(t) + \Delta\phi_s(t)$ . From eq. (2.25) and eq. (2.24), we can write the adiabaticity parameter  $\varepsilon$ , as follows [2]:

$$\varepsilon \approx \frac{1}{2\omega_{s0}(t)} \left| \tan \phi_s(t) \frac{d\phi_s(t)}{dt} \right| \quad (2.26)$$

- Constraints on the RF frequency modulation

From eq. 2.26, we can clearly see that  $\phi_s(t)$  and  $d\phi_s(t)/dt$  play deterministic roles for the adiabaticity when the frequency is modulated. Now let us deduce how the rf frequency modulation affects  $\phi_s(t)$  and  $d\phi_s(t)/dt$ . From eq. (2.14), we could get the following equation.

$$\frac{dR(t)}{dt} \left( \frac{\gamma_t^2}{\gamma^2} - 1 \right) f_0 = \frac{df(t)}{dt} R_0 \quad (2.27)$$

Substituting eq. 2.27 into eq. 2.21, we get

$$V \sin \phi_s = \frac{2\pi R_0 \rho B}{f_0 \left( \frac{1}{\gamma}^2 - \frac{1}{\gamma_t}^2 \right)} \left[ \frac{R(t)}{R_0} \right]^{\left( \frac{1}{\alpha_p} - 1 \right)} \frac{df(t)}{dt} \quad (2.28)$$

Because  $(R(t) - R_0)/R_0$  is about  $10^{-4}$ ,  $[1 + \frac{\Delta R}{R_0}]^{\left( \frac{1}{\alpha_p} - 1 \right)} \approx 1$ . We can get the relation between  $df(t)/dt$  and  $\phi_s$  from eq. 2.28.

$$V \sin \phi_s = \frac{2\pi R_0 \rho B}{f_0 \left( \frac{1}{\gamma}^2 - \frac{1}{\gamma_t}^2 \right)} \frac{df(t)}{dt} \quad (2.29)$$

From eq. 2.23, we know that the bucket area factor is determined by the synchronous phase change  $\Delta\phi_s$ . Based on eq. 2.29, we know that  $df(t)/dt$  is important for the bucket size.

In order to get the relation between  $d\phi_s(t)/dt$  and the frequency modulation, we get the time derivative of eq. 2.29

$$V \cos \phi_s \frac{d\phi_s}{dt} = \frac{2\pi R_0 \rho B}{f_0 \left( \frac{1}{\gamma}^2 - \frac{1}{\gamma_t}^2 \right)} \frac{df(t)/dt}{dt} \quad (2.30)$$

Based on the adiabaticity eq. (2.26),  $d\phi_s(t)/dt$  must be existing. So  $\frac{df(t)/dt}{dt}$  must be existing. It means that  $df(t)/dt$  and  $\phi_s(t)$  must be continuous. In a word, there are two constraints for the rf frequency modulation.

## 2.1. Introduction of the basic principles for the B2B transfer

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- The  $df(t)/dt$  of the rf frequency modulation must be small enough to guarantee the bucket size.
- The  $df(t)/dt$  of the rf frequency modulation must be continuous to guarantee the continuous synchronous phase.

### 2.1.4.2 Frequency beating method

The frequency beating method uses the effect of two RF signals of slightly different frequencies, perceived as periodic variations in phase difference whose rate is the difference between the two frequencies. The RF frequency of the source or the target or both synchrotrons is detuned long before the ejection, then the difference between the phase of the bunch and bucket is measured. Based on the measured phase, the synchronization is realized when the phase difference of the two RF frequencies corresponds to the ideal phase difference ( $\Delta\theta = 0^\circ$ ). The  $\Delta\theta$  is the mismatch between the bunch center and the corresponding bucket center. Because of the slightly different RF frequencies, a mismatch between the bunch and bucket centers exists. In principle, the B2B transfer requirement for FAIR allows a bunch to bucket center mismatch of  $1^\circ$ , which brings a symmetric time frame with respect to the time of the ideal phase difference, resulting in the maximum synchronization window for the frequency beating method, drawn in yellow, see Fig. 2.2. The red dashed line shows the time for the expected phase difference.

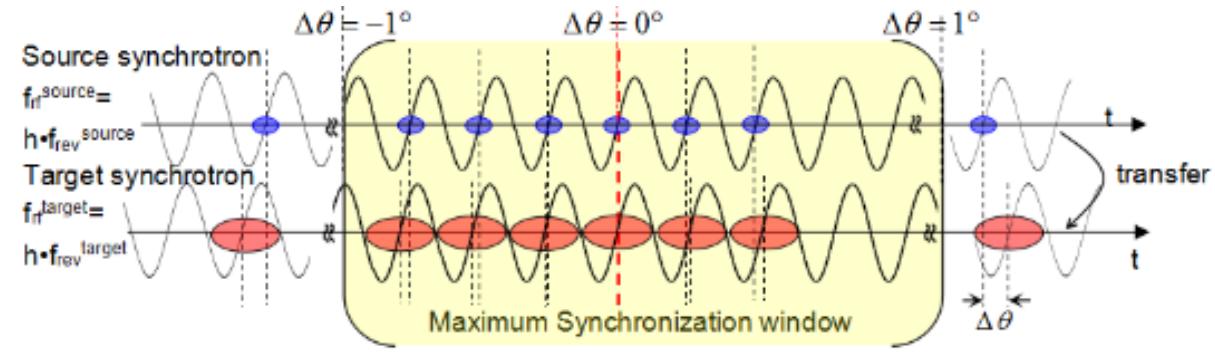


Figure 2.2: The illustration of the frequency beating method.

The RF frequency is detuned at the end of the ramp. During the rf frequency detune process, the magnetic field and radius excursion react and the momentum is not affected for the energy match.

- Longitudinal dynamics analysis

Because the momentum is not affected by the frequency change, namely  $\Delta p = 0$ , the general relation between the radial excursion and RF frequency change eq. (2.11) reduces to eq. (2.31) and the general relation between the magnetic field change and RF frequency change eq. (2.6) reduces to eq. (2.32).

$$\frac{\Delta f}{f} = -\frac{\Delta R}{R} \quad (2.31)$$

$$\frac{\Delta f}{f} = \frac{1}{\gamma_t^2} \times \frac{\Delta B}{B} \quad (2.32)$$

## **2.2. Infrastructures for the B2B transfer system**

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### **2.1.5 Bucket label**

After the synchronization, the bunch is synchronized to an arbitrary RF bucket. For the proper injection, we must know which buckets are already filled and which buckets should be filled by next injection cycle. The fast extraction can only proceed when the required bucket comes.

### **2.1.6 Synchronization of the extraction and injection kicker**

For the proper B2B transfer, the extraction and injection kickers must be synchronized with the beam.

- Extraction kicker

Here we discuss that all bunches are extracted by one time extraction kick. The flattop is at least one revolution period. The fall time is not constrained. If there is no empty RF bucket of the ring, the rise time of the extraction kicker must be shorter than the bunch gap. If there is at least one empty RF bucket, the rise of the magnetic field could be achieved within the gap of the empty RF buckets.

- Injectin kicker

For multi-batch injection, the rise time of the injection kicker must be shorter than the bunch gap. The flattop is determined by the length of the bunches to be injected. If all buckets must be filled, the fall time must be shorter than the bunch gap. If at least one bucket is kept empty, the fall of the magnetic field could be achieved within the gap of the empty RF buckets. If the ring needs only one time injection, the rise time is not constrained. The flattop determined by the length of the bunches to be injected. The fall time must be shorter than the bunch gap or the gap of the empty RF buckets.

### **2.1.7 Beam indication for the beam instrumentation**

In order to observe the beams and measure related parameters for accelerators and transfer lines, the beam instrumentation (BI) equipments must be synchronized and triggered within the beam schedule. For the B2B transfer, the data acquisition for the beam instrumentation equipments should be triggered before the bunch is extracted. Sometimes they should not be triggered too early because of the limitation of sampling time. So a pre-trigger is necessary, which indicates that the bunch will be extracted/injected soon.

## **2.2 Infrastructures for the B2B transfer system**

For the FAIR accelerator complex, synchronization of the B2B transfer will be realized by the FAIR control system and the Low-Level RF (LLRF) system. For the synchronization of LLRF system, the GMT system is complemented and linked to the Bunchphase Timing System (BuTiS).

## **2.2. Infrastructures for the B2B transfer system**

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### **2.2.1 FAIR control system**

The FAIR control system takes advantage of collaborations with CERN in using proven framework solutions like FESA, LSA, White Rabbit, etc. It consists of the equipment layer, middle layer and application layer. The equipment layer consists of equipment interfaces, GMT and software representations of the equipment (FESA) Front-End System Architecture. The middle layer provides service functionality both to the equipment layer and the application layer through the IP control system network. LSA is used for the Settings Management. The application layer combines the applications for operators as GUI applications or command line tools. The application layer and the middle layer only request what the FAIR accelerator complex should do and transmit set values to the equipment layer. The actual beam production is controlled by the GMT. The GMT system is synchronized to BuTiS. The SM supplies the schedule for the GMT by LSA.

#### **2.2.1.1 BuTiS**

Bunch Phase Timing System (BuTiS) [6] [7] serves as a campus-wide clocks distribution system with subnanosecond resolution and stability over distances of several hundred meters while maintaining 100ps per km timing stability. Two BuTiS reference clocks 10 MHz and 200 MHz and a trigger identification pulse at 100 kHz are generated centrally in the BuTiS center. A star-shaped optical fiber distribution network transfers these signals to BuTiS receivers all over the FAIR campus. A BuTiS receiver and a local reference synthesizer are installed in each supply room to produce the BuTiS reference clocks, which are in phase. For this purpose, a measurement setup in the BuTiS center continuously measures the optical signal transmission delay between the BuTiS center and the different BuTiS receivers. This measurement information is used to shift the phases of the signals generated in each local reference synthesizer for the delay compensation. The main task of BuTiS is the supply of the reference clock signals for Reference RF Signal in each rf supply rooms.

#### **2.2.1.2 GMT**

The GMT [1] is contained in the equipment layer. The main tasks of the GMT system are time synchronization of more than 2000 Front-End Controllers (FEC) with nanosecond accuracy, distribution of timing messages and subsequent generation of real-time actions by the nodes of the timing system. The GMT consists of the Timing Master (TM) and the White Rabbit (WR) timing network and integrates nodes. The timing master's interface to the upper layers, e.g. online schedule monitor, is modeled as a FESA device. The timing master is a logical device, containing the data master (DM), the clock master (CM) and the management master (MM). The data master receives a schedule for the operation of the FAIR accelerator complex from the Settings Management and provides the real-time scheduler by broadcasting messages to the WR timing network, which will be received and executed by the corresponding node at the designated time. The clock master is a dedicated White Rabbit switch. It is the topmost switch layer of the WR timing network and provides the grandmaster clock which is distributed to all other nodes in the timing network. The clock master derives its clock and timestamps from the BuTiS

## **2.2. Infrastructures for the B2B transfer system**

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clocks. All active components including receiver nodes and switches are registered to the management master. The management master monitor and manage the active components of the GMT system.

### **2.2.1.3 FESA**

The real-time front-end software architecture FESA [3] is a framework used to fully integrate the large amount of front-end equipments into the FAIR accelerator control system. FESA was developed by CERN and has already been implemented into the CERN control system. FESA develops FESA classes, the equipment-type specific front-end software. For a specific type of equipments, a FESA class implementation accesses to the control interface of the equipments. The FESA class models the equipment as device, so the FESA output is called device class. One device class can instanciate several devices and thus generally handles several independent pieces of equipments. FESA provides JAVA based graphical user interfaces (GUI) to design, deploy, instantiate and test the device classes. The FEC use FESA to implement generic and equipment specific functions in form of the device classes. Interaction with the equipment is synchronized with the GMT system.

FESA (Frontend Software Architecture) is a framework developed at CERN and is now developed further in collaboration with GSI for the FAIR project. It is a toolbox to model abstract device objects where equipment's process variables (sensors and actuators) are represented as properties. The specific equipment access is implemented in C++ by the developer and is linked by the toolchain to the device model to build a so called FESA class (Fig. 4). Then, one or more FESA classes are linked to the run-time core to build an x86-Linux executable. The FESA classes provide a uniform interface via the objectproperty model and a common middle-ware to the upper layers. The device properties are set and read using synchronous or asynchronous access methods (subscription). For time multiplexed operation of the accelerators, the FESA framework supports defining multiplexed properties. Before an accelerator schedule is started the setting properties of FESA classes are pre-supplied by LSA [6] for all scheduled beams with specific settings accordingly. At runtime, FESA's real time software actions are triggered by timing events, the actual beam specific data is then selected based on information carried by the timing event message and send to the equipment. For the FAIR project the necessary interaction with the timing receiver is realized in a lab-specific timing library of the FESA framework.

### **2.2.1.4 SM**

The SM is located in the middle layer of the control system. It supports off-line generation of synchrotron settings, sending these settings to all involved devices, and programming the schedule of the timing system. The SM uses the LSA (LHC Software Architecture) framework, which originates at CERN and is now developed further in collaboration with GSI for the FAIR project. The settings management is based on a physics model for accelerator optics, parameter space and overall relations between parameters and between accelerators. A standardized API allows accessing data in a common way as basis for generic client applications for all accelerators. Using the LSA-API, trim-applications can coherently modify synchrotron settings. E.g. the service generates timing constraints (e.g. ramp curve) as well as the

equipment's data settings (e.g. field) for all devices derived from physics parameters (e.g. beam energy). For FAIR the framework is extended to model the overall schedule of all accelerators. Beams are described as Beam Production Chains to allow a description from beam-source to beamtarget for settings organization and data correlation.

### 2.2.2 LLRF system

The FAIR low-level rf (LLRF) [4] system shall be usable in the existing synchrotrons SIS18 and experimental storage ring (ESR) as well as in the FAIR synchrotrons SIS100 and SIS300 and in the storage rings collector ring (CR), new experimental storage ring (ESR), and accumulator ring (RESR). It supports fast ramp rates and large frequency span for the acceleration of a variety of ion species. It supports different RF manipulations, including operation at different harmonic numbers, barrier bucket generation and bunch compression.

Cavities are driven from a supply room by a Reference RF Signal. Fig. 2.3 shows the typical cavity system with a Reference RF Signal. The cavity gets the RF signal from a local Cavity DDS (Direct Digital Synthesizer) unit, which receives RF Frequency Ramps from the Central Control System (CCS). A DSP-System (Digital Signal Processor) measures the phase between the Reference RF Signal and the gap voltage of the cavity. In the DSP system, a closed-loop control algorithm is implemented which generates frequency corrections for the local Cavity DDS. In this way, it is ensured that the phase of the gap voltage follows the phase of the reference RF signal. The Reference RF Signal distribution shown in Fig. 2.4 is located in each supply room. The virtual RF cavity is a virtual position in the synchrotron to which the Reference RF Signal corresponds. The Reference RF Signals in different supply rooms are synchronized by the BuTiS. BuTiS 200MHz and 100kHz clock signals are received by BuTiS receivers in different supply rooms in phase. In Fig. 2.4, a number of Group DDS units are located in each supply room, which are synchronized to BuTiS local reference. The Group DDS signals can be routed to the different cavity systems by a Switch Matrix. All cavities in a synchrotron could be providing with the same Group DDS signal. The cavities at different harmonic numbers could be realized by using Group DDS signals with different harmonic numbers. The Group DDS concept allows to synchronize a variety of cavities in a very flexible way.

All the cavities of SIS18 are driven from one supply room. The SIS100 cavities will be gathered in three acceleration sections, each of them is driven by a dedicated supply room.

### 2.2.3 MPS system

emergency kick

## 2.3 $U^{28+}$ beam from SIS18 to SIS100

In this document, we use  $U^{28+}$  B2B transfer from SIS18 to SIS100 as an example. So the supercycle of  $U^{28+}$  beam of SIS18 and stacking of  $U^{28+}$  beam of SIS100 are introduced in this section.

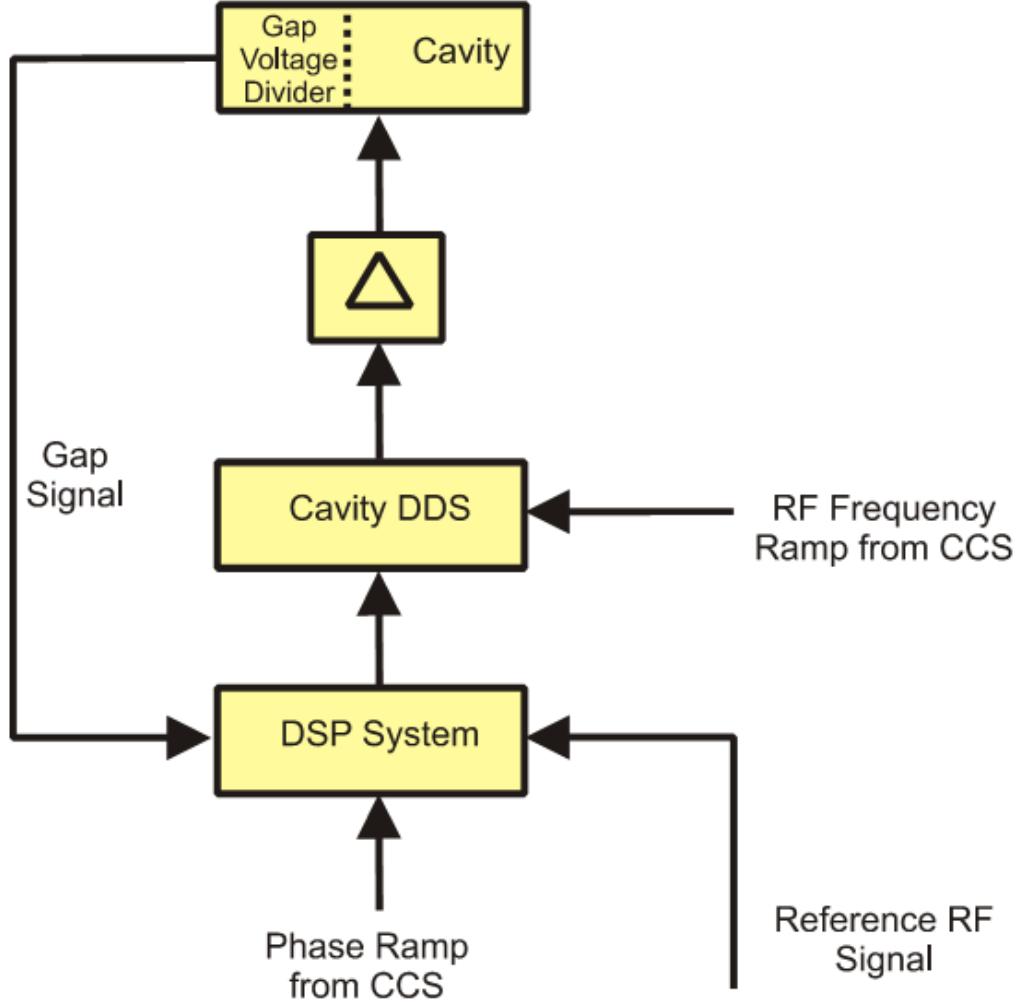


Figure 2.3: Local Cavity Synchronization

In Fig. 2.4, SIS100 is operated at harmonic number 10, it holds 10 buckets in total, indicated by the row of ellipses in the lower part of the figure. SIS18 is operated at harmonic number 2. The beam is accumulated using four consecutive injections of two bunches each from SIS18 into different buckets. These four consecutive cycles are called super cycle. When the injection from SIS18 is completed, 8 neighbouring buckets in SIS100 are filled. The bucket pattern is defined as the rules of the bucket filling. After that the complete beam of SIS100 is compressed in a single bunch at harmonic number 2.

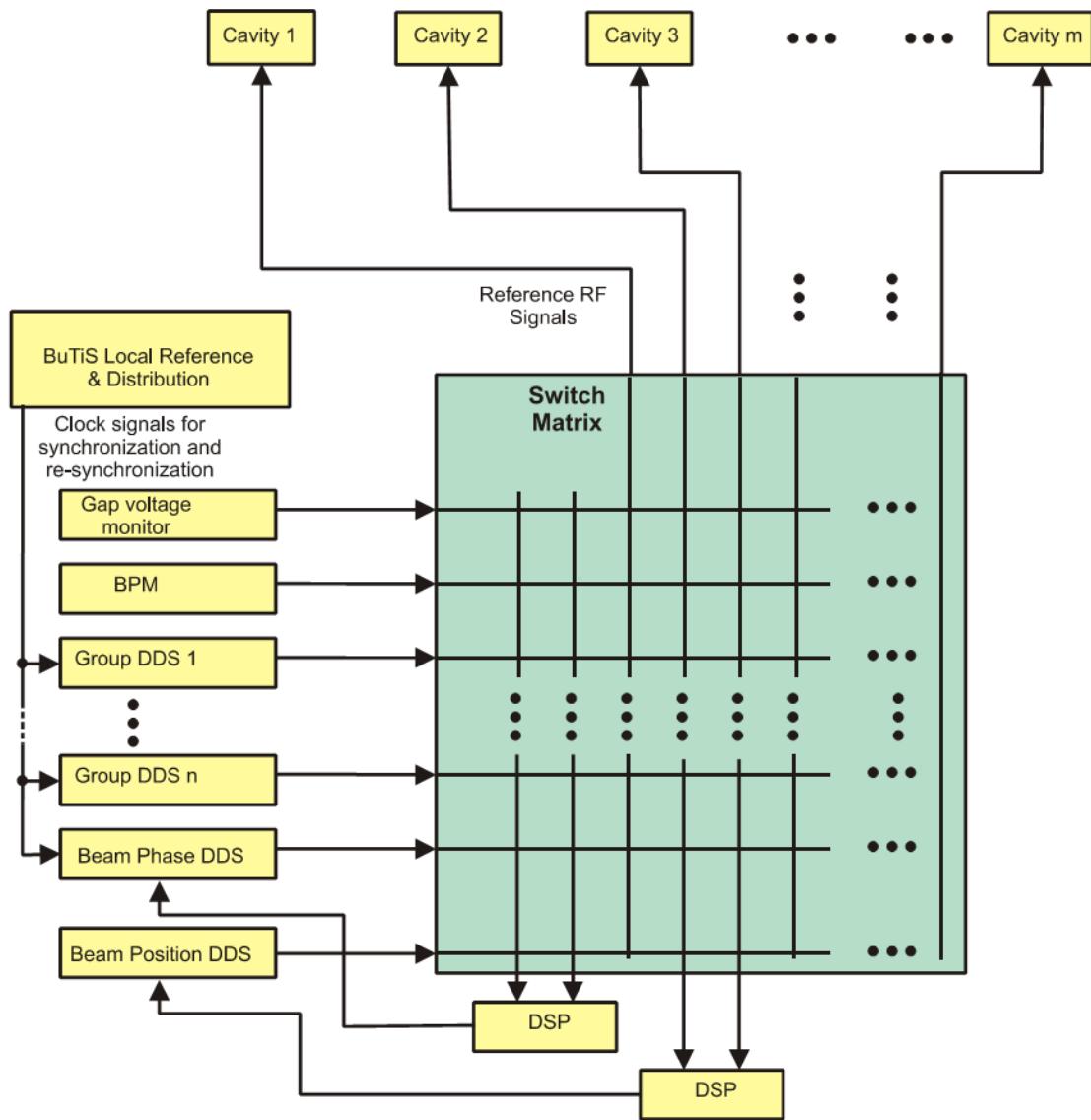


Figure 2.4: Reference RF Signal Distribution

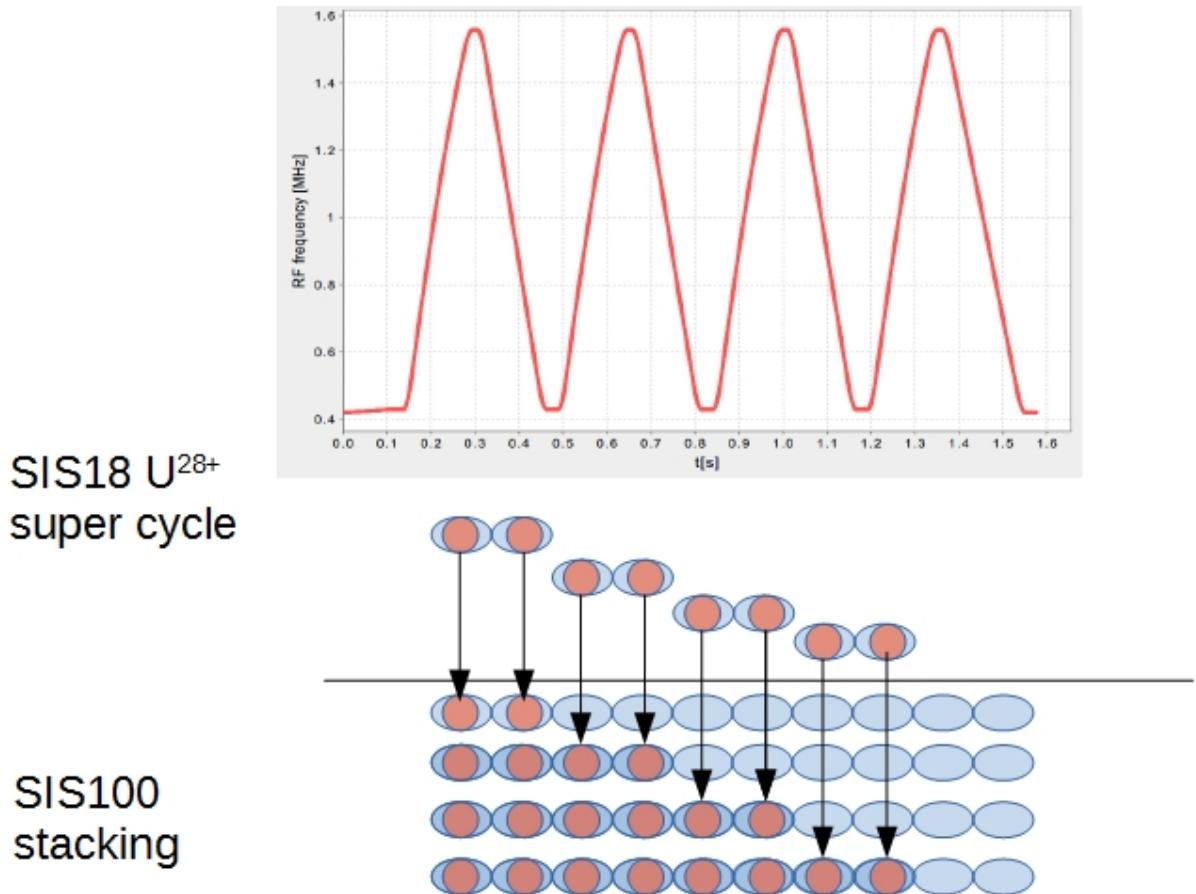


Figure 2.5:  $U^{28+}$  beam from SIS18 to SIS100

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# Chapter 3

## First idea on the B2B transfer system

### 3.1 Data acquisition from two synchrotrons

### 3.2 Coarse synchronization

### 3.3 Fine synchronization

After the synchronization, the bunch is synchronized to an arbitrary RF bucket. For the proper injection, we must know which buckets are already filled and which buckets should be filled by next injection cycle. So a reproduced signal at the target revolution frequency is used as the bucket marker, which labels bucket 1 of the target synchrotron. The SM knows the bucket pattern and a proper bucket offset will be applied on each injection cycle to the bucket marker. Fast extraction can only proceed when the required bucket comes. The extraction must be correctly synchronized with respect to a reference signal at the following frequency, which is called bucket marker.

#### 3.3.1 Synchronization of the extraction and injection kicker

Because the beam of two rings are synchronized with each other, the extraction and injection are synchronized indirectly. Thyratrons are used for kicker systems at FAIR accelerator.

For FAIR project, there are several different type of kicker system. Here we introduce SIS18 extraction, SIS100 injection and extracion/emergency kicker system.

The SIS100 extraction kicker system is used for the regular extraction and the emergency extraction by bipolar operation. It consists of eight kicker magnets. Each magnet is placed between the two cable capacitors. Both cable capacitors will be charged at the same time with a high voltage DC power supply. The polarity of the magnetic field changes with the direction of the discharge current, which are controled by two thyratron switches. One polarity directs the beam into the extraction channel, the other polarity directs the beam into an underground beam dump for an emergency case. The system produces rectangular pulses with different polarities of the kicker field.

### 3.3. Fine synchronization

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The SIS18 extraction and SIS100 injection kicker have the monopolar operation. Two cable capacitors will be charged at the same time with a high voltage DC power supply. By closing the main switch the capacitor is being discharged via the kicker magnet, which produces a rectangular kicker pulse. The pulse length can be modified by closing the dump switch in correlation with the main switch.

Fig. 3.1 shows the synchronization of the SIS18 extraction and SIS100 injection kicker for  $U^{28+}$  B2B transfer. Four batches of  $U^{28+}$  at 200 MeV/u are injected into eight out of ten buckets of SIS100. Each batch consists of two bunches. The 9th and 10th bucket may be used as bunch gap for the emergency kick. The SIS18 revolution frequency marker and SIS100 bucket markers represent time when the SIS18 bunch 1 (1st) and SIS100 bucket 1 (#1) passes by the virtual RF cavity, which is a virtual position in the synchrotron to which the Reference RF Signal corresponds. In Fig. 3.1, the numbers correspond to the consideration of following factors for the synchronization:

- Bucket pattern ( $delay_{bucket}$ . E.g.  $delay_{bucket}$  = One SIS18 revolution period. Bucket 3 and 4 will be filled)
- Compensation of Time-of-flight (TOF)
- Distance between the virtual RF cavity and the extraction/injection position ( $t_{src}$  and  $t_{trg}$ ).
- Extraction and injection kicker delays ( $D_{ext}$  and  $D_{inj}$ )

After the synchronization, the phase difference between the SIS18 and the SIS100 revolution frequency markers equals to the sum of  $t_{src}$ ,  $t_{trg}$  and TOF. The extraction kicker will be triggered by the extraction kick delay compensation,  $Th=1SIS1\ 00 + Th=1SIS18\ -TOF - t_{trg} - D_{ext}$  and the injection kicker will be triggered by the injection kick delay compensation,  $Th=1SIS1\ 00 + Th=1SIS1\ 8 - t_{trg} - D_{inj}$ . See Fig. 9. Both extraction and injection kick delay compensation values are provided by the SM.

#### 3.3.2 Beam indication for the beam instrumentation

For the beam instrumentation system at FAIR, the data acquisition is at a sampling rate of 1GS/s and the upper bound sampling time is 100us.

The beginning of the synchronizaiton window is used for the pre-trigger.

### 3.3. Fine synchronization

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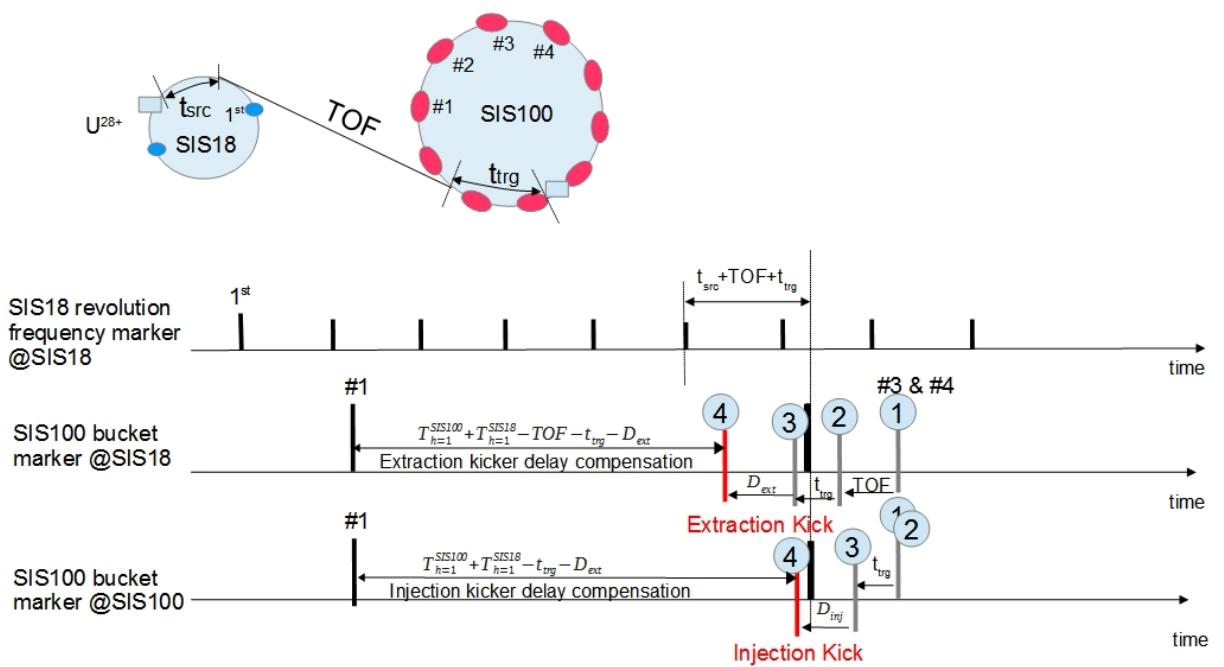


Figure 3.1: Synchronization of the SIS18 extraction and SIS100 injection kicker

# Chapter 4

## Concept of the B2B transfer system

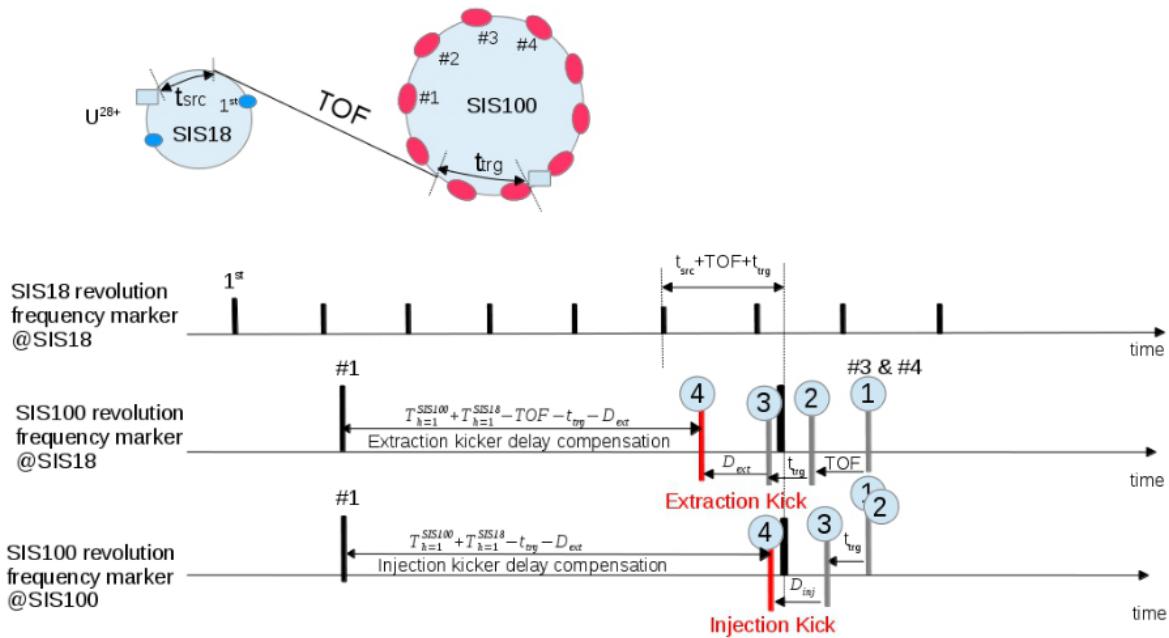


Figure 4.1: The illustration of  $U^{28+}$  B2B transfer from SIS18 to SIS100.

For the proper B2B transfer, the position of the bunch and bucket and the firing of the extraction and injection kicker must be precisely controlled. Fig. 4.1 illustrates the  $U^{28+}$  B2B transfer from SIS18 to SIS100. Before we explain the requirements of the B2B transfer system, some basic factors and their symbols are introduced.

- Bucket pattern ( $d_{pattern}$ , e.g.  $d_{pattern}$  = One SIS18 revolution period. Bucket 3 and 4 will be filled).
- Compensation of Time-of-flight (TOF).
- Distance between the virtual RF cavity and the extraction/injection position ( $t_{src}$  and  $t_{trg}$ ).
- Extraction and injection kicker delays ( $D_{ext}$  and  $D_{inj}$ ).

## 4.1. Realization of the basic B2B principles

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In Fig. 4.1, the SIS18 and SIS100 revolution frequency marker indicate the start of the first bunch and the first bucket. The extraction and injection kicker firing are time delay on the first bars of the SIS100 revolution frequency marker at SIS18 and SIS100, which are called extraction kicker delay and injecton kicker delay. The mentioned four factors are considered on the second bars of the SIS100 revolution frequency marker. After the RF synchronization, the phase difference between the SIS18 and the SIS100 revolution frequency markers equals to the sum of  $t_{src}$ ,  $t_{trg}$  and TOF.

- Extraction kick

For the injection of the bucket 3 and 4, the extraction kicker delay for the first bar of the SIS100 revolution frequency marker is  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18}$ , see ① at the SIS100 revolution frequency marker at SIS18. The extraction kicker must be fired TOF time eariler as the bucket passes the virtual RF cavity, so the extraction kicker delay is  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18} - TOF$ , see ②. The extraction kicker must be fired  $t_{trg}$  time eariler as the bucket passes the virtual RF cavity, so the extraction kicker delay is  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18} - TOF - t_{trg}$ , see ③. The extraction kicker must be fired  $D_{ext}$  time eariler for the kicker preparasion, so the extraction kicker delay is  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18} - TOF - t_{trg} - D_{ext}$ , see ④.

- Injection kick

For the injection of the bucket 3 and 4, the injection kicker delay for the first bar of the SIS100 revolution frequency marker is  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18}$ , see ① at the SIS100 revolution frequency marker at SIS100. The injection kicker must be fired  $t_{trg}$  time eariler as the bucket passes the virtual RF cavity, so the injection kicker delay is  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18} - t_{trg}$ , see ③. The injection kicker must be fired  $D_{inj}$  time eariler for the kicker preparasion, so the injection kicker delay is  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18} - t_{trg} - D_{inj}$ , see ④.

In order to realize the B2B transfer above, we specify how the basic B2B principles are realized for FAIR in Sec. 4.1. The standard procedure is defined and described in Sec. 4.2. The Sec. 4.3 and 4.4 describe the  $U^{28+}$  B2B process from SIS18 to SIS100 with both synchronization methods.

## 4.1 Realization of the basic B2B principles

In this section, I will explain how the basic B2B principles are realized based on the FAIR control system and LLRF system. Fig. 4.2 shows the topology of the B2B transfer system.

### 4.1.1 RF phase difference between two RF system

In order to get the phase difference between two RF systems, we make use of a shared reference signal at both source and target synchrotrons, which is called a Synchronization Reference Signal. It is with the fixed frequency and always in the same phase at two synchrotrons. It is a sine wave, whose frequency is a multiple of the BuTiS T0 100 kHz and whose zero-crossing is aligned with T0 edges in order to ensure the synchronization of the Synchronization Reference Signal in different

#### 4.1. Realization of the basic B2B principles

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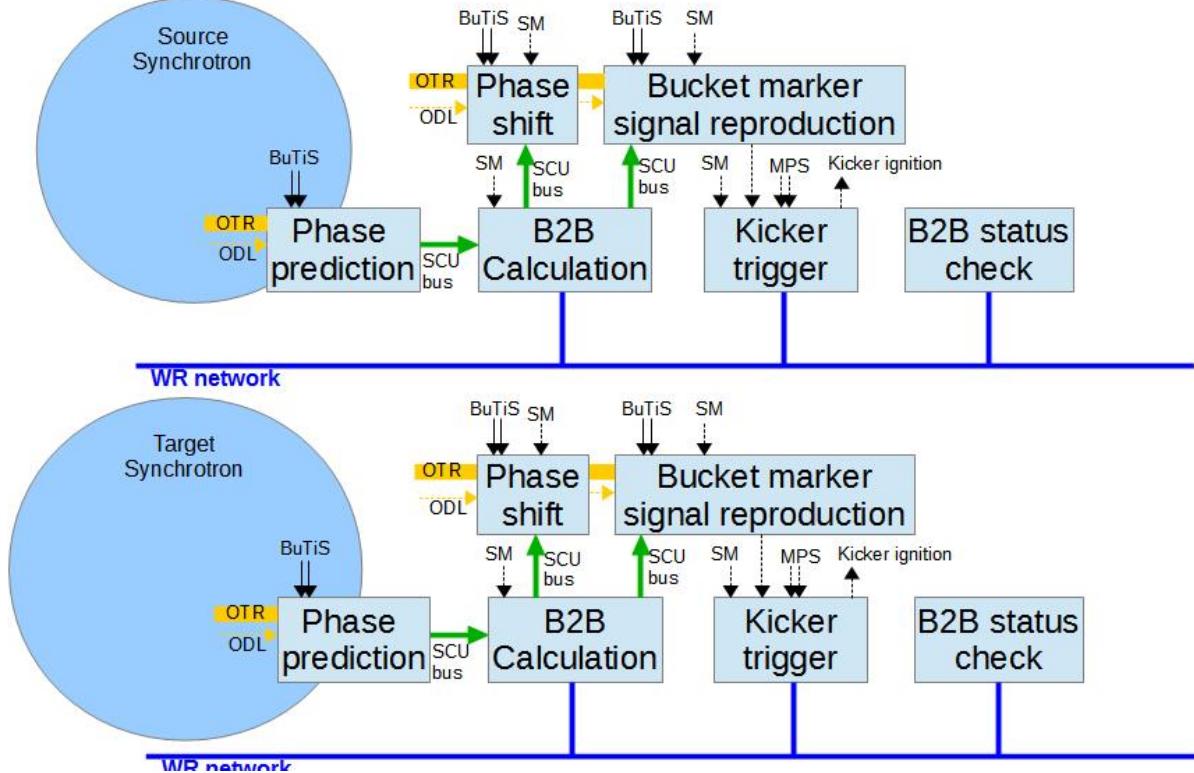


Figure 4.2: The topology of the B2B transfer system

synchrotrons. Fig. 4.3 shows the realization of the phase difference between two RF systems. Fig. 4.3 (a) and (b) illustrate the phase measurement and prediction in the source and target synchrotrons. The red sine waves in Fig. 4.3 (a) and (b) represent the Synchronization Reference Signals (100 kHz) in two synchrotrons and the black waves the Reference RF signals (e.g. 200 kHz) from the Group DDS. The phase difference  $\Delta\varphi_1$  between the Reference RF Signal and the Synchronization Reference Signal is measured by the Phase Advance Measurement (PAM) Module at the source synchrotrons and  $\Delta\varphi_2$  at the target synchrotron. The phase measurement is performed synchronously to an internal clock, which is represented by the blue dots. Based on a series of the phase difference measurements, the phase difference at any T0 edge  $\psi_1$  and  $\psi_2$  could be predicted in every synchrotron by the Phase Advance Prediction (PAP) Module, which is represented by the red diamonds in Fig. 4.3. For more details about the implementation and realization of the PAP and PAM modules, please see “Development of the LLRF system for a deterministic Bunch-to-Bucket transfer for FAIR“. Because the phase prediction is synchronized with T0 clocks and the Synchronization Reference Signal’s phase is  $0^\circ$  at T0 edges,  $\psi_1$  and  $\psi_2$  are the phase of the Reference RF Signals. In order to get the phase difference between two rf systems,  $\psi_1 - \psi_2$ , the phase of the target synchrotron is transferred by the B2B target SCU to the B2B source SCU at the source synchrotron via the WR network. The B2B source and target SCUs are installed in the source and target synchrotrons locally. The transfer of the phase is by the Timing frame TGM\_PHASE\_TIME, see Appendix A.

## 4.1. Realization of the basic B2B principles

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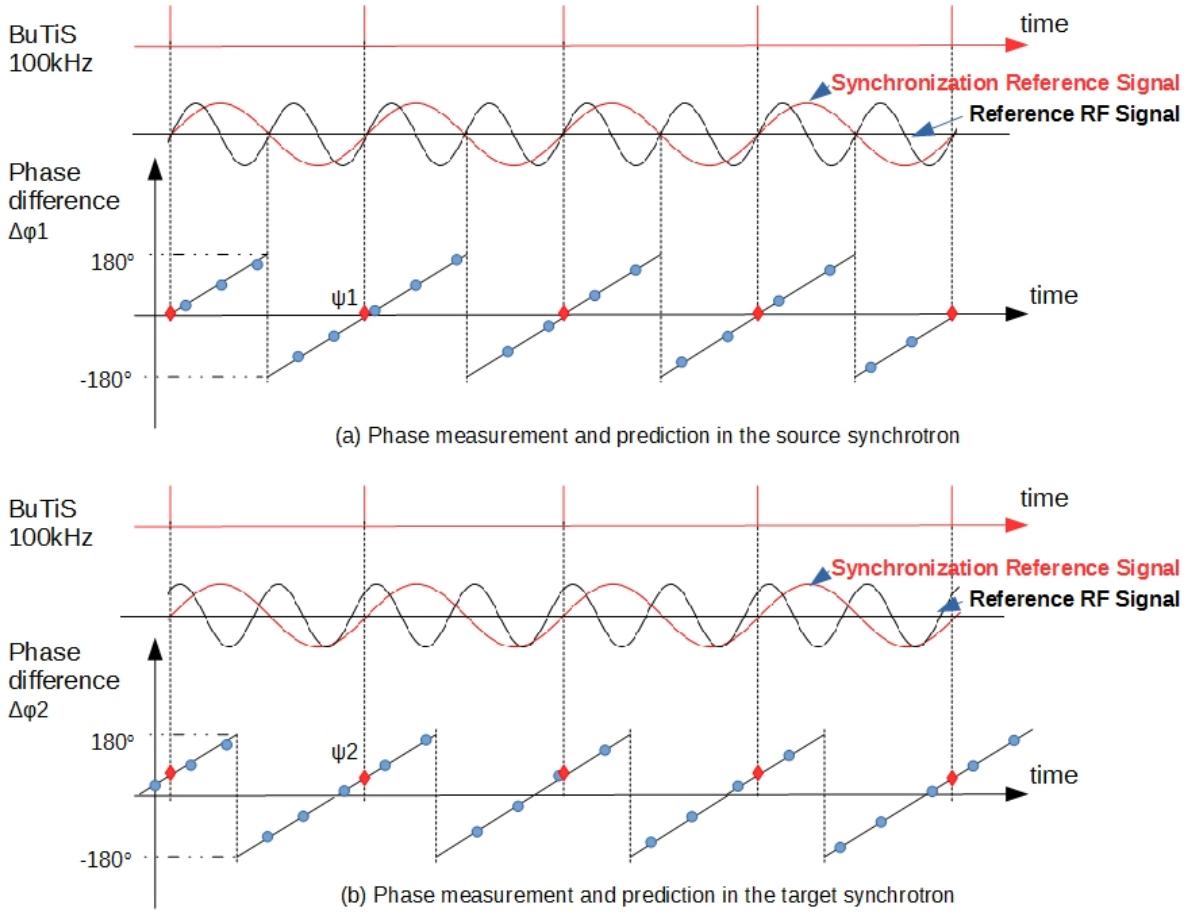


Figure 4.3: The realization of the phase difference between two synchrotrons

### 4.1.2 Rf phase difference synchronous to the absolute timestamp

Both B2B source and target SCUs could get the timestamp of every BuTiS T0 edge. When they receive the timing frame CMD\_START\_B2B at T0 edge, they need maximum 1  $\mu$ s to inform the PAP modules to start the phase prediction respectively. The PAP modules use e.g. 500  $\mu$ s for the prediction and updates the predicted phase every T0 edge. After 500  $\mu$ s, the B2B source and target SCUs need another maximum 1  $\mu$ s to get the predicted phase from the PAP modules and they also get the BuTiS T0 edge timestamp which corresponds to the predicted phase. Then the rf phase difference between two rf systems and the corresponding timestamp are known. Fig. 4.4 shows the synchronization of the rf phase difference to the timestamp.

### 4.1.3 RF synchronization

The B2B transfer system for FAIR is available for both the phase shift and frequency beating methods, see Sec. 2.1.3.

- RF synchronization with the phase shift method

## 4.1. Realization of the basic B2B principles

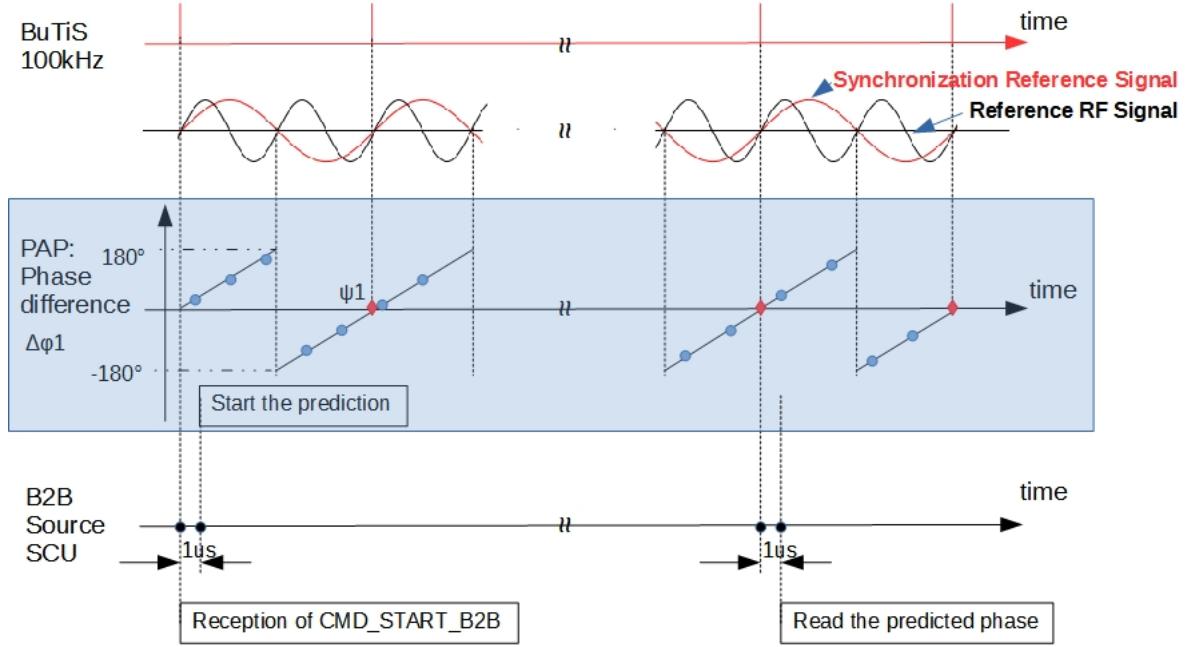


Figure 4.4: The synchronization of the rf phase difference to the timestamp

Eq. 4.1 gives the relation between the required phase shift and the frequency modulation.

$$\Delta\phi = 2\pi \int_{t_0}^{t_0+T} \Delta f(t) dt \quad (4.1)$$

The required phase shift is determined by the frequency offset  $\Delta f$  and the duration of the frequency modulation  $T$ . The phase shift must be executed adiabatically in order to guarantee the bucket size and continuous synchronous phase, see Sec. 2.1.3.1. We introduce a phase shift of up to  $\pm 180^\circ$  in the phase shift for FAIR. With the two criteria, a normalized frequency modulation profile  $f_{actual}$  for  $180^\circ$  can be precalculated. The actual frequency modulation profile  $f_{actual}$  is decided by the normalized frequency modulation profile and the required phase shift, see eq. 4.2. The required phase shift,  $\psi_1 - \psi_2 - (t_{src} + TOF + t_{trg}) \pm 180^\circ$ , is calculated by the B2B source SCU.

$$\frac{\psi_1 - \psi_2 - (t_{src} + TOF + t_{trg}) \pm 180^\circ}{180^\circ} = \frac{f_{actual}}{f_{normalized}} \quad (4.2)$$

Fig. 4.5 shows an example of a normalized and several actual frequency modulation profiles and the corresponding phase shift. The magenta profile is the normalized profile  $f_{normalized}$  with the phase shift of  $180^\circ$ . The blue is  $1/2f_{normalized}$  with the phase shift of  $90^\circ$  and the green is  $1/3f_{normalized}$  with  $60^\circ$ .

The B2B source SCU sends the required phase shift to the Phase Shift Module (PSM), which controls the phase shift of the Reference RF Signal of Group DDS by means of either frequency (Fig. 4.5 (a)) or phase (Fig. 4.5 (b)) modulation. The Reference RF Signal is routed to the different cavity systems by a Switch Matrix to realize the phase shift of all cavities on the synchrotron. For

## 4.1. Realization of the basic B2B principles

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more details about the implementation and realization of the PSM modules, please see “Development of the LLRF system for a deterministic Bunch-to-Bucket transfer for FAIR“.

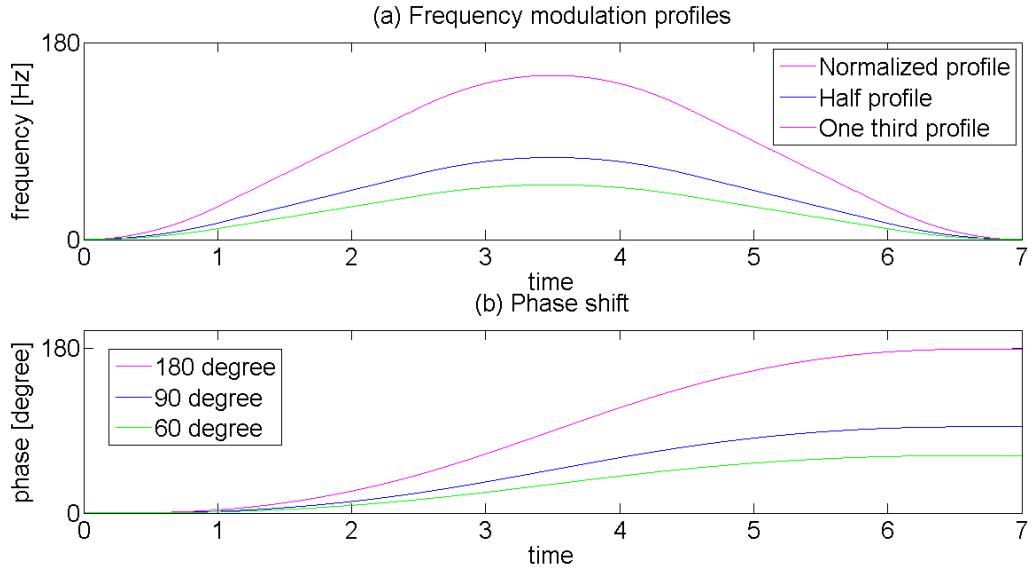


Figure 4.5: The normalized frequency modulation profile and the actual profile

A particular case of the B2B synchronization occurs, when the target synchrotron is empty, i.e. it did not capture any bunch yet, the phase shift can be done for the target synchrotron without adiabatical consideration (e.g. Phase jump is possible). In this case, the B2B source SCU sends the timing frame TGM\_PHASE\_JUMP to the B2B target SCU, which contains the required phase jump. After the B2B target SCU receives the timing frame, it sends the value to the PSM for the phase jump of the Group DDS of the target synchrotron.

- RF synchronization with the frequency beating method

The ratio of the circumference between many pair of machines in FAIR is not a perfect integer, e.g. SIS18 and ESR (injection orbit), SIS100 and CR, CR and HESR. so the RF synchronization is automatically with the frequency beating method. For the pairs with the perfect integer ratio of the circumference, e.g. SIS18 and SIS100, we detune the rf frequency of the source synchrotron by modifying the magnetic field and radial excursion to get the frequency beating.

### 4.1.4 WR network

### 4.1.5 B2B transfer status check

The B2B source SCU shall receive the trigger time of the extraction kicker and actual beam extraction time, TGM\_KICKER\_TRIGGER\_TIME\_S, from the source Trigger SCU via the WR network and also the trigger time of the injection kicker and actual beam injection time, TGM\_KICKER\_TRIGGER\_TIME\_T, from the target Trigger SCU via the WR network. The B2B source SCU is capable of examining the status

## 4.1. Realization of the basic B2B principles

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of the B2B transfer system and transferring the status and the actual beam injection time (TGM\_B2B\_STATUS) to the DM. If all components of the B2B transfer system work correctly and the B2B transfer process is accomplished, the status bit is ‘0’. Otherwise it is ‘1’. For this purpose, it shall do simple checking based on the extraction/injection trigger time and the actual beam extraction/injection time. E.g. Source trigger time < actual beam extraction time.

### 4.1.6 Bucket label

The B2B transfer system for FAIR needs the bucket label not only at the rf flattop, but also during the whole acceleration cycle. The former is used for the normal extraction and injection and the latter is used for the emergency kick of SIS100.

- Bucket label for the normal extraction and injection

For the bucket label for the normal extraction and injection, three steps are necessary. Fig. 4.6 shows these three steps for the  $U^{28+}$  bucket label of SIS100.

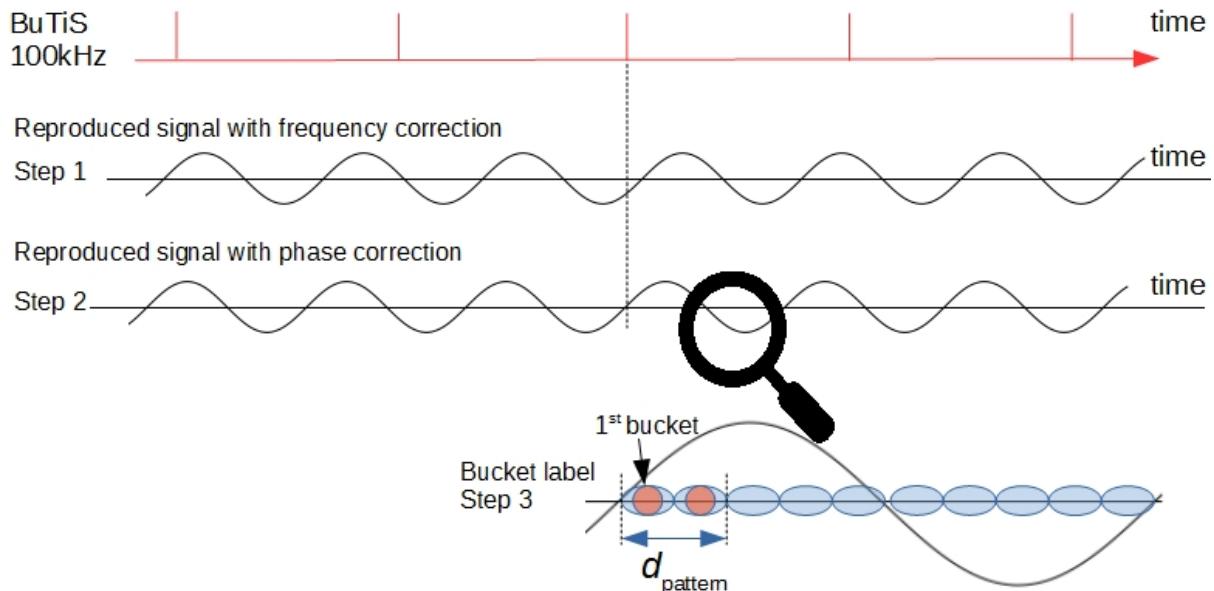


Figure 4.6: The realization of the bucket label for the normal extraction and injection.

- Step 1. Frequency correction

A signal with the same frequency as the Reference RF Signal at the flattop of the target synchrotron (e.g. RF revolution frequency of SIS100) is produced, which is called the reproduced signal. For the B2B transfer system for FAIR, the zero-crossing of the reproduced signal always indicates the start of the 1st bucket.

## 4.1. Realization of the basic B2B principles

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- Step 2. Phase correction

For the phase synchronization with the bucket, the bucket label signal must do phase correction at a specified T0 edge.

- Step 3. Bucket label

The SM manages the bucket pattern with the parameter of  $d_{pattern}$  on the reproduced signal. In Fig. 4.6, the 3rd and 4th buckets will be filled with  $d_{pattern}$ .

- Bunch gap label for the emergency extraction

Only for SIS100 emergency procedure, the bunch gap label is important during the whole acceleration cycle. There are two steps for the realization of the bunch gap label, see Fig. 4.7.

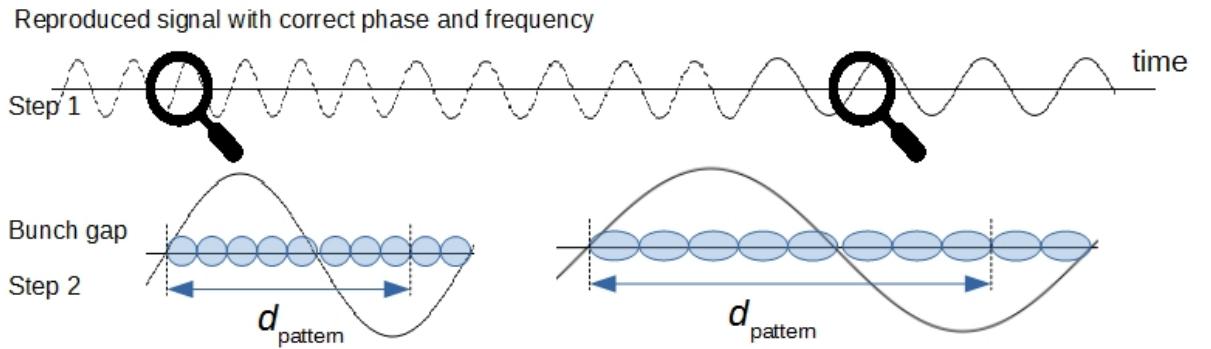


Figure 4.7: The realization of the bunch gap for the emergency extraction.

- Step 1. The reproduced signal is directly distributed from the switch matrix, which synchronizes with the Reference RF Signal in frequency and phase.

- Step 2. Bunch gap label

The SM informs the bunch gap with the parameter of  $d_{pattern}$  on the reproduced signal during the whole acceleration cycle. In Fig. 4.7, the 9th and 10th buckets services as the bunch gap. The  $d_{pattern}$  is with variable value, which is preloaded from the SM and applied to the reproduced signal on T0 edges.

### 4.1.7 Synchronization of the extraction and injection kicker

For the normal B2B extraction/injection, the synchronization window is a gating signal, within which the first reproduced signal will be selected. The extraction and injection kicker are synchronized with the bunch and bucket by the extraction and injection kicker delay compensation. If the inhibit signal of MPS is off, the kicker delay compensation must be considered for the kicker synchronization. The extraction kicker will be triggered by the extraction kick delay compensation,  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18} - TOF - t_{trg} - D_{ext}$  and the injection kicker will be triggered by

## 4.2. Basic procedure of the B2B transfer system for FAIR

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the injection kick delay compensation,  $T_{h=1}^{SIS100} + T_{h=1}^{SIS18} - t_{trg} - D_{inj}$ , see Fig. 4.1. Both extraction and injection kick delay compensation values are provided by the SM. If the inhibit signal is on, the normal injection and extraction trigger signals will be blocked.

For the SIS100 emergency kick, the extraction delay compensation is calculated by  $T_{h=1}^{SIS100} + d_{pattern} - t_{emg} - D_{emg}$ .  $t_{emg}$  is the distance between the virtual RF cavity and the emergency extraction position and  $D_{emg}$  the emergency kicker delay.

### 4.1.8 Beam indication for the beam instrumentation

Two timing frames will be send from the source synchrotron to the DM.

- Timing frame *TGM\_SYNCH\_WIN*

This time frame indicates the start of the synchronization window for the beam instrumentation.

- Timing frame *TGM\_B2B\_STATUS*

The source synchrotron is responsible for examining the status of the B2B transfer system and transferring the status and the actual beam injection time to the DM by *TGM\_B2B\_STATUS*. If all components of the B2B transfer system work correctly and the B2B transfer process is accomplished, the status bit is ‘0’. Otherwise it is ‘1’. For this purpose, The source synchrotron shall do simple checking based on the extraction/injection trigger time, the actual beam extraction/injection kick time. E.g. Source trigger time < actual beam extraction time.

## 4.2 Basic procedure of the B2B transfer system for FAIR

Fig. 4.8 illustrates the basic procedure of the B2B transfer with two different synchronization scenarios. The top part shows the chronological steps with the frequency beating method, while the bottom part shows the steps with the phase shift method. The emergency kickers can be triggered at any time during the acceleration cycle by the MPS. The yellow region shows the synchronization window. The purple region shows the valid time for the emergency kicker.

The B2B transfer process basically needs to follow six steps:

1. The DM announces the B2B transfer and freezes the beam-phase loop, when required.
2. The two synchrotrons measure the rf phase locally.
3. The source synchrotron gathers the measured rf phase from the target synchrotron.
4. The source synchrotron calculates the synchronization window with the kicker delay and sends it to both synchrotrons and to the DM. Besides, it reproduces the bucket label signal at the source synchrotron. For the phase shift method, the source synchrotron generally achieves the phase shift. But when the target synchrotron is empty, the phase shift is achieved at the target synchrotron.

## **4.2. Basic procedure of the B2B transfer system for FAIR**

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5. The trigger signal is generated for the kickers with the delay compensation.

6. The kicker electronics fire the kickers.

## 4.2. Basic procedure of the B2B transfer system for FAIR

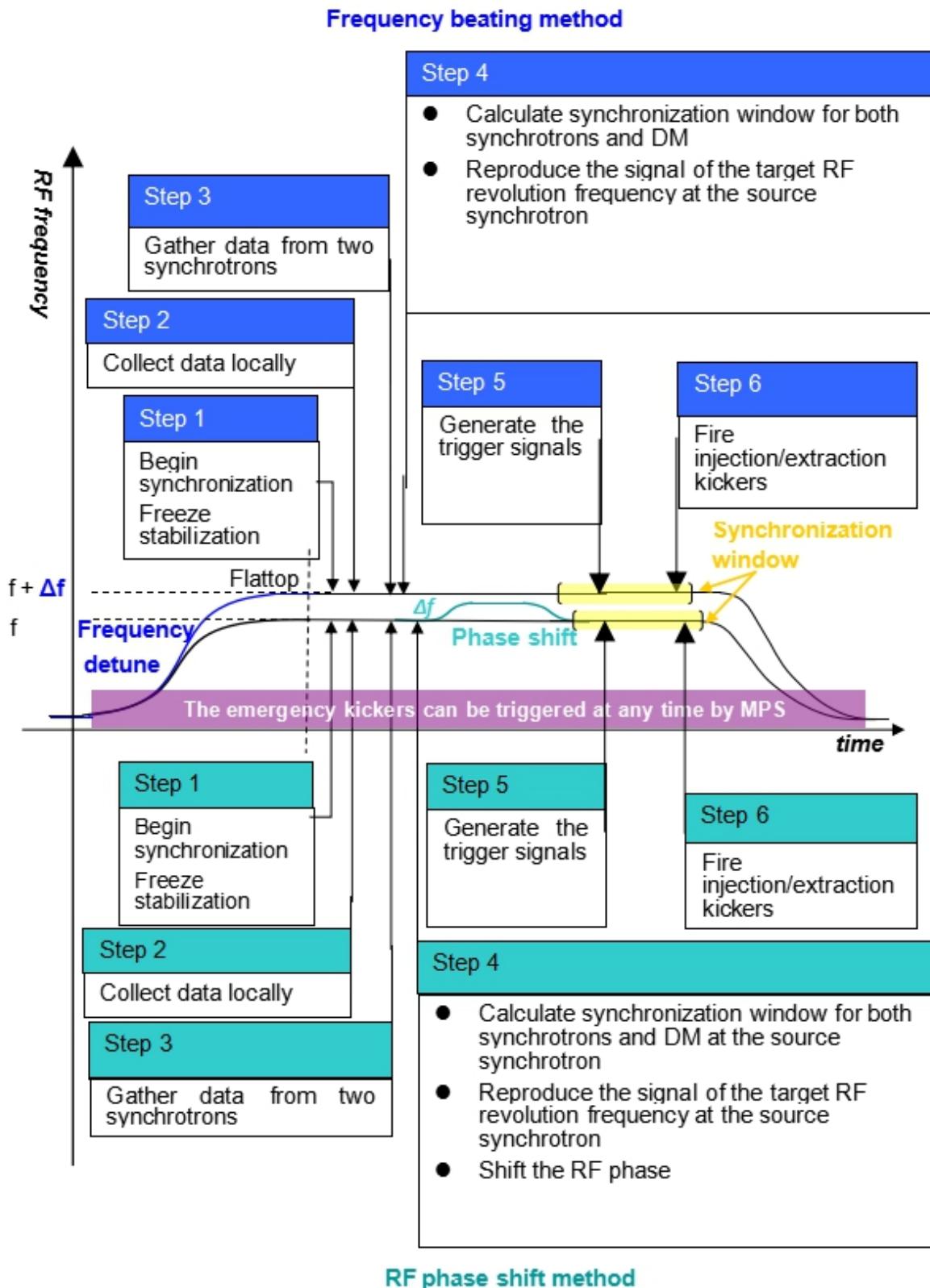


Figure 4.8: The procedure for the B2B transfer within one acceleration cycle. Shown are the frequency beating method (blue, top) and the phase shift method (green, bottom).

### 4.3. Description of the $U^{28+}$ B2B process from SIS18 to SIS100 with the phase shift method

## 4.3 Description of the $U^{28+}$ B2B process from SIS18 to SIS100 with the phase shift method

Here the  $U^{28+}$  at 200 meV/u B2B transfer from SIS18 to SIS100 will be described in detail. Fig. 4.9 shows one SIS18  $U^{28+}$  super cycle. It consists of four SIS18 cycles. Each cycle produces two bunches. From SIS18, four cycles of the  $U^{28+}$ , each of two bunches, are injected into eight out of ten buckets of SIS100. In each SIS18 cycle, the beam is accelerated to the top energy after injection. At the RF flattop, the synchronization is implemented with the phase shift method by modulating rf frequency. The ratio of the SIS100 circumference to the SIS18 circumference is 5. The harmonic number for SIS100 is 10 and for SIS18 is 2. At the flattop, the RF cavity frequency of SIS18 is 1.572 MHz as that of SIS100, so the phase difference between two RF signals is almost constant. To perform the B2B transfer, this phase difference must be corrected to compensate for the required phase difference by phase shift. The frequency ramp at the start and end of the SIS18 frequency modulation must be performed adiabatically. Here we use a parabola rf frequency modulation, more details please see Sec. 5.1.1. Then the time for a phase shift of  $180^\circ$  is 7 ms.

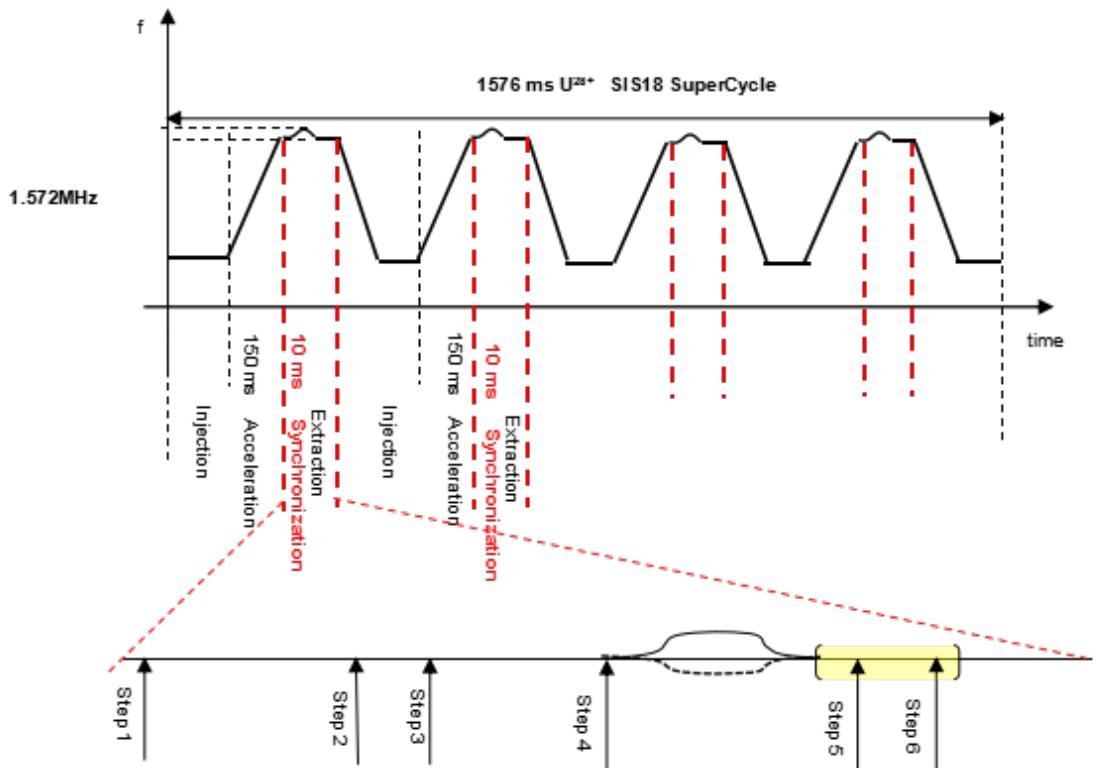


Figure 4.9: The B2B transfer inside one SIS18  $U^{28+}$  Super Cycle with the phase shift method.

## 4.4 Description of the $U^{28+}$ B2B process from SIS18 to SIS100 with the frequency beating method

For the frequency beating method of the  $U^{28+}$  at 200 meV/u B2B transfer from SIS18 to SIS100, we assume to detune 200 Hz for the SIS18 rf signal during the acceleration ramp. The beating frequency is 200 Hz and the synchronization period is 5 ms.

Fig. 4.10 illustrates the standard synchronization process with the frequency beating method. In order to guarantee that eight sequential buckets will be filled by eight bunches.

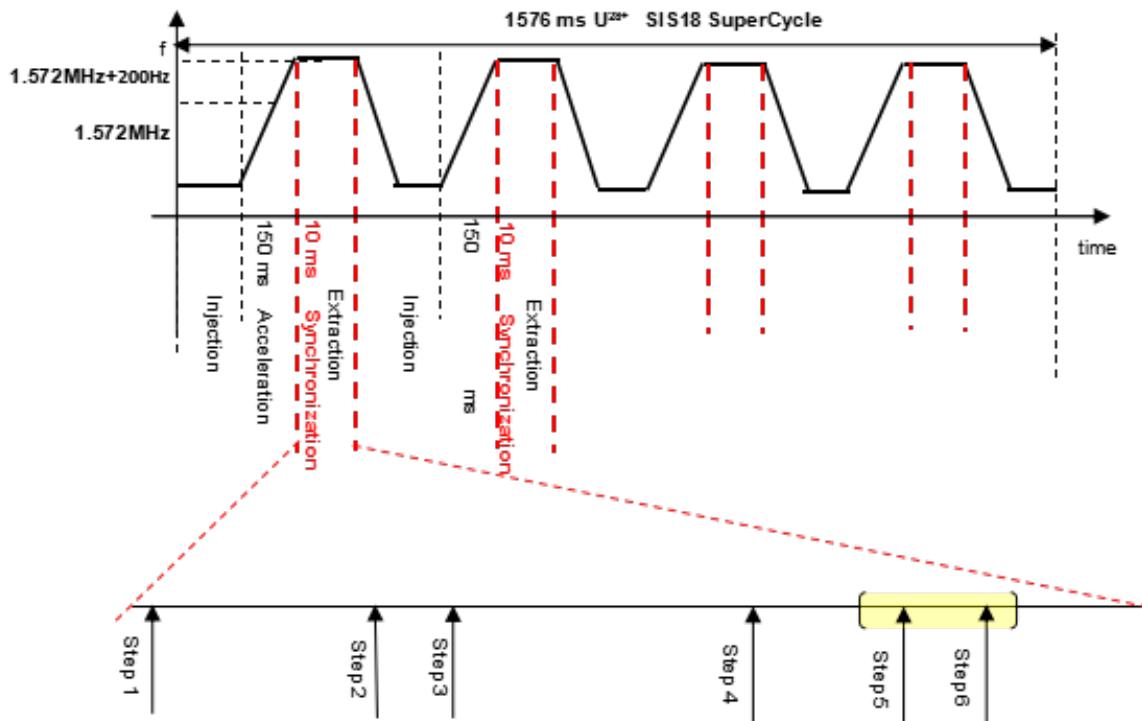


Figure 4.10: The B2B transfer inside one SIS18  $U^{28+}$  Super Cycle with the frequency beating method.

# Chapter 5

## Realization and systematic investigation of the B2B transfer system

This chapter concentrates on the realization and systematic investigation of the B2B transfer system. Both the phase shift and frequency beating synchronization methods are analyzed from the beam dynamic viewpoint. The GMT and kicker systematic considerations of the B2B transfer are investigated. Besides, the test setup from the timing aspect is built. All the analysis are based on  $U^{28+}$  B2B transfer from SIS18 to SIS100.

### 5.1 Investigation of two synchronization methods for $U^{28+}$ B2B transfer from SIS18 to SIS100 from the beam dynamics viewpoint

This section analyzes the phase shift and frequency beating methods from the beam-dynamics viewpoint for the synchronization of SIS18 with SIS100. In this chapter, the circumference of SIS18 and SIS100 are denoted by  $C_{SIS18}$  and  $C_{SIS100}$ , the revolution frequency by  $f_{h=1}^{SIS18}$  and  $f_{h=1}^{SIS100}$  and the rf frequency by  $f_{h=2}^{SIS18}$  and  $f_{h=10}^{SIS100}$ . Since SIS18 and SIS100 harmonic number are 2 and 10, the relationship between the revolution and rf frequencies are  $f_{h=2}^{SIS18} = 2f_{h=1}^{SIS18}$  and  $f_{h=10}^{SIS100} = 10f_{h=1}^{SIS100}$ . Since  $C_{SIS100}$  is five times as long as  $C_{SIS18}$ , we could get the relation  $f_{h=1}^{SIS18} = 5f_{h=1}^{SIS100}$  and  $f_{h=10}^{SIS100} = f_{h=2}^{SIS18}$ .

#### 5.1.1 Phase shift method

To achieve a required phase shift, the RF frequency is modulated away from the nominal value for a period of time and modulated back. Let  $\Delta\phi_{shift}$  be the phase shift to be achieved and  $\Delta f_{rf}(t)$  the RF frequency variation to accomplish it; then,

$$\Delta\phi_{shift} = 2\pi \int_{t_0}^{t_0+T} \Delta f_{rf}(t) dt \quad (5.1)$$

where  $T$  is the period of frequency modulation and  $t_0$  is the time at which the modulation begins. To make the frequency modulation effective, the stabilization

## 5.1. Investigation of two synchronization methods for $U^{28+}$ B2B transfer from SIS18 to SIS100 from the beam dynamics viewpoint

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system, beam-phase loop, must be frozen before the modulation begins.

The following four examples of frequency modulation are analyzed. Case (1) rectangle modulation, Case (2) triangular modulation, Case (3) sinusoidal modulation and Case (4) parabolic modulation. Here I assume the phase shift must be achieved within 7ms. These frequency modulations are shown in Fig. 5.1. All the four modulations give the same phase shift,  $\Delta\phi_{shift} = \pi$ , which is proved by substituting each form of  $\Delta f_{rf}(t)$  into eq. 5.1 and performing integration. Fig. 5.2 shows the time derivation of four rf frequency modulations, which are smaller than the maximum time derivative of rf frequency during the acceleration ramp 64Hz/ms for the adiabaticity consideration. The acceleration ramp is an adiabatical process.

Case (1)

$$\Delta f_{rf}(t) = \begin{cases} 50\text{Hz}/\text{ms} \times (t - t_0) & t_0 + 0 < t \leq t_0 + 2\text{ms} \\ 100\text{Hz} & t_0 + 2 < t \leq t_0 + 5\text{ms} \\ 100\text{Hz} - 50\text{Hz}/\text{ms} \times (t - t_0) & t_0 + 5\text{ms} < t \leq t_0 + 7\text{ms} \end{cases} \quad (5.2)$$

Case (2)

$$\Delta f_{rf}(t) = \begin{cases} \frac{10^3}{7 \times 3.5} \text{Hz}/\text{ms} \times (t - t_0) & t_0 + 0 < t \leq t_0 + 3.5\text{ms} \\ \frac{10^3}{7} \text{Hz} - \frac{10^3}{7 \times 3.5} \text{Hz}/\text{ms} \times (t - t_0 - 3.5\text{ms}) & t_0 + 3.5\text{ms} < t \leq t_0 + 7\text{ms} \end{cases} \quad (5.3)$$

Case (3)

$$\Delta f_{rf}(t) = \frac{10^3}{14} \text{Hz} \times \left(1 - \cos\left(\frac{2\pi}{7} \text{rad}/\text{ms} \times (t - t_0)\right)\right) \quad t_0 + 0 < t \leq t_0 + 7\text{ms} \quad (5.4)$$

Case (4)

$$\Delta f_{rf}(t) = \begin{cases} 30\text{Hz}/\text{ms}^2 \times (t - t_0)^2 & t_0 + 0 < t \leq t_0 + 1\text{ms} \\ 30\text{Hz} + 60\text{Hz}/\text{ms} \times (t - t_0 - 1\text{ms}) & t_0 + 1\text{ms} < t \leq t_0 + 2.5\text{ms} \\ 30\text{Hz}/\text{ms}^2 \times [5\text{ms} - (t - t_0 - 3.5\text{ms})]^2 & t_0 + 2.5\text{ms} < t \leq t_0 + 4.5\text{ms} \\ 30\text{Hz} + 60\text{Hz}/\text{ms} \times (6\text{ms} - t - t_0) & t_0 + 4.5\text{ms} < t \leq t_0 + 6\text{ms} \\ 30\text{Hz}/\text{ms}^2 \times [7\text{ms} - (t - t_0)]^2 & t_0 + 6\text{ms} < t \leq t_0 + 7\text{ms} \end{cases} \quad (5.5)$$

### 5.1.1.1 Longitudinal dynamic analysis for the simulation

In this section, the average radial excursion, the relative momentum shift, synchronous phase, bucket size and adiabaticity of four rf frequency modulations are analyzed.

- Average radial excursion

The average radial excursion is calculated for the four cases of rf frequency modulations by eq. (2.14). Fig. 5.3 shows the calculation result. The maximum average radial excursion of case (1) is  $2.93 \times 10^{-6}$  at the flat of the frequency modulation and that of case (2), case (3) and case (4) are  $4.17 \times 10^{-6}$ ,  $4.18 \times 10^{-6}$  and  $4.38 \times 10^{-6}$  at the midpoint 3.5ms of the frequency modulations. The maximum tolerant radial excursion of SIS18 is  $\pm 2.4 \times 10^{-4}$ . From the view point of the average radial excursion, four cases of rf frequency modulations are available.

## 5.1. Investigation of two synchronization methods for $U^{28+}$ B2B transfer from SIS18 to SIS100 from the beam dynamics viewpoint

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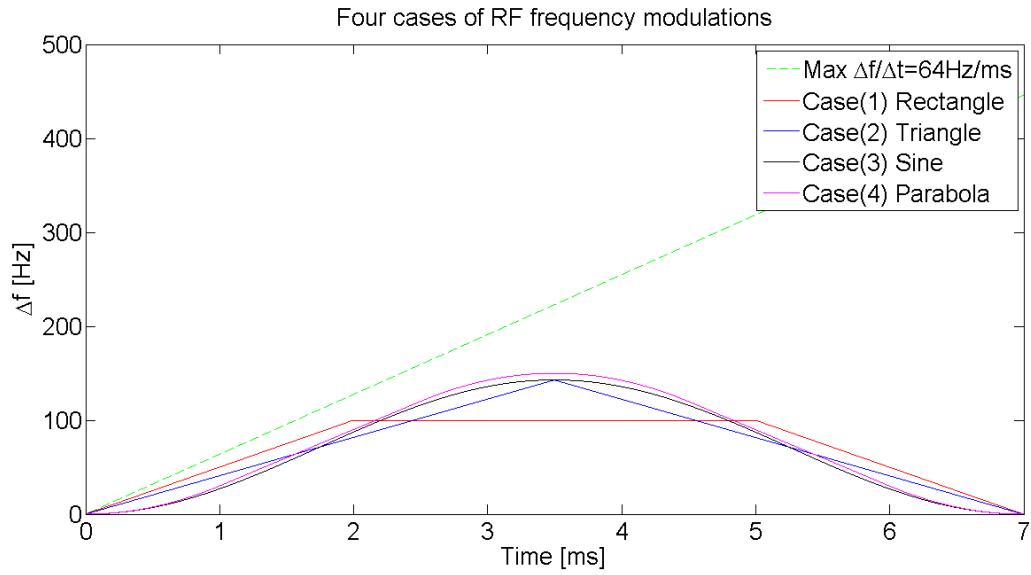


Figure 5.1: Examples of RF frequency modulation.

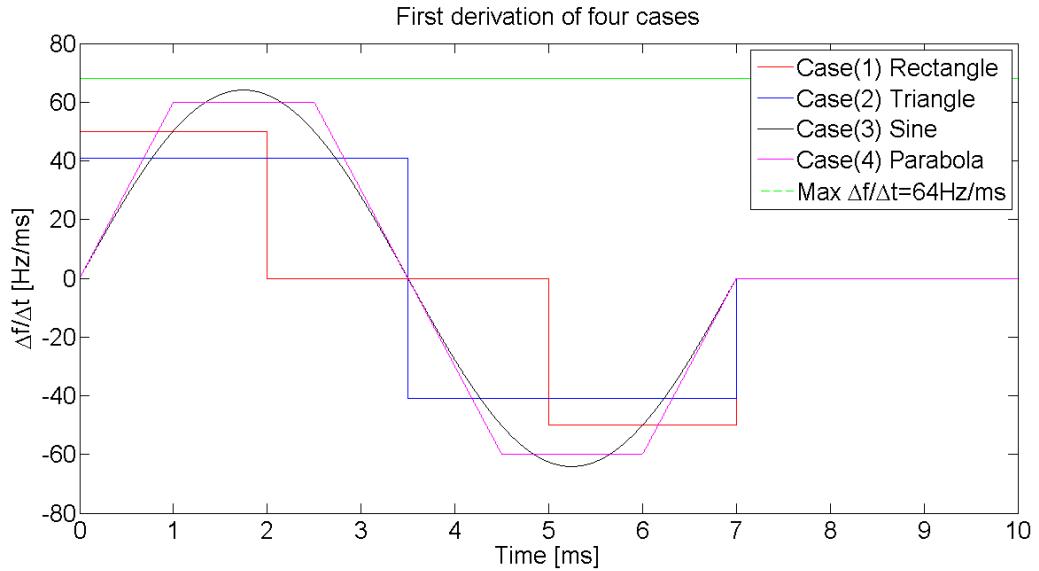


Figure 5.2: Time derivation of four modulations

- Relative momentum shift

The relative momentum shift is calculated for the four cases of rf frequency modulations by eq. (2.15). Fig. 5.4 shows the calculation result. The maximum relative momentum modulation of case (1) is  $9.83 \times 10^{-5}$  at the flat of the frequency modulation and that of case (2), case (3) and case (4) are  $1.38 \times 10^{-4}$ ,  $1.40 \times 10^{-4}$  and  $1.48 \times 10^{-4}$  at the midpoint 3.5ms of the frequency modulations. The maximum tolerant relative momentum shift of SIS18 is  $\pm 0.008$ . From the view point of the relative momentum shift, four cases of rf frequency modulations are available.

- Synchronous phase

## 5.1. Investigation of two synchronization methods for $U^{28+}$ B2B transfer from SIS18 to SIS100 from the beam dynamics viewpoint

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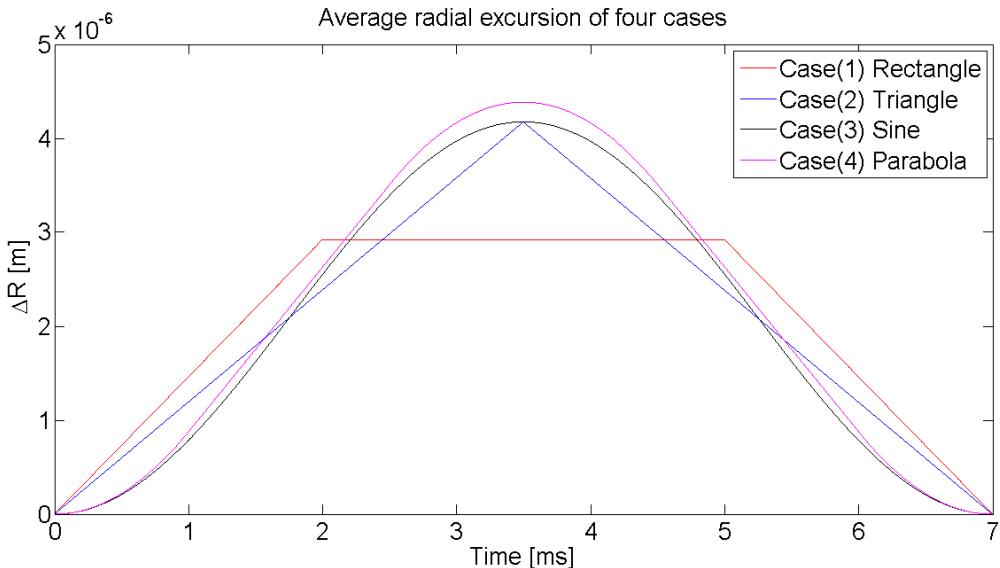


Figure 5.3: Average radial excursions of four cases.

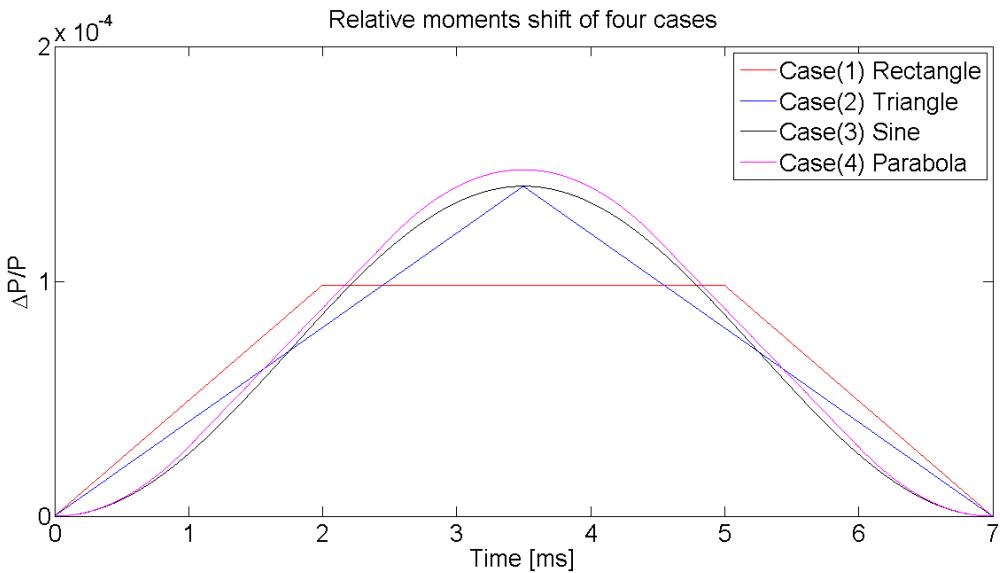


Figure 5.4: Relative momentum shift of four cases.

The rf frequency modulations make the synchronous phase deviate from the nominal value  $0^\circ$ . Fig. 5.5 shows the changes in the synchronous phase,  $\Delta\phi_s(t)$ . It is calculated by introducing values into eq. (??). For case (1), the phase jumps in  $\Delta\phi_s(t)$  appear at the start and end of the frequency modulation, and at two points where the slope of modulation changes from upward to flat and from flat to downward. For case (2), the phase jumps in  $\Delta\phi_s(t)$  appear at the start and end of the frequency modulation, and at the midpoint where the slope of modulation changes from upward to downward. For case (3) and (4), the synchronous phase  $\Delta\phi_s(t)$  during the modulations are continuous. The phase jumps are dangerous for the beam to follow. From the view point of the

## 5.1. Investigation of two synchronization methods for $U^{28+}$ B2B transfer from SIS18 to SIS100 from the beam dynamics viewpoint

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synchronous phase, four cases of rf frequency modulations are available.

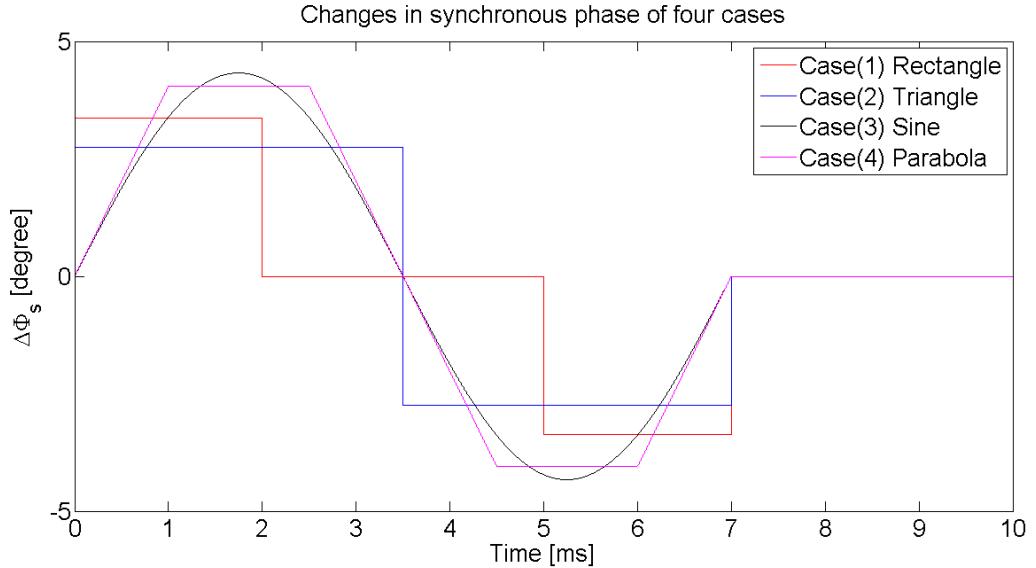


Figure 5.5: Changes in synchronous phase of four cases

- Bucket size

The bucket area factor  $\alpha_b(\phi_s)$  varies during rf frequency modulations. Before the modulations, the synchronous phase  $\phi_s=0^\circ$  and  $\alpha_b(0^\circ)=1$ . By introducing the changes in synchronous phase into eq. (5.6), we get the ratio of bucket areas of a running bucket to the stationary bucket for four cases, see Fig. (5.6).

$$\alpha_b(\phi_s) \approx (1 - \sin\phi_s)(1 - \sin\phi_s) \quad (5.6)$$

The running bucket size is larger than 88% of the stationary bucket for case (1). The running bucket size is larger than 90% of the stationary bucket for case (2). The running bucket size is larger than 86% of the stationary bucket for case (3) and (4). From the viewpoint of the bucket size, four rf frequency modulations are available.

- Adiabaticity

By substituting the values of  $d\Delta\phi_s(t)/dt$  obtained from Fig. 5.5 and the other appropriate values into eq. ??, we can calculate the adiabaticity parameter,  $\varepsilon$ , for the case (3) and (4), see Fig. 5.7. For the case (1) and (2), however, we cannot calculate  $d\Delta\phi_s(t)/dt$  from  $d\Delta\phi_s(t)$  shown in Fig. 5.5, because  $d\Delta\phi_s(t)$  changes discontinuously.

For case (4), the maximum of  $\varepsilon$ , 0.000059, occurs at 1ms, 2.5ms, 4.5ms and 6ms. From Fig. 5.5, we could see the change of the synchronous phase  $d\Delta\phi_s(t)/dt$  is big but smoothly at these time points. For case (3), the maximum of  $\varepsilon$  is 0.000030. So the frequency modulation is adiabatical for case (3) and (4).

## 5.1. Investigation of two synchronization methods for $U^{28+}$ B2B transfer from SIS18 to SIS100 from the beam dynamics viewpoint

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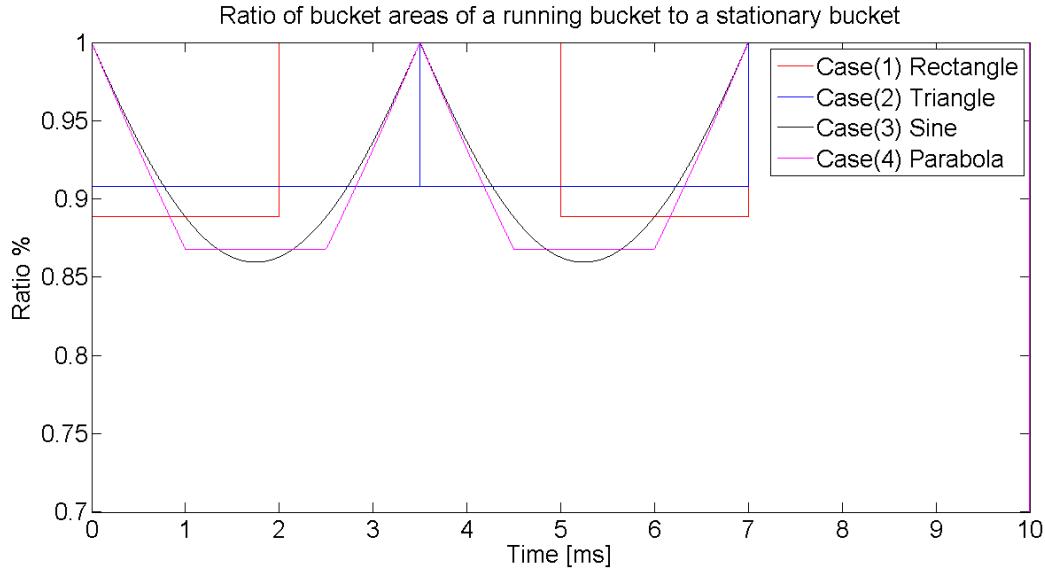


Figure 5.6: Ratio of bucket areas of a running bucket to the stationary bucket of four cases

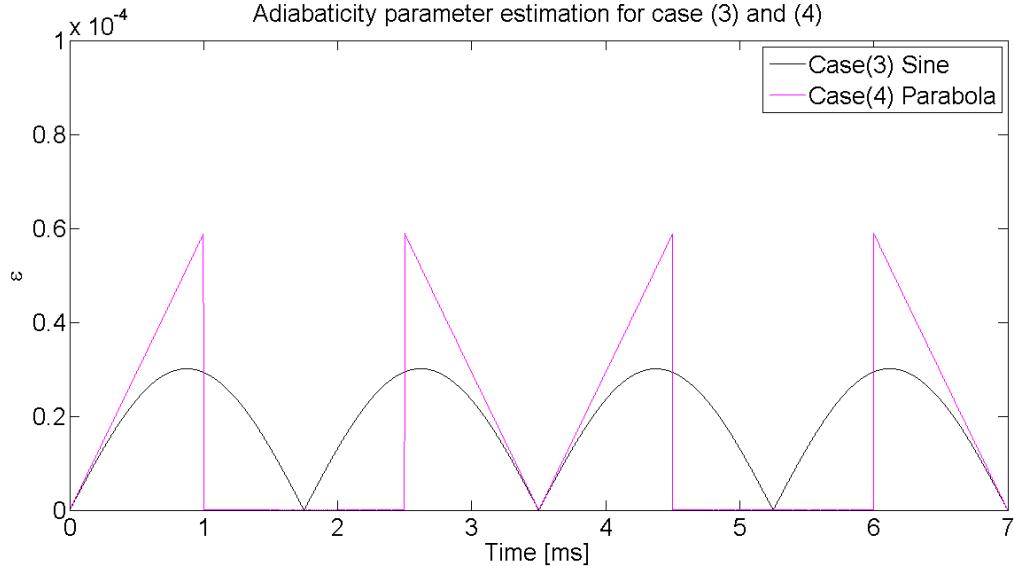


Figure 5.7: Adiabaticity parameter estimation of case (3) and (4)

### 5.1.1.2 Transverse dynamics analysis for the simulations

From Fig. 5.4, we could get the maximum momentum shift for four cases,  $9.83 \times 10^{-5}$ ,  $1.38 \times 10^{-4}$ ,  $1.40 \times 10^{-4}$  and  $1.48 \times 10^{-4}$ . For SIS18, the chromaticity  $Q_x$  and  $Q_y$  is 4.17 and 3.4. Substituting chromaticity and maximum momentum shift into eq. 2.16. We could get the chromatic tune shift  $\Delta Q_x$  and  $\Delta Q_y$  during rf modulations for four cases.

Case (1)

$$\Delta Q_x = 4.17 \times 9.83 \times 10^{-5} = 4.10 \times 10^{-4} \quad (5.7)$$

$$\Delta Q_y = 3.4 \times 9.83 \times 10^{-5} = 3.34 \times 10^{-4} \quad (5.8)$$

Case (2)

$$\Delta Q_x = 4.17 \times 1.38 \times 10^{-4} = 5.75 \times 10^{-4} \quad (5.9)$$

$$\Delta Q_y = 3.4 \times 1.38 \times 10^{-4} = 4.69 \times 10^{-4} \quad (5.10)$$

Case (3)

$$\Delta Q_x = 4.17 \times 1.40 \times 10^{-4} = 5.84 \times 10^{-4} \quad (5.11)$$

$$\Delta Q_y = 3.4 \times 1.40 \times 10^{-4} = 4.76 \times 10^{-4} \quad (5.12)$$

Case (4)

$$\Delta Q_x = 4.17 \times 1.48 \times 10^{-4} = 6.17 \times 10^{-4} \quad (5.13)$$

$$\Delta Q_y = 3.4 \times 1.48 \times 10^{-4} = 5.03 \times 10^{-4} \quad (5.14)$$

The chromatic tune shift for four cases are significantly small, which could be negligible.

### 5.1.2 Frequency beating method

In the case of the frequency beating method, we guarantee the extraction and injection energy always match, which means that the momentum is not affected by the frequency detune, namely  $\Delta p = 0$ , So the frequency beating method has no influence on the transverse dynamics.

#### 5.1.2.1 Longitudinal dynamics analysis of the frequency beating for SIS18

For the frequency beating method, the rf frequency de-tune is done accompanying with the RF ramp. Accepting to decentre the orbit by 8mm for the SIS18

$$\frac{\Delta R}{R} = \pm 2.4 \times 10^{-4} \quad (5.15)$$

From eq. 2.31 and eq. 2.32, the RF frequency and the magnetic field change at the  $U^{28+}$  extraction energy 200MeV/u ( $\gamma_t = 5.8$ ) are

$$\frac{\Delta f}{f} = \pm 2.4 \times 10^{-4} \quad (5.16)$$

$$\frac{\Delta B}{B} = \frac{\Delta f}{f} \gamma_t^2 = \pm 8.1 \times 10^{-3} \quad (5.17)$$

where the maximum RF frequency de-tune is approximate to 370 Hz at 1.57 MHz for the  $U^{28+}$ . Fig. 5.8 shows the rf frequency derivation during the rf ramp. In the simulation, I assume that the rf frequency is detuned at 0.2756s with  $6.08 \times 10^6$ Hz/s, see blue rectangle in Fig. 5.8. For the sake of simplicity, 200 Hz is used as the rf frequency detune. SIS18 needs approximate 33us to reach 200 Hz with  $6.08 \times 10^6$ Hz/s.

From eq. 2.31 and eq. 2.32, we could get the corresponding radial excursion and the magnetic field change during the detune process. The maximum radial excursion is  $-1.27 \times 10^{-4}$  at 33us of the rf detune process. The maximum magnetic field change is  $4.3 \times 10^{-3}$  at 33us of the rf detune process.

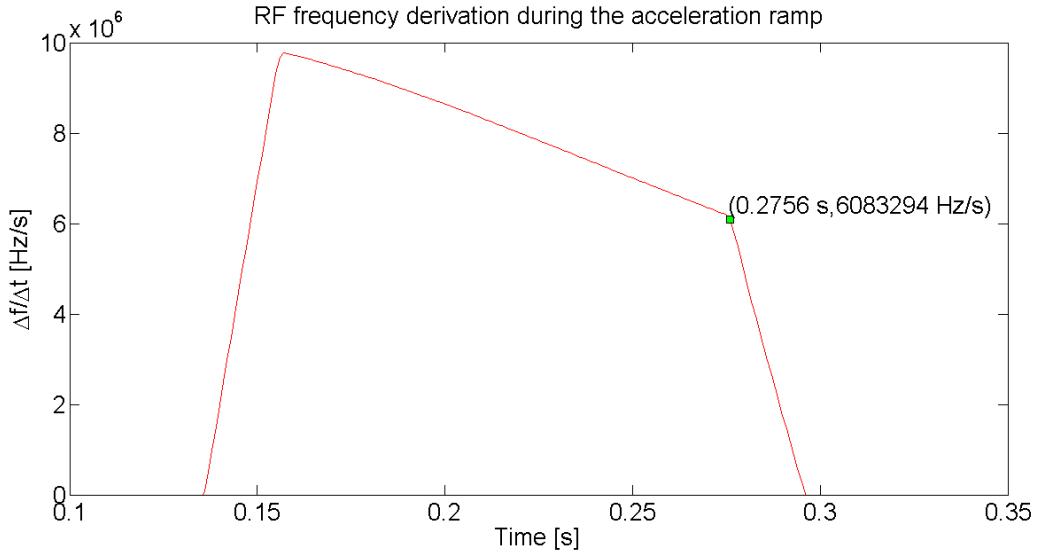


Figure 5.8: RF frequency derivation of the  $U^{28+}$  rf ramp

## 5.2 GMT systematic investigation for the B2B transfer system

GMT system plays a very important role for the B2B transfer system. It is responsible for the data collection, merging and redistribution. The main task of the data merging is the calculation of the synchronization window, within which the bunch could be injected into the correct bucket with the bunch to bucket center mismatch better than  $1^\circ$ . The data collection and redistribution make use of the WR network, so the measurement of the WR network latency is necessary.

### 5.2.1 Calculation of the synchronization window

According to the predicted phase advance, we could calculate the fine time for the alignment of two RF Reference Signals for both the phase shift and frequency beating methods. This time is called “best estimate of alignment” and denoted by  $t_{best}$ . See Fig. 5.9. Because of the uncertainty of the phase advance prediction and rf frequency modulation, the fine alignment lies between  $t_{best} - \delta t_{best}$  and  $t_{best} + \delta t_{best}$ .  $\delta t_{best}$  is called the uncertainty of the alignment and  $[t_{best} - \delta t_{best}, t_{best} + \delta t_{best}]$  is called “probable range of alignment”. In Sec.5.2.1.1 and Sec.5.2.1.2, the calculation of the best estimation of alignment and the probable range of alignment for the phase shift and frequency beating method will be explained. The probable range of alignment is within the synchronization window. For the correct selection of the same revolution frequency marker at different SCUs, the start of the synchronization window must be properly calculated. In Sec. 5.2.1.3, the calculation of the synchronization window will be explained.

For both the phase shift and frequency beating method, the calculation is based on the predicted phase advance. The phase advance prediction module extrapolates the rf phase  $\psi_{h=1}^{SIS100}$  for SIS100 rf h=1 (157kHz) signal and  $\psi_{h=1/5}^{SIS18}$  for SIS18 rf h=1/5 (157kHz) signal at  $t_\psi$ . The more time is spent for the phase advance prediction, the

## 5.2. GMT systematic investigation for the B2B transfer system

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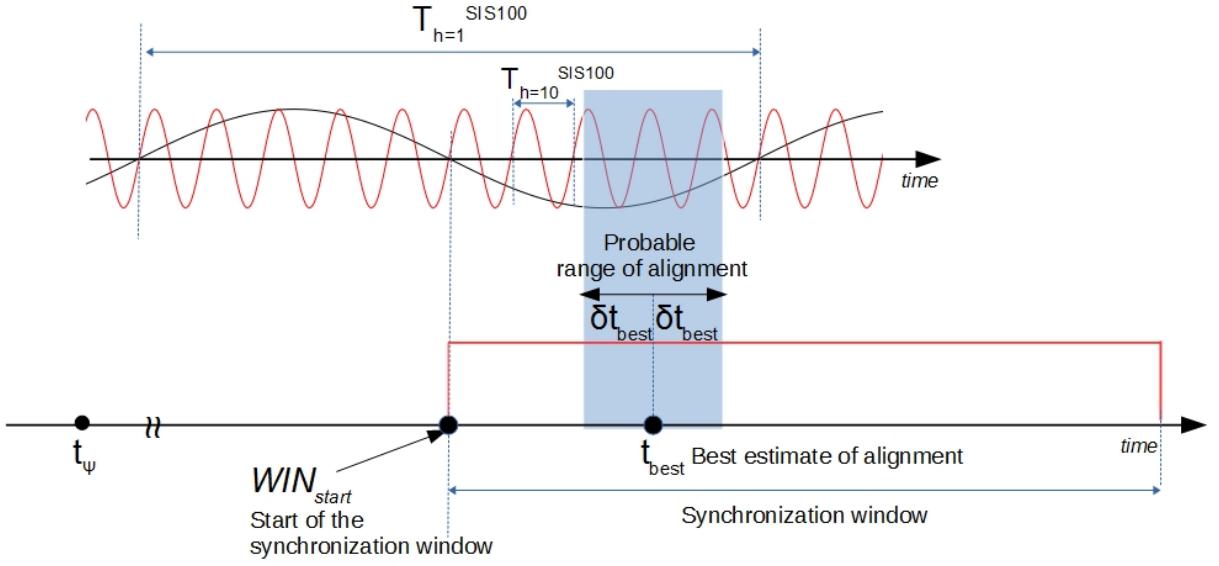


Figure 5.9: The illustration of the best estimate of alignment, the probable range of alignment and the synchronization window

better the predicted phase will be. More details about the phase advance measurement and phase advance prediction modules, please see Tibo's thesis. Fig. 5.10 illustrates some basic definition of symbols for the calculation.  $\phi_{h=2}^{SIS18}$  and  $\phi_{h=10}^{SIS100}$  are individual rf phase of SIS18 and SIS100 rf reference signals at  $t_\psi$ . The relationship between  $\phi_{h=2}^{SIS18}$ ,  $\phi_{h=10}^{SIS100}$  and  $\psi_{h=1/5}^{SIS18}$ ,  $\psi_{h=1}^{SIS100}$  are given by eq. 5.18 and eq. 5.19.

$$\phi_{h=2}^{SIS18} = \frac{\frac{\psi_{h=1/5}^{SIS18}}{360^\circ} \times T_{h=1/5}^{SIS18} \bmod T_{h=2}^{SIS18}}{T_{h=2}^{SIS18}} \times 360^\circ \quad (5.18)$$

$$\phi_{h=10}^{SIS100} = \frac{\frac{\psi_{h=1}^{SIS100}}{360^\circ} \times T_{h=1}^{SIS100} \bmod T_{h=10}^{SIS100}}{T_{h=10}^{SIS100}} \times 360^\circ \quad (5.19)$$

substituting  $T_{h=2}^{SIS18} \times 10 = T_{h=1/5}^{SIS18}$ ,  $T_{h=10}^{SIS100} \times 10 = T_{h=1}^{SIS100}$  into eq.5.18 and eq.5.19 yields

$$\phi_{h=2}^{SIS18} = \frac{\frac{\psi_{h=1/5}^{SIS18} \times 10}{360^\circ} \times T_{h=2}^{SIS18} \bmod T_{h=2}^{SIS18}}{T_{h=2}^{SIS18}} \times 360^\circ \quad (5.20)$$

$$\phi_{h=10}^{SIS100} = \frac{\frac{\psi_{h=1}^{SIS100} \times 10}{360^\circ} \times T_{h=10}^{SIS100} \bmod T_{h=10}^{SIS100}}{T_{h=10}^{SIS100}} \times 360^\circ \quad (5.21)$$

Here we explain the inevitable uncertainty of the phase advance prediction and rf frequency modulation.

- Uncertainty of the predicted phase advance

If the phase prediction time is 500us, the uncertainty of the predicted phase advance  $\delta t_\psi$  is 100ps. We calculate the uncertainty of the predicted phase advance,  $\delta\psi_{h=1}^{SIS100}$  and  $\delta\psi_{h=1/5}^{SIS18}$ , from the time to phase domain.

$$\delta t_\psi = 100ps \quad (5.22)$$

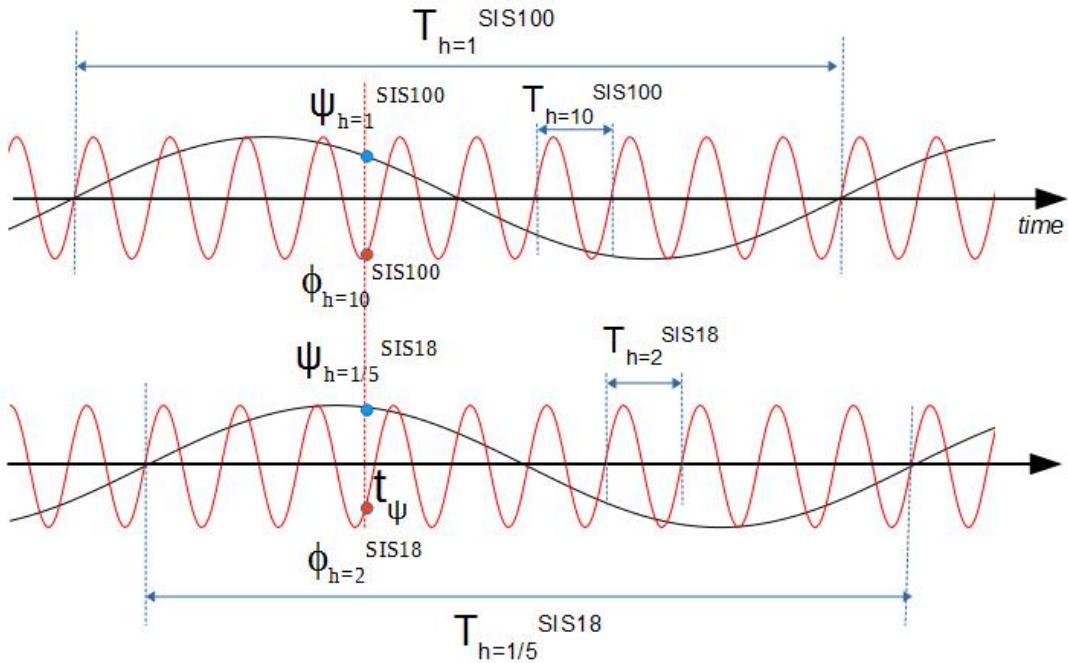


Figure 5.10: The illustration of symbols for the calculation

$$\delta\psi_{h=1/5}^{SIS18} = \delta\psi_{h=1}^{SIS100} = \frac{100ps}{1/157kHz} \times 360^\circ \approx 0.006^\circ \quad (5.23)$$

Based on the eq. 5.23, eq. 5.20 and eq. 5.21, the uncertainty of the phase at the rf reference frequencies of SIS18 and SIS100,  $\delta\phi_{h=10}^{SIS100}$  and  $\delta\phi_{h=2}^{SIS18}$ , is calculated.

$$\delta\phi_{h=2}^{SIS18} = \sqrt{\left(\frac{\partial\phi_{h=2}^{SIS18}}{\partial\psi_{h=2}^{SIS18}}\delta\psi_{h=2}^{SIS18}\right)^2} = \sqrt{(10 \times \delta\psi_{h=2}^{SIS18})^2} = 0.06^\circ \quad (5.24)$$

$$\delta\phi_{h=10}^{SIS100} = \sqrt{\left(\frac{\partial\phi_{h=10}^{SIS100}}{\partial\psi_{h=1}^{SIS100}}\delta\psi_{h=1}^{SIS100}\right)^2} = \sqrt{(10 \times \delta\psi_{h=1}^{SIS100})^2} = 0.06^\circ \quad (5.25)$$

- Uncertainty of the rf frequency modulation

For the rf frequency modulation, the jitter is  $0.2^\circ$  at 5.4MHz. We calculate the jitter in time domain, see eq. 5.26.

$$\delta\Delta f_{(t)} = \frac{0.2^\circ}{360^\circ} \times \frac{1}{5.4MHz} = 100ps \quad (5.26)$$

### 5.2.1.1 The best estimate of alignment and the probable range of alignment for the phase shift method

Different relation between  $\phi_{h=2}^{SIS18}$  and  $\phi_{h=10}^{SIS100}$  has different required phase adjustment for SIS18. Fig. 5.11 illustrates all scenarios of their relation and the required

## 5.2. GMT systematic investigation for the B2B transfer system

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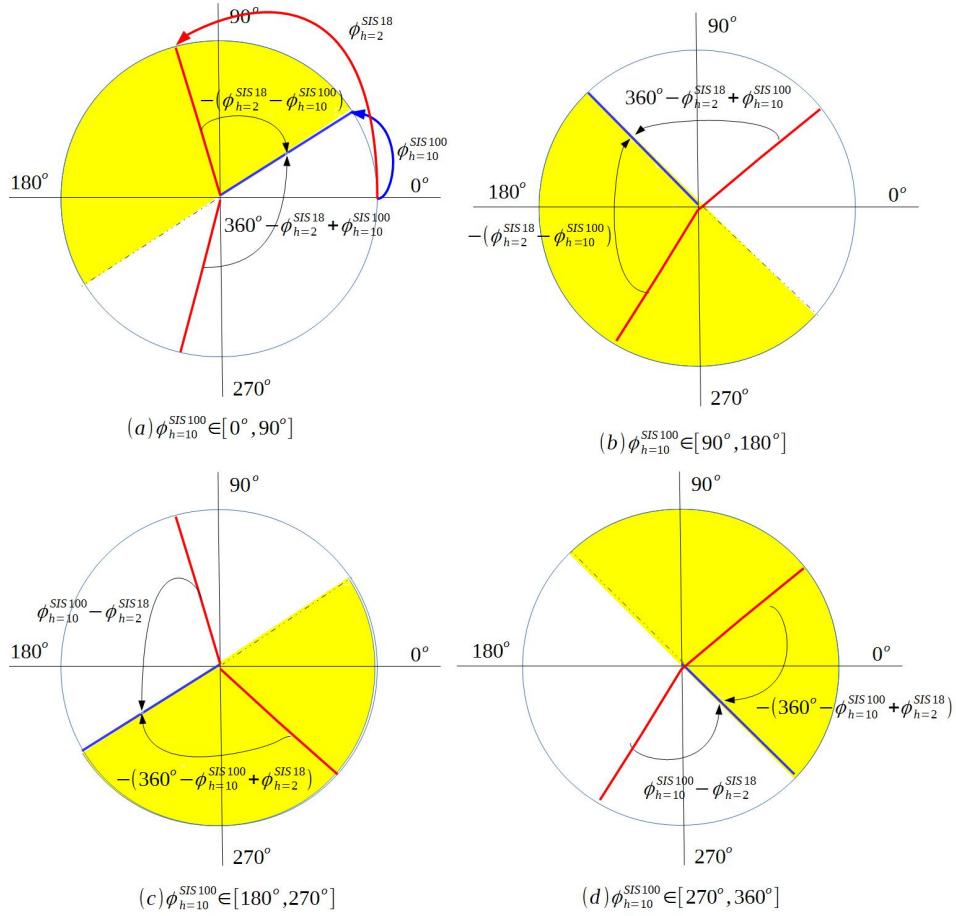


Figure 5.11: Scenarios for the phase shift method

phase adjustment for each scenario. We would like to introduce a phase shift of up to  $\pm 180^\circ$ . The blue and red line represents the phase of SIS100 and SIS18 RF Reference Signal. The clockwise arrow from the SIS18 to SIS100 rf phase represents the negative phase adjustment for SIS18 and the anticlockwise represents the positive phase adjustment. The required phase adjustment of SIS18 is denoted by  $\Delta\phi_{shift}$ .

- Scenario (a):  $\phi_{h=10}^{SIS100} \in [0, 90^\circ]$ , see Fig. 5.12 (a).
- $\phi_{h=10}^{SIS100} < \phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100} + 180^\circ$ , which denotes by the yellow semicircle in Fig. 5.12 (a). The phase adjustment is

$$\Delta\phi_{shift} = -(\phi_{h=2}^{SIS18} - \phi_{h=10}^{SIS100}) \quad (5.27)$$

- $\phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100}$  or  $\phi_{h=2}^{SIS18} > \phi_{h=10}^{SIS100} + 180^\circ$ , which denotes by the white semicircle in Fig. 5.12 (a). The phase adjustment is

$$\Delta\phi_{shift} = 360^\circ - \phi_{h=2}^{SIS18} + \phi_{h=10}^{SIS100} \quad (5.28)$$

- Scenario (b):  $\phi_{h=10}^{SIS100} \in [90, 180^\circ]$ , see Fig. 5.12 (b).
- $\phi_{h=10}^{SIS100} < \phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100} + 180^\circ$ , which denotes by the yellow semicircle in Fig. 5.12 (b). The phase adjustment is

$$\Delta\phi_{shift} = -(\phi_{h=2}^{SIS18} - \phi_{h=10}^{SIS100}) \quad (5.29)$$

## 5.2. GMT systematic investigation for the B2B transfer system

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- $\phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100}$  or  $\phi_{h=2}^{SIS18} > \phi_{h=10}^{SIS100} + 180^\circ$ , which denotes by the white semicircle in Fig. 5.12 (b). The phase adjustment is

$$\Delta\phi_{shift} = 360^\circ - \phi_{h=2}^{SIS18} + \phi_{h=10}^{SIS100} \quad (5.30)$$

- Scenario (c):  $\phi_{h=10}^{SIS100} \in [180, 270^\circ]$ , see Fig. 5.12 (c). The phase adjustment is

- $\phi_{h=2}^{SIS18} > \phi_{h=10}^{SIS100}$  or  $\phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100} + 180^\circ - 360^\circ$ , which denotes by the yellow semicircle in Fig. 5.12 (c). The phase adjustment is

$$\Delta\phi_{shift} = -(360^\circ - \phi_{h=10}^{SIS100} + \phi_{h=2}^{SIS18}) \quad (5.31)$$

- $\phi_{h=10}^{SIS100} - 180^\circ < \phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100}$ , which denotes by the white semicircle in Fig. 5.12 (c). The phase adjustment is

$$\Delta\phi_{shift} = \phi_{h=10}^{SIS100} - \phi_{h=2}^{SIS18} \quad (5.32)$$

- Scenario (d):  $\phi_{h=10}^{SIS100} \in [270, 360^\circ]$ , see Fig. 5.12 (d).

- $\phi_{h=10}^{SIS100} - 180^\circ < \phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100}$ , which denotes by the yellow semicircle in Fig. 5.12 (d). The phase adjustment is

$$\Delta\phi_{shift} = \phi_{h=10}^{SIS100} - \phi_{h=2}^{SIS18} \quad (5.33)$$

- $\phi_{h=2}^{SIS18} > \phi_{h=10}^{SIS100}$  or  $\phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100} + 180^\circ - 360^\circ$ , which denotes by the white semicircle in Fig. 5.12 (d).

$$\Delta\phi_{shift} = -(360^\circ - \phi_{h=10}^{SIS100} + \phi_{h=2}^{SIS18}) \quad (5.34)$$

The phase adjustment is achieved by the phase shift method within the upper bound time,  $T_{phase\_shift}^{upper\_bound}$ . For the  $U^{28+}$  B2B transfer from SIS18 to SIS100, we assume that  $T_{phase\_shift}^{upper\_bound}$  equals to 7ms, which means that the phase shift  $\Delta\phi_{shift}$  is achieved within 7ms. So the best estimate of alignment is expressed by

$$t_{best} = t_\psi + T_{phase\_shift}^{upper\_bound} \quad (5.35)$$

The uncertainty in the phase prediction  $\delta t_\psi$  is 100ps, see eq. 5.22. The phase shift uncertainty  $\delta\Delta\phi_{phase}$  is caused by the rf frequency modulation, whose jitter is 100ps, see eq. 5.26. The phase shift uncertainty equals to the uncertainty in the phase shift upper bound time,  $\delta T_{phase\_shift}^{upper\_bound} = 100$ ps. Both cause an uncertainty in the best estimate of alignment  $t_{best}$ .

$$\begin{aligned} \delta t_{best} &= \sqrt{\left(\frac{\partial t_{best}}{\partial t_\psi} \delta t_\psi\right)^2 + \left(\frac{\partial t_{best}}{\partial T_{phase\_shift}^{upper\_bound}} \delta T_{phase\_shift}^{upper\_bound}\right)^2} \\ &= \sqrt{(\delta t_\psi)^2 + (T_{phase\_shift}^{upper\_bound})^2} = \sqrt{100ps^2 + 100ps^2} \approx 140ps \end{aligned} \quad (5.36)$$

The uncertainty of the alignment for the phase shift method is about 140ps. So the proper range of alignment is  $[t_{best}-140ps, t_{best}+140ps]$  for  $U^{28+}$  B2B transfer from SIS18 to SIS100.

### 5.2.1.2 The best estimate of alignment and the probable range of alignment for the frequency beating method

Fig. 5.12 illustrates two scenarios for the frequency beating method. With the frequency beating method, SIS18 can only achieve positive phase adjustment, which is denoted by  $\Delta\phi_{adjustment}$ . Eq. 5.37 shows the best estimate of alignment for the phase adjustment of  $\Delta\phi_{adjustment}$ .

$$t_{best} = t_\psi + \frac{\Delta\phi_{adjustment}}{360^\circ \times \Delta f} \quad (5.37)$$

where  $\Delta f$  is the beating frequency.

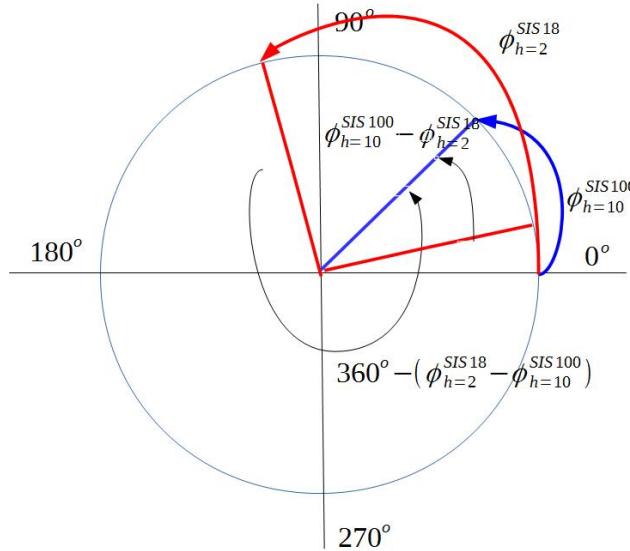


Figure 5.12: Two scenarios for the frequency beating method

According to the relation between  $\phi_{h=2}^{SIS18}$  and  $\phi_{h=10}^{SIS100}$ , there are two scenarios, see Fig. 5.12.

- Scenario (a):  $\phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100}$

$$\Delta\phi_{adjustment} = \phi_{h=10}^{SIS100} - \phi_{h=2}^{SIS18} \quad (5.38)$$

Replacing  $\Delta\phi_{adjustment}$  in eq. 5.37 with eq. 5.38, we have

$$t_{best} = t_\psi + \frac{\phi_{h=10}^{SIS100} - \phi_{h=2}^{SIS18}}{360^\circ \times \Delta f} \quad (5.39)$$

- Scenario (b):  $\phi_{h=2}^{SIS18} \geq \phi_{h=10}^{SIS100}$

$$\Delta\phi_{adjustment} = 360^\circ - (\phi_{h=2}^{SIS18} - \phi_{h=10}^{SIS100}) \quad (5.40)$$

Replacing  $\Delta\phi_{adjustment}$  in eq. 5.37 with eq. 5.40, we have

$$t_{best} = t_\psi + \frac{360^\circ - (\phi_{h=2}^{SIS18} - \phi_{h=10}^{SIS100})}{360^\circ \times \Delta f} \quad (5.41)$$

## 5.2. GMT systematic investigation for the B2B transfer system

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Based on these two scenarios, we could deduce the formula for the best estimate of alignment.

$$t_{best} = t_\psi + \frac{\Delta n \times 360^\circ - (\phi_{h=2}^{SIS18} - \phi_{h=10}^{SIS100})}{360^\circ \times \Delta f} \quad (5.42)$$

where  $\Delta n$  equals 0 when  $\phi_{h=2}^{SIS18} < \phi_{h=10}^{SIS100}$  and equals 1 when  $\phi_{h=2}^{SIS18} \geq \phi_{h=10}^{SIS100}$ .

The uncertainty of the alignment is the result of the propagation of uncertainties of the phase prediction and rf frequency detune, see eq. 5.43. Because the rf frequency detune has the long term stability,  $\int \delta \Delta f = 0$ , the uncertainty caused by rf frequency detune is 0. The uncertainty of the phase prediction  $\phi_{h=2}^{SIS18}$  and  $\phi_{h=10}^{SIS100}$  is  $0.06^\circ$ , see eq. 5.24 and eq. 5.25.  $\Delta f$  is 200Hz. The maximum  $\Delta n \times 2\pi - (\phi_{h=2}^{SIS18} - \phi_{h=10}^{SIS100})$  is  $2\pi$ .

$$\begin{aligned} \delta t_{best} &= \sqrt{\left(\frac{\partial t_{best}}{\partial \phi_{h=2}^{SIS18}} \delta \phi_{h=2}^{SIS18}\right)^2 + \left(\frac{\partial t_{best}}{\partial \phi_{h=10}^{SIS100}} \delta \phi_{h=10}^{SIS100}\right)^2 + \left(\frac{\partial t_{best}}{\partial \Delta f} \delta \Delta f\right)^2} \\ &= \sqrt{\left(\frac{-1}{2\pi \times \Delta f} \delta \phi_{h=2}^{SIS18}\right)^2 + \left(\frac{1}{2\pi \times \Delta f} \delta \phi_{h=10}^{SIS100}\right)^2 + \left(-\frac{\Delta n \times 2\pi - (\phi_{h=2}^{SIS18} - \phi_{h=10}^{SIS100})}{2\pi \times \Delta f^2} \delta \Delta f\right)^2} \\ &\leq \sqrt{\left(\frac{-1}{2\pi \times 200} 0.06^\circ\right)^2 + \left(\frac{1}{2\pi \times 200} 0.06^\circ\right)^2 + 0} \\ &\approx 1.178us \end{aligned} \quad (5.43)$$

From eq. 5.43 we could get the uncertainty of the alignment is 1.178us, so the probable range of alignment is  $[t_{best} - 1.178us, t_{best} + 1.178us]$ .

### 5.2.1.3 Calculation the synchronization window and its accuracy

In the last section, we get the probable range of alignment, within which the two rf frequency signals will be fine aligned with each other. The synchronization window is used to select the revolution frequency marker for the extraction and injection kicker firing, which is closest to the probable range of alignment, See Fig. 5.13. For the selection, the length of the synchronization window must be a least one SIS100 revolution period. The best estimate of the start of the synchronization window is exactly half revolution period before the selected revolution frequency marker. The blue and orange rectangles represent two scenarios of the probable range of alignment. In Fig. 5.13, the 2nd revolution frequency marker is the closest one to the probable range of alignment. The best estimate of the start of the synchronization window aligns with the negative zero crossing point of the revolution marker signal.

For SIS100, the rf phase of the revolution frequency is  $\psi_{h=1}^{SIS100}$  at  $t_\psi$ . We could calculate the rf phase  $\psi_{s.alignment}$  at the start of the probable rang of alignment,  $t_{best} - \delta t_{best}$ .

$$\psi_{s.alignment} = \frac{(t_{best} - \delta t_{best} - t_\psi - \frac{360^\circ - \psi_{h=1}^{SIS100}}{360^\circ} \times T_{h=1}^{SIS100}) \mod T_{h=1}^{SIS100} \times 360^\circ}{T_{h=1}^{SIS100}} \quad (5.44)$$

For the calculation of the best estimate of the start of the synchronization window, there are two scenarios.  $\Delta t_{win.correct}$  is the time correction for the start of the probable range of alignment to the best estimate of the start of the synchronization window, see Fig. 5.13.

## 5.2. GMT systematic investigation for the B2B transfer system

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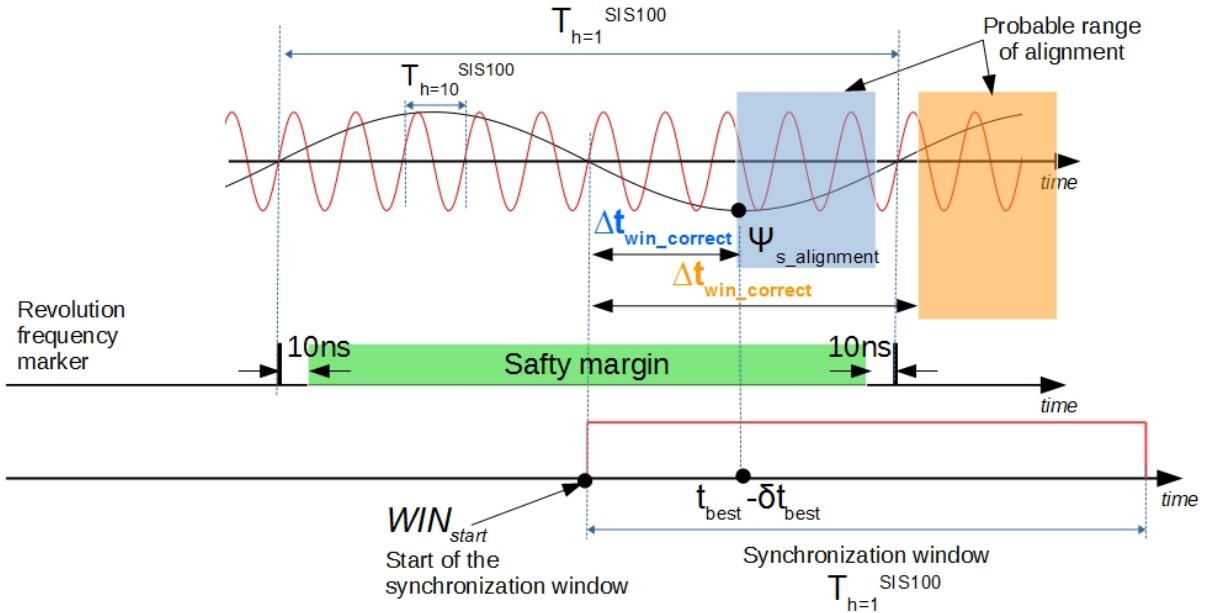


Figure 5.13: The illustration of the synchronization window and its accuracy

- $\psi_{s\_alignment} \in [0^\circ, 180^\circ]$ , the orange rectangle in Fig. 5.13

$$\Delta t_{win\_correct} = \frac{\psi_{s\_alignment}}{360^\circ} \times T_{h=1}^{SIS100} + \frac{T_{h=1}^{SIS100}}{2} \quad (5.45)$$

$$WIN_{start} = t_{best} - \delta t_{best} - \Delta t_{win\_correct} \quad (5.46)$$

- $\psi_{s\_alignment} \in [180^\circ, 360^\circ]$ , the blue rectangle in Fig. 5.13

$$\Delta t_{win\_correct} = \frac{\psi_{s\_alignment} - 180^\circ}{360^\circ} \times T_{h=1}^{SIS100} \quad (5.47)$$

$$WIN_{start} = t_{best} - \delta t_{best} - \Delta t_{win\_correct} \quad (5.48)$$

The actual start of the synchronization window is impossible to be exactly at the best estimate of the start of the synchronization window because of the precision and trueness [?]. The precision is defined as the closeness of agreement between the actual start of the synchronization window of different SCUs and the trueness as the closeness of agreement between the average actual start of the synchronization window of different SCUs and the best estimation start of the synchronization window. The precision comes from the random error, e.g. IO port TTL signal rising oscillation ????. The trueness is the systematic error, e.g. FPGA process time. The accuracy is defined as the closeness of agreement between the observed start and the best estimate of the start of the synchronization window, which is the sum of the precision and trueness. Because the B2B transfer system is used for all FAIR project, we must find the most stringent accuracy requirement. The shortest revolution period of the target machine is 433 ns, which comes from RIB transfer from CR to HESR. We keep 10ns as a forbidden range, which means that the actual start is not allowed 10 ns before and after the revolution frequency marker. The green

## 5.2. GMT systematic investigation for the B2B transfer system

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region in Fig. 5.13 represents the safty margin for the start of the synchronization window. So the accuracy of the start of the synchronization window is

$$Accuracy = \pm \frac{433 - 10 \times 2}{2} \approx \pm 200 \text{ ns} \quad (5.49)$$

### 5.2.2 Measurement of the WR network for the B2B transfer

GMT system implements the tree WR network topology. The WR network measurement is achieved by the Xena traffic generator, which offers a new class of professional Layer 2-3 Gigabit Ethernet test platform. It is used to measure the Frame loss rate<sup>1</sup>, latency<sup>2</sup> and jitter<sup>3</sup> for the WR network. For the measurement, Xena traffic generator sends the traffic streams with a unique stream ID for identifying latency, jitter and packet loss. The WR network for FAIR has the following traffic.

- DM Broadcast

DM forwards broadcast timing frames<sup>4</sup> with 110 bytes ethernet frame length downwards to all FECs. The average bandwidth for the DM broadcast is 100 Mbit/s. The burst<sup>5</sup> speed is 12 packets per 100  $\mu\text{s}$ .

- DM Unicast

DM sends 10Mbit/s unicast timing frames with 110 bytes ethernet frame length to some specified FECs at the burst speed of 3 packets per 300  $\mu\text{s}$ .

- B2B Unicast

The source B2B SCU sends the Timing frame with 110 bytes ethernet frame length upwards to the DM. For the B2B transfer upper bound time 10 ms of each supercycle, 2 unicast timing frames are send to the DM. The maximum repetition frequency is of the  $U^{28+}$  supercycle, 2.82 Hz. For the estimation of the upper bound bandwidth, we use 3Hz/s as the maximum repetition frequency. So the bandwidth is  $3 \text{ Hz/s} \times 2 \text{ packets/supercycle} \times 110 \text{ byte} \times 8 \text{ bit} \approx 5.5 \text{ kbit/s}$ .

- B2B Broadcast

Maximum 10 B2B broadcast timing frames with 110 ethernet frame length are sent within 10 ms. So the bandwidth is  $3 \text{ Hz/s} \times 10 \text{ packets/supercycle} \times 110 \text{ byte} \times 8 \text{ bit} \approx 26.5 \text{ kbit/s}$ .

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<sup>1</sup>The ratio of the number of the lost frames to the number of the theoretic received frames of a tested port.

<sup>2</sup>The time interval between the time of Xena port receiving frame and the time of another Xena port sending frame.

<sup>3</sup>The absolute value of the difference between the latency of two consecutive received frames belonging to the same stream from one Xena port to another Xena port.

[http://www.xenanetworks.com/wp-content/uploads/Measuring\\_Frame\\_latency\\_Variation.pdf](http://www.xenanetworks.com/wp-content/uploads/Measuring_Frame_latency_Variation.pdf)

<sup>4</sup><https://www-acc.gsi.de/wiki/Timing/TimingSystemEvent>

<sup>5</sup>A group of consecutive frames with shorter interframe gaps than frames arriving before or after the burst of frames.

## 5.2. GMT systematic investigation for the B2B transfer system

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- Management Traffic

The average bandwidth for the management traffic is 10 Mbit/s. It broadcasts packets with random ethernet frame length from 64 bytes to 1518 bytes.

The requirements for the B2B Broadcast and Unicast traffic are summarized in Tab. A.1.

Table 5.1: The B2B transfer requirements for the WR network

	Frame Loss Rate	Upper bound latency of WR network	Upper bound latency per WR switch layer
B2B Broadcast	$10^{-12}$	500 $\mu$ s	30 $\mu$ s
B2B Unicast	$10^{-12}$	500 $\mu$ s	30 $\mu$ s

A Virtual Local Area Network (VLAN) is a group of FECs in the WR network that is logically segmented by function or application, without regard to the physical locations of the FECs. For the WR network for FAIR, three VLANs with different priorities are applied according to the importance of the traffic.

## 5.2. GMT systematic investigation for the B2B transfer system

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### 5.2.2.1 WR network test setup

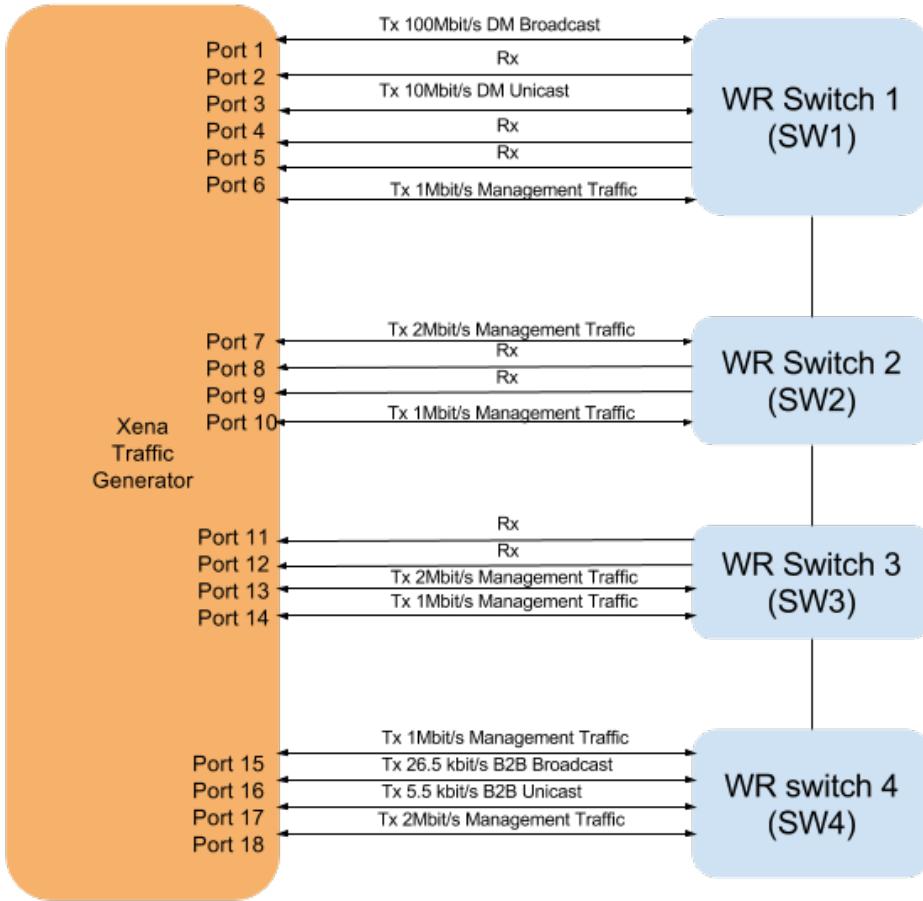


Figure 5.14: The WR network test setup

Based on the mentioned traffic, the measurement setup is built, see Fig. 5.14. Four WR switches are connected to the port 1 to 18 of the Xena traffic generator. All ports of four WR switches are assigned to three VLANs, VLAN 5, VLAN 6 and VLAN 7. Tab. 5.2 shows the bandwidth, VLAN, VLAN priority and usage of the traffic of each Xena port in details.

### 5.2.2.2 Frame loss rate test result for B2B frames

The frame loss rate of the stream from port 17 to port 1 is measured for the B2B Unicast frames. The frame loss rate of the stream from port 16 to other ports is measured for the B2B Broadcast frame. Fig. 5.15 shows the test result for both traffics. For the B2B Broadcast frames, the frame loss rate of each port is 0%. For the B2B Unicast frames, the frame loss rate of port 1 is 0%. So there is no B2B frame loss of the test WR network.

### 5.2.2.3 Latency and jitter test result for B2B frames

The latency and jitter of the stream from port 16 to other ports are measured.

## 5.2. GMT systematic investigation for the B2B transfer system

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Table 5.2: The traffic of Xena ports

Switch	Xena Port	Traffic	VLAN	Priority	Usage
WR switch 1	Port 1	100 Mbit/s 110bytes	7	7	DM Broadcast
WR switch 1	Port 2	Rx traffic			
WR switch 1	Port 3	10 Mbit/s 110bytes	7	7	DM Unicast
WR switch 1	Port 4	Rx traffic			
WR switch 1	Port 5	Rx traffic			
WR switch 1	Port 6	1 Mbit/s 64 - 1518 bytes	5	5	Management Broadcast
WR switch 2	Port 7	2 Mbit/s 64 - 1518 bytes	5	5	Management Broadcast
WR switch 2	Port 8	Rx traffic			
WR switch 2	Port 9	Rx traffic			
WR switch 2	Port 10	1 Mbit/s 64 - 1518 bytes	5	5	Management Broadcast
WR switch 3	Port 11	Rx traffic			
WR switch 3	Port 12	Rx traffic			
WR switch 3	Port 13	2 Mbit/s 64 - 1518 bytes	5	5	Management Broadcast
WR switch 3	Port 14	1 Mbit/s 64 - 1518 bytes	5	5	Management Broadcast
WR switch 4	Port 15	1 Mbit/s 64 - 1518 bytes	5	5	Management Broadcast
WR switch 4	Port 16	26.5 kbit/s 110bytes	6	6	B2B Broadcast
WR switch 4	Port 17	5.5 kbit/s 110bytes	7	7	B2B Unicast
WR switch 4	Port 18	2 Mbit/s 64 - 1518 bytes	5	5	Management Broadcast

- Latency and jitter for B2B Broadcast frames

- Average Latency and jitter

Fig. 5.16 shows the test result for the average latency and jitter for

## 5.2. GMT systematic investigation for the B2B transfer system

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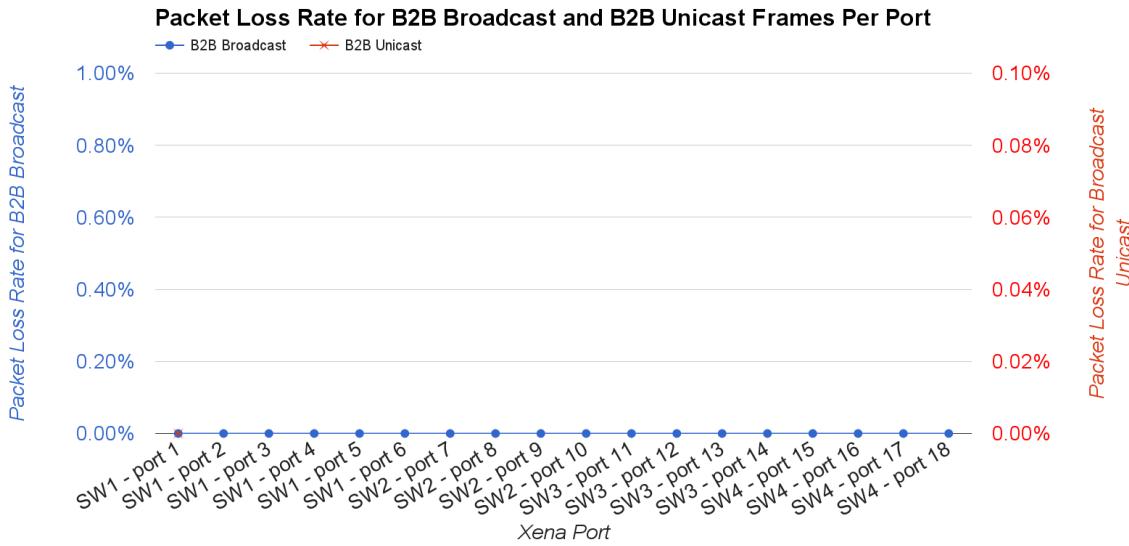


Figure 5.15: The frame loss rate for B2B Broadcast and B2B Unicast frames

the B2B Broadcast frames. The average latency of the stream going through the WR switch 4 is approximate 6  $\mu$ s. The average latency of the stream going through the WR switch 4 and 3 is approximate 8  $\mu$ s. The average latency of the stream going through the WR switch 4, 3 and 2 is approximate 11  $\mu$ s. The average latency of the stream going through the WR switch 4, 3, 2 and 1 is approximate 14  $\mu$ s. The average jitter of each port is 0 ns. From the viewpoint of the average jitter and latency, they meet the requirements of the B2B transfer.

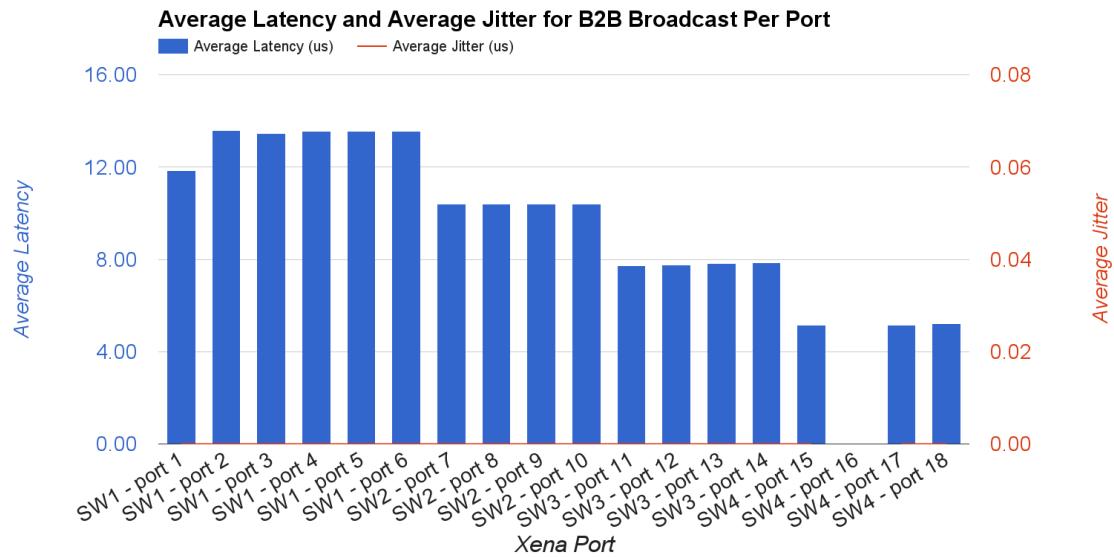


Figure 5.16: The average latency and jitter for B2B Broadcast frames

- Maximum Latency and jitter

## 5.2. GMT systematic investigation for the B2B transfer system

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Fig. 5.17 shows the test result for the maximum latency and jitter for the B2B Broadcast frames. The maximum latency and jitter of the stream going through the WR switch 4 is approximate 28  $\mu$ s and 25  $\mu$ s. The maximum latency and jitter of the stream going through the WR switch 4 and 3 is approximate 34  $\mu$ s and 25  $\mu$ s. The maximum latency and jitter of the stream going through the WR switch 4, 3 and 2 is approximate 37  $\mu$ s and 27  $\mu$ s. The maximum latency and jitter of the stream going through the WR switch 4, 3, 2 and 1 is approximate 41  $\mu$ s and 30  $\mu$ s.

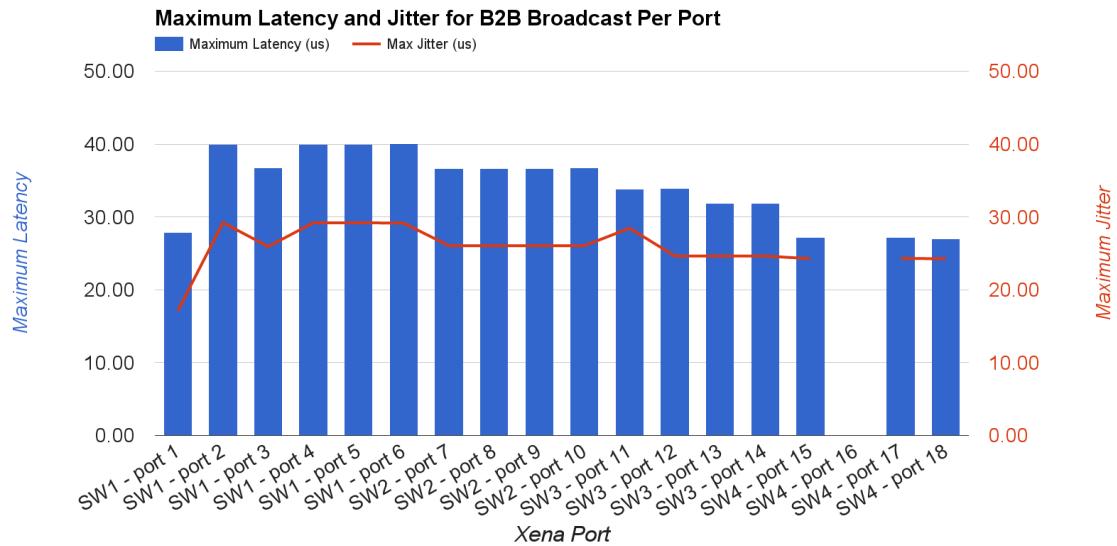


Figure 5.17: The maximum latency and jitter for B2B Broadcast frames

- Latency and jitter for B2B Unicast frames

For the B2B unicast frames, the latency and jitter of the stream from port 16 to port 1 are measured.

- Average Latency and jitter

For the B2B Unicast frames, 4 WR switch network has approximate 11  $\mu$ s average latency and 0  $\mu$ s average jitter.

- Maximum Latency and jitter

For the B2B unicast frames, 4 WR switch network has approximate 23  $\mu$ s maximum latency and 13  $\mu$ s maximum jitter.

More test results, please see the document -----

### 5.2.2.4 Result and conclusion

Tab. 5.3 shows the result of the test. The frame loss rate and latency meet the requirements of the B2B Broadcast and B2B Unicast traffic.

## 5.2. GMT systematic investigation for the B2B transfer system

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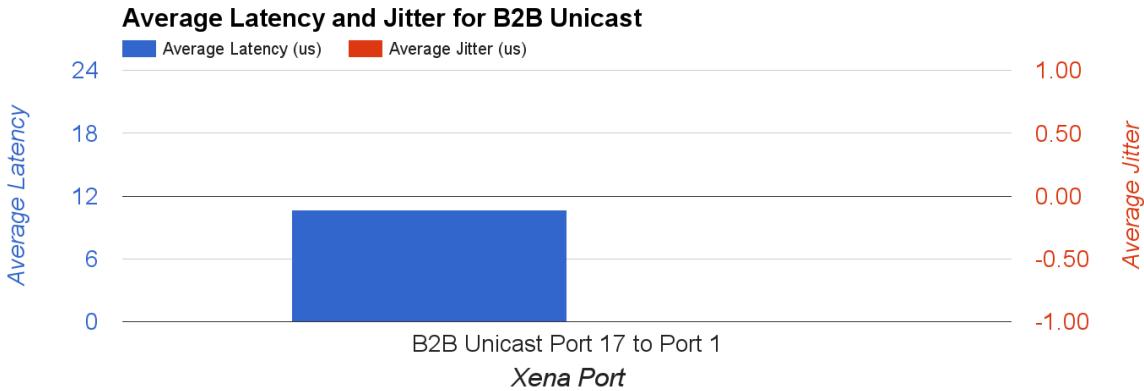


Figure 5.18: The average latency and jitter for B2B Unicast frames

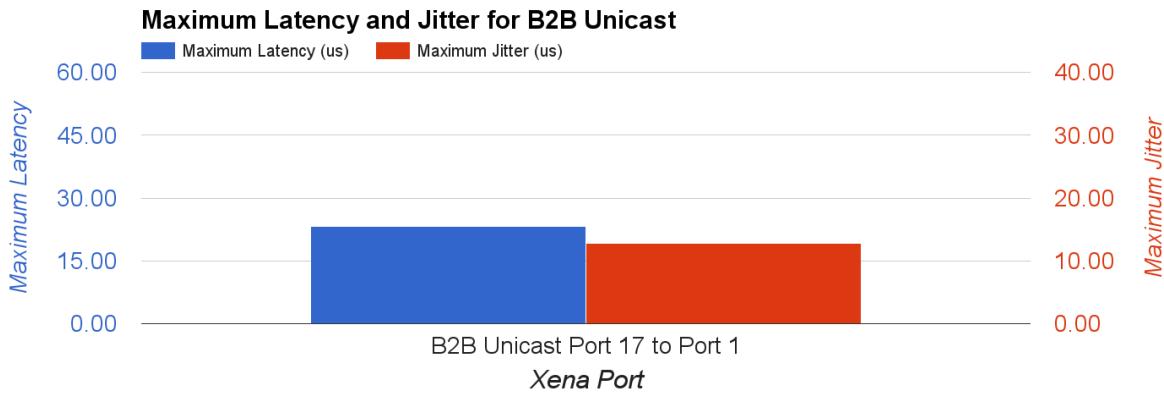


Figure 5.19: The maximum latency and jitter for B2B Unicast frames

Table 5.3: The result of the test

	Frame Loss Rate	Average Latency	Maximum Latency	Average Jitter	Maximum Jitter
B2B Broadcast	0 %	6 $\mu$ s/switch	28 $\mu$ s/switch	0 $\mu$ s/switch	25 $\mu$ s/switch
B2B Unicast	0 %	11 $\mu$ s/4switch 3 $\mu$ s/switch	23 $\mu$ s/4switch 6 $\mu$ s/switch	0 $\mu$ s/4switch 0 $\mu$ s/4switch	13 $\mu$ s/4switch 4 $\mu$ s/switch

For the B2B transfer system, the upper bound latency of the frames in the B2B Broadcast and B2B Unicast traffic is 500  $\mu$ s, see Sec.5.2.2. The latency of the WR network is decided by the layers of WR switches and the length of the optical fiber. The latency of the optical fiber is about 204 m/ $\mu$ s and the longest distance in the FAIR campus is around 2 km, so the latency of a 2 km optical fiber is about 10  $\mu$ s. The layers of WR switches plays a more important role in the latency.

- B2B Broadcast

### 5.3. Kicker systematic investigation for the B2B transfer system

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Here we calculate the layer of the WR switch between the B2B source SCU and B2B target SCU, between B2B source SCU and source trigger SCU and between B2B source SCU and target trigger SCU.

$$\frac{500 \mu\text{s} - 10 \mu\text{s}}{28 \mu\text{s}/\text{switch}} \approx 17 \quad (5.50)$$

- B2B Unicast

Here we calculate the layer of the WR switch between the B2B source SCU and DM.

$$\frac{500 \mu\text{s} - 10 \mu\text{s}}{6 \mu\text{s}/\text{switch}} \approx 81 \quad (5.51)$$

## 5.3 Kicker systematic investigation for the B2B transfer system

The SIS18 extraction kicker consists of 9 kicker units. In the existing topology, 5 kicker units are installed in the 1st crate and the other 4 units are in the 2nd crate. The width of each kicker unit is 0.25m and the distance between two kicker units is 0.09m. The distance between two crates is 19.167m. SIS100 injection kicker consists of 6 kicker units, which are equally located. The width of each kicker unit is 0.22m and the distance between two units is 0.23m. For the B2B transfer, the rise time of SIS18 extraction kicker and SIS100 injection kicker unit are 90ns and 1/20 of the revolution period. The rise time of these kickers must fit within the bunch gap, 25% of rf reference period. The bunch gap is denoted by G. All the analysis in this section dose not consider the jitter of the kicker trigger signal. Here we are discussing about the following possibilities.

- For SIS18, whether the kicker units in the 2nd crate could be fired a fixed delay after the firing of the kicker units in the 1st crate for ion beams over the whole range of stable isotopes.
- For SIS100, whether the kicker units could be fired instantaneously.

### 5.3.1 SIS18 extraction kicker units

Here we take three ion beams,  $H^+$ ,  $U^{28}$  and  $U^{73+}$ , to check the possibility, because the boundary ion species have the most stringent requirements. Fig. 5.20 shows three scenarios of the firing delay between two crates. Beam is firstly kicked by kicker units in the 1st crate and than kicked by the units in the 2nd crate to the transfer line. The yellow and red ellipse represents the position of the bunches, when the kicker units in the 1st and 2nd crate are fired. The number in the ellipse is used to tell different bunches. The head of the bunch is at the right side. The bunch 2 is firstly kicked. Here we assume that the kicker units in the same crate are triggered instantaneous. d denotes the distance between two crates. L denotes the distance from the leftmost to the rightmost kicker unit. D denotes the sum distance of d and the 2nd crate. d equals to 19.167 meter. L equals to 22.047m = d + 9 × 0.25m + 7 × 0.09m. D equals to 20.437m = d + 4 × 0.25m + 3 × 0.09m.

### 5.3. Kicker systematic investigation for the B2B transfer system

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Fig. 5.20 (a) is the easiest scenario. The kicker units in the 1st crate are fired when the tail of the bunch 1 passes by the 1st crate completely. The kicker units in the 2nd crate are fired when the tail of the bunch 1 passes by the 2nd crate completely. The delay for the firing two crates in this scenario is  $D/\beta c$ .

Fig. 5.20 (b) shows the scenario of the maximum delay between the firing of two crates. The kicker units in the 1st crate are fired when the tail of the bunch 1 passes by the 1st crate completely. The kicker units in the 2nd crate are fired 90ns before the head of the bunch 2 passes by it. The delay equals to  $G+d/\beta c - 90\text{ns}$ .

Fig. 5.20 (c) shows the scenario of the minimum delay. The kicker units in the 1st crate are fired 90ns before the head of the bunch 2 passes by it. The kicker units in the 2nd crate are fired when the bunch 1 passes by the 2nd crate. The delay is  $L/\beta c - G + 90\text{ns}$ .

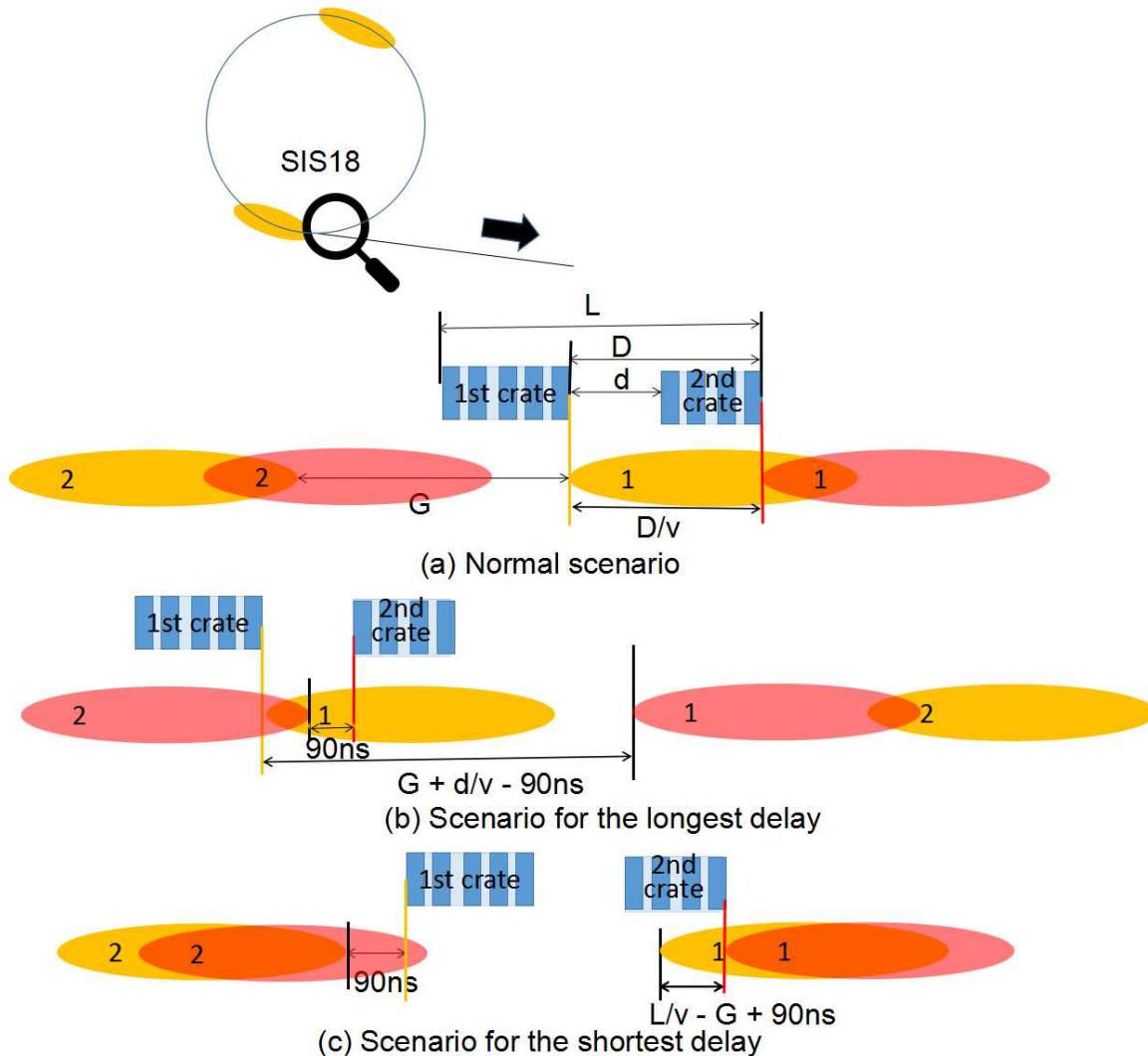


Figure 5.20: Three scenarios for the delay of SIS18 extraction kicker

Table 5.4 shows delay for three scenarios and related parameters. The fixed delay is determined primarily by the boundary delay range from  $H^+$ ,  $U^{28}$  and  $U^{73+}$  beams, the delay range for other heavy ion species beams must be contained in these boundary range. According to the result, a fixed delay is available for firing kicker units in two crate for different beams. e.g. 80ns.

Table 5.4: The delay for firing two crates of SIS18 extraction kicker

Beam	$\beta$	time $L/\beta c$	bunch gap G	minimum delay $L/\beta c-G+90\text{ns}$	delay $D/\beta c$	maximum delay $G+d/\beta c-90\text{ns}$
$H^+$	0.982	75ns	184ns	0ns	69ns	163ns
$U^{28}$	0.568	130ns	159ns	61ns	120ns	189ns
$U^{73+}$	0.872	84ns	104ns	70ns	78ns	92ns

### 5.3.2 SIS100 injection kicker units

Two bunches from SIS18 will be continuously injected into one RF bucket after the other in SIS100. See Fig. 5.5. The yellow ellipse represents the circulating bunch in SIS100 and the red one represents the bunch to be injected. The head of the bunch is at the left side. The preparation of the SIS100 injection kicker must be done during the bunch gap and it must be established for at least one SIS18 revolution period. For the instantaneous firing, all kicker units are fired only if the tail of the circulating bunch passes the leftmost kicker unit. The kicker pass time is the time needed for the tail of a bunch to pass from the rightmost unit to the leftmost kicker unit. The rise time of the kicker unit is 1/20 of the revolution period. Therefor the preparation time is the sum of the kicker pass time and rise time. The distance from the rightmost to the leftmost kicker unit is 3.79m,  $6 \times 0.22\text{m} + 5 \times 0.23\text{m}$ . If the preparation time is shorter than bunch gap, all kicker units could be fired instantaneous. Table 5.5 shows the preparation time for  $H^+$ ,  $U^{28}$  and  $U^{73+}$  beams and their bunch gap. The preparation time is much shorter than the bunch gap. So the kicker units could be fired instantaneous.

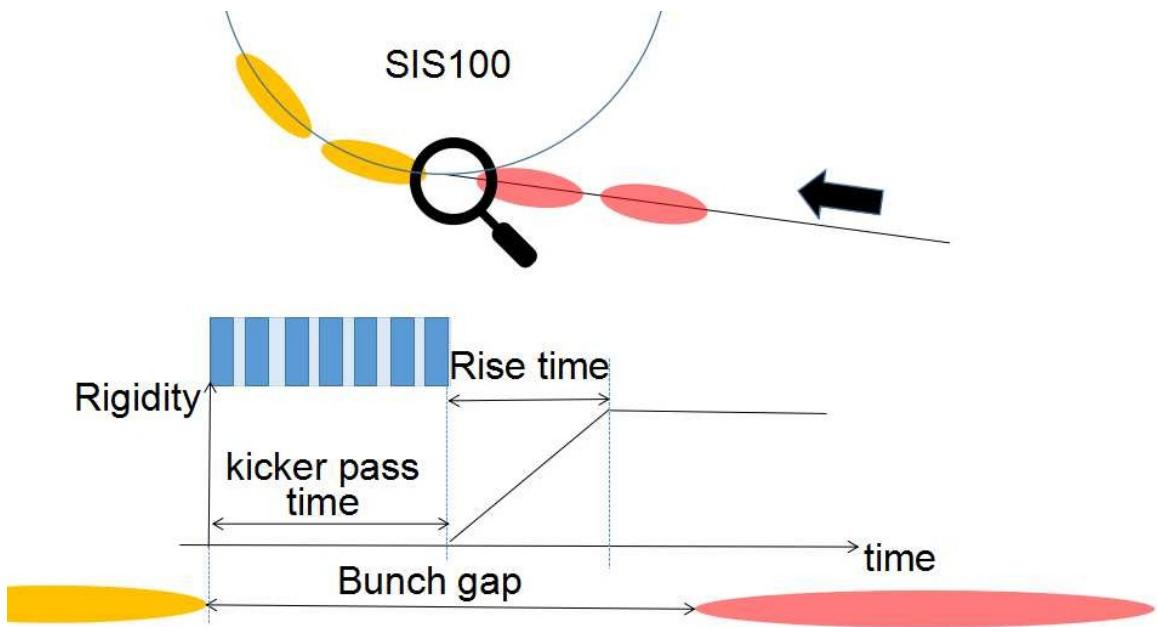


Figure 5.21: SIS100 injection kicker

## **5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system**

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Table 5.5: The delay for firing SIS00 injection kicker

Beam	$\beta$	kicker pass time $L/\beta c$	Rise time $1/20 \times T_{rev}^{SIS100}$	Preparation time $L/\beta c + 1/20 \times T_{rev}^{SIS100}$	bunch gap $2.25 \times T_{rev}^{SIS100}$
$H^+$	0.982	3ns	184ns	187ns	828ns
$U^{28}$	0.568	22ns	318ns	333ns	1431ns
$U^{73+}$	0.872	15ns	207ns	222ns	932ns

## **5.4 Test setup for the data collection, merging and redistribution of the B2B transfer system**

In this section, the test setup for the B2B transfer system is described, focusing only on the timing aspects.

### **5.4.1 Test functional requirement**

The test setup achieves the following functional requirement.

- After receiving the B2B beginning event, both the B2B source and target SCUs collect predicted phase equivalent data locally. The equivalence is a timestamp for the zero crossing point of the simulated RF Reference Signal of SIS18 and SIS100.
- The B2B target SCU transfers the frame containing the timestamp to the B2B source SCU.
- After receiving the data, the B2B source SCU calculates the synchronization window.
- The B2B source SCU sends the frame containing the beginning of the synchronization window to the WR network.
- After receiving the frame, the trigger SCU produces TTL output indicating the start of the synchronization window.

### 5.4.2 Test setup

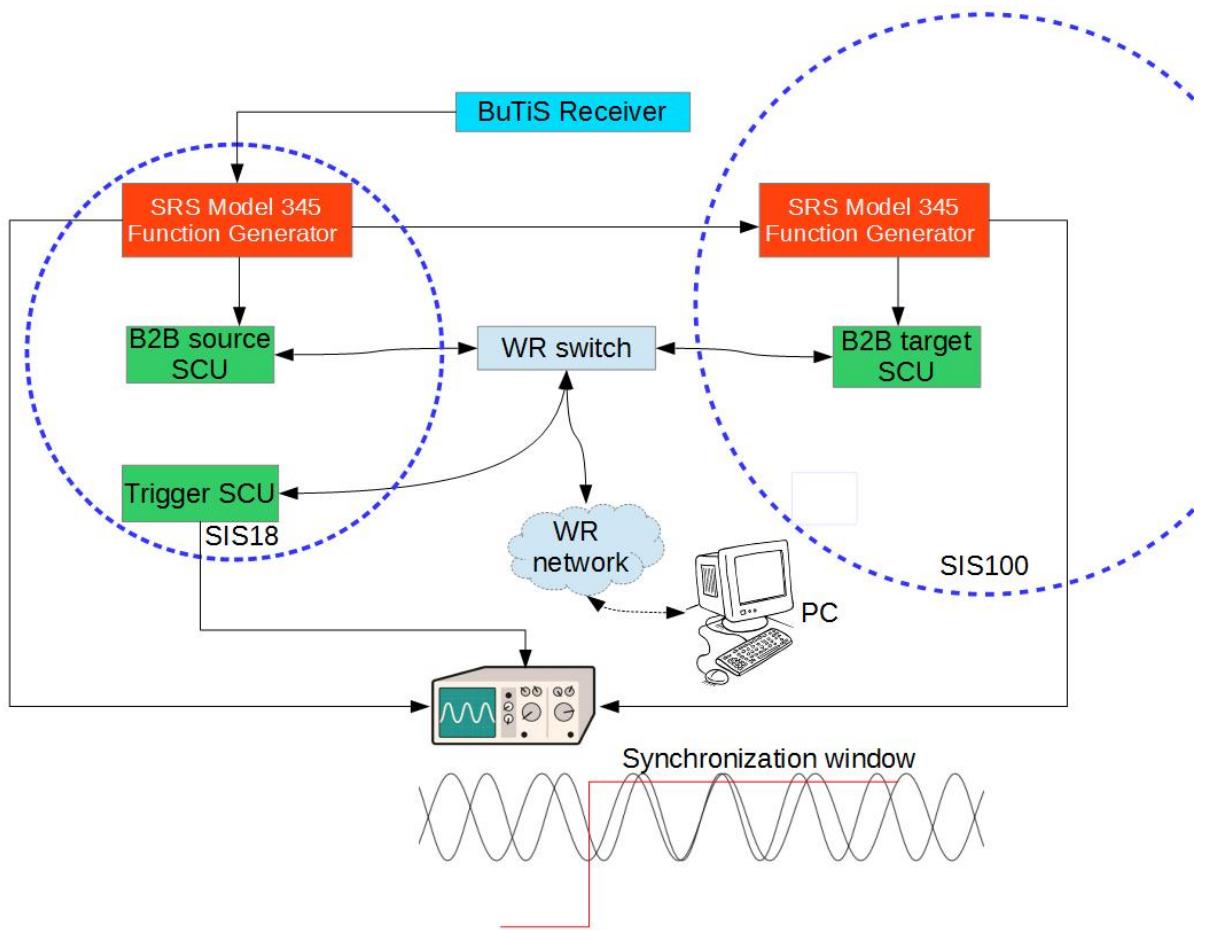


Figure 5.22: Schematic of the test setup

Fig. 5.22 shows the schematic of the test setup. In this test setup, two MODEL DS345 Synthesized Function Generators<sup>6</sup> are used, which are with the frequency accuracy of  $\pm 5$  ppm of the selected frequency to simulate RF Reference Signals of SIS18 and SIS100. DS345 of SIS18 is directly triggered by the 10 MHz of BuTiS receiver and DS345 of SIS100 is triggered by DS345 of SIS18. So both DS345s are synchronized to BuTiS. The B2B source SCU, B2B target SCU and trigger SCU are connected to the same WR switch, which connects to the timing network. PC<sup>7</sup> is used as a DM to produce the B2B start event. Besides, it monitors the status of the B2B transfer programs in all SCUs. The oscilloscope is used to monitor the alignment of the two simulated RF Reference Signals within the synchronization window provided by the trigger SCU.

Fig. 5.23 shows the front and back view of the test setup. DS345 of SIS18 produces the sine wave of 1.572 200 MHz frequency for the B2B source SCU. DS345 of SIS100 produces the sine wave of 1.572 000 MHz for the B2B target SCU. So the beating frequency is 200 Hz and the synchronization period is 5 ms.

<sup>6</sup><http://www.thinksrs.com/downloads/PDFs/Manuals/DS345m.pdf>

<sup>7</sup>A Linux personal computer is installed with the standard TR tools and library.  
<https://www-acc.gsi.de/wiki/Timing/TimingSystemNodesCurrentRelease>

## 5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system

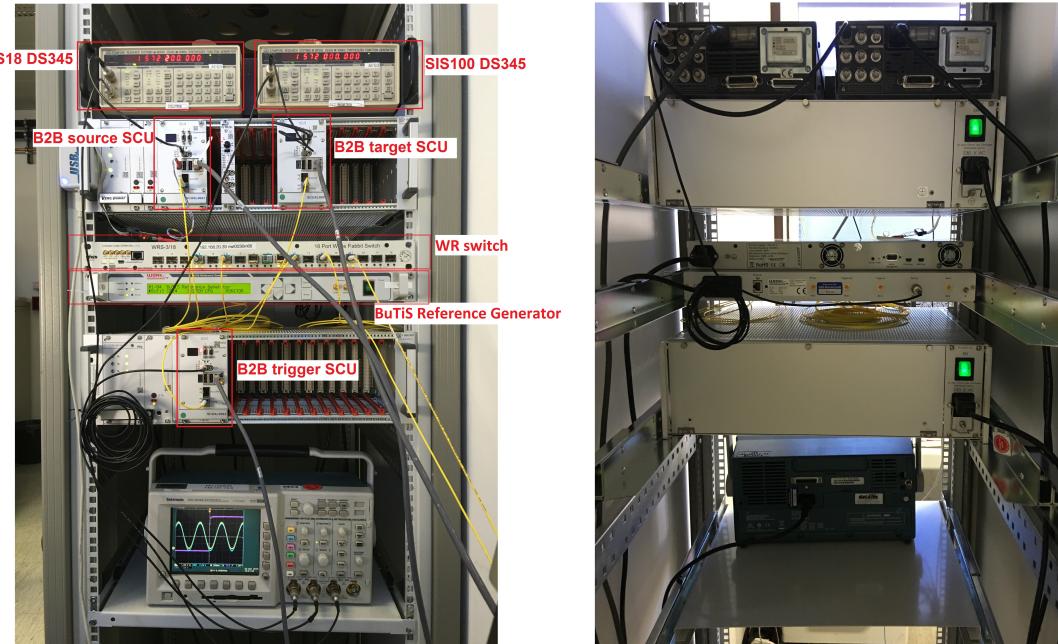


Figure 5.23: The front and back view of the test setup

### 5.4.3 The firmware of the B2B transfer system

The B2B source, B2B target and trigger SCUs have different firmware running on their soft CPU, LM32<sup>8</sup>. The firmware are activated by the B2B start timing frame, *CMD\_START\_B2B*, which indicates the source and target synchrotrons of the B2B transfer.

- Firmware for the B2B source SCU

The firmware for the B2B source SCU is the core program of the B2B transfer system. See Fig. 5.24.

- Step 1. The program waits for the *CMD\_START\_B2B* timing frame.
- Step 2. When it receives the timing frame *CMD\_START\_B2B*, it collects the predicted phase and checks whether it is within a proper range of  $0^\circ$  to  $360^\circ$ . If not, it sends a timing frame *TGM\_B2B\_ERROR* to the WR network and goes back to the step 1, which indicates the data error.
- Step 3. It waits for the *TGM\_PHASE\_TIME* timing frame from the B2B target SCU, which contains the predicted phase and the slop of the target synchrotron.
- Step 4. When it receives the timing frame *TGM\_PHASE\_TIME* within a specified timeout interval, it calculates the synchronization window, the phase shift/jump value and the phase correction value. Or it sends a timing frame *TGM\_B2B\_ERROR* to the WR network and goes back to the step 1, which indicates the timeout error of the frame. Besides, it checks whether the phase correction is in the range of  $0^\circ$  to  $360^\circ$  , the

<sup>8</sup>LatticeMico32 is a 32-bit microprocessor soft core from Lattice Semiconductor optimized for field-programmable gate arrays (FPGAs).

## 5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system

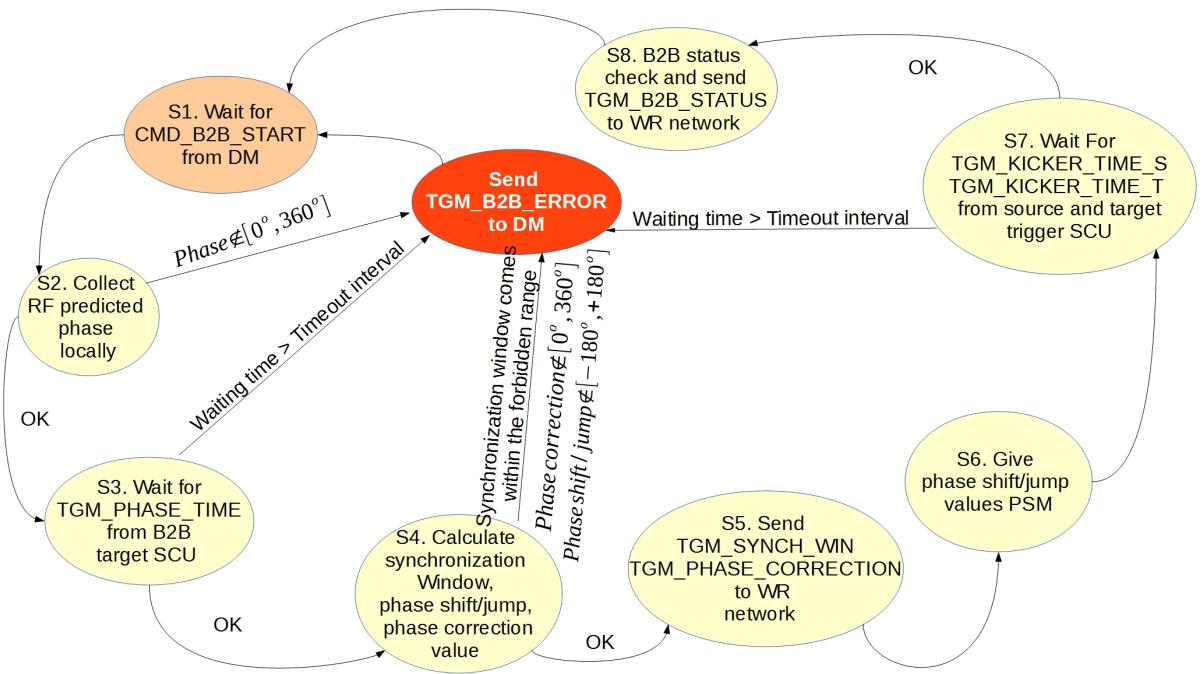


Figure 5.24: Flow chart of the firmware for B2B source SCU. Step is represented as S in the figure.

required phase shift in the range of  $-180^\circ$  to  $180^\circ$  and the start of the synchronization window not in the forbidden range. If at least one of them is not correct, it sends a timing frame TGM\_B2B\_ERROR to the WR network and goes back to the step 1, which indicates the calculation error.

- Step 5. It sends the timing frame TGM\_SYNCH\_WIN and TGM\_PHASE\_CORRECTION to the WR network. TGM\_SYNCH\_WIN indicates the start of the synchronization window and TGM\_PHASE\_CORRECTION is used for the trigger SCUs for the reproduction of the bucket label signal.
- Step 6. It gives the phase correction and phase shift/jump values to corresponding modules.
- Step 7. It waits for the timing frame TGM\_KICKER\_TIME\_S from the source trigger SCU and TGM\_KICKER\_TIME\_T from the target trigger SCU, which contains the extraction/injection kicker trigger and firing timestamp. When it does not receive the timing frames within a specified timeout interval, it sends a timing frame TGM\_B2B\_ERROR to the WR network and goes back to the step 1, which indicates the timeout error of the frame.
- Step 8. When it receives the timing frames mentioned in the step 7 within a specified timeout interval, it checks the B2B transfer status and sends TGM\_B2B\_STATUS to the WR network and goes to the step 1. The B2B transfer is successful, if the trigger time < the firing time of the extraction kicker of the source synchrotron, the trigger time < the firing time of the injection kicker of the target synchrotron and the firing time

## 5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system

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of the extraction kicker < the firing time of the injection kicker. Or the B2B transfer is failure.

- Firmware for the B2B target SCU

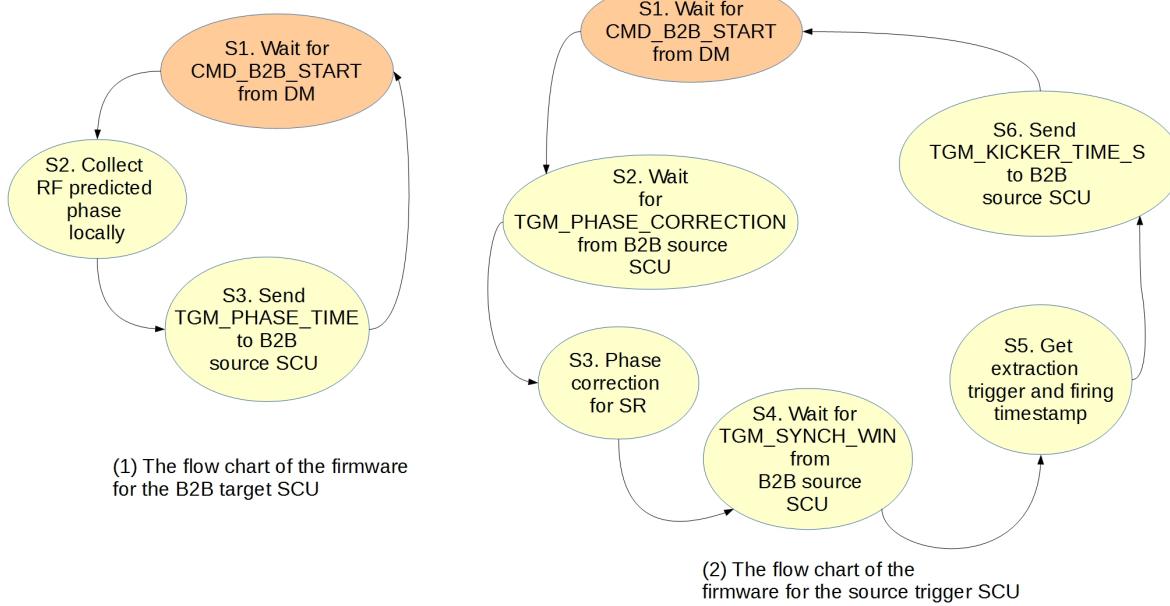


Figure 5.25: Flow chart of the firmware for B2B target SCU. Step is represented as S in the figure.

Fig. 5.25 (a) shows the flow chart of the program of the B2B target SCU.

- Step 1. The program waits for the CMD\_START\_B2B timing frame.
- Step 2. When it receives the timing frame CMD\_START\_B2B, it collects the predicted phase.
- Step 3. It sends the TGM\_PHASE\_TIME timing frame to the B2B source SCU and goes back to the step 1.

- Firmware for the trigger SCU

Fig. 5.25 (b) shows the flow chart of the program of the source trigger SCU. For the target trigger SCU, the flow chat is same only with the different name of the timing frame TGM\_KICKER\_TIME\_T.

- Step 1. The program waits for the CMD\_START\_B2B timing frame.
- Step 2. The program waits for the TGM\_PHASE\_CORRECTION timing frame.
- Step 3. The program gives the phase correction value to the corresponding module for the bucket label signal reproduction.

## 5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system

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- Step 4. When it receives the timing frame CMD\_START\_B2B, it waits for the timing frame TGM\_SYNCH\_WIN to indicate the synchronization window for the kicker trigger.
- Step 5. After the beam extraction, it collects the trigger and firing timestamp.
- Step 6. It sends the TGM\_KICKER\_TIME\_S timing frame to the B2B source SCU and goes back to the step 1.

### 5.4.4 The time constraints of the B2B transfer system

For the B2B transfer system, the time constraints are very important and strict. Fig. 5.26 shows the time constraint of the system. The *CMD\_START\_B2B* is executed at  $t_{B2B}$ . The RF phase prediction needs 500  $\mu$ s, so the B2B source and target SCUs collect the phase data at  $t_{B2B} + 500 \mu\text{s}$  and need about 450 ns for the data collection. The B2B source SCU receives the timing frame TGM\_PHASE\_TIME at around  $t_{B2B} + 500 \mu\text{s} + 450 \text{ ns} + 500 \mu\text{s} \approx t_{B2B} + 1 \text{ ms}$ . The second 500  $\mu$ s is the latency of the WR network. After that, the B2B source SCU needs about 100  $\mu$ s for the calculation, the timing frame TGM\_SYNCH\_WIN and TGM\_PHASE\_CORRECTION sending and data transferring to the corresponding module. TGM\_SYNCH\_WIN is sent at around  $t_{B2B} + 1 \text{ ms} + 100 \mu\text{s} \approx t_{B2B} + 1.1 \text{ ms}$ . The trigger SCU receives TGM\_PHASE\_CORRECTION and TGM\_SYNCH\_WIN at around  $t_{B2B} + 1.1 \text{ ms} + 500 \mu\text{s} \approx t_{B2B} + 1.6 \text{ ms}$ . The 500  $\mu$ s is the latency of the WR network. The start of the synchronization window must be later than  $t_{B2B} + 1.1 \text{ ms} + 2 \times 500 \mu\text{s} \approx t_{B2B} + 2.1 \text{ ms}$ , because the TGM\_SYNCH\_WIN must be transferred back to the DM and the DM transfers it further to the beam instrumentation devices via WR network. The upward to DM transfer needs maximum 500  $\mu$ s and the transfer from the DM to BI needs another 500  $\mu$ s. Because the upper bound B2B transfer time is 10 ms and there is no hard real time for the collection of the trigger and firing timestamps and timing frame TGM\_KICKER\_TIME\_S sending, we give 1 ms for the source trigger SCU to do this task and the source trigger SCU sends TGM\_KICKER\_TIME\_S at around  $t_{B2B} + 10 \text{ ms} + 1 \text{ ms} \approx t_{B2B} + 11 \text{ ms}$ . The same time constraints is also for the target trigger SCU. The B2B source SCU receives TGM\_KICKER\_TIME\_S and TGM\_KICKER\_TIME\_T at around  $t_{B2B} + 11 \text{ ms} + 500 \mu\text{s} \approx t_{B2B} + 11.5 \text{ ms}$ . The 500  $\mu$ s is the latency of the WR network. The B2B source SCU sends TGM\_B2B\_STATUS at around  $t_{B2B} + 11.5 \text{ ms} + 100 \mu\text{s} \approx t_{B2B} + 11.6 \text{ ms}$ . The BI devices receives the timing frame TGM\_B2B\_STATUS at around  $t_{B2B} + 11.6 \text{ ms} + 2 \times 500 \mu\text{s} \approx t_{B2B} + 12.6 \text{ ms}$ .

## 5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system

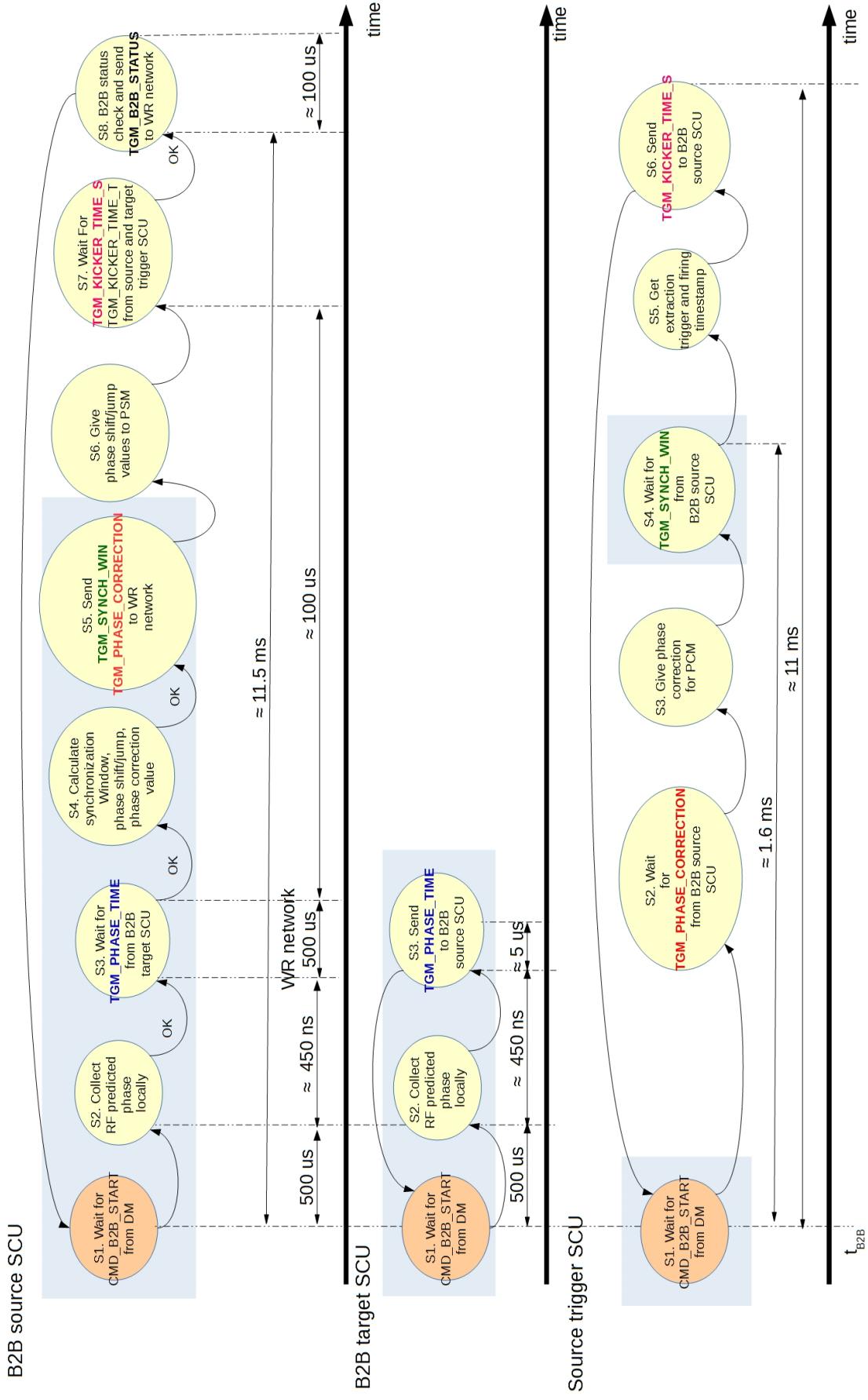


Figure 5.26: The time constraints of the B2B transfer system. The sent and received timing frame pairs have the same color. The test setup realizes the steps in the blue rectangle.

#### **5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system**

### 5.4.5 Test result

Because some modules of the B2B transfer system are still under the development, the test setup realizes parts of the whole function, mainly concentrated on the data collection from two simulated RF reference signals, the calculation of the synchronization window and the distribution of the start of the synchronization window. The steps with the blue rectangle in Fig. 5.26 are realized in this test setup. The test result of the B2B programs on B2B source, B2B target and trigger SCUs are shown as follows.

## 5.4. Test setup for the data collection, merging and redistribution of the B2B transfer system

---

WR network  
6 Event execution timestamp: GMT 1970–01–08 21:07:27.450028674

After both B2B source and target programs receive the *CMD\_START\_B2B* frame, they trigger another unit connected to the System-on-Chip<sup>9</sup> (SoC) bus to get the timestamp of the next zero crossing point of the DS345 sine waves, which is simulated as an equivalent to the predicted phase. The triggers of the B2B source and target SCUs are not simultaneous, namely the B2B source and target SCU do not get the timestamp of the adjacent zero crossing points of two RF simulated sine signals, see Line 10 and 14 of the test result of the B2B source SCU. All timestamp are shown in the format of Greenwich Mean Time (GMT). The timestamp got by the B2B source SCU is Thu, Jan 8, 1970, 21:07:27 0.445405856 second and the timestamp got by the B2B target SCU is Thu, Jan 8, 1970, 21:07:27 0.445364560 second. The time difference between two timestamps is 41.296  $\mu$ s. There are two reasons for the asynchronous triggers.

- The SoC bus might be granted to other program and B2B program must wait until it is free.
- The printout of the user friendly messages of the LM32 programs causes the non real time of the programs.

The difference between timestamps of the adjacent zero crossing points, 592ns, is the remainder resulting from 41.296us dividing SIS18 revolution period 636 051 ps. Based on eq. 5.52 and eq. 5.53,

$$\frac{T_{h=2}^{SIS18}}{5ms} = \frac{592ns}{\Delta t} \quad (5.52)$$

$$\frac{\Delta t}{T_{h=1}^{SIS18}} = 3634 \quad (5.53)$$

we could get that the beating time  $\Delta t$  is 4.622 818 ms and the number of the SIS18 revolution period is 3634 for the test.

For the real application of the B2B transfer system, in order to guarantee the time constraints of the B2B programs, see Fig. 5.26, the B2B source, target and trigger SCUs run only their corresponding B2B program. The SoC bus is occupied only by the B2B program. Besides, the programs running on LM32 are forbidden to print out any user friendly messages.

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<sup>9</sup>A system-on-chip is an integrated circuit that integrates all components of a computer or other electronic system into a single chip.

# **Chapter 6**

## **Existing transfer system and the transfer system of the FAIR accelerators**

**6.1 Existing transfer from SIS18 to ESR**

**6.2 B2B transfer from SIS18 to ESR to CRYRING**

# **Chapter 7**

## **Summary**

# **Chapter 8**

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# Appendix A

## Formelzeichen

### A.1 B2B frames

Table A.1: frames for the B2B transfer system

No	Fram Name	Event ID	Priority	Source	1
1	CMD_START_B2B		7	DM	Source a
2	TGM_PHASE_TIME		6	Target B2B SCU	Sou
3	TGM_SYNCH_WIN		6	Source B2B SCU	DM, source a
4	TGM_PHASE_CORRECTION		6	Source B2B SCU	Sour
5	TGM_KICKER_TRIGGER_TIME_S		6	Source Trigger SCU	Sou
6	TGM_KICKER_TRIGGER_TIME_T		6	Target Trigger SCU	Sou
7	TGM_KICK_EXE_S		6	Source Kicker SCU	Sou
8	TGM_KICK_EXE_T		6	Target Kicker SCU	Sou
9	TGM_B2B_STATUS		6	Source B2B SCU	
10	CMD_SYNCH_WIN		7	DM	Beam In
11	CMD_KICK_TIME_S		7	DM	BI 64 bits
12	TGM_PHASE_JUMP		6	Source B2B SCU	Tar

# **Appendix B**

## **List of Tables**

# **Appendix C**

## **List of Figures**

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