# Revised<sup>7</sup> Report on the Algorithmic Language Scheme

## Large Language, Red Edition

WG2 membership (Editors)

With major contributions from: SRFI authors

Dedicated to the memory of ...?

DRAFT May 28, 2017

#### Authors

TODO Rework this whole thing. I'm tentatively thinking that the title page should list the editors, followed by "Major Contributions by", and the SRFI authors, in alphabetical order. Acknowledgements should appear in alphabetical order, in the document, with each person listed once, no matter how many SRFIs they are credited for. Not totally sure what to do about the copyright notices, since many of the original notices say "All Rights Reserved", and the standard SRFI notice contradicts that, and only talks about "the Software". Suggest writing to the SRFI authors and asking them if it's permissible to put the derived documentation under the R7RS copyright (R7RS, p3), which is in my non-legal opinion equivalent to public domain.

• SRFI 1: List library. Olin Shivers. (scheme list)

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The design of this library benefited greatly from the feedback provided during the SRFI discussion phase. Among those contributing thoughtful commentary and suggestions, both on the mailing list and by private discussion, were Mike Ashley, Darius Bacon, Alan Bawden, Phil Bewig, Jim Blandy, Dan Bornstein, Per Bothner, Anthony Carrico, Doug Currie, Kent Dybvig, Sergei Egorov, Doug Evans, Marc Feeley, Matthias Felleisen, Will Fitzgerald, Matthew Flatt, Dan Friedman, Lars Thomas Hansen, Brian Harvey, Erik Hilsdale, Wolfgang Hukriede, Richard Kelsey, Donovan Kolbly, Shriram Krishnamurthi, Dave Mason, Jussi Piitulainen, David Pokorny, Duncan Smith, Mike Sperber, Maciej Stachowiak, Harvey J. Stein, John David Stone, and Joerg F. Wittenberger. I am grateful to them for their assistance.

I am also grateful the authors, implementors and documentors of all the systems mentioned in the rationale. Aubrey Jaffer and Kent Pitman should be noted for their work in producing Web-accessible versions of the R5RS and Common Lisp spec, which was a tremendous aid.

This is not to imply that these individuals necessarily endorse the final results, of course.

• SRFI 133: Vector Library. John Cowan (based on SRFI 43 by Taylor Campbell). (scheme vector)

Copyright (C) Taylor Campbell (2003). All rights reserved. (And John Cowan?)

These acknowledgements are copied from SRFI 43.

Thanks to Olin Shivers for his wonderfully complete list and string packages; to all the members of the #scheme IRC channel on Freenode who nitpicked a great deal, but also helped quite a lot in general, and helped test the reference implementation in various Scheme systems; to Michael Burschik for his numerous comments; to Sergei Egorov for helping to narrow down the procedures; to Mike Sperber for putting up with an extremely overdue draft; to Felix Winkelmann for continually bugging me about finishing up the SRFI so that it would be only overdue and not withdrawn; and to everyone else who gave questions, comments, thoughts, or merely attention to the SRFI.

• SRFI 132: Sort Libraries. John Cowan (based on SRFI 32 by Olin Shivers)

This document is copyright (C) Olin Shivers (1998, 1999). All Rights Reserved. (Copyright John Cowan as well?) Olin thanked the authors of the open source consulted when designing this library, particularly Richard O'Keefe, Donovan Kolbly and the MIT Scheme Team. John thanks Will Clinger for his detailed comments, and both Will Clinger and Alex Shinn for their implementation efforts.

• SRFI 113: Sets and Bags. John Cowan

Copyright (C) John Cowan 2013. All Rights Reserved.

• SRFI 14: Character-set Library. Olin Shivers.

Certain portions of this document – the specific, marked segments of text describing the R5RS procedures – were adapted with permission from the R5RS report.

All other text is copyright (C) Olin Shivers (1998, 1999, 2000). All Rights Reserved.

The design of this library benefited greatly from the feedback provided during the SRFI discussion phase. Among those contributing thoughtful commentary and suggestions, both on the mailing list and by private discussion, were Paolo Amoroso, Lars Arvestad, Alan Bawden, Jim Bender, Dan Bornstein, Per Bothner, Will Clinger, Brian Denheyer, Kent Dybvig, Sergei Egorov, Marc Feeley, Matthias Felleisen, Will Fitzgerald, Matthew Flatt, Arthur A. Gleckler, Ben Goetter, Sven Hartrumpf, Erik Hilsdale, Shiro Kawai, Richard Kelsey, Oleg Kiselyov, Bengt Kleberg,

Donovan Kolbly, Bruce Korb, Shriram Krishnamurthi, Bruce Lewis, Tom Lord, Brad Lucier, Dave Mason, David Rush, Klaus Schilling, Jonathan Sobel, Mike Sperber, Mikael Staldal, Vladimir Tsyshevsky, Donald Welsh, and Mike Wilson. I am grateful to them for their assistance.

I am also grateful the authors, implementors and documentors of all the systems mentioned in the introduction. Aubrey Jaffer should be noted for his work in producing Web-accessible versions of the R5RS spec, which was a tremendous aid.

This is not to imply that these individuals necessarily endorse the final results, of course.

During this document's long development period, great patience was exhibited by Mike Sperber, who is the editor for the SRFI, and by Hillary Sullivan, who is not.

• SRFI 125: Intermediate hash tables. John Cowan, Will Clinger.

Copyright (C) John Cowan (2015).

Some of the language of this SRFI is copied from SRFI 69 with thanks to its author, Panu Kalliokoski. However, he is not responsible for what I have done with it. Thanks to Will Clinger for providing the sample implementation, and to Taylan Ulrich Bayırlı/Kammer for his spirited review.

I also acknowledge the members of the SRFI 125, 126, and 128 mailing lists, especially Takashi Kato, Alex Shinn, Shiro Kawai, and Per Bothner.

• SRFI 116: Immutable List Library. John Cowan.

Copyright (C) John Cowan 2014. All Rights Reserved.

Without the work of Olin Shivers on SRFI 1, this SRFI would not exist. Everyone acknowledged there is transitively acknowledged here. This is not to imply that either Olin or anyone else necessarily endorses the final results, of course.

• SRFI 101: Purely Functional Random-Access Pairs and Lists. David Van Horn.

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I am grateful to the members of the Northeastern University Programming Research Laboratory and PLT (and their intersection) for discussions during the pre-draft development of this SRFI and the library that preceded it. We are all indebted to Okasaki for his elegant solution to this problem. Much of the specification is adapted from text intended to belong to the Scheme community; I thank the editors and authors of the RnRS series collectively for their efforts. I am grateful to Donovan Kolbly for serving as SRFI editor and to Taylor R Campbell, Robert Bruce Findler, Aubrey Jaffer, Shiro Kawai, and Alexey Radul for discussion during the draft period. I thank William D Clinger, Robert Bruce Findler, and Abdulaziz Ghuloum for help writing the implementations of quote specific to Larceny, Ikarus, and PLT, respectively. Support was provided by the National Science Foundation under Grant #0937060 to the Computing Research Association for the CIFellow Project.

• SRFI 134: Immutable Deques. Kevin Wortman, John Cowan.

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• SRFI 135: Immutable Texts. William D Clinger.

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For three decades, I have been hoping the Scheme standards would either make strings immutable or add a new data type of immutable texts; with Unicode, that hope became more urgent. During that time, I have discussed this with far more people than I can now remember. Most of those I do remember are among those acknowledged below by John Cowan or Olin Shivers, but I am pleased to add Lars T Hansen, Chris Hanson, Felix Klock, and Jonathan Rees to the list of those whose ideas (and counter-arguments!) have contributed to this SRFI.

John Cowan, the author of SRFI 130, deserves special thanks for blessing my desire to use SRFI 130 as the starting point for this SRFI, for designing the spans API whose implementations tested the key ideas of this SRFI's sample implementations, for chairing Working Group 2, and for a lot more I won't mention here.

To acknowledge all those who contributed to SRFI 130 and to its predecessor SRFI 13, written by Olin Shivers, I hereby reproduce John Cowan's acknowledgements from SRFI 130:

Thanks to the members of the SRFI 130 mailing list who made this SRFI what it now is, including Per Bothner, Arthur Gleckler, Shiro Kawai, Jim Rees, and especially Alex Shinn, whose idea it was to make cursors and indexes disjoint, and who provided the foof implementation. The following acknowledgements by Olin Shivers are taken from SRFI 13:

The design of this library benefited greatly from the feedback provided during the SRFI discussion phase. Among those contributing thoughtful commentary and suggestions, both on the mailing list and by private discussion, were Paolo Amoroso, Lars Arvestad, Alan Bawden, Jim Bender, Dan Bornstein, Per Bothner, Will Clinger, Brian Denheyer, Mikael Djurfeldt, Kent Dybvig, Sergei Egorov, Marc Feeley, Matthias Felleisen, Will Fitzgerald, Matthew Flatt, Arthur A. Gleckler, Ben Goetter, Sven Hartrumpf, Erik Hilsdale, Richard Kelsey, Oleg Kiselyov, Bengt Kleberg, Donovan Kolbly, Bruce Korb, Shriram Krishnamurthi, Bruce Lewis, Tom Lord, Brad Lucier, Dave Mason, David Rush, Klaus Schilling, Jonathan Sobel, Mike Sperber, Mikael Staldal, Vladimir Tsyshevsky, Donald Welsh, and Mike Wilson. I am grateful to them for their assistance.

I am also grateful to the authors, implementors and documentors of all the systems mentioned in the introduction. Aubrey Jaffer and Kent Pitman should be noted for their work in producing Web-accessible versions of the R5RS and Common Lisp spec, which was a tremendous aid. This is not to imply that these individuals necessarily endorse the final results, of course. During this document's long development period, great patience was exhibited by Mike Sperber, who is the editor for the SRFI, and by Hillary Sullivan, who is not.

As Olin said, we should not assume any of those individuals endorse this SRFI.

• SRFI 121: Generators. Shiro Kawai, John Cowan, Thomas Gilray.

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These procedures are drawn from the Gauche core and the Gauche module gauche.generator, with some renaming to make them more systematic, and with a few additions from the Python library itertools. Consequently, Shiro Kawai, the author of Gauche and its specifications, is listed as first author of this SRFI. John Cowan served as editor and shepherd. Thomas Gilray provided the sample implementation and a valuable critique of the SRFI. Special acknowledgements to Kragen Javier Sitaker for his extensive review.

• SRFI 127: Lazy Sequences. John Cowan.

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Without the work of Olin Shivers on SRFI 1, this SRFI would not exist. Everyone acknowledged there is transitively acknowledged here. This is not to imply that either Olin or anyone else necessarily endorses the final results, of course.

Special thanks to Shiro Kawai, whose Gauche implementation of lazy sequences inspired this one, and to Kragen Javier Sitaker, who did a thorough review.

• SRFI 41: Streams. Philip L. Bewig.

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Jos Koot sharpened my thinking during many e-mail discussions, suggested several discussion points in the text, and contributed the final version of stream-match. Michael Sperber and Abdulaziz Ghuloum gave advice on R6RS.

• SRFI 111: Boxes. John Cowan.

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• SRFI 117: Queues based on lists. John Cowan.

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• SRFI 124: Ephemerons.John Cowan.

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• SRFI 128: Comparators (reduced). John Cowan.

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This SRFI is a simplified and enhanced rewrite of SRFI 114, and shares some of its design rationale and all of its acknowledgements. The largest change is the replacement of the comparison procedure with the ordering procedure. This allowed most of the special-purpose comparators to be removed. In addition, many of the more specialized procedures, as well as all but one of the syntax forms, have been removed as unnecessary.

Special thanks to Taylan Ulrich Bayırlı/Kammer, whose insistence that SRFI 114 was unacceptable inspired this redesign. Jörg Wittenberger added Chicken-specific type declarations, which I have moved to comparators.scm, as it is a Chicken-specific library. He also provided Chicken-specific metadata and setup commands. Comments from Shiro Kawai, Alex Shinn, and Kevin Wortman guided me to the current design for bounds and salt.

Others: WG2 members.

Copyright notice

TODO This is really a report, rather than software. I think the statement below should be replaced by the (non-copyright) from the R<sup>7</sup>RS report: "We intend this report to belong to the entire Scheme com- munity, and so we grant permission to copy it in whole or in part without fee. In particular, we encourage implementers of Scheme to use this report as a starting point for manuals and other documentation, modifying it as necessary." The individual SRFI comments can be included as a list, along with a statement that says that each author has explicitly granted permission for free use of their work.

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6 Revised<sup>7</sup> Scheme Large, Red Edition **DRAFT** 

TODO Restore 2-column layout, once LaTeX artifacts have been fixed.

## **SUMMARY**

[This needs to be rewritten.]

This is a frozen version of the Red Edition ballot.

By unanimous consent, the libraries of R7RS-small are all required in implementations of the Red Edition. This document specifies the additional libraries required in the Red Edition.

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Programming languages should be designed not by piling feature on top of feature, but by removing the weaknesses and restrictions that make additional features appear necessary. Scheme demonstrates that a very small number of rules for forming expressions, with no restrictions on how they are composed, suffice to form a practical and efficient programming language that is flexible enough to support most of the major programming paradigms in use today.

The Revised<sup>7</sup> Report on The Algorithmic Language Scheme (R<sup>7</sup>RS) describes an elegant and powerful language that fulfills the promise of the previous paragraph. In some cases, e.g., when using Scheme as an extension language, that is all the programmer needs. Often, though, modern programmers expect a set of libraries that will provide the facilities they need to get the job done. Many Scheme implementations have provided such libraries, but often the libraries are implementation-specific. It would be desirable to standardize as many of them as possible.

Accordingly, the Scheme community embarked upon the collection of a group of Scheme Requests For Implementation, or SRFIs. These specify particular libraries that can be provided in a compatible way across implementations.

More recently, it was decided that R<sup>7</sup>RS would be a core language, dubbed "R<sup>7</sup>RS-Small", and that a Large language would be created by identifying particular SRFIs, and adapting them to form a consistent library collection.

This report, the Red Edition, is the first stage of defining R<sup>7</sup>RS-Large, concentrating primarily upon data structure support. Subsequent reports, also named for colors, will provide additional facilities.

TODO Check all descriptions to make sure that argument references are in appropriate font.

#### 1. Basic libraries

#### List library

[Red Edition item 1] The small language has a basic set of list-processing utilities. The large language extends this set substantially.

The names described in this section comprise the (scheme list) library.

TODO Some of these procedures duplicate those of the small language. Do we want that?

TODO Define "linear update" and "pure functional" procedures. I assume that other SRFIs use the same terms, so maybe in a "Definitions" section in the introduction?

#### Procedure Index

TODO I think this whole section can be deleted. There are a few comments here about how a procedure in this library extends one in Scheme-small. Those should probably be folded into the descriptions of the individual procedures.

Here is a short list of the procedures provided.

```
Constructors cons list
    xcons cons* make-list list-tabulate
    list-copy circular-list iota
Predicates pair? null?
    proper-list? circular-list? dotted-list?
    not-pair? null-list?
    list=
Selectors car cdr ... cddadr cddddr list-ref
    first second third fourth fifth
    sixth seventh eighth ninth tenth
    car+cdr
    take
               drop
    take-right drop-right
    take!
               drop-right!
    split-at
               split-at!
    last last-pair
```

### Miscellaneous: length, append, concatenate, reverse, zip & count length length+ append concatenate reverse append! concatenate! reverse! append-reverse append-reverse! zip unzip1 unzip2 unzip3 unzip4 unzip5 count Fold, unfold & map map for-each unfold pair-fold fold fold-right unfold-right pair-fold-right reduce reduce-right append-map append-map! map! pair-for-each filter-map map-in-order Filtering & partitioning filter partition remove filter! partition! remove! Searching member memq memv find find-tail any every list-index take-while drop-while take-while! span break span! break! Deleting delete delete-duplicates delete! delete-duplicates! Association lists assoc assq assv alist-cons alist-copy alist-delete alist-delete! Set operations on lists | lset<= lset= lset-adjoin lset-union lset-union! lset-intersection lset-intersection! lset-difference lset-difference! lset-xor lset-xor! lset-diff+intersection lset-diff+intersection! Primitive side-effects set-car! set-cdr! Four R4RS/R5RS list-processing procedures are extended by this library in backwards-compatible ways: map for-each Extended to take lists of unequal length member assoc Extended to take an optional comparison procedure. The following R4RS/R5RS list- and pair-processing procedures are also part of list-lib's exports, as defined by the R5RS: cons pair? null? car cdr ... cdddar cddddr set-car! set-cdr! list append reverse length list-ref memq memv assq assv The remaining two R4RS/R5RS list-processing procedures are *not* part of this library: list-tail renamed drop

see proper-list?, circular-list?

and dotted-list?

list?

The linear-update procedures in this library are

take! drop-right! split-at! append! concatenate! reverse! append-reverse! append-map! map! filter! partition! remove! take-while! span! break! delete! alist-delete! delete-duplicates! lset-adjoin! lset-union! lset-inters lset-difference! lset-xor! lset-diff+intersection!

#### Improper Lists

Scheme does not properly have a list type, just as C does not have a string type. Rather, Scheme has a binary-tuple type, from which one can build binary trees. There is an *interpretation* of Scheme values that allows one to treat these trees as lists. Further complications ensue from the fact that Scheme allows side-effects to these tuples, raising the possibility of lists of unbounded length, and trees of unbounded depth (that is, circular data structures).

However, there is a simple view of the world of Scheme values that considers every value to be a list of some sort. that is, every value is either

```
a "proper list" – a finite, nil-terminated list, such as:
(a b c)
()
(32)
```

a "dotted list" - a finite, non-nil terminated list, such as:
(a b c . d)
(x . y)
42
george

• or a "circular list" – an infinite, unterminated list.

Note that the zero-length dotted lists are simply all the non-null, non-pair values.

This view is captured by the predicates proper-list?, dotted-list?, and circular-list?. List-lib users should note that dotted lists are not commonly used, and are considered by many Scheme programmers to be an ugly artifact of Scheme's lack of a true list type. However, dotted lists do play a noticeable role in the *syntax* of Scheme, in the "rest" parameters used by n-ary lambdas: (lambda (x y . rest) ...).

Dotted lists are *not* fully supported by list-lib. Most procedures are defined only on proper lists – that is, finite, nilterminated lists. The procedures that will also handle circular or dotted lists are specifically marked. While this design decision restricts the domain of possible arguments one can pass to these procedures, it has the benefit of allowing the procedures to catch the error cases where programmers inadvertently pass scalar values to a list procedure by accident, *e.g.*, by switching the arguments to a procedure call.

#### Errors

TODO Rewrite this section so it matches  $R^7RS$ . Ideally, nothing additional regarding errors should need to appear in this Report, because the error language should match  $R^7RS$ .

Note that statements of the form "it is an error" merely mean "don't do that." They are not a guarantee that a conforming implementation will "catch" such improper use by, for example, raising some kind of exception. Regrettably, R5RS Scheme requires no firmer guarantee even for basic operators such as car and cdr, so there's little point in requiring these procedures to do more. Here is the relevant section of the R5RS:

When speaking of an error situation, this report uses the phrase "an error is signalled" to indicate that implementations must detect and report the error. If such wording does not appear in the discussion of an error, then implementations are not required to detect or report the error, though they are encouraged to do so. An error situation that implementations are not required to detect is usually referred to simply as "an error."

For example, it is an error for a procedure to be passed an argument that the procedure is not explicitly specified to handle, even though such domain errors are seldom mentioned in this report. Implementations may extend a procedure's domain of definition to include such arguments.

#### Notation

TODO Move this to the beginning of the Report, as part of a standardized "Notation" section, and reformat. Check that these notations are consistent with those in R<sup>7</sup>RS.

list A proper (finite, nil-terminated) list

clist A proper or circular list

flist A finite (proper or dotted) list

A pair pair Any value x, y, d, aobject, value Any value

A natural number (an integer  $\geq = 0$ ) n, i

A procedure proc

A procedure whose return value is treated pred

as a boolean

A boolean procedure taking two arguments

It is an error to pass a circular or dotted list to a procedure not defined to accept such an argument.

#### Constructors

(cons a d)  $\rightarrow pair$ list library procedure

The primitive constructor. Returns a newly allocated pair whose car is a and whose cdr is d. The pair is guaranteed to be different (in the sense of eqv?) from every existing object.

```
(cons 'a '())
                        \Rightarrow (a)
(cons '(a) '(b c d)) \Rightarrow ((a) b c d)
(cons "a" '(b c))
                        => ("a" b c)
                        => (a . 3)
(cons 'a 3)
(cons '(a b) 'c)
                        => ((a b) . c)
```

(list  $object \dots$ )  $\rightarrow list$ 

list library procedure

Returns a newly allocated list of its arguments.

(list 'a (+ 3 4) 'c) 
$$\Rightarrow$$
 (a 7 c) (list)  $\Rightarrow$  ()

(xcons d a)  $\rightarrow pair$ 

list library procedure

(lambda (d a) (cons a d))

Of utility only as a value to be conveniently passed to higher-order procedures.

$$(xcons '(b c) 'a) \Rightarrow (a b c)$$

The name stands for "eXchanged CONS."

$$(cons* elt_1 elt_2 ...) \rightarrow object$$

list library procedure

Like list, but the last argument provides the tail of the constructed list, returning

```
(cons elt1 (cons elt2 (cons ... eltn)))
```

This function is called list\* in Common Lisp and about half of the Schemes that provide it, and cons\* in the other half.

(make-list 
$$n \ fill$$
)  $\rightarrow list$   
(make-list  $n$ )  $\rightarrow list$ 

list library procedure list library procedure

Returns an n-element list, whose elements are all the value fill. If the fill argument is not given, the elements of the list may be arbitrary values.

```
(make-list 4 'c) => (c c c c)
```

(list-tabulate  $n \ init-proc$ )  $\rightarrow list$ 

list library procedure

Returns an n-element list. Element i of the list, where 0 i n, is produced by (init-proc i). No guarantee is made about the dynamic order in which init-proc is applied to these indices.

```
(list-tabulate 4 values) => (0 1 2 3)
```

(list-copy flist)  $\rightarrow flist$ 

list library procedure

Copies the spine of the argument. TODO More detail.

(circular-list  $elt_1$   $elt_2$  ...)  $\rightarrow list$ 

list library procedure

Constructs a circular list of the elements.

```
(circular-list 'z 'q) \Rightarrow (z q z q z q ...)
```

```
(iota count \ start \ step) \rightarrow list (iota count) \rightarrow list
```

list library procedure list library procedure

Returns a list containing the elements

```
(start start+step ... start+(count-1)*step)
```

The start and step parameters default to 0 and 1, respectively. This procedure takes its name from the APL primitive.

```
(iota 5) => (0 1 2 3 4)
(iota 5 0 -0.1) => (0 -0.1 -0.2 -0.3 -0.4)
```

#### **Predicates**

Note: the predicates proper-list?, circular-list?, and dotted-list? partition the entire universe of Scheme values.

(proper-list? x)  $\rightarrow$  boolean list library procedureReturns true iff x is a proper list – a finite, nil-terminated list.

TODO I'm not sure where this stuff should go. Maybe at the beginning of the section?

More carefully: The empty list is a proper list. A pair whose cdr is a proper list is also a proper list:

Note that this definition rules out circular lists. This function is required to detect this case and return false.

Nil-terminated lists are called "proper" lists by R5RS and Common Lisp. The opposite of proper is improper.

R5RS binds this function to the variable list?.

```
(not (proper-list? x)) = (or (dotted-list? x) (circular-list? x))
```

TODO This needs to be rewritten; definitions should be moved to a "Definitions" section at the front.

```
(circular-list? x) \rightarrow boolean
```

list library procedure

True if x is a circular list. A circular list is a value such that for every  $n \ge 0$ ,  $cdr^n(x)$  is a pair.

Terminology: The opposite of circular is finite.

```
(not (circular-list? x)) = (or (proper-list? x) (dotted-list? x))
```

```
(dotted-list? x) \rightarrow boolean
```

list library procedure

True if x is a finite, non-nil-terminated list. That is, there exists an  $n \ge 0$  such that  $cdr^n(x)$  is neither a pair nor (). This includes non-pair, non-() values (e.g. symbols, numbers), which are considered to be dotted lists of length 0.

```
(not (dotted-list? x)) = (or (proper-list? x) (circular-list? x))
```

```
(pair? object) \rightarrow boolean
```

list library procedure

Returns #t if object is a pair; otherwise, #f.

```
(pair? '(a . b)) =>
                    #t
(pair? '(a b c)) =>
(pair? '())
                =>
(pair? '#(a b)) =>
                    #f
(pair? 7)
                => #f
(pair? 'a)
                => #f
```

(null?  $object) \rightarrow boolean$ 

list library procedure

Returns #t if object is the empty list; otherwise, #f.

```
(null-list? list) \rightarrow boolean
```

list library procedure

list is a proper or circular list. This procedure returns true if the argument is the empty list (), and false otherwise. It is an error to pass this procedure a value which is not a proper or circular list. This procedure is recommended as the termination condition for list-processing procedures that are not defined on dotted lists.

```
(not-pair? x) \rightarrow boolean
```

list library procedure

```
(lambda (x) (not (pair? x)))
```

Provided as a procedure as it can be useful as the termination condition for list-processing procedures that wish to handle all finite lists, both proper and dotted.

```
(list= elt_1 elt_2 ...) \rightarrow boolean
```

list library procedure

Determines list equality, given an element-equality procedure. Proper list A equals proper list B if they are of the same length, and their corresponding elements are equal, as determined by elt=. If the element-comparison procedure's first argument is from list<sub>i</sub>, then its second argument is from list<sub>i+1</sub>, i.e. it is always called as (elt= a b) for a an element of list A, and b an element of list B.

In the n-ary case, every list<sub>i</sub> is compared to list<sub>i+1</sub> (as opposed, for example, to comparing list<sub>1</sub> to every list<sub>i</sub>, for i>1). If there are no list arguments at all, list= simply returns true.

It is an error to apply list= to anything except proper lists. While implementations may choose to extend it to circular lists, note that it cannot reasonably be extended to dotted lists, as it provides no way to specify an equality procedure for comparing the list terminators.

Note that the dynamic order in which the elt= procedure is applied to pairs of elements is not specified. For example, if list= is applied to three lists, A, B, and C, it may first completely compare A to B, then compare B to C, or it may compare the first elements of A and B, then the first elements of B and C, then the second elements of A and B, and so forth.

The equality procedure must be consistent with eq?. That is, it must be the case that

```
(eq? x y) => (elt= x y).
```

Note that this implies that two lists which are eq? are always list=, as well; implementations may exploit this fact to "short-cut" the element-by-element comparisons.

```
(list= eq?) => #t ; Trivial cases
(list= eq? '(a)) => #t
```

#### Selectors

```
(\operatorname{car}\ pair) 	o boolean list library procedure (\operatorname{cdr}\ pair) 	o boolean list library procedure
```

These functions return the contents of the car and cdr field of their argument, respectively. Note that it is an error to apply them to the empty list.

```
(car '(a b c))
                                   (cdr '(a b c))
                                                            (b c)
(car '((a) b c d)) =>
                                    (cdr '((a) b c d)) =>
                                                             (b c d)
                         (a)
(car '(1 . 2))
                                    (cdr '(1 . 2))
                                                            2
                    =>
                        1
                                                        =>
(car '())
                        *error*
                                    (cdr '())
                                                            *error*
```

```
\begin{array}{ll} (\operatorname{caar}\ pair) \to boolean & \text{list library procedure} \\ (\operatorname{cadr}\ pair) \to boolean & \text{list library procedure} \\ \vdots & \\ (\operatorname{cdddar}\ pair) \to boolean & \text{list library procedure} \\ (\operatorname{cddddr}\ pair) \to boolean & \text{list library procedure} \\ \end{array}
```

These procedures are compositions of car and cdr, where for example caddr could be defined by

```
(define caddr (lambda (x) (car (cdr (cdr x))))).
```

Arbitrary compositions, up to four deep, are provided. There are twenty-eight of these procedures in all.

```
(list-ref clist i) \rightarrow value list library procedure
```

Returns the  $i^{th}$  element of clist. (This is the same as the car of (drop clist i).) It is an error if i >= n, where n is the length of clist.

```
(list-ref '(a b c d) 2) \Rightarrow c
```

```
(first pair) \rightarrow value
                                                                                                                         list library procedure
(second pair) \rightarrow value
                                                                                                                         list library procedure
(third pair) \rightarrow value
                                                                                                                         list library procedure
(fourth pair) \rightarrow value
                                                                                                                         list library procedure
(fifth pair) \rightarrow value
                                                                                                                         list library procedure
(sixth pair) \rightarrow value
                                                                                                                         list library procedure
(seventh pair) \rightarrow value
                                                                                                                         list library procedure
(eighth pair) \rightarrow value
                                                                                                                         list library procedure
(nineth pair) \rightarrow value
                                                                                                                         list library procedure
(tenth pair) \rightarrow value
                                                                                                                         list library procedure
```

Synonyms for car, cadr, caddr, ...

```
(third '(a b c d e)) \Rightarrow c
```

```
(car+cdr pair) \rightarrow x y
```

list library procedure

Returns the car and cdr of pair as two values.

```
(lambda (p) (values (car p) (cdr p)))
```

This can, of course, be implemented more efficiently by a compiler.

```
(take x \ i) \rightarrow list
(drop \ x \ i) \rightarrow object
```

list library procedure list library procedure

take returns the first i elements of list x.

drop returns all but the first i elements of list x.

```
(take '(a b c d e) 2) \Rightarrow (a b)
(drop '(a b c d e) 2) \Rightarrow (c d e)
```

x may be any value – a proper, circular, or dotted list:

```
(take '(1 2 3 . d) 2) \Rightarrow (1 2)
(drop '(1 2 3 . d) 2) \Rightarrow (3 . d)
(take '(1 2 3 . d) 3) \Rightarrow (1 2 3)
(drop '(1 2 3 . d) 3) \Rightarrow d
```

For a legal i, take and drop partition the list in a manner which can be inverted with append:

```
(append (take x i) (drop x i)) = x
```

drop is exactly equivalent to performing i cdr operations on x; the returned value shares a common tail with x. If the argument is a list of non-zero length, take is guaranteed to return a freshly-allocated list, even in the case where the entire list is taken, e.g. (take lis (length lis)).

```
(take-right flist i) \rightarrow object
(drop-right flist i) \rightarrow list
```

list library procedure list library procedure

take-right returns the last i elements of flist.

drop-right returns all but the last i elements of flist.

```
(take-right '(a b c d e) 2) \Rightarrow (d e)
(drop-right '(a b c d e) 2) \Rightarrow (a b c)
```

The returned list may share a common tail with the argument list.

flist may be any finite list, either proper or dotted:

```
(take-right '(1 2 3 . d) 2) \Rightarrow (2 3 . d)
(drop-right '(1 2 3 . d) 2) \Rightarrow (1)
(take-right '(1 2 3 . d) 0) => d
(drop-right '(1 2 3 . d) 0) \Rightarrow (1 2 3)
```

For a legal i, take-right and drop-right partition the list in a manner which can be inverted with append:

```
(append (take flist i) (drop flist i)) = flist
```

take-right's return value is guaranteed to share a common tail with flist. If the argument is a list of non-zero length, drop-right is guaranteed to return a freshly-allocated list, even in the case where nothing is dropped, e.q. (drop-right lis 0).

```
(take! x i) \rightarrow list
(drop-right! flist i) \rightarrow list
```

list library procedure list library procedure

take! and drop-right! are "linear-update" variants of take and drop-right: the procedure is allowed, but not required, to alter the argument list to produce the result.

If x is circular, take! may return a shorter-than-expected list:

```
(take! (circular-list 1 3 5) 8) \Rightarrow (1 3)
(take! (circular-list 1 3 5) 8) => (1 3 5 1 3 5 1 3)
```

```
(split-at x i) \rightarrow list \ object
(split-at! x \ i) \rightarrow list \ object
```

list library procedure list library procedure

split-at splits the list x at index i, returning a list of the first i elements, and the remaining tail. It is equivalent to

```
(values (take x i) (drop x i))
```

split-at! is the linear-update variant. It is allowed, but not required, to alter the argument list to produce the result.

```
(split-at '(a b c d e f g h) 3) =>
   (a b c)
   (defgh)
```

```
(last pair) \rightarrow object
(last-pair pair) \rightarrow pair
```

list library procedure list library procedure

last returns the last element of the non-empty, finite list pair. last-pair returns the last pair in the non-empty, finite list pair.

```
(last '(a b c)) \Rightarrow c
(last-pair '(a b c)) \Rightarrow (c)
```

#### Miscellaneous

```
(length list) \rightarrow integer
(length+ list) \rightarrow integer or #f
```

list library procedure list library procedure

Both length and length+ return the length of the argument. It is an error to pass a value to length which is not a proper list (finite and nil-terminated). In particular, this means an implementation may diverge or signal an error when length is applied to a circular list.

length+, on the other hand, returns #F when applied to a circular list.

The length of a proper list is a non-negative integer n such that cdr applied n times to the list produces the empty list.

```
(append list_1 ...) \rightarrow list
(append! list_1 ...) \rightarrow list
```

list library procedure list library procedure

append returns a list consisting of the elements of  $list_1$  followed by the elements of the other list parameters.

```
(append '(x) '(y))
                         => (x y)
(append '(a) '(b c d))
                         => (a b c d)
(append '(a (b)) '((c))) => (a (b) (c))
```

The resulting list is always newly allocated, except that it shares structure with the final list; argument. This last argument may be any value at all; an improper list results if it is not a proper list. All other arguments must be proper lists.

```
(append '(a b) '(c . d)) \Rightarrow (a b c . d)
(append '() 'a)
                           => a
(append '(x y))
                           => (x y)
                           => ()
(append)
```

append! is the "linear-update" variant of append – it is allowed, but not required, to alter cons cells in the argument lists to construct the result list. The last argument is never altered; the result list shares structure with this parameter.

```
(concatenate list-of-lists) \rightarrow value
(concatenate! list-of-lists) \rightarrow value
```

list library procedure list library procedure

These functions append the elements of their argument together. That is, concatenate returns

```
(apply append list-of-lists)
```

or, equivalently,

```
(reduce-right append '() list-of-lists)
```

concatenate! is the linear-update variant, defined in terms of append! instead of append.

Note that some Scheme implementations do not support passing more than a certain number (e.g., 64) of arguments to an n-ary procedure. In these implementations, the (apply append ...) idiom would fail when applied to long lists, but concatenate would continue to function properly.

As with append and append!, the last element of the input list may be any value at all.

```
(reverse list) \rightarrow list
(reverse! list) \rightarrow list
```

list library procedure list library procedure

reverse returns a newly allocated list consisting of the elements of list in reverse order.

```
(reverse '(a b c)) \Rightarrow (c b a)
(reverse '(a (b c) d (e (f))))
    => ((e (f)) d (b c) a)
```

reverse! is the linear-update variant of reverse. It is permitted, but not required, to alter the argument's cons cells to produce the reversed list.

```
(append-reverse rev-head tail) \rightarrow list
(append-reverse! rev-head\ tail) \rightarrow list
```

list library procedure list library procedure

append-reverse returns (append (reverse rev-head) tail). It is provided because it is a common operation - a common list-processing style calls for this exact operation to transfer values accumulated in reverse order onto the front of another list, and because the implementation is significantly more efficient than the simple composition it replaces. (But note that this pattern of iterative computation followed by a reverse can frequently be rewritten as a recursion, dispensing with the reverse and append-reverse steps, and shifting temporary, intermediate storage from the heap to the stack, which is typically a win for reasons of cache locality and eager storage reclamation.)

append-reverse! is just the linear-update variant - it is allowed, but not required, to alter rev-head's cons cells to construct the result.

```
(zip clist_1 clist_2 ...) \rightarrow list
```

list library procedure

```
(lambda lists (apply map list lists))
```

If zip is passed n lists, it returns a list as long as the shortest of these lists, each element of which is an n-element list comprised of the corresponding elements from the parameter lists.

```
(zip '(one two three)
     '(1 2 3)
     '(odd even odd even odd even))
   => ((one 1 odd) (two 2 even) (three 3 odd))
(zip '(1 2 3)) \Rightarrow ((1) (2) (3))
```

At least one of the argument lists must be finite:

(zip '(3 1 4 1) (circular-list #f #t))

```
=> ((3 #f) (1 #t) (4 #f) (1 #t))
(unzip1 list) \rightarrow list
                                                                                                                          list library procedure
(unzip2 list) \rightarrow list list
                                                                                                                          list library procedure
                                                                                                                          list library procedure
(unzip3 list) \rightarrow list list list
(unzip4 \ list) \rightarrow list \ list \ list \ list
                                                                                                                          list library procedure
(unzip5 list) \rightarrow list list list list
                                                                                                                          list library procedure
```

unzip1 takes a list of lists, where every list must contain at least one element, and returns a list containing the initial element of each such list. That is, it returns (map car lists). unzip2 takes a list of lists, where every list must contain at least two elements, and returns two values: a list of the first elements, and a list of the second elements. unzip3 does the same for the first three elements of the lists, and so forth.

```
(unzip2 '((1 one) (2 two) (3 three))) =>
    (1 \ 2 \ 3)
    (one two three)
```

(count  $clist_1$   $clist_2$  ...)  $\rightarrow integer$ 

list library procedure

TODO The ellipsis wasn't present in the original. Is this a mistake?

pred is a procedure taking as many arguments as there are lists and returning a single value. It is applied element-wise to the elements of the lists, and a count is tallied of the number of elements that produce a true value. This count is returned. count is "iterative" in that it is guaranteed to apply pred to the list elements in a left-to-right order. The counting stops when the shortest list expires.

```
(count even? '(3 1 4 1 5 9 2 5 6)) \Rightarrow 3
(count < '(1 2 4 8) '(2 4 6 8 10 12 14 16)) => 3
At least one of the argument lists must be finite:
(count < '(3 1 4 1) (circular-list 1 10)) => 2
```

#### Fold, unfold, and map

```
(fold kons \ knil \ clist_1 \ clist_2 \ ...) \rightarrow value
```

list library procedure

;; How many symbols in LIS?

```
The fundamental list iterator.
First, consider the single list-parameter case. If clist_1 = (e_1 \ e_2 \ ... \ e_n), then this procedure returns
(kons en ... (kons e2 (kons e1 knil)) ...)
That is, it obeys the (tail) recursion
(fold kons knil lis) = (fold kons (kons (car lis) knil) (cdr lis))
(fold kons knil '()) = knil
Examples:
(fold + 0 lis)
                           ; Add up the elements of LIS.
(fold cons '() lis)
                           ; Reverse LIS.
(fold cons tail rev-head)
                                ; See APPEND-REVERSE.
```

```
(fold (lambda (x count) (if (symbol? x) (+ count 1) count))
      lis)
;; Length of the longest string in LIS:
(fold (lambda (s max-len) (max max-len (string-length s)))
     lis)
```

If n list arguments are provided, then the kons function must take n+1 parameters: one element from each list, and the "seed" or fold state, which is initially knil. The fold operation terminates when the shortest list runs out of values:

```
(fold cons*'()'(a b c)'(1 2 3 4 5)) \Rightarrow (c 3 b 2 a 1)
```

At least one of the list arguments must be finite.

```
(fold-right kons knil clist<sub>1</sub> clist<sub>2</sub> ...) \rightarrow value
```

list library procedure

The fundamental list recursion operator.

First, consider the single list-parameter case. If  $clist_1 = (e1 \ e2 \ ... \ en)$ , then this procedure returns

```
(kons e1 (kons e2 ... (kons en knil)))
```

That is, it obeys the recursion

```
(fold-right kons knil lis) = (kons (car lis) (fold-right kons knil (cdr lis)))
(fold-right kons knil '()) = knil
```

Examples:

```
(fold-right cons '() lis)
                                 ; Copy LIS.
```

```
;; Filter the even numbers out of LIS.
(fold-right (lambda (x 1) (if (even? x) (cons x 1) 1)) '() lis))
```

If n list arguments are provided, then the kons function must take n+1 parameters: one element from each list, and the "seed" or fold state, which is initially knil. The fold operation terminates when the shortest list runs out of values:

```
(fold-right cons* '() '(a b c) '(1 2 3 4 5)) => (a 1 b 2 c 3)
```

At least one of the list arguments must be finite.

```
(pair-fold kons knil clist<sub>1</sub> clist<sub>2</sub> ...) \rightarrow value
```

list library procedure

Analogous to fold, but kons is applied to successive sublists of the lists, rather than successive elements – that is, kons is applied to the pairs making up the lists, giving this (tail) recursion:

```
(pair-fold kons knil lis) = (let ((tail (cdr lis)))
                              (pair-fold kons (kons lis knil) tail))
(pair-fold kons knil '()) = knil
```

For finite lists, the kons function may reliably apply set-cdr! to the pairs it is given without altering the sequence of execution.

Example:

```
;;; Destructively reverse a list.
(pair-fold (lambda (pair tail) (set-cdr! pair tail) pair) '() lis))
```

At least one of the list arguments must be finite.

```
(pair-fold-right kons knil clist<sub>1</sub> clist<sub>2</sub> ...) \rightarrow value
```

list library procedure

Holds the same relationship with fold-right that pair-fold holds with fold. Obeys the recursion

```
(pair-fold-right kons knil lis) =
     (kons lis (pair-fold-right kons knil (cdr lis)))
(pair-fold-right kons knil '()) = knil
Example:
(pair-fold-right cons '() '(a b c)) \Rightarrow ((a b c) (b c) (c))
At least one of the list arguments must be finite.
(reduce f ridentity list) \rightarrow value
                                                                                                list library procedure
reduce is a variant of fold.
ridentity should be a "right identity" of the procedure f - that is, for any value x acceptable to f,
(f \times ridentity) = x
reduce has the following definition:
If list = (), return ridentity;
Otherwise, return (fold f (car list) (cdr list)).
...in other words, we compute (fold f ridentity list).
Note that ridentity is used only in the empty-list case. You typically use reduce when applying f is expensive and you'd
like to avoid the extra application incurred when fold applies f to the head of list and the identity value, redundantly
producing the same value passed in to f. For example, if f involves searching a file directory or performing a database
query, this can be significant. In general, however, fold is useful in many contexts where reduce is not (consider the
examples given in the fold definition – only one of the five folds uses a function with a right identity. The other four
may not be performed with reduce).
Note: MIT Scheme and Haskell flip F's arg order for their reduce and fold functions.
;; Take the max of a list of non-negative integers.
(reduce max 0 nums); i.e., (apply max 0 nums)
(reduce-right f ridentity list) \rightarrow value
                                                                                                list library procedure
reduce-right is the fold-right variant of reduce. It obeys the following definition:
(reduce-right f ridentity '()) = ridentity
(reduce-right f ridentity '(e1)) = (f e1 ridentity) = e1
(reduce-right f ridentity '(e1 e2 ...)) =
     (f e1 (reduce f ridentity (e2 ...)))
...in other words, we compute (fold-right f ridentity list).
;; Append a bunch of lists together.
;; I.e., (apply append list-of-lists)
(reduce-right append '() list-of-lists)
(unfold p f g seed tail\text{-}gen) \rightarrow list
                                                                                                list library procedure
(unfold p \ f \ g \ seed) \rightarrow list
                                                                                                list library procedure
unfold is best described by its basic recursion:
(unfold p f g seed) =
     (if (p seed) (tail-gen seed)
         (cons (f seed)
                (unfold p f g (g seed))))
```

**p** Determines when to stop unfolding.

list library procedure

list library procedure

- **f** Maps each seed value to the corresponding list element.
- g Maps each seed value to next seed value.

**seed** The "state" value for the unfold.

tail-gen Creates the tail of the list; defaults to (lambda (x) '())

In other words, we use g to generate a sequence of seed values

```
seed, g(seed), g<sup>2</sup>(seed), g<sup>3</sup>(seed), ...
```

These seed values are mapped to list elements by f, producing the elements of the result list in a left-to-right order. P says when to stop.

unfold is the fundamental recursive list constructor, just as fold-right is the fundamental recursive list consumer. While unfold may seem a bit abstract to novice functional programmers, it can be used in a number of ways:

```
;; List of squares: 1^2 ... 10^2
(unfold (lambda (x) (> x 10))
        (lambda (x) (* x x))
   (lambda (x) (+ x 1))
   1)
(unfold null-list? car cdr lis); Copy a proper list.
;; Read current input port into a list of values.
(unfold eof-object? values (lambda (x) (read)) (read))
;; Copy a possibly non-proper list:
(unfold not-pair? car cdr lis
             values)
;; Append HEAD onto TAIL:
(unfold null-list? car cdr head
              (lambda (x) tail))
```

Interested functional programmers may enjoy noting that fold-right and unfold are in some sense inverses. That is, given operations knull?, kar, kdr, kons, and knil satisfying

```
(kons (kar x) (kdr x)) = x and (knull? knil) = \#t
then
(fold-right kons knil (unfold knull? kar kdr x)) = x
and
(unfold knull? kar kdr (fold-right kons knil x)) = x.
```

This combinator sometimes is called an "anamorphism;" when an explicit tail-gen procedure is supplied, it is called an "apomorphism."

```
(unfold-right p \ f \ g \ seed \ tail) \rightarrow list
(unfold-right p \ f \ g \ seed) \rightarrow list
unfold-right constructs a list with the following loop:
(let lp ((seed seed) (lis tail))
  (if (p seed) lis
        (lp (g seed)
             (cons (f seed) lis))))
```

- **p** Determines when to stop unfolding.
- **f** Maps each seed value to the corresponding list element.

tail list terminator; defaults to '().

In other words, we use g to generate a sequence of seed values seed, g(seed), g<sup>2</sup>(seed), g<sup>3</sup>(seed), ...

These seed values are mapped to list elements by f, producing the elements of the result list in a right-to-left order. P says when to stop.

unfold-right is the fundamental iterative list constructor, just as fold is the fundamental iterative list consumer. While unfold-right may seem a bit abstract to novice functional programmers, it can be used in a number of ways:

Interested functional programmers may enjoy noting that fold and unfold-right are in some sense inverses. That is, given operations knull?, kar, kdr, kons, and knil satisfying

```
(kons (kar x) (kdr x)) = x and (knull? knil) = #t then (fold kons knil (unfold-right knull? kar kdr x)) = x and (unfold-right knull? kar kdr (fold kons knil x)) = x.
```

This combinator presumably has some pretentious mathematical name; interested readers are invited to communicate it to the author. TODO Do we want to say anything about this?

```
(map proc clist_1 clist_2 ...) \rightarrow list
```

list library procedure

proc is a procedure taking as many arguments as there are list arguments and returning a single value. map applies proc element-wise to the elements of the lists and returns a list of the results, in order. The dynamic order in which proc is applied to the elements of the lists is unspecified.

This procedure is extended from its R5RS specification to allow the arguments to be of unequal length; it terminates when the shortest list runs out.

At least one of the argument lists must be finite:

```
(map + '(3 1 4 1) (circular-list 1 0)) \Rightarrow (4 1 5 1)
```

```
(for-each proc \ clist_1 \ clist_2 \ ...) \rightarrow unspecified
```

list library procedure

[R5RS+] The arguments to for-each are like the arguments to map, but for-each calls proc for its side effects rather than for its values. Unlike map, for-each is guaranteed to call proc on the elements of the lists in order from the first element(s) to the last, and the value returned by for-each is unspecified.

```
(let ((v (make-vector 5)))
 (for-each (lambda (i)
              (vector-set! v i (* i i)))
            '(0 1 2 3 4))
 v) => #(0 1 4 9 16)
```

This procedure is extended from its R5RS specification to allow the arguments to be of unequal length; it terminates when the shortest list runs out.

At least one of the argument lists must be finite.

```
(append-map f clist_1 clist_2 ...) \rightarrow value
                                                                                                          list library procedure
(append-map! f \ clist_1 \ clist_2 \ ...) \rightarrow value
                                                                                                          list library procedure
Equivalent to
 (apply append (map f clist1 clist2 ...))
and
 (apply append! (map f clist1 clist2 ...))
```

Map f over the elements of the lists, just as in the map function. However, the results of the applications are appended together to make the final result. append-map uses append to append the results together; append-map! uses append!.

The dynamic order in which the various applications of f are made is not specified.

Example:

```
(append-map! (lambda (x) (list x (-x))) '(1 3 8))
   => (1 -1 3 -3 8 -8)
```

At least one of the list arguments must be finite.

```
(map! f \ list_1 \ clist_2 \ ...) \rightarrow list
```

list library procedure

Linear-update variant of map - map! is allowed, but not required, to alter the cons cells of list1 to construct the result list.

The dynamic order in which the various applications of f are made is not specified. In the n-ary case, clist<sub>2</sub>, clist<sub>3</sub>, ... must have at least as many elements as list<sub>1</sub>.

```
(map-in-order \ f \ clist_1 \ clist_2 \ ...) \rightarrow list
```

list library procedure

A variant of the map procedure that guarantees to apply f across the elements of the list; arguments in a left-to-right order. This is useful for mapping procedures that both have side effects and return useful values.

At least one of the list arguments must be finite.

```
(pair-for-each f clist_1 clist_2 ...) \rightarrow unspecific
```

list library procedure

TODO I think the above should be "unspecified", but in the original it says "unspecific". Correct?

Like for-each, but f is applied to successive sublists of the argument lists. That is, f is applied to the cons cells of the lists, rather than the lists' elements. These applications occur in left-to-right order.

The f procedure may reliably apply set-cdr! to the pairs it is given without altering the sequence of execution.

```
(pair-for-each (lambda (pair) (display pair) (newline)) '(a b c)) ==>
  (a b c)
  (b c)
  (c)
```

At least one of the list arguments must be finite.

```
(filter-map f clist_1 clist_2 ...) \rightarrow list
```

list library procedure

Like map, but only true values are saved.

```
(filter-map (lambda (x) (and (number? x) (* x x))) '(a 1 b 3 c 7)) => (1 9 49)
```

The dynamic order in which the various applications of f are made is not specified.

At least one of the list arguments must be finite.

#### Filtering and partitioning

TODO introduction

```
(filter pred\ list) \rightarrow list
```

list library procedure

Return all the elements of list that satisfy predicate pred. The list is not disordered – elements that appear in the result list occur in the same order as they occur in the argument list. The returned list may share a common tail with the argument list. The dynamic order in which the various applications of pred are made is not specified.

```
(filter even? '(0 7 8 8 43 -4)) \Rightarrow (0 8 8 -4)
```

```
(partition pred\ list) \rightarrow list\ list
```

list library procedure

Partitions the elements of list with predicate pred, and returns two values: the list of in-elements and the list of outelements. The list is not disordered – elements occur in the result lists in the same order as they occur in the argument list. The dynamic order in which the various applications of pred are made is not specified. One of the returned lists may share a common tail with the argument list.

```
(partition symbol? '(one 2 3 four five 6)) =>
  (one four five)
  (2 3 6)
```

(remove  $pred\ list$ )  $\rightarrow list$ 

list library procedure

Returns list without the elements that satisfy predicate pred:

```
(lambda (pred list) (filter (lambda (x) (not (pred x))) list))
```

The list is not disordered – elements that appear in the result list occur in the same order as they occur in the argument list. The returned list may share a common tail with the argument list. The dynamic order in which the various applications of pred are made is not specified.

```
(remove even? '(0 7 8 8 43 -4)) => (7 43)
```

```
(filter! pred\ list) \rightarrow list\ library\ procedure
(partition! pred\ list) \rightarrow list\ library\ procedure
(remove! pred\ list) \rightarrow list
list library procedure
```

Linear-update variants of filter, partition and remove. These procedures are allowed, but not required, to alter the cons cells in the argument list to construct the result lists.

#### Searching

TODO reorganize this introductory material, some of it belongs in the procedure entries.

The following procedures all search lists for a leftmost element satisfying some criteria. This means they do not always examine the entire list; thus, there is no efficient way for them to reliably detect and signal an error when passed a dotted or circular list. Here are the general rules describing how these procedures work when applied to different kinds of lists:

**Proper lists:** The standard, canonical behavior happens in this case.

**Dotted lists:** It is an error to pass these procedures a dotted list that does not contain an element satisfying the search criteria. That is, it is an error if the procedure has to search all the way to the end of the dotted list. However, this SRFI does not specify anything at all about the behavior of these procedures when passed a dotted list containing an element satisfying the search criteria. It may finish successfully, signal an error, or perform some third action. Different implementations may provide different functionality in this case; code which is compliant with this SRFI may not rely on any particular behavior. Future SRFI's may refine SRFI-1 to define specific behavior in this case. In brief, SRFI-1 compliant code may not pass a dotted list argument to these procedures.

Circular lists: It is an error to pass these procedures a circular list that does not contain an element satisfying the search criteria. Note that the procedure is not required to detect this case; it may simply diverge. It is, however, acceptable to search a circular list if the search is successful – that is, if the list contains an element satisfying the search criteria.

Here are some examples, using the find and any procedures as canonical representatives:

```
;; Proper list -- success
(find even? '(1 2 3))
(any even? '(1 2 3))
                        => #t
;; proper list -- failure
(find even? '(1 7 3))
(any even? '(1 7 3))
                        => #f
;; Failure is error on a dotted list.
(find even? '(1 3 . x)) \Rightarrow error
(any even? '(1 3 . x)) \Rightarrow error
;; The dotted list contains an element satisfying the search.
;; This case is not specified -- it could be success, an error,
;; or some third possibility.
(find even? '(1 2 . x)) => error/undefined
(any even? '(1 2 . x)) => error/undefined; success, error or other.
;; circular list -- success
(find even? (circular-list 1 6 3)) => 6
(any even? (circular-list 1 6 3)) => #t
;; circular list -- failure is error. Procedure may diverge.
(find even? (circular-list 1 3)) => error
(any even? (circular-list 1 3)) => error
```

(find  $pred\ clist$ )  $\rightarrow value$ 

list library procedure

Return the first element of clist that satisfies predicate pred; false if no element does.

```
(find even? '(3 1 4 1 5 9)) \Rightarrow 4
```

Note that find has an ambiguity in its lookup semantics – if find returns #f, you cannot tell (in general) if it found a #f element that satisfied pred, or if it did not find any element at all. In many situations, this ambiguity cannot arise

```
(cond ((find-tail pred lis) => (lambda (pair) ...)) ; Handle (CAR PAIR)
      (else ...)) ; Search failed.
```

```
(find-tail pred\ clist) \rightarrow pair\ or\ \#f
```

list library procedure

Return the first pair of clist whose car satisfies pred. If no pair does, return false.

find-tail can be viewed as a general-predicate variant of the member function.

Examples:

```
(find-tail even? '(3 1 37 -8 -5 0 0)) => (-8 -5 0 0)
(find-tail even? '(3 1 37 -5)) => #f

;; MEMBER X LIS:
(find-tail (lambda (elt) (equal? x elt)) lis)
```

In the circular-list case, this procedure "rotates" the list.

Find-tail is essentially drop-while, where the sense of the predicate is inverted: Find-tail searches until it finds an element satisfying the predicate; drop-while searches until it finds an element that doesn't satisfy the predicate.

```
(take-while pred\ clist) \rightarrow list (take-while! pred\ clist) \rightarrow list
```

list library procedure list library procedure

Returns the longest initial prefix of clist whose elements all satisfy the predicate pred.

Take-while! is the linear-update variant. It is allowed, but not required, to alter the argument list to produce the result

```
(take-while even? '(2 18 3 10 22 9)) \Rightarrow (2 18)
```

```
(drop-while pred\ clist) \rightarrow list
```

list library procedure

Drops the longest initial prefix of clist whose elements all satisfy the predicate pred, and returns the rest of the list.

```
(drop-while even? '(2 18 3 10 22 9)) \Rightarrow (3 10 22 9)
```

The circular-list case may be viewed as "rotating" the list.

```
(span pred clist) \rightarrow list clistlist library procedure(span! pred list) \rightarrow list listlist library procedure(break pred clist) \rightarrow list clistlist library procedure(break! pred list) \rightarrow list listlist library procedure
```

span splits the list into the longest initial prefix whose elements all satisfy pred, and the remaining tail. break inverts the sense of the predicate: the tail commences with the first element of the input list that satisfies the predicate.

In other words: span finds the intial span of elements satisfying pred, and break breaks the list at the first element satisfying pred.

span is equivalent to

span! and break! are the linear-update variants. They are allowed, but not required, to alter the argument list to produce the result.

```
(span even? '(2 18 3 10 22 9)) =>
 (218)
 (3\ 10\ 22\ 9)
(break even? '(3 1 4 1 5 9)) =>
 (3\ 1)
 (4159)
```

(any pred clist<sub>1</sub> clist<sub>2</sub> ...)  $\rightarrow$  value

list library procedure

Applies the predicate across the lists, returning true TODO #t? if the predicate returns true on any application.

If there are n list arguments  $clist_1$  ...  $clist_n$ , then pred must be a procedure taking n arguments and returning a single value, interpreted as a boolean (that is, #f means false, and any other value means true).

any applies pred to the first elements of the clist; parameters. If this application returns a true value, any immediately returns that value. Otherwise, it iterates, applying pred to the second elements of the clistic parameters, then the third, and so forth. The iteration stops when a true value is produced or one of the lists runs out of values; in the latter case, any returns #f. The application of pred to the last element of the lists is a tail call.

Note the difference between find and any - find returns the element that satisfied the predicate; any returns the true value that the predicate produced.

Like every, any's name does not end with a question mark – this is to indicate that it does not return a simple boolean (#t or #f), but a general value.

```
(any integer? '(a 3 b 2.7))
(any integer? '(a 3.1 b 2.7)) => #f
(any < '(3 1 4 1 5))
       '(2 7 1 8 2)) => #t
```

(every  $pred\ clist_1\ clist_2\ ...) \rightarrow value$ 

list library procedure

Applies the predicate across the lists, returning true if the predicate returns true on every application.

If there are n list arguments clist<sub>1</sub> ... clist<sub>n</sub>, then pred must be a procedure taking n arguments and returning a single value, interpreted as a boolean (that is, #f means false, and any other value means true).

every applies pred to the first elements of the clist; parameters. If this application returns false, every immediately returns false. Otherwise, it iterates, applying pred to the second elements of the clist; parameters, then the third, and so forth. The iteration stops when a false value is produced or one of the lists runs out of values. In the latter case, every returns the true value produced by its final application of pred. The application of pred to the last element of the lists is a tail call.

If one of the clist, has no elements, every simply returns #t.

Like any, every's name does not end with a question mark – this is to indicate that it does not return a simple boolean (#t or #f), but a general value.

```
(list-index pred clist_1 clist_2) \rightarrow integer or #f
```

list library procedure

Return the index of the leftmost element that satisfies pred.

If there are n list arguments clist<sub>1</sub> ... clist<sub>n</sub>, then pred must be a function taking n arguments and returning a single value, interpreted as a boolean (that is, #f means false, and any other value means true).

list-index applies pred to the first elements of the clist; parameters. If this application returns true, list-index immediately returns zero. Otherwise, it iterates, applying pred to the second elements of the clist, parameters, then the third, and so forth. When it finds a tuple of list elements that cause pred to return true, it stops and returns the zero-based index of that position in the lists.

The iteration stops when one of the lists runs out of values; in this case, list-index returns #f.

(list-index even? '(3 1 4 1 5 9)) => 2

```
(list-index < '(3 1 4 1 5 9 2 5 6) '(2 7 1 8 2)) => 1
(list-index = '(3 1 4 1 5 9 2 5 6) '(2 7 1 8 2)) => #f
```

```
\begin{array}{ll} (\texttt{member} \ x \ list \ =) \rightarrow list \\ (\texttt{member} \ x \ list) \rightarrow list \\ (\texttt{memq} \ x \ list) \rightarrow list \\ (\texttt{memv} \ x \ list) \rightarrow list \\ \end{array} list library procedure (\texttt{memv} \ x \ list) \rightarrow list \\ (\texttt{memv} \ x \ list) \rightarrow list \\ \end{array} list library procedure
```

[R5RS+] These procedures return the first sublist of list whose car is x, where the sublists of list are the non-empty lists returned by (drop list i) for i less than the length of list. If x does not occur in list, then #f is returned. memq uses eq? to compare x with the elements of list, while memv uses eqv?, and member uses equal?.

```
(memq 'a '(a b c))
                             =>
                                 (a b c)
(memq 'b '(a b c))
                                 (b c)
(memq 'a '(b c d))
                                 #f
(memq (list 'a) '(b (a) c)) =>
(member (list 'a)
        '(b (a) c))
                                 ((a) c)
(memg 101 '(100 101 102))
                             =>
                                 *unspecified*
(memv 101 '(100 101 102))
                                (101 102)
                             =>
```

member is extended from its R5RS definition to allow the client to pass in an optional equality procedure = used to compare keys.

The comparison procedure is used to compare the elements e<sub>i</sub> of list to the key x in this way:

```
(= x ei) ; list is (E1 ... En)
```

That is, the first argument is always x, and the second argument is one of the list elements. Thus one can reliably find the first element of list that is greater than five with (member 5 list <)

Note that fully general list searching may be performed with the find-tail and find procedures, e.g.

(find-tail even? list); Find the first elt with an even key.

#### Deletion

```
(delete x \ list =) \rightarrow listlist library procedure(delete x \ list) \rightarrow listlist library procedure(delete! x \ list =) \rightarrow listlist library procedure???(delete! x \ list) \rightarrow listlist library procedure???
```

delete uses the comparison procedure =, which defaults to equal?, to find all elements of list that are equal to x, and deletes them from list. The dynamic order in which the various applications of = are made is not specified.

The list is not disordered – elements that appear in the result list occur in the same order as they occur in the argument list. The result may share a common tail with the argument list.

Note that fully general element deletion can be performed with the remove and remove! procedures, e.g.:

```
;; Delete all the even elements from LIS: (remove even? lis)
```

The comparison procedure is used in this way: (= x ei). That is, x is always the first argument, and a list element is always the second argument. The comparison procedure will be used to compare each element of list exactly once; the order in which it is applied to the various  $e_i$  is not specified. Thus, one can reliably remove all the numbers greater than five from a list with (delete 5 list <)

delete! is the linear-update variant of delete. It is allowed, but not required, to alter the cons cells in its argument list to construct the result.

```
(delete-duplicates list = ) \rightarrow list
                                                                                                                   list library procedure
                                                                                                                   list library procedure
(delete-duplicates list) \rightarrow list
(delete-duplicates! list = ) \rightarrow list
                                                                                                                   list library procedure
(delete-duplicates! list) \rightarrow list
                                                                                                                   list library procedure
```

delete-duplicates removes duplicate elements from the list argument. If there are multiple equal elements in the argument list, the result list only contains the first or leftmost of these elements in the result. The order of these surviving elements is the same as in the original list - delete-duplicates does not disorder the list (hence it is useful for "cleaning up" association lists).

The = parameter is used to compare the elements of the list; it defaults to equal?. If x comes before y in list, then the comparison is performed (= x y). The comparison procedure will be used to compare each pair of elements in list no more than once; the order in which it is applied to the various pairs is not specified.

Implementations of delete-duplicates are allowed to share common tails between argument and result lists – for example, if the list argument contains only unique elements, it may simply return exactly this list.

Be aware that, in general, delete-duplicates runs in time  $O(n^2)$  for n-element lists. Uniquifying long lists can be accomplished in O(n lg n) time by sorting the list to bring equal elements together, then using a linear-time algorithm to remove equal elements. Alternatively, one can use algorithms based on element-marking, with linear-time results.

delete-duplicates! is the linear-update variant of delete-duplicates; it is allowed, but not required, to alter the cons cells in its argument list to construct the result.

```
(delete-duplicates '(a b a c a b c z)) => (a b c z)
;; Clean up an alist:
(delete-duplicates '((a . 3) (b . 7) (a . 9) (c . 1))
                   (lambda (x y) (eq? (car x) (car y))))
   => ((a . 3) (b . 7) (c . 1))
```

#### Association lists

An "association list" (or "alist") is a list of pairs. The car of each pair contains a key value, and the cdr contains the associated data value. They can be used to construct simple look-up tables in Scheme. Note that association lists are probably inappropriate for performance-critical use on large data; in these cases, hash tables or some other alternative should be employed.

```
(assoc key \ alist =) \rightarrow pair \ or \ \#f
                                                                                                                            list library procedure
(assoc key\ alist) \rightarrow pair\ or\ \#f
                                                                                                                            list library procedure
(assq key\ alist) \rightarrow pair\ or\ \#f
                                                                                                                            list library procedure
(assv key\ alist) \rightarrow pair\ or\ \#f
                                                                                                                            list library procedure
```

[R5RS+] alist must be an association list – a list of pairs. These procedures find the first pair in alist whose car field is key, and returns that pair. If no pair in alist has key as its car, then #f is returned. assq uses eq? to compare key with the car fields of the pairs in alist, while assv uses equ? and assoc uses equal?.

```
(define e '((a 1) (b 2) (c 3)))
(assq 'a e)
                                             (a 1)
(assq 'b e)
                                             (b 2)
(assq 'd e)
                                             #f
(assq (list 'a) '(((a)) ((b)) ((c))))
                                             #f
                                         =>
(assoc (list 'a) '(((a)) ((b)) ((c)))) \Rightarrow ((a))
(assq 5 '((2 3) (5 7) (11 13)))
                                         *unspecified*
(assv 5 '((2 3) (5 7) (11 13)))
                                         (57)
```

assoc is extended from its R5RS definition to allow the client to pass in an optional equality procedure = used to compare keys.

The comparison procedure is used to compare the elements e<sub>i</sub> of list to the key parameter in this way:

```
(= key (car ei)) ; list is (E1 ... En)
```

That is, the first argument is always key, and the second argument is one of the list elements. Thus one can reliably find the first entry of alist whose key is greater than five with (assoc 5 alist <)

Note that fully general alist searching may be performed with the find-tail and find procedures, e.g.

```
;; Look up the first association in alist with an even key: (find (lambda (a) (even? (car a))) alist)
```

```
(alist-cons key\ datum\ alist) \rightarrow alist
```

list library procedure

```
(lambda (key datum alist) (cons (cons key datum) alist))
```

Cons a new alist entry mapping key to datum onto alist.

```
(alist-copy alist) \rightarrow alist
```

list library procedure

Make a fresh copy of alist. This means copying each pair that forms an association as well as the spine of the list, i.e.

```
(lambda (a) (map (lambda (elt) (cons (car elt) (cdr elt))) a))
```

```
(alist-delete key \ alist = ) \rightarrow alist list library procedure (alist-delete key \ alist) \rightarrow alist list library procedure (alist-delete! key \ alist = ) \rightarrow alist list library procedure??? (alist-delete! key \ alist) \rightarrow alist list library procedure???
```

alist-delete deletes all associations from alist with the given key, using key-comparison procedure =, which defaults to equal? The dynamic order in which the various applications of = are made is not specified.

Return values may share common tails with the alist argument. The alist is not disordered – elements that appear in the result alist occur in the same order as they occur in the argument alist.

The comparison procedure is used to compare the element keys  $k_i$  of alist's entries to the key parameter in this way: (= key ki). Thus, one can reliably remove all entries of alist whose key is greater than five with (alist-delete 5 alist <)

alist-delete! is the linear-update variant of alist-delete. It is allowed, but not required, to alter cons cells from the alist parameter to construct the result.

#### Set operations on lists

These procedures implement operations on sets represented as lists of elements. They all take an = argument used to compare elements of lists. This equality procedure is required to be consistent with eq?. That is, it must be the case that

```
(eq? x y) => (= x y).
```

Note that this implies, in turn, that two lists that are eq? are also set-equal by any legal comparison procedure. This allows for constant-time determination of set operations on eq? lists.

Be aware that these procedures typically run in time O(n \* m) for n- and m-element list arguments. Performance-critical applications operating upon large sets will probably wish to use other data structures and algorithms.

```
(lset<== list_1 ...) \rightarrow boolean
```

list library procedure

Returns true iff every list<sub>i</sub> is a subset of list<sub>i+1</sub>, using = for the element-equality procedure. List A is a subset of list B if every element in A is equal to some element of B. When performing an element comparison, the = procedure's first argument is an element of A; its second, an element of B.

```
(lset \le eq? '(a) '(a b a) '(a b c c)) => #t
(lset \le eq?) => #t
                                 ; Trivial cases
(lset <= eq? '(a)) => #t
```

(lset= 
$$= list_1 \ list_2 \ ...$$
)  $\rightarrow boolean$ 

list library procedure

Returns true iff every list<sub>i</sub> is set-equal to list<sub>i+1</sub>, using = for the element-equality procedure. "Set-equal" simply means that  $list_i$  is a subset of  $list_{i+1}$ , and  $list_{i+1}$  is a subset of  $list_i$ . The = procedure's first argument is an element of  $list_i$ ; its second is an element of  $list_{i+1}$ .

```
(lset= eq? '(b e a) '(a e b) '(e e b a)) => #t
                               ; Trivial cases
(lset= eq?) => #t
(lset= eq? '(a)) => #t
```

```
(lset-adjoin = list \ elt_1 \ ...) \rightarrow list
```

list library procedure

Adds the  $elt_i$  elements not already in the list parameter to the result list. The result shares a common tail with the list parameter. The new elements are added to the front of the list, but no guarantees are made about their order. The = parameter is an equality procedure used to determine if an  $elt_i$  is already a member of list. Its first argument is an element of list; its second is one of the  $elt_i$ .

The list parameter is always a suffix of the result – even if the list parameter contains repeated elements, these are not reduced.

```
(lset-adjoin eq? '(a b c d c e) 'a 'e 'i 'o 'u) \Rightarrow (u o i a b c d c e)
```

```
(lset-union = list_1 ...) \rightarrow list
```

list library procedure

Returns the union of the lists, using = for the element-equality procedure.

The union of lists A and B is constructed as follows:

- If A is the empty list, the answer is B (or a copy of B).
- Otherwise, the result is initialised to be list A (or a copy of A).
- Proceed through the elements of list B in a left-to-right order. If b is such an element of B, compare every element r of the current result list to b: (= r b). If all comparisons fail, b is consed onto the front of the result.

However, there is no guarantee that = will be applied to every pair of arguments from A and B. In particular, if A is eq? to B, the operation may immediately terminate.

In the n-ary case, the two-argument list-union operation is simply folded across the argument lists.

```
(lset-union eq? '(a b c d e) '(a e i o u)) =>
    (u o i a b c d e)
;; Repeated elements in LIST1 are preserved.
(lset-union eq? '(a a c) '(x a x)) \Rightarrow (x a a c)
;; Trivial cases
(lset-union eq?) => ()
(lset-union eq? '(a b c)) \Rightarrow (a b c)
```

list library procedure

Returns the intersection of the lists, using = for the element-equality procedure.

The intersection of lists A and B is comprised of every element of A that is = to some element of B: (= a b), for a in A, and b in B. Note this implies that an element which appears in B and multiple times in list A will also appear multiple times in the result.

The order in which elements appear in the result is the same as they appear in  $list_1$  – that is, lset-intersection essentially filters  $list_1$ , without disarranging element order. The result may share a common tail with  $list_1$ .

In the n-ary case, the two-argument list-intersection operation is simply folded across the argument lists. However, the dynamic order in which the applications of = are made is not specified. The procedure may check an element of list<sub>1</sub> for membership in every other list before proceeding to consider the next element of list<sub>1</sub>, or it may completely intersect list<sub>1</sub> and list<sub>2</sub> before proceeding to list<sub>3</sub>, or it may go about its work in some third order.

```
(lset-intersection eq? '(a b c d e) '(a e i o u)) => (a e)
```

```
;; Repeated elements in LIST1 are preserved.
(lset-intersection eq? '(a x y a) '(x a x z)) => '(a x a)
```

(lset-intersection eq? '(a b c)) => (a b c) ; Trivial case

```
(lset-difference = list_1 list_2 ...) \rightarrow list
```

list library procedure

Returns the difference of the lists, using = for the element-equality procedure – all the elements of list<sub>1</sub> that are not = to any element from one of the other list<sub>i</sub> parameters.

The = procedure's first argument is always an element of list<sub>1</sub>; its second is an element of one of the other list<sub>i</sub>. Elements that are repeated multiple times in the list<sub>1</sub> parameter will occur multiple times in the result. The order in which elements appear in the result is the same as they appear in list<sub>1</sub> – that is, lset-difference essentially filters list<sub>1</sub>, without disarranging element order. The result may share a common tail with list<sub>1</sub>. The dynamic order in which the applications of = are made is not specified. The procedure may check an element of list<sub>1</sub> for membership in every other list before proceeding to consider the next element of list<sub>1</sub>, or it may completely compute the difference of list<sub>1</sub> and list<sub>2</sub> before proceeding to list<sub>3</sub>, or it may go about its work in some third order.

```
(lset-difference eq? '(a b c d e) '(a e i o u)) \Rightarrow (b c d)
```

(lset-difference eq? '(a b c)) => (a b c); Trivial case

```
(lset-xor = list_1 ...) \rightarrow list
```

list library procedure

Returns the exclusive-or of the sets, using = for the element-equality procedure. If there are exactly two lists, this is all the elements that appear in exactly one of the two lists. The operation is associative, and thus extends to the n-ary case – the elements that appear in an odd number of the lists. The result may share a common tail with any of the list $_i$  parameters.

More precisely, for two lists A and B, A xor B is a list of

- every element a of A such that there is no element b of B such that (= a b), and
- every element b of B such that there is no element a of A such that (= b a).

However, an implementation is allowed to assume that = is symmetric - that is, that

```
(= a b) => (= b a).
```

This means, for example, that if a comparison (= a b) produces true for some a in A and b in B, both a and b may be removed from inclusion in the result.

In the n-ary case, the binary-xor operation is simply folded across the lists.

```
(lset-xor eq? '(a b c d e) '(a e i o u)) \Rightarrow (d c b i o u)
;; Trivial cases.
(lset-xor eq?) => ()
(lset-xor eq? '(a b c d e)) \Rightarrow (a b c d e)
(lset-diff+intersection = list_1 list_2 ...) \rightarrow list list
                                                                                                 list library procedure
Returns two values – the difference and the intersection of the lists. Is equivalent to
(values (lset-difference = list1 list2 ...)
         (lset-intersection = list1
                                  (lset-union = list2 ...)))
```

but can be implemented more efficiently.

The = procedure's first argument is an element of  $list_1$ ; its second is an element of one of the other  $list_i$ .

Either of the answer lists may share a common tail with list<sub>1</sub>. This operation essentially partitions list<sub>1</sub>.

```
(lset-union! = list_1 ...) \rightarrow list
                                                                                                                        list library procedure
(lset-intersection! = list_1 \ list_2 \ ...) \rightarrow list
                                                                                                                        list library procedure
(lset-difference! = list_1 list_2 ...) \rightarrow list
                                                                                                                        list library procedure
                                                                                                                        list library procedure
(lset-xor! = list_1 ...) \rightarrow list
(lset-diff+intersection! = list_1 list_2 ...) \rightarrow list list
                                                                                                                        list library procedure
```

These are linear-update variants. They are allowed, but not required, to use the cons cells in their first list parameter to construct their answer. lset-union! is permitted to recycle cons cells from any of its list arguments.

#### Primitive side-effects

These two procedures are the primitive, R5RS side-effect operations on pairs.

```
(set-car! pair\ object) \rightarrow unspecified
                                                                                               list library procedure
(set-cdr! pair object) → unspecified
                                                                                               list library procedure
[R5RS] These procedures store object in the car and cdr field of pair, respectively. The value returned is unspecified.
(define (f) (list 'not-a-constant-list))
(define (g) '(constant-list))
(set-car! (f) 3) => *unspecified*
(set-car! (g) 3) => *error*
```

#### References & links

TODO What of this should survive in the final document?

```
This document, in HTML: http://srfi.schemers.org/srfi-1/srfi-1.html
Source code for the reference implementation: http://srfi.schemers.org/srfi-1/srfi-1-reference.scm
Archive of SRFI-1 discussion-list email: http://srfi.schemers.org/srfi-1/mail-archive/maillist.html
SRFI web site: http://srfi.schemers.org/
```

```
[CommonLisp] Common Lisp: the Language
```

```
Guy L. Steele Jr. (editor).
```

Digital Press, Maynard, Mass., second edition 1990.

Available at http://www.elwood.com/alu/table/references.htm#cltl2.

The Common Lisp "HyperSpec," produced by Kent Pitman, is essentially the ANSI spec for Common Lisp: http://www.harlequin.com/education/books/HyperSpec/.

[R5RS] Revised<sup>5</sup> report on the algorithmic language Scheme.

R. Kelsey, W. Clinger, J. Rees (editors).

Higher-Order and Symbolic Computation, Vol. 11, No. 1, September, 1998.

and ACM SIGPLAN Notices, Vol. 33, No. 9, October, 1998.

Available at http://www.schemers.org/Documents/Standards/.

#### 2. Vector libraries

[Red Edition item 2] What vector library should R7RS-large provide?

This SRFI proposes a comprehensive library of vector operations accompanied by a freely available and complete reference implementation. The reference implementation is unencumbered by copyright, and useable with no modifications on any Scheme system that is R5RS-compliant. It also provides several hooks for implementation-specific optimization as well.

The names described in this section comprise the (scheme vector) library.

#### **Procedure Index**

Here is an index of the procedures provided by this package. Those marked by *italics* are also provided in R7RS-small.

Constructors make-vector vector vector vector-unfold

vector-unfold-right vector-copy vector-reverse-copy

vector-append vector-concatenate vector-append-subvectors

Predicates vector? vector-empty? vector=

Selectors vector-ref vector-length

Iteration vector-fold vector-fold-right vector-map

vector-map! vector-for-each vector-count

vector-cumulate

Searching vector-index vector-index-right vector-skip

vector-skip-right vector-binary-search vector-any

vector-every vector-partition

Mutators vector-set! vector-swap! vector-fill!

vector-reverse! vector-copy! vector-reverse-copy!

vector-unfold! vector-unfold-right!

Conversion vector->list reverse-vector->list list->vector

reverse-list->vector vector->string string->vector

#### Notation

TODO Unify with notation in the rest of the Report, move to a common section.

In this section containing specifications of procedures, the following notation is used to specify parameters and return values:

(f arg<sub>1</sub> arg<sub>2</sub> ...) -> something Indicates a function f takes the parameters arg1 arg2 ... and returns a value of the type something. If something is unspecified, then f returns a single implementation-dependent value; this SRFI does not specify what it returns, and in order to write portable code, the return value should be ignored.

vec The argument in this place must be a vector, i.e. it must satisfy the predicate vector?.

- i, j, start, size The argument in this place must be a exact nonnegative integer, i.e. it must satisfy the predicates exact?, integer? and either zero? or positive?. The third case of it indicates the index at which traversal begins; the fourth case of it indicates the size of a vector.
- end The argument in this place must be a exact positive integer, i.e. it must satisfy the predicates exact?, integer? and positive?. This indicates the index directly before which traversal will stop — processing will occur until the the index of the vector is end. It is the closed right side of a range.
- f The argument in this place must be a function of one or more arguments, which returns (except as noted otherwise) exactly one value.
- pred? The argument in this place must be a function of one or more arguments that returns one value, which is treated as a boolean.
- x, y, z, seed, knil, fill, key, value The argument in this place may be any Scheme value.
- [something] Indicates that something is an optional argument; it needn't necessarily be applied. Something needn't necessarily be one thing; for example, this usage of it is perfectly valid: [start [end]] and is indeed used quite often.

something ... Indicates that zero or more somethings are allowed to be arguments.

something<sub>1</sub> something<sub>2</sub> ... Indicates that at least one something must be arguments.

something<sub>1</sub> something<sub>2</sub> ... something<sub>n</sub> Exactly equivalent to the previous argument notation, but this also indicates that n will be used later in the procedure description.

It should be noted that all of the procedures that iterate across multiple vectors in parallel stop iterating and produce the final result when the end of the shortest vector is reached. The sole exception is vector=, which automatically returns #f if the vectors' lengths vary.

#### Constructors

```
(make-vector \ size \ fill) \rightarrow vector
(make-vector \ size) \rightarrow vector
```

vector library procedure vector library procedure

[R7RS-small] Creates and returns a vector of size size. If fill is specified, all the elements of the vector are initialized to fill. Otherwise, their contents are indeterminate. Example:

```
(make-vector 5 3)
\#(3 3 3 3 3)
```

(vector x ...)  $\rightarrow vector$ 

vector library procedure

[R7RS-small] Creates and returns a vector whose elements are x .... Example:

```
(vector 0 1 2 3 4)
\#(0 1 2 3 4)
```

(vector-unfold f length initial-seed ...)  $\rightarrow vector$ 

vector library procedure

The fundamental vector constructor. Creates a vector whose length is length and iterates across each index k between 0 and length, applying f at each iteration to the current index and current seeds, in that order, to receive n + 1 values: first, the element to put in the kth slot of the new vector and n new seeds for the next iteration. It is an error for the number of seeds to vary between iterations. Note that the termination condition is different from the unfold procedure of SRFI 1. Examples:

```
(vector-unfold ( (i x) (values x (- x 1))) 10 0) \#(0 -1 -2 -3 -4 -5 -6 -7 -8 -9)
```

Construct a vector of the sequence of integers in the range [0,n).

```
(vector-unfold values n)
\#(0 1 2 ... n-2 n-1)
```

Copy vector.

(vector-unfold-right f length initial-seed ...)  $\rightarrow$  vector

vector library procedure

Like vector-unfold, but it uses f to generate elements from right-to-left, rather than left-to-right. The first index used is *length* - 1. Note that the termination condition is different from the unfold-right procedure of SRFI 1. Examples: Construct a vector of pairs of non-negative integers whose values sum to 4.

```
(vector-unfold-right ( (i x) (values (cons i x) (+ x 1))) 5 0) \ (0 . 4) (1 . 3) (2 . 2) (3 . 1) (4 . 0))
```

Reverse vector.

```
(\text{vector-unfold-right ( (i x)} \\ (\text{values (vector-ref vector x)} \\ (+ x 1))) \\ (\text{vector-length vector)} \\ 0)
```

```
(vector-copy vec\ start\ end) \rightarrow vector
(vector-copy vec\ start) \rightarrow vector
(vector-copy vec) \rightarrow vector
```

vector library procedure vector library procedure vector library procedure

[R7RS-small] Allocates a new vector whose length is end - start and fills it with elements from vec, taking elements from vec starting at index start and stopping at index end. start defaults to 0 and end defaults to the value of (vector-length vec). SRFI 43 provides an optional fill argument to supply values if end is greater than the length of vec. Neither R7RS-small nor this SRFI requires support for this argument. Examples:

```
(vector-copy '\#(a b c d e f g h i))
\#(a b c d e f g h i)
(vector-copy '\#(a b c d e f g h i) 6)
\#(g h i)
(vector-copy '\#(a b c d e f g h i) 3 6)
\#(d e f)
```

(vector-reverse-copy  $vec\ start\ end$ ) ightarrow vector

vector library procedure

Like vector-copy, but it copies the elements in the reverse order from vec. Example:

```
(vector-reverse-copy '\#(5 4 3 2 1 0) 1 5) \#(1 2 3 4)
```

```
(vector-append vec \dots) \rightarrow vector
```

vector library procedure

[R7RS-small] Returns a newly allocated vector that contains all elements in order from the subsequent locations in vec .... Examples:

```
(vector-append '\mbox{}'(x) '\mbox{}'(y))
\#(x y)
(vector-append '\#(a) '\#(b c d))
\#(a b c d)
(vector-append '\#(a \#(b)) '\#(\#(c)))
\#(a \#(b) \#(c))
```

(vector-concatenate list-of-vectors)  $\rightarrow vector$ 

vector library procedure

Appends each vector in list-of-vectors. This is equivalent to: (apply vector-append list-of-vectors) However, it may be implemented better. Example: (vector-concatenate '(#(a b) #(c d))) #(a b c d)

(vector-append-subvectors [vec start end] ...)  $\rightarrow$  vector

vector library procedure

TODO Check the signature on this one.

Returns a vector that contains every element of each vec from start to end in the specified order. This procedure is a generalization of vector-append. Example: (vector-append-subvectors '#(a b c d e) 0 2 '#(f g

```
h i j) 2 4)
#(a b h i)
```

#### **Predicates**

#f

(vector? x)  $\rightarrow boolean$ vector library procedure

[R7RS-small] Disjoint type predicate for vectors: this returns #t if x is a vector, and #f if otherwise. Examples: (vector? '#(a b c))

```
(vector? '(a b c))
#t.
                         (vector? #t)
#f
#f
                         (vector? '#())
                         (vector? '())
#t
```

(vector-empty? vec)  $\rightarrow boolean$ 

vector library procedure

```
Returns #t if vec is empty, i.e. its length is 0, and #f if not. Examples:
                                                                                 (vector-empty? '#(a))
                          (vector-empty? '#(()))
```

#f (vector-empty? '#(#())) (vector-empty? '#()) #f #t

```
(vector= elt=? vec \dots) \rightarrow boolean
```

vector library procedure

Vector structure comparator, generalized across user-specified element comparators. Vectors a and b are considered equal by vector= iff their lengths are the same, and for each respective element Ea and Eb, (elt=? Ea returns a true value. Elt=? is always applied to two arguments. Element comparison must be consistent with eq; that is, if (eq? Ea Eb) results in a true value, then (elt=? Ea Eb) must also result in a true value. This may be exploited to avoid unnecessary element comparisons. (The reference implementation does, but it does not consider the situation where elt=? is in fact itself eq? to avoid yet more unnecessary comparisons.) If there are only zero or one vector arguments, #t is automatically returned. The dynamic order in which comparisons of elements and of vectors are performed is left completely unspecified; do not rely on a particular order. Examples: (vector= eq? '#(a b c d) '#(a b c d))

```
(vector= eq? '#(a b c d) '#(a b d c))
#t
                       (vector = '#(1 2 3 4 5) '#(1 2 3 4))
#f
                       (vector = '#(1 2 3 4) '#(1 2 3 4))
#f
```

```
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```

```
#t The two trivial cases. (vector= eq?)

#t (vector= eq? '#(a))

#t Note the fact that we don't use vector literals in the next two — it is unspecified whether or not literal vectors with the same external representation are eq?. (vector= eq? (vector (vector 'a)) (vector (vector 'a)))

#f (vector= equal? (vector (vector 'a)) (vector (vector 'a)))
```

#### Selectors

# TODO introduction

(vector-ref  $vec\ i$ )  $\rightarrow value$ 

vector library procedure

[R7RS-small] Vector element dereferencing: returns the value that the location in vec at i is mapped to in the store. Indexing is based on zero. I must be within the range [0, (vector-length vec)). Example: (vector-ref '#(a b c d) 2)

С

(vector-length vec)  $\rightarrow exact nonnegative integer$ 

vector library procedure

[R7RS-small] Returns the length of vec, the number of locations reachable from vec. (The careful word 'reachable' is used to allow for 'vector slices,' whereby vec refers to a larger vector that contains more locations that are unreachable from vec. This SRFI does not define vector slices, but later SRFIs may.) Example: (vector-length '#(a b c))

#### Iteration

# TODO introduction

```
(vector-fold kons \ knil \ vec_1 \ vec_2 \ ...) \rightarrow value
                                                                                                vector library procedure
The fundamental vector iterator. Kons is iterated over each value in all of the vectors, stopping at the end of the shortest;
kons is applied as
                               (kons state
                                                            (vector-ref
                                                                                                                   (vector-ref
state is the current state value — the current state value begins with knil, and becomes whatever kons returned on
the previous iteration —, and i is the current index. The iteration is strictly left-to-right. Examples: Find the longest
string's length in vector-of-strings.
(vector-fold ( (len str)
                                                             (max (string-length str) len))
duce a list of the reversed elements of vec.
                                                                                                                           '() vec)
(vector-fold ( (tail elt) (cons elt tail))
the number of even numbers in vec.
(vector-fold ( (counter n)
                                                                                                            (if (even? n) (+ cour
(vector-fold-right kons \ knil \ vec_1 \ vec_2 \ ...) \rightarrow value
                                                                                                vector library procedure
```

(vector-map ( (x y) (\* x y))

(vector-map  $f \ vec_1 \ vec_2 \ \dots) \rightarrow vector$ 

#(1 4 9 16)

vector library procedure

(vector-unfold

[R7RS-small] Constructs a new vector of the shortest size of the vector arguments. Each element at index i of the new vector is mapped from the old vectors by (f (vector-ref vec1 i) (vector-ref The dynamic order of application of f is unspecified. Examples: (vector-map ( (x) (\* x x))

#(5 8 9 8 5) (let ((count 0))

```
(vector-map ( (ignored-elt)
(set! count (+ count 1))
count)
'#(a b)))
#(1 2) OR #(2 1)
```

(vector-map!  $f \ vec_1 \ vec_2 \ \dots) \rightarrow unspecified$ 

vector library procedure

Similar to vector-map, but rather than mapping the new elements into a new vector, the new mapped elements are destructively inserted into vec1. Again, the dynamic order of application of f unspecified, so it is dangerous for f to apply either vector-ref or vector-set! to vec1 in f.

```
(vector-for-each f \ vec_1 \ vec_2 \ ...) \rightarrow unspecified
```

vector library procedure

[R7RS-small] Simple vector iterator: applies f to the corresponding list of parallel elements from vec1 vec2 in the range [0, length), where length is the length of the smallest vector argument passed. In contrast with vector-map, f is reliably applied to each subsequent element, starting at index 0, in the vectors. Example: (vector-for-each ( (x) '#("foo" "bar" "baz" "quux" "zot"))

Displays:

foo bar baz quux zot

(vector-count  $pred?\ vec_1\ vec_2\ ...) \rightarrow exact\ nonnegative\ integer$ 

vector library procedure

Counts the number of parallel elements in the vectors that satisfy pred?, which is applied, for each index i in the range [0, length) where length is the length of the smallest vector argument, to each parallel element in the vectors, in order. Examples: (vector-count even?

3

2

```
(vector-count <</pre>
```

'#(3 1 4 1 5 9 2 5 6))

'#(1 3 6 9) '#(2 4 6 8 10 12))

(vector-cumulate  $f \ knil \ vec$ )  $\rightarrow vector$ 

vector library procedure

Returns a newly allocated vector new with the same length as vec. Each element i of new is set to the result of invoking f on  $new_{i-1}$  and  $vec_i$ , except that for the first call on f, the first argument is knil. The new vector is returned.

Note that the order of arguments to vector-cumulate was changed by errata-3 on 2016/9/2.

```
Example:
                    (vector-cumulate + 0 '#(3 1 4 1 5 9 2 5 6))
#(3 4 8 9 14 23 25 30 36)
```

#### Searching

```
(vector-index pred? vec_1 vec_2 \dots) \rightarrow exact nonnegative integer or #f
                                                                                                 vector library procedure
Finds & returns the index of the first elements in vec1 vec2
                                                                       ... that satisfy pred?. If no matching element is
                                                                               (vector-index even? '#(3 1 4 1 5 9))
found by the end of the shortest vector, #f is returned. Examples:
```

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```
2 (vector-index < '#(3 1 4 1 5 9 2 5 6) '#(2 7 1 8 2))
1 (vector-index = '#(3 1 4 1 5 9 2 5 6) '#(2 7 1 8 2))
#f
```

(vector-index-right  $pred?\ vec_1\ vec_2\ ...$ )  $\rightarrow exact\ nonnegative\ integer\ or\ \#f$  vector library procedure

Like vector-index, but it searches right-to-left, rather than left-to-right, and all of the vectors *must* have the same length.

```
(vector-skip pred? vec_1 vec_2 ...) \rightarrow exact nonnegative integer or \#f vector library procedure Finds & returns the index of the first elements in vec1 vec2 ... that do not satisfy pred? If all the values in the vectors satisfy pred? until the end of the shortest vector, this returns \#f. This is equivalent to: (vector-index ( (x1 x2 ...) (not (pred? x1)
```

ample: (vector-skip number? '#(1 2 a b 3 4 c d))

2

vector library procedure

Like vector-skip, but it searches for a non-matching element right-to-left, rather than left-to-right, and it is an error if all of the vectors do not have the same length. This is equivalent to: (vector-index-right ( x2 x2

(vector-binary-search vec value cmp)  $\rightarrow$  exact nonnegative integer or #f

(vector-skip-right  $pred? vec_1 vec_2 \dots$ )  $\rightarrow exact nonnegative integer or #f$ 

vector library procedure

Similar to vector-index and vector-index-right, but instead of searching left to right or right to left, this performs a binary search. If there is more than one element of *vec* that matches *value* in the sense of *cmp*, vector-binary-search may return the index of any of them.

cmp should be a procedure of two arguments and return a negative integer, which indicates that its first argument is less than its second, zero, which indicates that they are equal, or a positive integer, which indicates that the first argument is greater than the second argument. An example cmp might be: (char1 char2)

char2)

(vector-any  $pred?\ vec_1\ vec_2\ ...) \rightarrow value\ or\ \#f$ 

vector library procedure

-1)

Finds the first set of elements in parallel from vec1 vec2 ... for which pred? returns a true value. If such a parallel set of elements exists, vector-any returns the value that pred? returned for that set of elements. The iteration is strictly left-to-right.

```
(vector-every pred?\ vec_1\ vec_2\ ...) \rightarrow value\ or\ \#f
```

vector library procedure

If, for every index i between 0 and the length of the shortest vector argument, the set of elements (vector-ref vec1 satisfies pred?, vector-every returns the value that pred? returned for the last set of elements, at the last index of the shortest vector. The iteration is strictly left-to-right.

```
(vector-partition pred?\ vec) 
ightarrow vector
```

vector library procedure

A vector the same size as vec is newly allocated and filled with all the elements of vec that satisfy pred? in their original order followed by all the elements that do not satisfy pred, also in their original order. Two values are returned, the newly allocated vector and the index of the leftmost element that does not satisfy pred.

#### Mutators

(vector-set!  $vec\ i\ value$ )  $\rightarrow unspecified$ 

vector library procedure

[R7RS-small] Assigns the contents of the location at i in vec to value.

(vector-swap!  $vec\ i\ j$ )  $\rightarrow unspecified$ 

vector library procedure

Swaps or exchanges the values of the locations in vec at i & j.

```
(vector-fill! vec\ fill\ start\ end) \rightarrow unspecified
(vector-fill! vec\ fill\ start) \rightarrow unspecified
(vector-fill! vec fill) \rightarrow unspecified
```

vector library procedure vector library procedure

vector library procedure

[R7RS-small] Assigns the value of every location in vec between start, which defaults to 0 and end, which defaults to the length of vec, to fill.

```
(vector-reverse! vec start end) \rightarrow unspecified
(vector-reverse! vec\ start) \rightarrow unspecified
(vector-reverse! vec) \rightarrow unspecified
```

vector library procedure vector library procedure

vector library procedure

Destructively reverses the contents of the sequence of locations in vec between start and end. Start defaults to 0 and end defaults to the length of vec. Note that this does not deeply reverse.

```
(vector-copy! to at from start end) \rightarrow unspecified
(vector-copy! to at from start) \rightarrow unspecified
(vector-copy! to at from) \rightarrow unspecified
```

vector library procedure vector library procedure vector library procedure

[R7RS-small] Copies the elements of vector from between start and end to vector to, starting at at. The order in which elements are copied is unspecified, except that if the source and destination overlap, copying takes place as if the source is first copied into a temporary vector and then into the destination. This can be achieved without allocating storage by making sure to copy in the correct direction in such circumstances.

```
(vector-reverse-copy! to at from start end) \rightarrow unspecified
(vector-reverse-copy! to at from start) \rightarrow unspecified
(vector-reverse-copy! to at from) \rightarrow unspecified
```

vector library procedure vector library procedure vector library procedure

Like vector-copy!, but the elements appear in to in reverse order.

(vector-reverse!

target

```
(vector-unfold! f vec start end initial-seed ...) \rightarrow unspecified
```

vector library procedure

Like vector-unfold, but the elements are copied into the vector vec starting at element start rather than into a newly allocated vector. Terminates when end-start elements have been generated.

```
(vector-unfold-right! f vec start end initial-seed ...) \rightarrow unspecified
```

vector library procedure

Like vector-unfold!, but the elements are copied in reverse order into the vector vec starting at the index preceding end.

### Conversion

 $\begin{array}{lll} \text{(vector->list} \textit{vector library procedure} \\ \text{vector library procedure} \\ \text{vector library procedure} \\ \end{array}$ 

[R7RS-small] Creates a list containing the elements in vec between start, which defaults to 0, and end, which defaults to the length of vec.

(reverse-vector->list vec start end)  $\rightarrow proper-list$ vector library procedure(reverse-vector->list vec start)  $\rightarrow proper-list$ vector library procedure(reverse-vector->list vec)  $\rightarrow proper-list$ vector library procedure

Like vector->list, but the resulting list contains the elements in reverse of vector.

(list->vector proper-list)  $\rightarrow vector$ 

vector library procedure

[R7RS-small] Creates a vector of elements from proper-list.

(reverse-list->vector proper-list)  $\rightarrow vector$ 

vector library procedure

Like list->vector, but the resulting vector contains the elements in reverse of proper-list.

[R7RS-small] Creates a vector containing the elements in string between start, which defaults to 0, and end, which defaults to the length of string.

 (vector->string vec start end)  $\rightarrow$  string
 vector library procedure

 (vector->string vec start)  $\rightarrow$  string
 vector library procedure

 (vector->string vec)  $\rightarrow$  string
 vector library procedure

[R7RS-small] Creates a string containing the elements in vec between start, which defaults to 0, and end, which defaults to the length of vec. It is an error if the elements are not characters.

#### References

TODO move to consolidated reference list.

**R5RS** R5RS: The Revised<sup>5</sup> Report on Scheme

R. Kelsey, W. Clinger, J. Rees (editors).

Higher-Order and Symbolic Computation, Vol. 11, No. 1, September, 1998 and

ACM SIGPLAN Notices, Vol. 33, No. 9, October, 1998

Available at: http://www.schemers.org/Documents/Standards/R5RS/

**R7RS-small** R7RS: The Revised Report on Scheme

A. Shinn et al. (editors).

Available at: http://r7rs.org

**SRFI** SRFI: Scheme Request for Implementation

The SRFI website can be found at: http://srfi.schemers.org/

The SRFIs mentioned in this document are described later.

SRFI 1 SRFI 1: List Library

A SRFI of list processing procedures, written by Olin Shivers.

Available at: http://srfi.schemers.org/srfi-1/

SRFI 13 SRFI 13: String Library

A SRFI of string processing procedures, written by Olin Shivers.

Available at: http://srfi.schemers.org/srfi-13/

SRFI 23 SRFI 23: Error Reporting Mechanism

A SRFI that defines a new primitive (error) for reporting that an error occurred, written by Stephan Houben.

Available at: http://srfi.schemers.org/srfi-23/

SRFI 43 SRFI 43: Vector Library (draft)

The direct predecessor of this SRFI, written by Taylor Campbell.

Available at: http://srfi.schemers.org/srfi-43/

Editor: Arthur A. Gleckler

# String library

[Red Edition item 3] As no consensus was achieved on a string library, no string library is provided in the Red Edition; one might be provided later.

This section is left in as a placeholder, and will be removed later in the editing process.

#### 3. Sorting library

[Red Edition item 4] What sorting library should R7RS-large provide?

SRFI 132 is an edited version of the withdrawn SRFI 32, with the algorithm-specific procedures removed and a few additional procedures; it provides sortedness testing, stable and unstable sorting, merging, duplicate removal, median, and selection. R6RS provides only stable sorting and merging.

This SRFI describes the API for a full-featured sort toolkit. The names described in this section comprise the (scheme sort) library.

# Procedure naming and functionality

Most of the procedures described below are variants of two basic operations: sorting and merging. These procedures are consistently named by composing a set of basic lexemes to indicate what they do.

Lexeme Meaning vector The procedure operates upon vectors. The procedure operates upon lists. list This lexeme indicates that the sort is a stable one. stable The procedure sorts its input data set by some ordering function. sort The procedure merges two ordered data sets into a single ordered result. merge ļ Procedures that end in! are allowed, and sometimes required, to reuse their input storage to construct their answer.

#### Types of parameters and return values

In the procedures specified below:

- A *lis* parameter is a list.
- A v parameter is a vector.
- An = parameter is an equality predicate. See SRFI 128 for the requirements on equality predicates. Note that neither this SRFI nor its sample implementation depend on SRFI 128.

- A < parameter is an ordering predicate. See SRFI 128 for the requirements on ordering predicates. TODO use le? as a clearer name.
- A start parameter or start and end parameter pair are exact non-negative integers such that 0 <= start <= end <= (vector-length v), where v is the related vector parameter. If not specified, they default to 0 and the length of the vector, respectively. They are interpreted to select the range [start, end), that is, all elements from index start (inclusive) up to, but not including, index end.

Passing values to procedures with these parameters that do not satisfy these constraints is an error.

If a procedure is said to return "an unspecified value", this means that nothing at all is said about what the procedure returns, except that it returns one value.

#### **Predicates**

TODO Change textless to le? throughout this section.

```
(list-sorted? < lis) \rightarrow booleansort library procedure(vector-sorted? < v start end) \rightarrow booleansort library procedure(vector-sorted? < v start) \rightarrow booleansort library procedure(vector-sorted? < v) \rightarrow booleansort library procedure
```

These procedures return true iff their input list or vector is in sorted order, as determined by <. Specifically, they return #f iff there is an adjacent pair ... X Y ... in the input list or vector such that Y < X in the sense of <. The optional *start* and *end* range arguments restrict vector-sorted? to examining the indicated subvector.

These procedures are equivalent to the SRFI 95 sorted? procedure when applied to lists or vectors respectively, except that they do not accept a key procedure.

# General sort procedures

These procedures provide basic sorting and merging functionality suitable for general programming. The procedures are named by their semantic properties, i.e., what they do to the data (sort, stable sort, and so forth).

```
 \begin{array}{ll} (\mbox{list-sort} & < \mbox{\it list}??? & \mbox{sort library procedure} \\ (\mbox{list-stable-sort} & < \mbox{\it list}??? & \mbox{sort library procedure} \\ \end{array}
```

These procedures do not alter their inputs, but are allowed to return a value that shares a common tail with a list argument.

The list-stable-sort procedure is equivalent to the R6RS list-sort procedure. It is also equivalent to the SRFI 95 sort procedure when applied to lists, except that it does not accept a key procedure.

```
 \begin{array}{ll} \text{(list-sort!} & < \textit{lis}) \rightarrow \textit{list????} & \text{sort library procedure} \\ \text{(list-stable-sort!} & < \textit{lis}) \rightarrow \textit{list???} & \text{sort library procedure} \\ \end{array}
```

These procedures are linear update operators — they are allowed, but not required, to alter the cons cells of their arguments to produce their results. They return a sorted list containing the same elements as *lis*.

The list-stable-sort! procedure is equivalent to the SRFI 95 sort! procedure when applied to lists, except that it does not accept a key procedure.

```
(vector-sort < v \ start \ end) \rightarrow vector ???sort library procedure(vector-sort < v \ start) \rightarrow vector ???sort library procedure(vector-sort < v \ end) \rightarrow vector ???sort library procedure(vector-stable-sort < v \ start \ end) \rightarrow vector ???sort library procedure
```

```
(vector-stable-sort \langle v | start \rangle \rightarrow vector ???
(vector-stable-sort \langle v \rangle \rightarrow vector???
```

sort library procedure sort library procedure

These procedures do not alter their inputs, but allocate a fresh vector as their result, of length end - start. The vector-stable-sort procedure with no optional arguments is equivalent to the R6RS vector-sort procedure. It is also equivalent to the SRFI 95 sort procedure when applied to vectors, except that it does not accept a key procedure.

```
(vector-sort! < v \ start \ end) \rightarrow vector???
                                                                                                             sort library procedure
                                                                                                             sort library procedure
(vector-sort! < v \ start) \rightarrow vector???
(vector-sort! < v) \rightarrow vector???
                                                                                                             sort library procedure
(vector-stable-sort! < v \ start \ end) \rightarrow vector???
                                                                                                             sort library procedure
(vector-stable-sort! < v \ start) \rightarrow vector???
                                                                                                             sort library procedure
(vector-stable-sort! < v) \rightarrow vector???
                                                                                                             sort library procedure
```

These procedures sort their data in-place. (But note that vector-stable-sort! may allocate temporary storage proportional to the size of the input — there are no known O(n lg n) stable vector sorting algorithms that run in constant space.) They return an unspecified value.

The vector-sort! procedure with no optional arguments is equivalent to the R6RS vector-sort! procedure.

### Merge procedures

All four merge operations are stable: an element of the initial list  $lis_1$  or vector  $v_1$  will come before an equal-comparing element in the second list  $lis_2$  or vector  $v_2$  in the result.

```
(list-merge \langle lis_1 \ lis_2 \rangle \rightarrow list???
```

sort library procedure

This procedure does not alter its inputs, and is allowed to return a value that shares a common tail with a list argument.

This procedure is equivalent to the SRFI 95 merge procedure when applied to lists, except that it does not accept a key procedure.

```
(list-merge! \langle lis_1 \ lis_2 \rangle \rightarrow list???
```

sort library procedure

This procedure makes only a single, iterative, linear-time pass over its argument lists, using set-cdr!s to rearrange the cells of the lists into the list that is returned — it works "in place." Hence, any cons cell appearing in the result must have originally appeared in an input. It returns the sorted input.

Additionally, list-merge! is iterative, not recursive — it can operate on arguments of arbitrary size without requiring an unbounded amount of stack space. The intent of this iterative-algorithm commitment is to allow the programmer to be sure that if, for example, list-merge! is asked to merge two ten-million-element lists, the operation will complete without performing some extremely (possibly twenty-million) deep recursion.

This procedure is equivalent to the SRFI 95 merge! procedure when applied to lists, except that it does not accept a key procedure.

```
(vector-merge \langle v_1 \ v_2 \ start_1 \ end_1 \ start_2 \ end_2) \rightarrow vector???
                                                                                                                              sort library procedure
(vector-merge \langle v_1 \ v_2 \ start_1 \ end_1 \ start_2) \rightarrow vector???
                                                                                                                              sort library procedure
(vector-merge \langle v_1 \ v_2 \ start_1 \ end_1 \rangle \rightarrow vector???
                                                                                                                              sort library procedure
(vector-merge < v_1 \ v_2 \ start_1) \rightarrow vector???
                                                                                                                              sort library procedure
(vector-merge < v_1 \ v_2) \rightarrow vector???
                                                                                                                              sort library procedure
```

This procedure does not alter its inputs, and returns a newly allocated vector of length  $(end_1 - start_1) + (end_2 - start_2)$ .

This procedure is equivalent to the SRFI 95 merge procedure when applied to vectors, except that it does not accept a key procedure.

```
(vector-merge! < to from_1 from_2 start start_1 end_1 start_2 end_2) \rightarrow vector???
                                                                                                           sort library procedure
                                                                                                           sort library procedure
(vector-merge! < to from_1 from_2 start start_1 end_1 start_2) \rightarrow vector???
```

```
(vector-merge! < to from_1 from_2 start start_1 end_1) \rightarrow vector???
                                                                                                           sort library procedure
                                                                                                           sort library procedure
(vector-merge! < to from_1 from_2 start start_1) \rightarrow vector???
(vector-merge! < to from_1 from_2 start) \rightarrow vector???
                                                                                                           sort library procedure
(vector-merge! < to from_1 from_2) \rightarrow vector???
                                                                                                           sort library procedure
```

This procedure writes its result into vector to, beginning at index start, for indices less than end, which is defined as start  $+ (end_1 - start_1) + (end_2 - start_2)$ . The target subvector to[start, end) may not overlap either of the source subvectors  $from_1[start_1, end_1]$  and  $from_2[start_2, end_2]$ . It returns an unspecified value.

This procedure is equivalent to the SRFI 95 merge! procedure when applied to lists, except that it does not accept a key procedure.

# Deleting duplicate neighbors

These procedures delete adjacent duplicate elements from a list or a vector, using a given element-equality procedure. The first/leftmost element of a run of equal elements is the one that survives. The list or vector is not otherwise disordered.

These procedures are linear time — much faster than the  $O(n^2)$  general duplicate-element deletion procedures that do not assume any "bunching" of elements provided by SRFI 1. If you want to delete duplicate elements from a large list or vector, sort the elements to bring equal items together, then use one of these procedures, for a total time of O(n lg n).

The equality procedure is always invoked as (= x y), where x comes before y in the containing list or vector.

```
(list-delete-neighbor-dups = lis) \rightarrow list??
```

sort library procedure

This procedure does not alter its input list, but its result may share storage with the input list.

```
(list-delete-neighbor-dups! = lis) \rightarrow list???
```

sort library procedure

This procedure mutates its input list in order to construct its result. It makes only a single, iterative, linear-time pass over its argument, using set-cdr!s to rearrange the cells of the list into the final result — it works "in place." Hence, any cons cell appearing in the result must have originally appeared in the input.

```
(vector-delete-neighbor-dups = v \ start \ end) \rightarrow vector???
                                                                                                        sort library procedure
(vector-delete-neighbor-dups = v \ start) \rightarrow vector???
                                                                                                        sort library procedure
(vector-delete-neighbor-dups = v) \rightarrow vector???
                                                                                                        sort library procedure
```

This procedure does not alter its input vector, but rather newly allocates and returns a vector to hold the result.

```
(vector-delete-neighbor-dups! = v \ start \ end) \rightarrow vector???
                                                                                                       sort library procedure
(vector-delete-neighbor-dups! = v \ start) \rightarrow vector???
                                                                                                       sort library procedure
(vector-delete-neighbor-dups! = v) \rightarrow vector??
                                                                                                       sort library procedure
```

This procedure reuses its input vector to hold the answer, packing it into the index range [start, newend), where newend is the non-negative exact integer that is returned as its value. The vector is not altered outside the range [start, newend). Examples:

```
(list-delete-neighbor-dups = '(1 1 2 7 7 7 0 -2 -2))
               => (1 2 7 0 -2)
    (vector-delete-neighbor-dups = '#(1 1 2 7 7 7 0 -2 -2))
               => #(1 2 7 0 -2)
    (vector-delete-neighbor-dups < \ '\#(1\ 1\ 2\ 7\ 7\ 7\ 0\ -2\ -2)\ 3\ 7))
               => #(7 0 -2)
;; Result left in v[3,9):
(let ((v (vector 0 0 0 1 1 2 2 3 3 4 4 5 5 6 6)))
  (cons (vector-delete-neighbor-dups! < v 3)</pre>
        v))
              => (9 . #(0 0 0 1 2 3 4 5 6 4 4 5 5 6 6))
```

# Finding the median

These procedures do not have SRFI 32 counterparts. They find the median element of a vector after sorting it in accordance with an ordering procedure. If the number of elements in v is odd, the middlemost element of the sorted result is returned. If the number of elements is zero, knil is returned. Otherwise, mean is applied to the two middlemost elements in the order in which they appear in v, and whatever it returns is returned. If mean is omitted, then the default mean procedure is (lambda (a b) (/ (+ a b) 2), but this procedure is applicable to non-numeric values as well.

```
sort library procedure
(vector-find-median < v \ knil \ mean) \rightarrow value???
(vector-find-median < v \ knil) \rightarrow value???
                                                                                                             sort library procedure
```

This procedure does not alter its input vector, but rather newly allocates a vector to hold the intermediate result. Runs in O(n) time.

```
(vector-find-median! < v \ knil \ mean) \rightarrow value???
                                                                                                            sort library procedure
(vector-find-median! < v \ knil) \rightarrow value???
                                                                                                            sort library procedure
```

This procedure reuses its input vector to hold the intermediate result, leaving it sorted, but is otherwise the same as vector-find-median. Runs in  $O(n \ln n)$  time. TODO Should that be  $O(n \ln n)$ ? And aren't there median algorithms that run in O(n) time?

#### Selection

These procedures do not have SRFI 32 counterparts.

```
(vector-select! < v \ k \ start \ end) \rightarrow value ???
                                                                                                                        sort library procedure
(vector-select! < v \ k \ start) \rightarrow value???
                                                                                                                        sort library procedure
(vector-select! \langle v | k \rangle \rightarrow value???
                                                                                                                        sort library procedure
```

This procedure returns the kth smallest element (in the sense of the < argument) of the region of a vector between start and end. Elements within the range may be reordered, whereas those outside the range are left alone. Runs in O(n)time.

```
(vector-separate! < v \ k \ start \ end) \rightarrow unspecified
                                                                                                                      sort library procedure
(vector-separate! < v \ k \ start) \rightarrow unspecified
                                                                                                                      sort library procedure
(vector-separate! \langle v | k \rangle \rightarrow unspecified
                                                                                                                      sort library procedure
```

This procedure places the smallest k elements (in the sense of the < argument) of the region of a vector between start and end into the first k positions of that range, and the remaining elements into the remaining positions. Otherwise, the elements are not in any particular order. Elements outside the range are left alone. Runs in O(n) time. Returns an unspecified value.

Editor: Arthur A. Gleckler

#### 4. Sets and maps

# General sets and bags

[Red Edition item 5] What general set and bag library should R7RS-large provide?

SRFI 113 provides linear-update sets and bags, which can be mutable or immutable according to the implementer's preference. Since the interface of SRFI 113 depends on SRFI 114, which has been replaced by SRFI 128, voting for SRFI 113 will cause your vote on comparator libraries to be automatically changed to SRFI 128.

TODO Incorporate these post-finalization notes into the text, if not already done. Maybe comparators should come before this SRFI?

Post-finalization note 1: Because SRFI 114 has been deprecated by SRFI 128, it is recommended that implementers make use of SRFI 128 rather than SRFI 114 comparators where comparators are specified in this SRFI. Specifically, the procedures set, bag, set-unfold, bag-unfold, set-map, list->set, list->bag, and alist->bag, should accept SRFI 128 rather than SRFI 114 comparators as arguments. By the same token, the results of set-element-comparator and bag-element-comparator, as well as the values of set-comparator and bag-comparator, should be SRFI 128 comparators. The sample implementation has been updated to depend on SRFI 128 rather than SRFI 114.

Post-finalization note 2: The order of arguments of set-map and set-unfold are not consistent with those of hash-table-map and hash-table-unfold in SRFI 125. Both SRFI 113 and SRFI 125 are going to be part of R7RS large (also known as the Red Edition), and the plan is to make them consistent there, following the order in SRFI 125. Furthermore, SRFI 146 (in draft status at the time of this writing) uses the order of SRFI 125. Since this problem was discovered after SRFI 113 was finalized, and it wasn't an error in the SRFI, it's too late to fix it here. However, John Cowan, the author, encourages implementers to consider adopting the order of SRFI 125. Thanks to Marc Nieper-Wißkirchen for reporting this mismatch, and for providing a version of SRFI 113 with the recommended argument order in the implementation of SRFI 146.

Sets and bags (also known as multisets) are unordered collections that can contain any Scheme object. Sets enforce the constraint that no two elements can be the same in the sense of the set's associated equality predicate; bags do not.

The names described in this section comprise the (scheme set) library.

Sets and bags are mutually disjoint, and disjoint from other types of Scheme objects.

It is an error for any procedure defined in this SRFI to be invoked on sets or bags with distinct comparators (in the sense of eq?).

It is an error to mutate any object while it is contained in a set or bag.

It is an error to add an object to a set or bag which does not satisfy the type test predicate of the comparator.

It is an error to add or remove an object for a set or a bag while iterating over it.

The procedures of this SRFI, by default, are "pure functional": they do not alter their parameters. However, this SRFI also defines "linear-update" procedures, all of whose names end in !. They have hybrid pure-functional/side-effecting semantics: they are allowed, but not required, to side-effect one of their parameters in order to construct their result. An implementation may legally implement these procedures as pure, side-effect-free functions, or it may implement them using side effects, depending upon the details of what is the most efficient or simple to implement in terms of the underlying representation.

It is an error to rely upon these procedures working by side effect. For example, this is not guaranteed to work:

```
(let* ((set1 (set 'a 'b 'c))
                             ; set1 = {a,b,c}.
      (set2 (set-adjoin! set1 'd))); Add d to {a,b,c}.
 set1); Could be either {a,b,c} or {a,b,c,d}.
```

However, this is well-defined:

```
(let ((set1 (set 'a 'b 'c)))
  (set-adjoin! set1 'd)); Add d to {a,b,c}.
```

So clients of these procedures write in a functional style, but must additionally be sure that, when the procedure is called, there are no other live pointers to the potentially-modified set or bag (hence the term "linear update").

There are two benefits to this convention:

- Implementations are free to provide the most efficient possible implementation, either functional or side-effecting.
- Programmers may nonetheless continue to assume that sets are purely functional data structures: they may be reliably shared without needing to be copied, uniquified, and so forth.

In practice, these procedures are most useful for efficiently constructing sets and bags in a side-effecting manner, in some limited local context, before passing the set or bag outside the local construction scope to be used in a functional manner.

Scheme provides no assistance in checking the linearity of the potentially side-effected parameters passed to these functions — there's no linear type checker or run-time mechanism for detecting violations.

Note that if an implementation uses no side effects at all, it is allowed to return existing sets and bags rather than newly allocated ones, even where this SRFI explicitly says otherwise.

# Comparator restrictions

Implementations of this SRFI are allowed to place restrictions on the comparators that the procedures accept. In particular, an implementation may require comparators to provide a comparison procedure. Alternatively, an implementation may require comparators to provide a hash function, unless the equality predicate of the comparator is eq?, eqv?, equal?, string=?, or string-ci=?. Implementations must not require the provision of both a comparison procedure and a hash function.

#### Index

- Constructors: set, set-contains?, set-unfold
- Predicates: set?, set-empty?, set-disjoint?
- Accessors: set-member, set-element-comparator
- Updaters: set-adjoin, set-adjoin!, set-replace, set-replace!, set-delete, set-delete!, set-delete-all, set-delete-all!, set-search!
- The whole set: set-size, set-find, set-count, set-any?, set-every?
- Mapping and folding: set-map, set-for-each, set-fold, set-filter, set-filter!, set-remove, set-remove!, set-partition, set-partition!
- Copying and conversion: set-copy, set->list, list->set, list->set!
- Subsets: set=?, set<?, set>?, set<=?, set>=?
- Set theory operations: set-union, set-intersection, set-difference, set-xor, set-union!, set-intersection!, set-difference!, set-xor!
- Additional bag procedures: bag-sum, bag-sum!, bag-product, bag-product!, bag-element-count, bag-for-each-unique, bag-fold-unique, bag-increment!, bag-decrement!, bag->set, set->bag, set->bag!
- Comparators: set-comparator, bag-comparator

# Set procedures

(set comparator element ...)  $\rightarrow$  set

set library procedure

Returns a newly allocated empty set. The *comparator* argument is a SRFI 114 comparator, which is used to control and distinguish the elements of the set. The *elements* are used to initialize the set.

(set-unfold comparator stop? mapper successor seed)  $\rightarrow$  set

set library procedure

Create a newly allocated set as if by set using comparator. If the result of applying the predicate stop? to seed is true, return the set. Otherwise, apply the procedure mapper to seed. The value that mapper returns is added to the set. Then get a new seed by applying the procedure successor to seed, and repeat this algorithm.

#### Predicates

 $(\text{set? }obj) \rightarrow boolean$  set library procedure

Returns #t if obj is a set, and #f otherwise.

(set-contains?  $set\ element$ )  $\rightarrow boolean$ 

Returns #t if *element* is a member of *set* and #f otherwise.

 $(set-empty? set) \rightarrow boolean$  set library procedure

Returns #t if set has no elements and #f otherwise.

(set-disjoint?  $set_1 \ set_2$ )  $\rightarrow boolean$  set library procedure

Returns #t if  $set_1$  and  $set_2$  have no elements in common and #f otherwise.

#### Accessors

(set-member set element default)  $\rightarrow value???$ 

set library procedure

set library procedure

Returns the element of set that is equal, in the sense of set's equality predicate, to element. If element is not a member of set, default is returned.

(set-element-comparator set)  $\rightarrow comparator$ 

set library procedure

Returns the comparator used to compare the elements of set.

### Updaters

(set-adjoin  $set \ element \dots) \rightarrow set???$ 

set library procedure

The set-adjoin procedure returns a newly allocated set that uses the same comparator as set and contains all the values of set, and in addition each element unless it is already equal (in the sense of the comparator) to one of the existing or newly added members. It is an error to add an element to set that does not return #t when passed to the type test procedure of the comparator.

(set-adjoin!  $set \ element \dots) \rightarrow set???$ 

set library procedure

The set-adjoin! procedure is the same as set-adjoin, except that it is permitted to mutate and return the set argument rather than allocating a new set. (set-replace set element)  $\rightarrow set$ ???

The set-replace procedure returns a newly allocated set that uses the same comparator as set and contains all the values of set except as follows: If element is equal (in the sense of set's comparator) to an existing member of set, then that member is omitted and replaced by element. If there is no such element in set, then set is returned unchanged.

(set-replace!  $set \ element$ )  $\rightarrow set$ ???

set library procedure

The set-replace! procedure is the same asset-replace, except that it is permitted to mutate and return the set argument rather than allocating a new set.

(set-delete set element ...)  $\rightarrow set????$  (set-delete! set element ...)  $\rightarrow set???$ 

set library procedure set library procedure (set-delete-all set element-list)  $\rightarrow$  set??? (set-delete-all! set element-list)  $\rightarrow$  set??? set library procedure set library procedure

The set-delete procedure returns a newly allocated set containing all the values of set except for any that are equal (in the sense of set's comparator) to one or more of the elements. Any element that is not equal to some member of the set is ignored.

The set-delete! procedure is the same as set-delete, except that it is permitted to mutate and return the set argument rather than allocating a new set.

The set-delete-all and set-delete-all! procedures are the same as set-delete and set-delete!, except that they accept a single argument which is a list of elements to be deleted.

(set-search! set element failure success)  $\rightarrow$  set???? obj??

set library procedure

The set is searched for element. If it is not found, then the failure procedure is tail-called with two continuation arguments, insert and ignore, and is expected to tail-call one of them. If element is found, then the success procedure is tail-called with the matching element of set and two continuations, update and remove, and is expected to tail-call one of them.

The effects of the continuations are as follows (where obj is any Scheme object):

- Invoking (insert obj) causes element to be inserted into set.
- Invoking (ignore obj) causes set to remain unchanged.
- Invoking (update new-element obj) causes new-element to be inserted into set in place of element.
- Invoking (remove obj) causes the matching element of set to be removed from it.

In all cases, two values are returned: the possibly updated set and obj.

# The whole set

(set-size set)  $\rightarrow integer$ 

set library procedure

Returns the number of elements in *set* as an exact integer.

(set-find predicate set failure)  $\rightarrow$  object???

set library procedure

Returns an arbitrarily chosen element of set that satisfies predicate, or the result of invoking failure with no arguments if there is none.

(set-count predicate set)  $\rightarrow integer$ 

set library procedure

Returns the number of elements of set that satisfy predicate as an exact integer.

(set-any? predicate set)  $\rightarrow boolean???$ ?

set library procedure

Returns #t if any element of set satisfies predicate, or #f otherwise. Note that this differs from the SRFI 1 analogue because it does not return an element of the set.

(set-every? predicate set)  $\rightarrow boolean$ ???

set library procedure

Returns #t if every element of set satisfies predicate, or #f otherwise. Note that this differs from the SRFI 1 analogue because it does not return an element of the set.

# Mapping and folding

```
(set-map comparator proc set) \rightarrow boolean???
```

set library procedure

Applies proc to each element of set in arbitrary order and returns a newly allocated set, created as if by (set comparator), which contains the results of the applications. For example:

```
(set-map string-ci-comparator
        symbol->string (set eq? 'foo 'bar 'baz))
             => (set string-ci-comparator "foo" "bar" "baz")
```

Note that, when proc defines a mapping that is not 1:1, some of the mapped objects may be equivalent in the sense of comparator's equality predicate, and in this case duplicate elements are omitted as in the set constructor. For example:

```
(set-map (lambda (x) (quotient x 2))
        integer-comparator
         (set integer-comparator 1 2 3 4 5))
=> (set integer-comparator 0 1 2)
```

If the elements are the same in the sense of eqv?, it is unpredictable which one will be preserved in the result.

```
(set-for-each proc\ set) \rightarrow unspecified???
```

set library procedure

Applies proc to set in arbitrary order, discarding the returned values. Returns an unspecified result.

```
(set-fold proc\ nil\ set) \rightarrow object???
```

set library procedure

Invokes proc on each member of set in arbitrary order, passing the result of the previous invocation as a second argument. For the first invocation, nil is used as the second argument. Returns the result of the last invocation, or nil if there was no invocation.

```
(set-filter predicate set) \rightarrow set???
```

set library procedure

Returns a newly allocated set with the same comparator as set, containing just the elements of set that satisfy predicate.

```
(set-filter! predicate set) \rightarrow set???
```

set library procedure

A linear update procedure that returns a set containing just the elements of set that satisfy predicate.

```
(set-remove predicate set) \rightarrow set???
```

set library procedure

Returns a newly allocated set with the same comparator as set, containing just the elements of set that do not satisfy predicate.

```
(set-remove! predicate set) \rightarrow set???
```

set library procedure

A linear update procedure that returns a set containing just the elements of set that do not satisfy predicate.

```
(set-partition predicate\ set) \rightarrow set??? set???
```

set library procedure

Returns two values: a newly allocated set with the same comparator as set that contains just the elements of set that satisfy predicate, and another newly allocated set, also with the same comparator, that contains just the elements of set that do not satisfy predicate.

```
(set-partition! predicate \ set) \rightarrow set??? set???
```

set library procedure

A linear update procedure that returns two sets containing the elements of set that do and do not, respectively, not satisfy predicate.

# Copying and conversion

(set-copy set)  $\rightarrow set$ ???

set library procedure

Returns a newly allocated set containing the elements of set, and using the same comparator.

 $(set->list set) \rightarrow list???$ 

set library procedure

Returns a newly allocated list containing the members of set in unspecified order.

(list->set comparator list)  $\rightarrow$  set???

set library procedure

Returns a newly allocated set, created as if by set using comparator, that contains the elements of list. Duplicate elements (in the sense of the equality predicate) are omitted.

(list->set! set listprocedureset????

Returns a set that contains the elements of both set and list. Duplicate elements (in the sense of the equality predicate) are omitted.

#### Subsets

Note: The following three predicates do not obey the trichotomy law and therefore do not constitute a total order on

TODO Explain how elements are compared. Via their comparators?

(set=?  $set_1$   $set_2$  ...)  $\rightarrow boolean$ ???

set library procedure

Returns #t if each set contains the same elements.

 $(set<?) \rightarrow procedure$ 

set library  $set_1 set_2 ...$ 

boolean???

Returns #t if each set other than the last is a proper subset of the following set, and #f otherwise.

 $(set>?set_1 \ set_2 \ ...) \rightarrow boolean????$ 

set library procedure

Returns #t if each set other than the last is a proper superset of the following set, and #f otherwise.

(set<=?  $set_1$   $set_2$  ...)  $\rightarrow boolean$ ???

set library procedure

Returns #t if each set other than the last is a subset of the following set, and #f otherwise.

(set>=?  $set_1$   $set_2$  ...)  $\rightarrow boolean???$ ?

set library procedure

Returns #t if each set other than the last is a superset of the following set, and #f otherwise.

#### Set theory operations

```
(set-union set_1 set_2 ...) \rightarrow set????set library procedure(set-intersection set_1 set_2 ...) \rightarrow set???set library procedure(set-difference set_1 set_2 ...) \rightarrow set???set library procedure(set-xor set_1 set_2) \rightarrow set???set library procedure
```

Return a newly allocated set that is the union, intersection, asymmetric difference, or symmetric difference of the *sets*. Asymmetric difference is extended to more than two sets by taking the difference between the first set and the union of the others. Symmetric difference is not extended beyond two sets. Elements in the result set are drawn from the first set in which they appear.

```
(set-union! set_1 set_2 ...) \rightarrow set???set library procedure(set-intersection! set_1 set_2 ...) \rightarrow set???set library procedure(set-difference! set_1 set_2 ...) \rightarrow set???set library procedure(set-xor! set_1 set_2) \rightarrow set???set library procedure
```

Linear update procedures returning a set that is the union, intersection, asymmetric difference, or symmetric difference of the *sets*. Asymmetric difference is extended to more than two sets by taking the difference between the first set and the union of the others. Symmetric difference is not extended beyond two sets. Elements in the result set are drawn from the first set in which they appear.

#### Bag procedures

Bags are like sets, but can contain the same object more than once. However, if two elements that are the same in the sense of the equality predicate, but not in the sense of eqv?, are both included, it is not guaranteed that they will remain distinct when retrieved from the bag. It is an error for a single procedure to be invoked on bags with different comparators.

TODO This must be rewritten in standard Scheme entry format.

The procedures for creating and manipulating bags are the same as those for sets, except that set is replaced by bag in their names, and that adjoining an element to a bag is effective even if the bag already contains the element. If two elements in a bag are the same in the sense of the bag's comparator, the implementation may in fact store just one of them

The bag-union, bag-intersection, bag-difference, and bag-xor procedures (and their linear update analogues) behave as follows when both bags contain elements that are equal in the sense of the bags' comparator:

- For bag-union, the number of equal elements in the result is the largest number of equal elements in any of the original bags.
- For bag-intersection, the number of equal elements in the result is the smallest number of equal elements in any of the original bags.
- For bag-difference, the number of equal elements in the result is the number of equal elements in the first bag, minus the number of elements in the other bags (but not less than zero).
- For bag-xor, the number of equal elements in the result is the absolute value of the difference between the number of equal elements in the first and second bags.

# Additional bag procedures

```
(bag-sum set_1 set_2 ...) \rightarrow bag??? set library procedure set library procedure set library procedure
```

TODO are those really set arguments in bag-sum?

The bag-sum procedure returns a newly allocated bag containing all the unique elements in all the bags, such that the count of each unique element in the result is equal to the sum of the counts of that element in the arguments. It differs from bag-union by treating identical elements as potentially distinct rather than attempting to match them up.

The bag-sum! procedure is equivalent except that it is linear-update.

```
(bag-product n \ baq) \rightarrow baq???
                                                                                                                   set library procedure
(bag-product! n \ bag) \rightarrow bag???
                                                                                                                   set library procedure
```

The bag-product procedure returns a newly allocated bag containing all the unique elements in bag, where the count of each unique element in the bag is equal to the count of that element in bag multiplied by n.

The bag-product! procedure is equivalent except that it is linear-update.

```
(bag-unique-size bag) \rightarrow integer???
```

set library procedure

Returns the number of unique elements of bag TODO as an exact integer???.

```
(bag-element-count bag\ element) \rightarrow integer??
```

set library procedure

Returns an exact integer representing the number of times that *element* appears in baq.

```
(bag-for-each-unique proc\ bag) \rightarrow unspecified???
```

set library procedure

Applies proc to each unique element of bag in arbitrary order, passing the element and the number of times it occurs in baq, and discarding the returned values. Returns an unspecified result.

```
(bag-fold-unique proc\ nil\ bag) \rightarrow value???
```

set library procedure

Invokes proc on each unique element of bag in arbitrary order, passing the number of occurrences as a second argument and the result of the previous invocation as a third argument. For the first invocation, nil is used as the third argument. Returns the result of the last invocation.

```
(bag-increment! bag element count) \rightarrow bag???
(bag-decrement! bag element count) \rightarrow bag???
```

set library procedure set library procedure

Linear update procedures that return a bag with the same elements as bag, but with the element count of element in bag increased or decreased by the exact integer *count* (but not less than zero).

```
(bag->set bag) \rightarrow set???
(set->bag set) \rightarrow bag???
(set->bag! bag set) \rightarrow bag???
```

set library procedure set library procedure

set library procedure

The bag->set procedure returns a newly allocated set containing the unique elements (in the sense of the equality predicate) of baq. The set->bag procedure returns a newly allocated bag containing the elements of set. The set->bag! procedure returns a bag containing the elements of both bag and set. In all cases, the comparator of the result is the same as the comparator of the argument or arguments.

```
(bag->alist bag) \rightarrow alist???
(alist->bag comparator alist) \rightarrow baq???
```

set library procedure set library procedure

The bag->alist procedure returns a newly allocated alist whose keys are the unique elements of bag and whose values are the number of occurrences of each element. The alist->bag returning a newly allocated bag based on comparator, where the keys of alist specify the elements and the corresponding values of alist specify how many times they occur.

# Comparators

TODO This section must be expanded.

The following comparators are used to compare sets or bags, and allow sets of sets, bags of sets, etc.

set-comparator

bag-comparator

Note that these comparators do not provide comparison procedures, as there is no ordering between sets or bags. It is an error to compare sets or bags with different element comparators.

Editor: Mike Sperber

# Character sets

[Red Edition item 6] What character set library should R7RS-large provide?

SRFI 14 provides linear-update sets and bags, which can be mutable or immutable according to the implementer's preference. The contents are limited to characters.

#### Abstract

The ability to efficiently represent and manipulate sets of characters is an unglamorous but very useful capability for text-processing code – one that tends to pop up in the definitions of other libraries. Hence it is useful to specify a general substrate for this functionality early. This SRFI defines a general library that provides this functionality. It is accompanied by a reference implementation for the spec. The reference implementation is fairly efficient, straightforwardly portable, and has a "free software" copyright. The implementation is tuned for "small" 7 or 8 bit character types, such as ASCII or Latin-1; the data structures and algorithms would have to be altered for larger 16 or 32 bit character types such as Unicode – however, the specs have been carefully designed with these larger character types in mind. Several forthcoming SRFIs can be defined in terms of this one:

- string library
- delimited input procedures (e.g., read-line)
- regular expressions

TODO is there any "tuning" needed of the spec itself for Unicode, as opposed to the reference implementation? I think not, but the above paragraph did give me pause. Also, references throughout the document are to older versions of the Unicode standard. I would hope we would in this document be able to limit ourselves to referring only to the Unicode character classes, which should only change in new editions of the standard by adding new characters to existing classes. If we're not careful, this spec will need to be revised for each new edition of the standard.

TODO the "forthcoming" SRFIs listed above do not seem to be included in the Red Edition.

TODO The library name is (scheme charset), but the names are prefixed by char-set-.... Recipe for disaster? The names described in this section comprise the (scheme charset) library.

#### Variable Index

Here is the complete set of bindings – procedural and otherwise – exported by this library. In a Scheme system that has a module or package system, these procedures should be contained in a module named "char-set-lib".

Predicates & comparison char-set? char-set= char-set<= char-set-hash

```
Iterating over character sets char-set-cursor char-set-ref
    char-set-cursor-next end-of-char-set?
    char-set-fold char-set-unfold char-set-unfold!
    char-set-for-each char-set-map
```

# Creating character sets char-set-copy char-set

```
list->char-set string->char-set
    list->char-set! string->char-set!
    char-set-filter ucs-range->char-set
    char-set-filter! ucs-range->char-set!
    ->char-set
Querying character sets char-set->list char-set->string
    char-set-size char-set-count
    char-set-contains?
    char-set-every char-set-any
Character-set algebra char-set-adjoin char-set-delete
    char-set-adjoin! char-set-delete!
    char-set-complement char-set-union
    char-set-complement! char-set-union!
    char-set-intersection
    char-set-intersection!
    char-set-difference char-set-xor
    char-set-difference! char-set-xor!
    char-set-diff+intersection
    char-set-diff+intersection!
Standard character sets char-set:lower-case char-set:upper-case
    char-set:title-case
    char-set:letter char-set:digit
    char-set:letter+digit
    char-set:graphic
                        char-set:printing
    char-set:whitespace
    char-set:iso-control char-set:punctuation
    char-set:symbol
    char-set:hex-digit char-set:blank
    char-set:ascii
    char-set:empty char-set:full
```

# Specification

In the following procedure specifications:

- A cs parameter is a character set.
- An s parameter is a string.
- A char parameter is a character.
- A char-list parameter is a list of characters.
- A pred parameter is a unary character predicate procedure, returning a true/false value when applied to a character.
- An obj parameter may be any value at all.

Passing values to procedures with these parameters that do not satisfy these types is an error.

Unless otherwise noted in the specification of a procedure, procedures always return character sets that are distinct (from the point of view of the linear-update operations) from the parameter character sets. For example, char-set-adjoin is guaranteed to provide a fresh character set, even if it is not given any character parameters.

Parameters given in square brackets are optional. Unless otherwise noted in the text describing the procedure, any prefix of these optional parameters may be supplied, from zero arguments to the full list. When a procedure returns multiple values, this is shown by listing the return values in square brackets, as well. So, for example, the procedure with signature

```
halts? f [x init-store] -> [boolean integer]
```

would take one (f), two (f, x) or three (f, x, init-store) input parameters, and return two values, a boolean and an integer.

TODO I'll be changing the entries so they match the R7RS entry format, i.e., multiple prototypes for optional arguments.

A parameter followed by "..." means zero-or-more elements. So the procedure with the signature

```
sum-squares x ... -> number
```

takes zero or more arguments (x ...), while the procedure with signature

```
spell-check doc dict1 dict2 ... -> string-list
```

takes two required parameters (doc and dict<sub>1</sub>) and zero or more optional parameters (dict<sub>2</sub> ...).

#### General procedures

```
(char-set? obj) \rightarrow boolean
```

charset library???

Is the object obj a character set?

```
(char-set= cs_1 ...) \rightarrow boolean
```

charset library???

Are the character sets equal?

Boundary cases:

```
(char-set=) => true
(char-set= cs) => true
```

Rationale: transitive binary relations are generally extended to n-ary relations in Scheme, which enables clearer, more concise code to be written. While the zero-argument and one-argument cases will almost certainly not arise in first-order uses of such relations, they may well arise in higher-order cases or macro-generated code. *E.g.*, consider

```
(apply char-set= cset-list)
```

This is well-defined if the list is empty or a singleton list. Hence we extend these relations to any number of arguments. Implementors have reported actual uses of n-ary relations in higher-order cases allowing for fewer than two arguments. The way of Scheme is to handle the general case; we provide the fully general extension.

A counter-argument to this extension is that R5RS's transitive binary arithmetic relations (=, <, etc.) require at least two arguments, hence this decision is a break with the prior convention – although it is at least one that is backwards-compatible. (char-set<=  $cs_1$  ...)  $\rightarrow$  boolean

charset library???

Returns true if every character set  $cs_i$  is a subset of character set  $cs_{i+1}$ .

Boundary cases:

```
(char-set<=) => true
(char-set<= cs) => true
```

Rationale: See char-set= for discussion of zero- and one-argument applications. Consider testing a list of char-sets for monotonicity with

```
(apply char-set<= cset-list)
```

```
(char-set-hash \ cs \ bound) \rightarrow integer
(char-set-hash cs) \rightarrow integer
```

charset library??? charset library???

Compute a hash value for the character set cs. Bound is a non-negative exact integer specifying the range of the hash function. A positive value restricts the return value to the range [0,bound).

If bound is either zero or not given, the implementation may use an implementation-specific default value, chosen to be as large as is efficiently practical. For instance, the default range might be chosen for a given implementation to map all strings into the range of integers that can be represented with a single machine word.

Invariant:

```
(char-set= cs1 cs2) => (= (char-set-hash cs1 b) (char-set-hash cs2 b))
A legal but nonetheless discouraged implementation:
(define (char-set-hash cs . maybe-bound) 1)
```

Rationale: allowing the user to specify an explicit bound simplifies user code by removing the mod operation that typically accompanies every hash computation, and also may allow the implementation of the hash function to exploit a reduced range to efficiently compute the hash value. E.q., for small bounds, the hash function may be computed in a fashion such that intermediate values never overflow into bignum integers, allowing the implementor to provide a fixnum-specific "fast path" for computing the common cases very rapidly.

# Iterating over character sets

```
(char-set-cursor cset) \rightarrow cursor
                                                                                                                  charset library???
(char-set-ref \ cset \ cursor) \rightarrow char
                                                                                                                  charset library???
                                                                                                                  charset library???
(char-set-cursor-next cset cursor) \rightarrow cursor
(end-of-char-set? cursor) \rightarrow boolean
                                                                                                                  charset library???
```

Cursors are a low-level facility for iterating over the characters in a set. A cursor is a value that indexes a character in a char set. char-set-cursor produces a new cursor for a given char set. The set element indexed by the cursor is fetched with char-set-ref. A cursor index is incremented with char-set-cursor-next; in this way, code can step through every character in a char set. Stepping a cursor "past the end" of a char set produces a cursor that answers true to end-of-char-set?. It is an error to pass such a cursor to char-set-ref or to char-set-cursor-next.

A cursor value may not be used in conjunction with a different character set; if it is passed to char-set-ref or char-set-cursor-next with a character set other than the one used to create it, the results and effects are undefined.

Cursor values are not necessarily distinct from other types. They may be integers, linked lists, records, procedures or other values. This license is granted to allow cursors to be very "lightweight" values suitable for tight iteration, even in fairly simple implementations.

Note that these primitives are necessary to export an iteration facility for char sets to loop macros.

Example:

```
(define cs (char-set \#G \#\ \#\ \#\ \#\ \#\ \#\ \#\ )
;; Collect elts of CS into a list.
(let lp ((cur (char-set-cursor cs)) (ans '()))
 (if (end-of-char-set? cur) ans
      (lp (char-set-cursor-next cs cur)
          (cons (char-set-ref cs cur) ans))))
 => (#\G #\T #\a #\c #\e #\h)
;; Equivalently, using a list unfold (from SRFI 1):
(unfold-right end-of-char-set?
              (curry char-set-ref cs)
          (curry char-set-cursor-next cs)
          (char-set-cursor cs))
 => (#\G #\T #\a #\c #\e #\h)
```

Rationale: Note that the cursor API's four functions "fit" the functional protocol used by the unfolders provided by the list, string and char-set SRFIs (see the example above). By way of contrast, here is a simpler, two-function API that was rejected for failing this criterion. Besides char-set-cursor, it provided a single function that mapped a cursor and a character set to two values, the indexed character and the next cursor. If the cursor had exhausted the character set, then this function returned false instead of the character value, and another end-of-char-set cursor. In this way, the other three functions of the current API were combined together.

```
(char-set-fold kons \ knil \ cs) \rightarrow object
```

charset library???

This is the fundamental iterator for character sets. Applies the function kons across the character set cs using initial state value knil. That is, if cs is the empty set, the procedure returns knil. Otherwise, some element c of cs is chosen; let cs' be the remaining, unchosen characters. The procedure returns

```
(char-set-fold kons (kons c knil) cs')
Examples:
;; CHAR-SET-MEMBERS
(lambda (cs) (char-set-fold cons '() cs))
;; CHAR-SET-SIZE
(lambda (cs) (char-set-fold (lambda (c i) (+ i 1)) 0 cs))
;; How many vowels in the char set?
(lambda (cs)
  (char-set-fold (lambda (c i) (if (vowel? c) (+ i 1) i))
                   0 cs))
(char-set-unfold f p g seed base-cs) \rightarrow char-set
                                                                                               charset library???
(char-set-unfold f p g seed) \rightarrow char-set
                                                                                               charset library???
(char-set-unfold! f p g seed base-cs) \rightarrow char-set
                                                                                               charset library???
```

This is a fundamental constructor for char-sets.

(define (char-set-unfold p f g seed base-cs)

- $\bullet$  G is used to generate a series of "seed" values from the initial seed: seed, (g seed), (g<sup>2</sup> seed), (g<sup>3</sup> seed), ...
- P tells us when to stop when it returns true when applied to one of these seed values.
- F maps each seed value to a character. These characters are added to the base character set base-cs to form the result; base-cs defaults to the empty set. char-set-unfold! adds the characters to base-cs in a linear-update – it is allowed, but not required, to side-effect and use base-cs's storage to construct the result.

More precisely, the following definitions hold, ignoring the optional-argument issues:

```
(char-set-unfold! p f g seed (char-set-copy base-cs)))
(define (char-set-unfold! p f g seed base-cs)
  (let lp ((seed seed) (cs base-cs))
        (if (p seed) cs
                                                          ; P says we are done.
            (lp (g seed)
                                                          ; Loop on (G SEED).
                (char-set-adjoin! cs (f seed))))))
                                                          ; Add (F SEED) to set.
(Note that the actual implementation may be more efficient.)
Examples:
(port->char-set p) = (char-set-unfold eof-object? values
                                        (lambda (x) (read-char p))
                                        (read-char p))
(list->char-set lis) = (char-set-unfold null? car cdr lis)
```

```
(char-set-for-each proc\ cs) \rightarrow unspecified
```

charset library???

Apply procedure proc to each character in the character set cs. Note that the order in which proc is applied to the characters in the set is not specified, and may even change from one procedure application to another.

Nothing at all is specified about the value returned by this procedure; it is not even required to be consistent from call to call. It is simply required to be a value (or values) that may be passed to a command continuation, e.g. as the value of an expression appearing as a non-terminal subform of a begin expression. Note that in R5RS, this restricts the procedure to returning a single value; non-R5RS systems may not even provide this restriction.

```
(char-set-map proc cs) \rightarrow char-set
```

charset library???

proc is a char->char procedure. Apply it to all the characters in the char-set cs, and collect the results into a new character set.

Essentially lifts proc from a char->char procedure to a char-set -> char-set procedure.

Example:

(char-set-map char-downcase cset)

### Creating character sets

```
(char-set-copy cs) \rightarrow char-set
```

charset library???

Returns a copy of the character set cs. "Copy" means that if either the input parameter or the result value of this procedure is passed to one of the linear-update procedures described below, the other character set is guaranteed not to be altered.

A system that provides pure-functional implementations of the linear-operator suite could implement this procedure as the identity function - so copies are *not* guaranteed to be distinct by eq?.

```
(char-set char_1 ...) \rightarrow char-set
```

charset library???

Return a character set containing the given characters.

```
(list->char-set char-list\ base-cs) \rightarrow char-set
(list->char-set char-list) \rightarrow char-set
(list->char-set! char-list\ base-cs) \rightarrow char-set
```

charset library procedure charset library procedure charset library procedure

Return a character set containing the characters in the list of characters char-list.

If character set base-cs is provided, the characters from char-list are added to it. list->char-set! is allowed, but not required, to side-effect and reuse the storage in base-cs; list->char-set produces a fresh character set.

```
(string->char-set s base-cs) \rightarrow char-set (string->char-set s) \rightarrow char-set (string->char-set! s base-cs) \rightarrow char-set
```

charset library procedure charset library procedure charset library procedure

Return a character set containing the characters in the string s.

If character set base-cs is provided, the characters from s are added to it. string->char-set! is allowed, but not required, to side-effect and reuse the storage in base-cs; string->char-set produces a fresh character set.

```
(char-set-filter pred\ cs\ base-cs) \rightarrow char-set
(char-set-filter pred\ cs) \rightarrow char-set
(char-set-filter! pred\ cs\ base-cs) \rightarrow char-set
```

charset library procedure charset library procedure charset library procedure

Returns a character set containing every character c in cs such that (pred c) returns true.

If character set base-cs is provided, the characters specified by pred are added to it. char-set-filter! is allowed, but not required, to side-effect and reuse the storage in base-cs; char-set-filter produces a fresh character set.

An implementation may not save away a reference to pred and invoke it after char-set-filter or char-set-filter! returns – that is, "lazy," on-demand implementations are not allowed, as pred may have external dependencies on mutable data or have other side-effects.

Rationale: This procedure provides a means of converting a character predicate into its equivalent character set; the cs parameter allows the programmer to bound the predicate's domain. Programmers should be aware that filtering a character set such as char-set:full could be a very expensive operation in an implementation that provided an extremely large character type, such as 32-bit Unicode. An earlier draft of this library provided a simple predicate->char-set procedure, which was rejected in favor of char-set-filter for this reason.

```
(ucs-range->char-set lower upper error? base-cs) \rightarrow char-set (ucs-range->char-set lower upper) \rightarrow char-set (ucs-range->char-set! lower upper error? base-cs) \rightarrow char-set
```

charset library procedure charset library procedure charset library procedure

Lower and upper are exact non-negative integers; lower <= upper.

Returns a character set containing every character whose ISO/IEC 10646 UCS-4 code lies in the half-open range [lower,upper).

- If the requested range includes unassigned UCS values, these are silently ignored (the current UCS specification has "holes" in the space of assigned codes).
- If the requested range includes "private" or "user space" codes, these are handled in an implementation-specific manner; however, a UCS- or Unicode-based Scheme implementation should pass them through transparently.
- If any code from the requested range specifies a valid, assigned UCS character that has no corresponding representative in the implementation's character type, then (1) an error is raised if error? is true, and (2) the code is ignored if error? is false (the default). This might happen, for example, if the implementation uses ASCII characters, and the requested range includes non-ASCII characters.

If character set base-cs is provided, the characters specified by the range are added to it. ucs-range->char-set! is allowed, but not required, to side-effect and reuse the storage in base-cs; ucs-range->char-set produces a fresh character set.

Note that ASCII codes are a subset of the Latin-1 codes, which are in turn a subset of the 16-bit Unicode codes, which are themselves a subset of the 32-bit UCS-4 codes. We commit to a specific encoding in this routine, regardless of the underlying representation of characters, so that client code using this library will be portable. *I.e.*, a conformant Scheme implementation may use EBCDIC or SHIFT-JIS to encode characters; it must simply map the UCS characters from the given range into the native representation when possible, and report errors when not possible.

```
(->char-set x) \rightarrow char-set
```

charset library procedure

Coerces x into a char-set. X may be a string, character or char-set. A string is converted to the set of its constituent characters; a character is converted to a singleton set; a char-set is returned as-is. This procedure is intended for use by other procedures that want to provide "user-friendly," wide-spectrum interfaces to their clients.

#### Querying character sets

(char-set-size cs)  $\rightarrow integer$ 

charset library procedure

Returns the number of elements in character set cs.

(char-set-count pred cs)  $\rightarrow integer$ 

charset library procedure

Apply pred to the chars of character set cs, and return the number of chars that caused the predicate to return true.

```
(char-set->list cs) \rightarrow character-list
```

charset library procedure

This procedure returns a list of the members of character set cs. The order in which cs's characters appear in the list is not defined, and may be different from one call to another.

```
(char-set->string cs) \rightarrow string
```

charset library procedure

This procedure returns a string containing the members of character set cs. The order in which cs's characters appear in the string is not defined, and may be different from one call to another.

```
(char-set-contains? cs \ char) \rightarrow boolean
```

charset library procedure

This procedure tests char for membership in character set cs.

The MIT Scheme character-set package called this procedure char-set-member?, but the argument order isn't consistent with the name.

```
(char-set-every pred cs) \rightarrow boolean
(char-set-any pred cs) \rightarrow boolean
```

charset library procedure charset library procedure

The char-set-every procedure returns true if predicate pred returns true of every character in the character set cs. Likewise, char-set-any applies pred to every character in character set cs, and returns the first true value it finds. If no character produces a true value, it returns false. The order in which these procedures sequence through the elements of cs is not specified.

Note that if you need to determine the actual character on which a predicate returns true, use char-set-any and arrange for the predicate to return the character parameter as its true value, e.g.

```
(char-set-any (lambda (c) (and (char-upper-case? c) c))
              cs)
```

# Character-set algebra

```
(char-set-adjoin cs \ char_1 \ ...) \rightarrow char-set
(char-set-delete cs char_1 ...) \rightarrow char-set
```

charset library procedure charset library procedure

Add/delete the char<sub>i</sub> characters to/from character set cs.

```
(char-set-adjoin! cs \ char_1 \ ...) \rightarrow char-set
(char-set-delete! cs char_1 ...) \rightarrow char-set
```

charset library procedure charset library procedure

Linear-update variants. These procedures are allowed, but not required, to side-effect their first parameter.

```
(char-set-complement cs) \rightarrow char-set
                                                                                                          charset library procedure
(char-set-union cs_1 ...) \rightarrow char-set
                                                                                                          charset library procedure
                                                                                                          charset library procedure
(char-set-intersection cs_1 ...) \rightarrow char-set
(char-set-difference cs_1 cs_2 ...) \rightarrow char-set
                                                                                                          charset library procedure
(char-set-xor cs_1 ...) \rightarrow char-set
                                                                                                          charset library procedure
(char-set-diff+intersection cs_1 cs_2 ...) \rightarrow char-set char-set
                                                                                                          charset library procedure
```

These procedures implement set complement, union, intersection, difference, and exclusive-or for character sets. The union, intersection and xor operations are n-ary. The difference function is also n-ary, associates to the left (that is, it computes the difference between its first argument and the union of all the other arguments), and requires at least one argument.

Boundary cases:

```
(char-set-union) => char-set:empty
(char-set-intersection) => char-set:full
(char-set-xor) => char-set:empty
(char-set-difference cs) => cs
```

char-set-diff+intersection returns both the difference and the intersection of the arguments – it partitions its first parameter. It is equivalent to

but can be implemented more efficiently.

Programmers should be aware that char-set-complement could potentially be a very expensive operation in Scheme implementations that provide a very large character type, such as 32-bit Unicode. If this is a possibility, sets can be complimented with respect to a smaller universe using char-set-difference.

These are linear-update variants of the set-algebra functions. They are allowed, but not required, to side-effect their first (required) parameter.

char-set-diff+intersection! is allowed to side-effect both of its two required parameters,  $cs_1$  and  $cs_2$ .

TODO why does diff+intersection have  $cs_3$ ?

# Standard character sets

# TODO Convert to entry format?

Several character sets are predefined for convenience:

```
char-set:lower-case Lower-case letters
char-set:upper-case Upper-case letters
char-set:letter Title-case letters
```

char-set:letter Letters char-set:digit Digits

char-set:letter+digit Letters and digits

char-set:whitespace Whitespace characters
char-set:iso-control The ISO control characters
char-set:punctuation Punctuation characters
char-set:symbol Symbol characters

char-set:hex-digit A hexadecimal digit: 0-9, A-F, a-f
char-set:blank Blank characters — horizontal whitespace

char-set:ascii All characters in the ASCII set.

Note that there may be characters in char-set:letter that are neither upper or lower case—this might occur in implementations that use a character type richer than ASCII, such as Unicode. A "graphic character" is one that would put ink on your page. While the exact composition of these sets may vary depending upon the character type provided by the underlying Scheme system, here are the definitions for some of the sets in an ASCII implementation:

char-set:lower-case a-z char-set:upper-case A-Z

A-Z and a-z char-set:letter char-set:digit 0123456789

char-set:punctuation  $!"#\%"()*,-./:;?@[\]_{}$ 

\$+<=>^`|~ char-set:symbol

char-set:whitespace Space, newline, tab, form feed,

vertical tab, carriage return

Space and tab char-set:blank

char-set:graphic letter + digit + punctuation + symbol

char-set:printing graphic + whitespace char-set:iso-control ASCII 0-31 and 127

Note that the existence of the char-set:ascii set implies that the underlying character set is required to be at least as rich as ASCII (including ASCII's control characters).

Rationale: The name choices reflect a shift from the older "alphabetic/numeric" terms found in R5RS and Posix to newer, Unicode-influenced "letter/digit" lexemes.

### Unicode, Latin-1 and ASCII definitions of the standard character sets

TODO Does this belong here? Would it not be better to refer to external Java documentation, and/or Unicode standard?

In Unicode Scheme implementations, the base character sets are compatible with Java's Unicode specifications. For ASCII or Latin-1, we simply restrict the Unicode set specifications to their first 128 or 256 codes, respectively. Scheme implementations that are not based on ASCII, Latin-1 or Unicode should attempt to preserve the sense or spirit of these definitions.

The following descriptions frequently make reference to the "Unicode character database." This is a file, available at URL

### ftp://ftp.unicode.org/Public/UNIDATA/UnicodeData.txt

Each line contains a description of a Unicode character. The first semicolon-delimited field of the line gives the hex value of the character's code; the second field gives the name of the character, and the third field gives a two-letter category. Other fields give simple 1-1 case-mappings for the character and other information; see

# ftp://ftp.unicode.org/Public/UNIDATA/UnicodeData.html

for further description of the file's format. Note in particular the two-letter category specified in the the third field, which is referenced frequently in the descriptions below.

#### char-set:lower-casechar-set:lower-case

For Unicode, we follow Java's specification: a character is lowercase if

- $\bullet$  it is not in the range [U+2000,U+2FFF], and
- the Unicode attribute table does not give a lowercase mapping for it, and
- at least one of the following is true:
  - the Unicode attribute table gives a mapping to uppercase for the character, or
  - the name for the character in the Unicode attribute table contains the words "SMALL LETTER" or "SMALL LIGATURE".

The lower-case ASCII characters are

abcdefghijklmnopgrstuvwxyz

Latin-1 adds another 33 lower-case characters to the ASCII set:

```
00B5
     MICRO SIGN
     LATIN SMALL LETTER SHARP S
00DF
00E0
     LATIN SMALL LETTER A WITH GRAVE
     LATIN SMALL LETTER A WITH ACUTE
00E1
00E2
      LATIN SMALL LETTER A WITH CIRCUMFLEX
      LATIN SMALL LETTER A WITH TILDE
00E3
     LATIN SMALL LETTER A WITH DIAERESIS
00E4
00E5
     LATIN SMALL LETTER A WITH RING ABOVE
      LATIN SMALL LETTER AE
00E6
      LATIN SMALL LETTER C WITH CEDILLA
00E7
00E8
      LATIN SMALL LETTER E WITH GRAVE
00E9
      LATIN SMALL LETTER E WITH ACUTE
     LATIN SMALL LETTER E WITH CIRCUMFLEX
00EA
00EB
     LATIN SMALL LETTER E WITH DIAERESIS
00EC
     LATIN SMALL LETTER I WITH GRAVE
00ED
     LATIN SMALL LETTER I WITH ACUTE
00EE
     LATIN SMALL LETTER I WITH CIRCUMFLEX
      LATIN SMALL LETTER I WITH DIAERESIS
00EF
00F0
     LATIN SMALL LETTER ETH
     LATIN SMALL LETTER N WITH TILDE
00F1
00F2
     LATIN SMALL LETTER O WITH GRAVE
00F3
     LATIN SMALL LETTER O WITH ACUTE
00F4
     LATIN SMALL LETTER O WITH CIRCUMFLEX
      LATIN SMALL LETTER O WITH TILDE
00F5
     LATIN SMALL LETTER O WITH DIAERESIS
00F6
00F8
      LATIN SMALL LETTER O WITH STROKE
      LATIN SMALL LETTER U WITH GRAVE
00F9
      LATIN SMALL LETTER U WITH ACUTE
00FA
00FB
     LATIN SMALL LETTER U WITH CIRCUMFLEX
00FC
     LATIN SMALL LETTER U WITH DIAERESIS
     LATIN SMALL LETTER Y WITH ACUTE
00FD
     LATIN SMALL LETTER THORN
00FE
00FF
      LATIN SMALL LETTER Y WITH DIAERESIS
```

Note that three of these have no corresponding Latin-1 upper-case character:

```
00B5 MICRO SIGN
00DF LATIN SMALL LETTER SHARP S
00FF LATIN SMALL LETTER Y WITH DIAERESIS
```

(The compatibility micro character uppercases to the non-Latin-1 Greek capital mu; the German sharp s character uppercases to the pair of characters "SS," and the capital y-with-diaeresis is non-Latin-1.)

(Note that the Java spec for lowercase characters given at

http://java.sun.com/docs/books/jls/html/javalang.doc4.html#14345

is inconsistent. U+00B5 MICRO SIGN fulfills the requirements for a lower-case character (as of Unicode 3.0), but is not given in the numeric list of lower-case character codes.)

(Note that the Java spec for isLowerCase() given at

http://java.sun.com/products/jdk/1.2/docs/api/java/lang/Character.html#isLowerCase(char)

gives three mutually inconsistent definitions of "lower case." The first is the definition used in this SRFI. Following text says "A character is considered to be lowercase if and only if it is specified to be lowercase by the Unicode 2.0 standard (category Ll in the Unicode specification data file)." The former spec excludes U+00AA FEMININE ORDINAL INDICATOR and U+00BA MASCULINE ORDINAL INDICATOR; the later spec includes them. Finally, the spec enumerates a list of characters in the Latin-1 subset; this list excludes U+00B5 MICRO SIGN, which is included in both of the previous specs.)

#### char-set:upper-casechar-set:upper-case

For Unicode, we follow Java's specification: a character is uppercase if

- it is not in the range [U+2000,U+2FFF], and
- the Unicode attribute table does not give an uppercase mapping for it (this excludes titlecase characters), and
- at least one of the following is true:
  - the Unicode attribute table gives a mapping to lowercase for the character, or
  - the name for the character in the Unicode attribute table contains the words "CAPITAL LETTER" or "CAPITAL LIGATURE".

The upper-case ASCII characters are

# ABCDEFGHIJKLMNOPQRSTUVWXYZ

Latin-1 adds another 30 upper-case characters to the ASCII set:

```
LATIN CAPITAL LETTER A WITH GRAVE
00C0
      LATIN CAPITAL LETTER A WITH ACUTE
00C1
00C2
      LATIN CAPITAL LETTER A WITH CIRCUMFLEX
     LATIN CAPITAL LETTER A WITH TILDE
00C3
00C4
      LATIN CAPITAL LETTER A WITH DIAERESIS
      LATIN CAPITAL LETTER A WITH RING ABOVE
00C5
00C6
      LATIN CAPITAL LETTER AE
      LATIN CAPITAL LETTER C WITH CEDILLA
00C7
      LATIN CAPITAL LETTER E WITH GRAVE
00C8
00C9
      LATIN CAPITAL LETTER E WITH ACUTE
00CA
     LATIN CAPITAL LETTER E WITH CIRCUMFLEX
00CB
      LATIN CAPITAL LETTER E WITH DIAERESIS
00CC
      LATIN CAPITAL LETTER I WITH GRAVE
     LATIN CAPITAL LETTER I WITH ACUTE
00CD
00CE
      LATIN CAPITAL LETTER I WITH CIRCUMFLEX
00CF
      LATIN CAPITAL LETTER I WITH DIAERESIS
     LATIN CAPITAL LETTER ETH
00D0
      LATIN CAPITAL LETTER N WITH TILDE
00D1
00D2
     LATIN CAPITAL LETTER O WITH GRAVE
00D3
     LATIN CAPITAL LETTER O WITH ACUTE
00D4
      LATIN CAPITAL LETTER O WITH CIRCUMFLEX
00D5
      LATIN CAPITAL LETTER O WITH TILDE
      LATIN CAPITAL LETTER O WITH DIAERESIS
00D6
00D8
      LATIN CAPITAL LETTER O WITH STROKE
      LATIN CAPITAL LETTER U WITH GRAVE
00D9
00DA
     LATIN CAPITAL LETTER U WITH ACUTE
00DB
     LATIN CAPITAL LETTER U WITH CIRCUMFLEX
      LATIN CAPITAL LETTER U WITH DIAERESIS
00DC
00DD
     LATIN CAPITAL LETTER Y WITH ACUTE
```

# char-set:title-casechar-set:title-case

LATIN CAPITAL LETTER THORN

00DE

In Unicode, a character is titlecase if it has the category Lt in the character attribute database. There are very few of these characters; here is the entire 31-character list as of Unicode 3.0:

01F2

- LATIN CAPITAL LETTER D WITH SMALL LETTER Z WITH CARON 01C5LATIN CAPITAL LETTER L WITH SMALL LETTER J 01C8
- 01CBLATIN CAPITAL LETTER N WITH SMALL LETTER J
- LATIN CAPITAL LETTER D WITH SMALL LETTER Z GREEK CAPITAL LETTER ALPHA WITH PSILI AND PROSGEGRAMMENI 1F88
- 1F89 GREEK CAPITAL LETTER ALPHA WITH DASIA AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER ALPHA WITH PSILI AND VARIA AND PROSGEGRAMMENI 1F8A
- 1F8BGREEK CAPITAL LETTER ALPHA WITH DASIA AND VARIA AND PROSGEGRAMMENI
- 1F8C GREEK CAPITAL LETTER ALPHA WITH PSILI AND OXIA AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER ALPHA WITH DASIA AND OXIA AND PROSGEGRAMMENI 1F8D
- 1F8E GREEK CAPITAL LETTER ALPHA WITH PSILI AND PERISPOMENI AND PROSGEGRAMMENI
- 1F8F GREEK CAPITAL LETTER ALPHA WITH DASIA AND PERISPOMENI AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER ETA WITH PSILI AND PROSGEGRAMMENI 1F98
- 1F99 GREEK CAPITAL LETTER ETA WITH DASIA AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER ETA WITH PSILI AND VARIA AND PROSGEGRAMMENI 1F9A
- 1F9B GREEK CAPITAL LETTER ETA WITH DASIA AND VARIA AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER ETA WITH PSILI AND OXIA AND PROSGEGRAMMENI 1F9C
- 1F9D GREEK CAPITAL LETTER ETA WITH DASIA AND OXIA AND PROSGEGRAMMENI
- 1F9EGREEK CAPITAL LETTER ETA WITH PSILI AND PERISPOMENI AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER ETA WITH DASIA AND PERISPOMENI AND PROSGEGRAMMENI 1F9F
- GREEK CAPITAL LETTER OMEGA WITH PSILI AND PROSGEGRAMMENI 1FA8
- 1FA9 GREEK CAPITAL LETTER OMEGA WITH DASIA AND PROSGEGRAMMENI
- 1FAA GREEK CAPITAL LETTER OMEGA WITH PSILI AND VARIA AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER OMEGA WITH DASIA AND VARIA AND PROSGEGRAMMENI 1FAB
- GREEK CAPITAL LETTER OMEGA WITH PSILI AND OXIA AND PROSGEGRAMMENI 1FAC
- 1FAD GREEK CAPITAL LETTER OMEGA WITH DASIA AND OXIA AND PROSGEGRAMMENI
- GREEK CAPITAL LETTER OMEGA WITH PSILI AND PERISPOMENI AND PROSGEGRAMMENI 1FAE
- GREEK CAPITAL LETTER OMEGA WITH DASIA AND PERISPOMENI AND PROSGEGRAMMENI 1FAF
- 1FBC GREEK CAPITAL LETTER ALPHA WITH PROSGEGRAMMENI
- 1FCC GREEK CAPITAL LETTER ETA WITH PROSGEGRAMMENI
- GREEK CAPITAL LETTER OMEGA WITH PROSGEGRAMMENI

There are no ASCII or Latin-1 titlecase characters.

# char-set:letterchar-set:letter

In Unicode, a letter is any character with one of the letter categories (Lu, Ll, Lt, Lm, Lo) in the Unicode character database.

There are 52 ASCII letters

abcdefghijklmnopqrstuvwxyz

ABCDEFGHIJKLMNOPQRSTUVWXYZ

There are 117 Latin-1 letters. These are the 115 characters that are members of the Latin-1 char-set:lower-case and char-set:upper-case sets, plus

00AA FEMININE ORDINAL INDICATOR

MASCULINE ORDINAL INDICATOR

(These two letters are considered lower-case by Unicode, but not by Java or SRFI 14.)

## char-set:digitchar-set:digit

In Unicode, a character is a digit if it has the category Nd in the character attribute database. In Latin-1 and ASCII, the only such characters are 0123456789. In Unicode, there are other digit characters in other code blocks, such as Gujarati digits and Tibetan digits.

# char-set:hex-digitchar-set:hex-digit

The only hex digits are 0123456789abcdefABCDEF.

## char-set:letter+digitchar-set:letter+digit

The union of char-set:letter and char-set:digit.

# char-set:graphicchar-set:graphic

A graphic character is one that would put ink on paper. The ASCII and Latin-1 graphic characters are the members of

char-set:letter
char-set:digit
char-set:punctuation
char-set:symbol

# char-set:printingchar-set:printing

A printing character is one that would occupy space when printed, *i.e.*, a graphic character or a space character. char-set:printing is the union of char-set:whitespace and char-set:graphic.

# char-set:whitespacechar-set:whitespace

In Unicode, a whitespace character is either

- a character with one of the space, line, or paragraph separator categories (Zs, Zl or Zp) of the Unicode character database.
- U+0009 Horizontal tabulation (\t control-I)
- U+000A Line feed (\n control-J)
- U+000B Vertical tabulation (\v control-K)
- U+000C Form feed (\f control-L)
- U+000D Carriage return (\r control-M)

There are 24 whitespace characters in Unicode 3.0:

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```
HORIZONTAL TABULATION
0009
                                    \t control-I
000A
      LINE FEED
                                    \n control-J
000B
      VERTICAL TABULATION
                                    \v control-K
                                    \f control-L
000C
      FORM FEED
000D
      CARRIAGE RETURN
                                    \r control-M
0020
      SPACE
                                    Zs
00A0
      NO-BREAK SPACE
                                    Zs
1680
      OGHAM SPACE MARK
                                    Zs
      EN QUAD
                                    Z_{S}
2000
2001
      EM QUAD
2002
      EN SPACE
                                    Z_{S}
2003
      EM SPACE
                                    Zs
2004
      THREE-PER-EM SPACE
                                    Z_{S}
2005
      FOUR-PER-EM SPACE
                                    Z_{\rm S}
2006
      SIX-PER-EM SPACE
                                    Z_{S}
2007
      FIGURE SPACE
                                    7.5
2008
      PUNCTUATION SPACE
                                    Z_{S}
2009
      THIN SPACE
                                    Z_{S}
      HAIR SPACE
200A
                                    Zs
200B
      ZERO WIDTH SPACE
                                    Z_{S}
2028
      LINE SEPARATOR
                                    Z1
2029
      PARAGRAPH SEPARATOR
                                    Zp
202F
      NARROW NO-BREAK SPACE
                                    Z_{\rm S}
3000
      IDEOGRAPHIC SPACE
                                    Z_{S}
```

The ASCII whitespace characters are the first six characters in the above list – line feed, horizontal tabulation, vertical tabulation, form feed, carriage return, and space. These are also exactly the characters recognised by the Posix isspace() procedure. Latin-1 adds the no-break space.

Note: Java's isWhitespace() method is incompatible, including

```
0009HORIZONTAL TABULATION(\t control-I)001CFILE SEPARATOR(control-\)001DGROUP SEPARATOR(control-])001ERECORD SEPARATOR(control-^)001FUNIT SEPARATOR(control-_)
```

and excluding

#### 00A0 NO-BREAK SPACE

Java's excluding the no-break space means that tokenizers can simply break character streams at "whitespace" boundaries. However, the exclusion introduces exceptions in other places, e.g. char-set:printing is no longer simply the union of char-set:graphic and char-set:whitespace.

#### char-set:iso-controlchar-set:iso-control

The ISO control characters are the Unicode/Latin-1 characters in the ranges [U+0000,U+001F] and [U+007F,U+009F]. ASCII restricts this set to the characters in the range [U+0000,U+001F] plus the character U+007F.

Note that Unicode defines other control characters which do not belong to this set (hence the qualifying prefix "iso-" in the name). This restriction is compatible with the Java IsiSOControl() method.

## char-set:punctuationchar-set:punctuation

In Unicode, a punctuation character is any character that has one of the punctuation categories in the Unicode character database (Pc, Pd, Ps, Pe, Pi, Pf, or Po.)

ASCII has 23 punctuation characters:

# !"#%&'()\*,-./:;?@[\] {}

Latin-1 adds six more:

```
00A1
     INVERTED EXCLAMATION MARK
00AB
     LEFT-POINTING DOUBLE ANGLE QUOTATION MARK
00AD
     SOFT HYPHEN
00B7
     MIDDLE DOT
00BB
     RIGHT-POINTING DOUBLE ANGLE QUOTATION MARK
00BF
     INVERTED QUESTION MARK
```

Note that the nine ASCII characters \$+<=>^`|~ are not punctuation. They are "symbols."

# char-set:symbolchar-set:symbol

In Unicode, a symbol is any character that has one of the symbol categories in the Unicode character database (Sm, Sc, Sk, or So). There are nine ASCII symbol characters:

```
$+<=>^`|~
```

Latin-1 adds 18 more:

```
00A2
      CENT SIGN
00A3
      POUND SIGN
00A4
      CURRENCY SIGN
00A5
      YEN SIGN
00A6
      BROKEN BAR
00A7
      SECTION SIGN
00A8
      DIAERESIS
      COPYRIGHT SIGN
00A9
00AC
      NOT SIGN
00AE
     REGISTERED SIGN
00AF
      MACRON
00B0
      DEGREE SIGN
      PLUS-MINUS SIGN
00B1
00B4
      ACUTE ACCENT
00B6
      PILCROW SIGN
00B8
      CEDILLA
00D7
      MULTIPLICATION SIGN
00F7
      DIVISION SIGN
```

# char-set:blankchar-set:blank

Blank chars are horizontal whitespace. In Unicode, a blank character is either

- a character with the space separator category (Zs) in the Unicode character database.
- U+0009 Horizontal tabulation (\t control-I)

There are eighteen blank characters in Unicode 3.0:

```
HORIZONTAL TABULATION
                                    \t control-I
0009
0020
      SPACE
                                   Zs
00A0
     NO-BREAK SPACE
                                   Z_{S}
      OGHAM SPACE MARK
                                   Z_{S}
1680
2000
      EN QUAD
                                   Z_{\rm S}
      EM QUAD
2001
                                   Zs
      EN SPACE
2002
                                    7s
2003
      EM SPACE
                                   Zs
2004
      THREE-PER-EM SPACE
                                    Z_{S}
2005
      FOUR-PER-EM SPACE
2006
      SIX-PER-EM SPACE
                                    Z_{S}
2007
      FIGURE SPACE
                                    Z_{S}
2008
      PUNCTUATION SPACE
                                    Z_{S}
2009
      THIN SPACE
200A
     HAIR SPACE
                                   Z_{\rm S}
200B
     ZERO WIDTH SPACE
                                   Zs
202F
      NARROW NO-BREAK SPACE
                                   Z_{S}
3000
      IDEOGRAPHIC SPACE
```

The ASCII blank characters are the first two characters above – horizontal tab and space. Latin-1 adds the no-break space.

Java doesn't have the concept of "blank" characters, so there are no compatibility issues.

### References & linksReferences & links

```
[Java] The following URLs provide documentation on relevant Java classes.
    http://java.sun.com/products/jdk/1.2/docs/api/java/lang/Character.html
    http://java.sun.com/products/jdk/1.2/docs/api/java/lang/String.html
    http://java.sun.com/products/jdk/1.2/docs/api/java/lang/StringBuffer.html
    http://java.sun.com/products/jdk/1.2/docs/api/java/text/Collator.html
    http://java.sun.com/products/jdk/1.2/docs/api/java/text/package-summary.html
[MIT-Scheme] http://www.swiss.ai.mit.edu/projects/scheme/
[R5RS] Revised<sup>5</sup> report on the algorithmic language Scheme.
     R. Kelsey, W. Clinger, J. Rees (editors).
    Higher-Order and Symbolic Computation, Vol. 11, No. 1, September, 1998.
    and ACM SIGPLAN Notices, Vol. 33, No. 9, October, 1998.
     Available at http://www.schemers.org/Documents/Standards/.
[SRFI] The SRFI web site.
    http://srfi.schemers.org/
[SRFI-14] SRFI-14: String libraries.
    http://srfi.schemers.org/srfi-14/
     This document, in HTML: http://srfi.schemers.org/srfi-14/srfi-14.html
     This document, in plain text format: http://srfi.schemers.org/srfi-14/srfi-14.txt
     Source code for the reference implementation: http://srfi.schemers.org/srfi-14/srfi-14.scm
     Scheme 48 module specification, with typings: http://srfi.schemers.org/srfi-14/srfi-14-s48-module.
     Regression-test suite: http://srfi.schemers.org/srfi-14/srfi-14-tests.scm
[Unicode] http://www.unicode.org/
[UnicodeData] The Unicode character database.
     ftp://ftp.unicode.org/Public/UNIDATA/UnicodeData.txt
     ftp://ftp.unicode.org/Public/UNIDATA/UnicodeData.html
```

# Hash tables

[Red Edition item 7] What hash table library should R7RS-large provide?

SRFI 69 is a basic hash table library. SRFI 125 is an upward compatible extension of it. Likewise, R6RS provides a basic hash table library, of which SRFI 126 is an upward compatible extension. Since the interface of SRFI 125 depends on SRFI 128, voting for SRFI 125 will cause your vote on comparator libraries to be automatically changed to SRFI 128.

TODO This section specifies some procedures that are then labelled "deprecated". Should they remain?

TODO This section makes references to R6RS and Common Lisp. Should those references remain?

This SRFI defines an interface to hash tables, which are widely recognized as a fundamental data structure for a wide variety of applications. A hash table is a data structure that:

- Is disjoint from all other types.
- Provides a mapping from objects known as keys to corresponding objects known as values.
  - Keys may be any Scheme objects in some kinds of hash tables, but are restricted in other kinds.
  - Values may be any Scheme objects.
- Has no intrinsic order for the key-value associations it contains.
- Provides an equality predicate which defines when a proposed key is the same as an existing key. No table may contain more than one value for a given key.
- Provides a hash function which maps a candidate key into a non-negative exact integer.
- Supports mutation as the primary means of setting the contents of a table.
- Provides key lookup and destructive update in (expected) amortized constant time, provided a satisfactory hash function is available.
- Does not guarantee that whole-table operations work in the presence of concurrent mutation of the whole hash table (values may be safely mutated).

The names described in this section comprise the (scheme hash-table) library.

#### Pronunciation

The slash in the names of some procedures can be pronounced "with".

## Specification

The procedures in this SRFI are in the (srfi 125) library (or (srfi :125) on R6RS).

All references to "executing in expected amortized constant time" presuppose that a satisfactory hash function is available. Arbitrary or impure hash functions can make a hash of any implementation.

Hash tables are allowed to cache the results of calling the equality predicate and hash function, so programs cannot rely on the hash function being called exactly once for every primitive hash table operation: it may be called zero, one, or more times.

It is an error if the procedure argument of hash-table-find, hash-table-count, hash-table-map, hash-table-for-each, hash-table-map!, hash-table-map->list, hash-table-fold or hash-table-prune! mutates the hash table being walked.

It is an error to pass two hash tables that have different comparators or equality predicates to any of the procedures of this SRFI.

Implementations are permitted to ignore user-specified hash functions in certain circumstances. Specifically, if the equality predicate, whether passed as part of a comparator or explicitly, is more fine-grained (in the sense of R7RS-small section 6.1) than equal?, the implementation is free — indeed, is encouraged — to ignore the user-specified hash function and use something implementation-dependent. This allows the use of addresses as hashes, in which case the keys must be rehashed if they are moved by the garbage collector. Such a hash function is unsafe to use outside the context of implementation-provided hash tables. It can of course be exposed by an implementation as an extension, with suitable warnings against inappropriate uses.

It is an error to mutate a key during or after its insertion into a hash table in such a way that the hash function of the table will return a different result when applied to that key.

#### Index

- Constructors: make-hash-table, hash-table, hash-table-unfold, alist->hash-table
- Predicates: hash-table?, hash-table-contains?, hash-table-exists? (deprecated), hash-table-empty?, hash-table=?, hash-table-mutable?
- Accessors: hash-table-ref, hash-table-ref/default
- Mutators: hash-table-set!, hash-table-delete!, hash-table-intern!, hash-table-update!, hash-table-update!/defau hash-table-pop!, hash-table-clear!
- The whole hash table: hash-table-size, hash-table-keys, hash-table-values, hash-table-entries, hash-table-find, hash-table-count
- Mapping and folding: hash-table-map, hash-table-for-each, hash-table-walk (deprecated), hash-table-map!, hash-table-map->list, hash-table-fold, hash-table-prune!
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- Hash tables as sets: hash-table-union!, hash-table-merge! (deprecated), hash-table-intersection!, hash-table-differ hash-table-xor!
- Hash functions and reflectivity (deprecated): hash, string-hash, string-ci-hash, hash-by-identity, hash-table-equivalent hash-table-hash-function

## Constructors

 $(make-hash-table\ comparator\ arg\ ...) \rightarrow hash-table??? \\ (make-hash-table\ comparator) \rightarrow hash-table??? \\ (make-hash-table\ equality-predicate\ hash-function\ arg\ ...) \rightarrow hash-table??? \\ (make-hash-table\ equality-predicate\ hash-function) \rightarrow hash-table??? \\ (make-hash-table\ equality-predicate\ arg\ ...) \rightarrow hash-table??? \\ (make-hash-table\ equality-predicate) \rightarrow hash-table?? \\ (make-hash-table\ equality-predicate) \rightarrow hash-table? \\ (make-hash-table\ equality-predicate) \rightarrow hash-tabl$ 

Returns a newly allocated hash table whose equality predicate and hash function are extracted from *comparator*. Alternatively, for backward compatibility with SRFI 69 the equality predicate and hash function can be passed as separate arguments; this usage is deprecated.

As mentioned above, implementations are free to use an appropriate implementation-dependent hash function instead of the specified hash function, provided that the specified equality predicate is a refinement of the equal? predicate. This applies whether the hash function and equality predicate are passed as separate arguments or packaged up into a comparator.

If an equality predicate rather than a comparator is provided, the ability to omit the *hash-function* argument is severely limited. The implementation must provide hash functions appropriate for use with the predicates eq?, eqv?, equal?,

string=?, and string-ci=?, and may extend this list. But if any unknown equality predicate is provided without a hash function, an error should be signaled. The constraints on equality predicates and hash functions are given in SRFI

The meaning of any further arguments is implementation-dependent. However, implementations which support the ability to specify the initial capacity of a hash table should interpret a non-negative exact integer as the specification of that capacity. In addition, if the symbols thread-safe, weak-keys, ephemeral-keys, weak-values, or ephemeral-values are present, implementations should create thread-safe hash tables, hash tables with weak keys or ephemeral keys, or hash tables with weak or ephemeral values respectively. Implementations are free to use ephemeral keys or values when weak keys or values respectively have been requested. To avoid collision with the hash-function argument, none of these arguments can be procedures.

(R6RS make-eq-hashtable, make-eqv-hashtable, and make-hashtable; Common Lisp make-hash-table)

(hash-table comparator key value ...)  $\rightarrow hash-table$ ???

hash-table library procedure

TODO I've been converting entry descriptions to match R7RS, with separate prototypes for omitted arguments, that doesn't work here, because the number of keys and values doesn't match. Fix somehow.

Returns a newly allocated hash table, created as if by make-hash-table using comparator. For each pair of arguments, an association is added to the new hash table with key as its key and value as its value. If the implementation supports immutable hash tables, this procedure returns an immutable hash table. If the same key (in the sense of the equality predicate) is specified more than once, it is an error.

(hash-table-unfold stop? mapper successor seed comparator  $arg ...) \rightarrow ????$ 

hash-table library procedure

TODO This one looks garbled from the Pandoc conversion. Check against SRFI.

Create a new hash table as if by make-hash-table using comparator and the args. If the result of applying the predicate stop? to seed is true, return the hash table. Otherwise, apply the procedure mapper to seed. Mapper returns two values, which are inserted into the hash table as the key and the value respectively. Then get a new seed by applying the procedure *successor* to *seed*, and repeat this algorithm.

```
(alist->hash-table alist comparator arg ...) \rightarrow hash-table???
                                                                                                hash-table library procedure
(alist->hash-table alist equality-predicate hash-function arg ...) → hash-table ???
                                                                                                hash-table library procedure
(alist->hash-table alist equality-predicate hash-function) \rightarrow hash-table???
                                                                                                hash-table library procedure
                                                                                                hash-table library procedure
(alist->hash-table alist equality-predicate arg ...) \rightarrow hash-table???
(alist->hash-table alist equality-predicate) \rightarrow hash-table ???
                                                                                                hash-table library procedure
```

Returns a newly allocated hash-table as if by make-hash-table using comparator and the args. It is then initialized from the associations of alist. Associations earlier in the list take precedence over those that come later. The second form TODO and subsequent forms is for compatibility with SRFI 69, and is deprecated.

#### **Predicates**

(hash-table? obj)  $\rightarrow boolean$ ???

hash-table library procedure

Returns #t if obj is a hash table, and #f otherwise. (R6RS hashtable?; Common Lisp hash-table-p)

```
(hash-table-contains? hash-table\ key) \rightarrow boolean???
(hash-table-exists? hash-table\ key) \rightarrow boolean???
```

hash-table library procedure hash-table library procedure

Returns #t if there is any association to key in hash-table, and #f otherwise. Must execute in expected amortized constant time. The hash-table-exists? procedure is the same as hash-table-contains?, is provided for backward compatibility with SRFI 69, and is deprecated. (R6RS hashtable-contains?)

(hash-table-empty? hash-table)  $\rightarrow boolean$ ???

hash-table library procedure

Returns #t if hash-table contains no associations, and #f otherwise.

(hash-table=? value-comparator hash-table<sub>1</sub> hash-table<sub>2</sub>)  $\rightarrow boolean$ ???

hash-table library procedure

Returns #t if  $hash-table_1$  and  $hash-table_2$  have the same keys (in the sense of their common equality predicate) and each key has the same value (in the sense of value-comparator), and #f otherwise.

(hash-table-mutable? hash-table)  $\rightarrow boolean$ ???

hash-table library procedure

Returns #t if the hash table is mutable. Implementations may or may not support immutable hash tables. (R6RS hashtable-mutable?)

#### Accessors

The following procedures, given a key, return the corresponding value.

(hash-table-ref hash-table key failure success)  $\rightarrow$  value??? (hash-table-ref hash-table key failure)  $\rightarrow$  value??? (hash-table-ref hash-table key)  $\rightarrow$  value???

hash-table library procedure hash-table library procedure hash-table library procedure

Extracts the value associated to key in hash-table, invokes the procedure success on it, and returns its result; if success is not provided, then the value itself is returned. If key is not contained in hash-table and failure is supplied, then failure is invoked on no arguments and its result is returned. Otherwise, it is an error. Must execute in expected amortized constant time, not counting the time to call the procedures. SRFI 69 does not support the success procedure.

(hash-table-ref/default  $hash-table\ key\ default) \rightarrow value \ref{eq:constraint}$ ?

hash-table library procedure

Semantically equivalent to, but may be more efficient than, the following code:

(hash-table-ref hash-table key (lambda () default))

(R6RS hashtable-ref; Common Lisp gethash)

#### Mutators

The following procedures alter the associations in a hash table either unconditionally, or conditionally on the presence or absence of a specified key. It is an error to add an association to a hash table whose key does not satisfy the type test predicate of the comparator used to create the hash table.

(hash-table-set! hash-table arg ...)  $\rightarrow unspecified$ 

hash-table library procedure

Repeatedly mutates *hash-table*, creating new associations in it by processing the arguments from left to right. The *args* alternate between keys and values. Whenever there is a previous association for a key, it is deleted. It is an error if the type check procedure of the comparator of *hash-table*, when invoked on a key, does not return #t. Likewise, it is an error if a key is not a valid argument to the equality predicate of *hash-table*. Returns an unspecified value. Must execute in expected amortized constant time per key. SRFI 69, R6RS hashtable-set! and Common Lisp (setf gethash) do not handle multiple associations.

(hash-table-delete!  $hash-table\ key\ ...$ )  $\rightarrow integer$ 

hash-table library procedure

Deletes any association to each key in hash-table and returns the number of keys that had associations. Must execute in expected amortized constant time per key. SRFI 69, R6RS hashtable-delete!, and Common Lisp remhash do not handle multiple associations.

(hash-table-intern!  $hash-table\ key\ failure$ )  $\rightarrow value$ ???

hash-table library procedure

Effectively invokes hash-table-ref with the given arguments and returns what it returns. If key was not found in hash-table, its value is set to the result of calling failure. Must execute in expected amortized constant time.

TODO If failure is invoked, is that the return value of hash-table-intern!?

(hash-table-update! hash-table key updater failure success) → unspecified??? (hash-table-update! hash-table key updater failure)  $\rightarrow$  unspecified???

hash-table library procedure hash-table library procedure hash-table library procedure

(hash-table-update! hash-table key updater)  $\rightarrow$  unspecified???

Semantically equivalent to, but may be more efficient than, the following code:

(hash-table-set! hash-table key (updater (hash-table-ref hash-table key failure success)))

Must execute in expected amortized constant time. Returns an unspecified value. (SRFI 69 and R6RS hashtable-update! do not support the *success* procedure)

(hash-table-update!/default hash-table key updater default)  $\rightarrow$  unspecified???

hash-table library procedure

Semantically equivalent to, but may be more efficient than, the following code:

(hash-table-set! hash-table key (updater (hash-table-ref/default hash-table key default)))

Must execute in expected amortized constant time. Returns an unspecified value.

(hash-table-pop! hash-table)  $\rightarrow key???$  value???

hash-table library procedure

Chooses an arbitrary association from hash-table and removes it, returning the key and value as two values.

(hash-table-clear! hash-table)  $\rightarrow unspecified$ ???

hash-table library procedure

Delete all the associations from hash-table. (R6RS hashtable-clear!; Common Lisp clrhash)

#### The whole hash table

These procedures process the associations of the hash table in an unspecified order.

(hash-table-size hash-table)  $\rightarrow integer$ ???

hash-table library procedure

Returns the number of associations in hash-table as an exact integer. Should execute in constant time. (R6RS hashtable-size; Common Lisp hash-table-count.)

(hash-table-keys hash-table)  $\rightarrow list$ 

hash-table library procedure

Returns a newly allocated list of all the keys in hash-table. R6RS hashtable-keys returns a vector.

(hash-table-values hash-table)  $\rightarrow list$ 

hash-table library procedure

Returns a newly allocated list of all the keys in hash-table.

(hash-table-entries hash-table)  $\rightarrow list\ list$ 

hash-table library procedure

Returns two values, a newly allocated list of all the keys in hash-table and a newly allocated list of all the values in hash-table in the corresponding order. R6RS hash-table-entries returns vectors.

(hash-table-find proc hash-table failure)  $\rightarrow value \ or \ \#f?$ ??

hash-table library procedure

For each association of hash-table, invoke proc on its key and value. If proc returns true, then hash-table-find returns what proc returns. If all the calls to proc return #f, return the result of invoking the thunk failure.

(hash-table-count pred hash-table)  $\rightarrow$  integer???

hash-table library procedure

For each association of hash-table, invoke pred on its key and value. Return the number of calls to pred which returned true.

# Mapping and folding

These procedures process the associations of the hash table in an unspecified order.

(hash-table-map  $proc\ comparator\ hash-table) \rightarrow hash-table \ref{eq:proc}$ 

hash-table library procedure

Returns a newly allocated hash table as if by (make-hash-table comparator). Calls proc for every association in hash-table with the value of the association. The key of the association and the result of invoking proc are entered into the new hash table. Note that this is not the result of lifting mapping over the domain of hash tables, but it is considered more useful.

(hash-table-for-each proc hash-table)  $\rightarrow$  unspecified???? (hash-table-walk hash-table proc)  $\rightarrow$  unspecified

hash-table library procedure hash-table library procedure

Calls *proc* for every association in *hash-table* with two arguments: the key of the association and the value of the association. The value returned by *proc* is discarded. Returns an unspecified value. The hash-table-walk procedure is equivalent to hash-table-for-each with the arguments reversed, is provided for backward compatibility with SRFI 69, and is deprecated. (Common Lisp maphash)

(hash-table-map!  $proc\ hash-table$ )  $\rightarrow unspecified$ ???

hash-table library procedure

Calls *proc* for every association in *hash-table* with two arguments: the key of the association and the value of the association. The value returned by *proc* is used to update the value of the association. Returns an unspecified value.

(hash-table-map->list  $proc\ hash-table$ )  $\rightarrow list$ 

hash-table library procedure

Calls *proc* for every association in *hash-table* with two arguments: the key of the association and the value of the association. The values returned by the invocations of *proc* are accumulated into a list, which is returned.

(hash-table-fold  $proc\ seed\ hash-table$ )  $\rightarrow\ value\ \ref{eq:proc}\ \ref{eq:proc}$  (hash-table-fold  $hash-table\ proc\ seed$ )  $\rightarrow\ value\ \ref{eq:proc}\ \ref{eq:proc}$ 

hash-table library procedure hash-table library procedure

Calls proc for every association in hash-table with three arguments: the key of the association, the value of the association, and an accumulated value val. Val is seed for the first invocation of procedure, and for subsequent invocations of proc, the returned value of the previous invocation. The value returned by hash-table-fold is the return value of the last invocation of proc. The order of arguments with hash-table as the first argument is provided for SRFI 69 compatibility, and is deprecated.

(hash-table-prune!  $proc\ hash-table$ )  $\rightarrow unspecified$ ???

hash-table library procedure

Calls proc for every association in hash-table with two arguments, the key and the value of the association, and removes all associations from hash-table for which proc returns true. Returns an unspecified value.

# Copying and conversion

(hash-table-copy  $hash-table\ mutable?$ )  $\rightarrow hash-table???$  (hash-table-copy hash-table?)  $\rightarrow hash-table???$ 

hash-table library procedure hash-table library procedure

Returns a newly allocated hash table with the same properties and associations as *hash-table*. If the second argument is present and is true, the new hash table is mutable. Otherwise it is immutable provided that the implementation supports immutable hash tables. SRFI 69 hash-table-copy does not support a second argument. (R6RS hashtable-copy)

(hash-table-empty-copy hash-table)  $\rightarrow hash-table$ ???

hash-table library procedure

Returns a newly allocated mutable hash table with the same properties as hash-table, but with no associations.

(hash-table->alist hash-table)  $\rightarrow alist???$ 

hash-table library procedure

Returns an alist with the same associations as hash-table in an unspecified order.

#### Hash tables as sets

hash-table library procedure (hash-table-union!  $hash-table_1$   $hash-table_2$ )  $\rightarrow hash-table$ ??? (hash-table-merge!  $hash-table_1$   $hash-table_2$ )  $\rightarrow hash-table$ ??? hash-table library procedure

Adds the associations of  $hash-table_2$  to  $hash-table_1$  and returns  $hash-table_1$ . If a key appears in both hash tables, its value is set to the value appearing in hash-table<sub>1</sub>. Returns hash-table<sub>1</sub>. The hash-table-merge! procedure is the same as hash-table-union!, is provided for compatibility with SRFI 69, and is deprecated.

(hash-table-intersection!  $hash-table_1$   $hash-table_2$ )  $\rightarrow hash-table$ ???

hash-table library procedure

Deletes the associations from hash-table<sub>1</sub> which don't also appear in hash-table<sub>2</sub> and returns hash-table<sub>1</sub>.

(hash-table-difference!  $hash-table_1$   $hash-table_2$ )  $\rightarrow hash-table$ 

hash-table library procedure

Deletes the associations of  $hash-table_1$  whose keys are also present in  $hash-table_2$  and returns  $hash-table_1$ .

(hash-table-xor!  $hash-table_1$   $hash-table_2$ )  $\rightarrow hash-table$ 

hash-table library procedure

Deletes the associations of  $hash-table_1$  whose keys are also present in  $hash-table_2$ , and then adds the associations of hash-table<sub>1</sub> whose keys are not present in hash-table<sub>1</sub> to hash-table<sub>1</sub>. Returns hash-table<sub>1</sub>.

# Hash functions and reflectivity

TODO If we are removing deprecated features, then this whole section goes. If it remains, I will reformat it.

These functions are made part of this SRFI solely for compatibility with SRFI 69, and are deprecated.

(hash obj)

The same as SRFI 128's default-hash procedure, except that it must accept (and should ignore) an optional second argument.

(string-hash obj)

Similar to SRFI 128's string-hash procedure, except that it must accept (and should ignore) an optional second argument. It is incompatible with the procedure of the same name exported by SRFI 128 and SRFI 126.

(string-ci-hash obj)

Similar to SRFI 128's string-ci-hash procedure, except that it must accept (and should ignore) an optional second argument. It is incompatible with the procedure of the same name exported by SRFI 128 and SRFI 126.

(hash-by-identity obj)

The same as SRFI 128's default-hash procedure, except that it must accept (and should ignore) an optional second argument. However, if the implementation replaces the hash function associated with the eq? predicate with an implementation-dependent alternative, it is an error to call this procedure at all.

(hash-table-equivalence-function hash-table)

Returns the equivalence procedure used to create hash-table.

(hash-table-hash-function hash-table)

Returns the hash function used to create hash-table. However, if the implementation has replaced the user-specified hash function with an implementation-specific alternative, the implementation may return #f instead.

Editor: Arthur A. Gleckler

#### **5**. **Immutability**

# Immutable pairs and lists

[Red Edition item 8] What immutable pair/list library should R7RS-large provide?

DRAFT

SRFI 116 is a variant of SRFI 1 for immutable pairs, which are a separate data type from ordinary Scheme pairs. Only a few functional update procedures are provided. Procedure names are prefixed with "i".

TODO Much of this SRFI repeats text from SRFI-1. Could some of it be reduced?

Post-finalization note: One sentence has been added to the section "The procedures" below, and several errors in the examples have been silently corrected. These do not affect the conformance conditions for this SRFI.

Scheme currently does not provide immutable pairs corresponding to its existing mutable pairs, although most uses of pairs do not exploit their mutability. The Racket system takes the radical approach of making Scheme's pairs immutable, and providing a minimal library of mutable pairs with procedures named mpair?, mcons, mcar, mcdr, set-mcar!, set-mcdr!. This SRFI takes the opposite approach of leaving Scheme's pairs unchanged and providing a full set of routines for creating and dealing with immutable pairs. The sample implementation is portable (to systems with SRFI 9) and efficient.

The names described in this section comprise the (scheme ilist) library.

#### Procedure Index

Deleting idelete

Here is a short list of the procedures provided by this SRFI.

```
Constructors ipair ilist
    xipair ipair* make-ilist ilist-tabulate
    ilist-copy iiota
Predicates ipair?
    proper-ilist?/ilist? dotted-ilist?
    not-ipair? null-ilist?
    ilist=
Selectors icar icdr ... icddadr icddddr ilist-ref
    ifirst isecond ithird ifourth ififth
    isixth iseventh ieighth ininth itenth
    icar+icdr
                idrop/ilist-tail
    itake
    itake-right idrop-right
    isplit-at
    ilast last-ipair
Miscellaneous: length, append, concatenate, reverse, zip & count ilength
    iappend iconcatenate ireverse iappend-reverse
    izip iunzip1 iunzip2 iunzip3 iunzip4 iunzip5
    icount
Fold, unfold & map imap
                                ifor-each
    ifold
                iunfold
                               ipair-fold
                                                ireduce
    ifold-right iunfold-right ipair-fold-right ireduce-right
    iappend-map ipair-for-each ifilter-map
                                                imap-in-order
Filtering & partitioning ifilter ipartition iremove
Searching imember imemy imemv
                  ifind-tail
    ifind
    iany ievery
    ilist-index
    itake-while
                  idrop-while
    ispan ibreak
```

idelete-duplicates

```
Immutable association lists iassoc iassq iassv
    ialist-cons ialist-delete
```

Replacement replace-icar replace-icdr

```
Conversion pair->ipair ipair->pair
    list->ilist ilist->list
    tree->itree itree->tree
    gtree->itree gtree->tree
```

Procedure application iapply

```
Comparators ipair-comparator
                                      ilist-comparator
    make-ilist-comparator
                            make-improper-ilist-comparator
   make-icar-comparator
                            make-icdr-comparator
```

# Quotation

TODO Sort out where this goes. Some of this definitely belongs in the Rationale, while some of the rest belongs here. Rather than "recommending", something slightly stronger is needed?

The various Scheme standards permit, but do not require, Scheme implementations to treat quoted pairs and lists as immutable. Thus whereas the expression (let ((foo (list 1 2 3))) (set-car! foo 10) foo) evaluates to (10 2 3), the value of (let ((foo '(1 2 3))) (set-car! foo 10) foo) is not portable, and is in fact an error.

This SRFI recommends that implementations that provide both this SRFI and immutable quotations should cause quotations to return the same immutable pairs that this SRFI describes. This means that the standard Scheme pair and list operations, as well as libraries like SRFI 1 which are built on them, should accept both mutable and immutable pairs: thus (car (ilist 1 2)) should evaluate to 1.

This SRFI further recommends that read should return mutable pairs and lists when reading list structure. No recommendation is made about the behavior of write, display, and similar output procedures on immutable lists.

To make life easier for Scheme programmers, given that many implementations do not provide immutable quotation, the syntax keyword iq is provided as part of this SRFI. It is analogous to quote, taking an arbitrary number of literals and constructing an ilist from them, with any pairs in the literals converted to ipairs. It is useful for providing constant ipairbased objects. Note that pairs within literal vectors or other implementation-dependent literals will not be converted. Unfortunately, there is no ilist analogue of ', so we save keystrokes by using iq rather than iquote and omitting the top-level parentheses.

#### Notation

The templates given below obey the following conventions for procedure formals:

ilist A proper (()-terminated) ilist dilist A proper or dotted ilist An immutable pair ipair x, y, d, a Any value

Any value object, value

A natural number (an integer  $\geq = 0$ ) n, i

proc A procedure

A procedure whose return value is treated as a boolean pred

A boolean procedure taking two arguments

To interpret the examples, pretend that they are executed on a Scheme that prints immutable pairs and lists with the syntax of mutable ones.

It is an error to pass a dotted ilist to a procedure not defined to accept such an argument.

Added after finalization: Implementers should extend the Scheme predicate equal? to descend into immutable pairs in the same way that it descends into mutable pairs.

(ipair a d)  $\rightarrow ipair$ 

ilist library procedure

The primitive constructor. Returns a newly allocated ipair whose icar is a and whose icdr is d. The ipair is guaranteed to be different (in the sense of eqv?) from every existing object.

(ilist  $object \dots) \rightarrow ilist$ 

ilist library procedure

Returns a newly allocated ilist of its arguments.

(xipair d a)  $\rightarrow ipair$ 

ilist library procedure

(lambda (d a) (ipair a d))

Of utility only as a value to be conveniently passed to higher-order procedures.

```
(xipair (iq b c) 'a) \Rightarrow (a b c)
```

The name stands for "eXchanged Immutable PAIR."

```
(ipair* elt_1 elt_2 ...) \rightarrow object
```

ilist library procedure

Like ilist, but the last argument provides the tail of the constructed ilist, returning

```
(ipair elt1 (ipair elt2 (ipair ... eltn)))
(ipair* 1 2 3 4) => (1 2 3 . 4)
(ipair* 1) => 1
```

```
(make-ilist n \ fill) \rightarrow ilist
(make-ilist n) \rightarrow ilist
```

ilist library procedure

ilist library procedure

Returns an n-element ilist, whose elements are all the value fill. If the fill argument is not given, the elements of the ilist may be arbitrary values.

```
(make-ilist 4 'c) => (c c c c)
```

```
(ilist-tabulate n \ init-proc) \rightarrow ilist
```

ilist library procedure

Returns an n-element ilist. Element i of the ilist, where  $0 \le i \le n$ , is produced by (init-proc i). No guarantee is made about the dynamic order in which init-proc is applied to these indices.

```
(ilist-tabulate 4 values) => (0 1 2 3)
```

```
(ilist-copy dilist) \rightarrow dilist
```

ilist library procedure

Copies the spine of the argument, including the ilist tail.

```
(iiota count \ start \ step) \rightarrow ilist ilist library procedure (iiota count \ start) \rightarrow ilist ilist library procedure (iiota count) \rightarrow ilist ilist library procedure ilist library procedure
```

Returns an ilist containing the elements

The start and step parameters default to 0 and 1, respectively. This procedure takes its name from the APL primitive.

```
(iiota 5) => (0 1 2 3 4)
(iiota 5 0 -0.1) => (0 -0.1 -0.2 -0.3 -0.4)
```

#### **Predicates**

```
(proper-ilist? x) \rightarrow boolean
(ilist? x) \rightarrow boolean
```

ilist library procedure ilist library procedure

These identifiers are bound either to the same procedure, or to procedures of equivalent behavior. In either case, true is returned iff x is a proper ilist—a ()-terminated ilist.

More carefully: The empty list is a proper ilist. An ipair whose icdr is a proper ilist is also a proper ilist. Everything else is a dotted ilist. This includes non-ipair, non-() values (e.g. symbols, numbers, mutable pairs), which are considered to be dotted ilists of length 0.

```
(dotted-ilist? x) \rightarrow boolean
```

ilist library procedure

True if x is a finite, non-nil-terminated ilist. That is, there exists an  $n \ge 0$  such that  $icdr^n(x)$  is neither an ipair nor (). This includes non-ipair, non-() values (e.g. symbols, numbers), which are considered to be dotted ilists of length 0.

```
(dotted-ilist? x) = (not (proper-ilist? x))
```

```
(ipair? object) \rightarrow boolean
```

ilist library procedure

Returns #t if object is an ipair; otherwise, #f.

```
(ipair? (ipair 'a 'b)) => #t
(ipair? (iq a b c)) => #t
(ipair? (cons 1 2)) => #f
(ipair? '()) => #f
(ipair? '#(a b)) => #f
(ipair? 7) => #f
(ipair? 'a) => #f
```

```
(null-ilist? ilist) \rightarrow boolean
```

ilist library procedure

Ilist is a proper ilist. This procedure returns true if the argument is the empty list (), and #f otherwise. It is an error to pass this procedure a value which is not a proper ilist. This procedure is recommended as the termination condition for ilist-processing procedures that are not defined on dotted ilists.

```
(not-ipair? x) \rightarrow boolean
```

ilist library procedure

```
(lambda (x) (not (ipair? x)))
```

Provided as a procedure as it can be useful as the termination condition for ilist-processing procedures that wish to handle all ilists, both proper and dotted.

 $(el) \rightarrow =$  ilist<sub>1</sub> ...proceduren

ilist library t

Determines ilist equality, given an element-equality procedure. Proper ilist A equals proper ilist B if they are of the same length, and their corresponding elements are equal, as determined by elt=. If the element-comparison procedure's first

In the n-ary case, every ilist<sub>i</sub> is compared to ilist<sub>i+1</sub> (as opposed, for example, to comparing ilist<sub>1</sub> to ilist<sub>i</sub>, for i>1). If there are no ilist arguments at all, ilist= simply returns true.

It is an error to apply ilist= to anything except proper ilists. It cannot reasonably be extended to dotted ilists, as it provides no way to specify an equality procedure for comparing the ilist terminators.

Note that the dynamic order in which the elt= procedure is applied to pairs of elements is not specified. For example, if ilist= is applied to three ilists, A, B, and C, it may first completely compare A to B, then compare B to C, or it may compare the first elements of A and B, then the first elements of B and C, then the second elements of A and B, and so forth.

The equality procedure must be consistent with eq?. That is, it must be the case that

```
(eq? x y) => (elt= x y).
```

Note that this implies that two ilists which are eq? are always ilist=, as well; implementations may exploit this fact to "short-cut" the element-by-element comparisons.

```
(ilist= eq?) => #t ; Trivial cases
(ilist= eq? (iq a)) => #t
```

#### **Selectors**

```
\begin{array}{ll} (\text{icar } \textit{ipair}) \rightarrow \textit{value} & \text{ilist library procedure} \\ (\text{icdr } \textit{ipair}) \rightarrow \textit{value} & \text{ilist library procedure} \end{array}
```

These procedures return the contents of the icar and icdr field of their argument, respectively. Note that it is an error to apply them to the empty ilist.

```
(icar (iq a b c))
                                       (icdr (iq a b c))
                                                                  (b c)
                             a
(icar (iq (a) b c d))
                                        (icdr (iq (a) b c d)) \Rightarrow (b c d)
                         =>
                             (a)
(icar (ipair 1 2))
                                        (icdr (ipair 1 2))
                         =>
                             1
                                                               =>
                                                                   2
(icar '())
                             *error* (icdr '())
                         =>
                                                              => *error*
```

```
\begin{array}{ll} (\text{icaar } ipair) \rightarrow value & \text{ilist library procedure} \\ (\text{icadr } ipair) \rightarrow value & \text{ilist library procedure} \\ \vdots & \\ (\text{icdddar } ipair) \rightarrow value & \text{ilist library procedure} \\ (\text{icddddr } ipair) \rightarrow value & \text{ilist library procedure} \\ \end{array}
```

These procedures are compositions of icar and icdr, where for example icaddr could be defined by

```
(define icaddr (lambda (x) (icar (icdr (icdr x))))).
```

Arbitrary compositions, up to four deep, are provided. There are twenty-eight of these procedures in all.

```
(ilist-ref ilist i) \rightarrow value ilist library procedure
```

Returns the  $i^{th}$  element of ilist. (This is the same as the icar of (idrop ilist i).) It is an error if i >= n, where n is the length of ilist.

```
(ilist-ref (iq a b c d) 2) \Rightarrow c
```

```
(ifirstipair) \rightarrow object
(isecondipair) \rightarrow object
(ithirdipair) \rightarrow object
(ifourthipair) \rightarrow object
(ififthipair) \rightarrow object
(isixthipair) \rightarrow object
(iseventhinair) \rightarrow object
(ieighthipair) \rightarrow object
(ininthipair) \rightarrow object
(itenthipair) \rightarrow object
```

Synonyms for car, cadr, caddr, ...

```
(ithird '(a b c d e)) \Rightarrow c
```

```
(icar+icdr ipair) \rightarrow x y
```

The fundamental ipair deconstructor:

```
(lambda (p) (values (icar p) (icdr p)))
```

This can, of course, be implemented more efficiently by a compiler.

```
(itake x \ i) \rightarrow ilist
(idrop x \ i) \rightarrow object
(ilist-tail x i) \rightarrow object
```

itake returns the first i elements of ilist x.

idrop returns all but the first i elements of ilist x.

ilist-tail is either the same procedure as idrop or else a procedure with the same behavior.

```
(itake (iq a b c d e) 2) => (a b)
(idrop (iq a b c d e) 2) \Rightarrow (c d e)
```

x may be any value—a proper or dotted ilist:

```
(itake (ipair 1 (ipair 2 (ipair 3 'd)))
(idrop (ipair 1 (ipair 2 (ipair 3 'd))) 2) => (3 . d)
(itake (ipair 1 (ipair 2 (ipair 3 'd))) 3) => (1 2 3)
(idrop (ipair 1 (ipair 2 (ipair 3 'd))) 3) => d
```

For a legal i, itake and idrop partition the ilist in a manner which can be inverted with iappend:

```
(iappend (itake x i) (idrop x i)) = x
```

idrop is exactly equivalent to performing i icdr operations on x; the returned value shares a common tail with x.

```
(itake-right dilist\ i) \rightarrow object
(idrop-right dilist i) \rightarrow ilist
```

ilist library procedure ilist library procedure

itake-right returns the last i elements of dilist.

idrop-right returns all but the last i elements of dilist.

```
(itake-right (iq a b c d e) 2) \Rightarrow (d e)
(idrop-right (iq a b c d e) 2) => (a b c)
```

The returned ilist may share a common tail with the argument ilist.

dilist may be any ilist, either proper or dotted:

ilist library procedure ilist library procedure

ilist library procedure

ilist library procedure

ilist library procedure

ilist library procedure

```
(itake-right (iq ipair 1 (ipair 2 (ipair 3 'd))) 2) => (2 3 . d)
(idrop-right (ipair 1 (ipair 2 (ipair 3 'd))) 2) => (1)
(itake-right (ipair 1 (ipair 2 (ipair 3 'd))) 0) => d
(idrop-right (ipair 1 (ipair 2 (ipair 3 'd))) 0) => (1 2 3)
```

For a legal i, itake-right and idrop-right partition the ilist in a manner which can be inverted with iappend:

```
(iappend (itake dilist i) (idrop dilist i)) = dilist
```

itake-right's return value is guaranteed to share a common tail with dilist.

```
(isplit-at x i) \rightarrow ilist object
```

ilist library procedure

isplit-at splits the ilist x at index i, returning an ilist of the first i elements, and the remaining tail. It is equivalent to (values (itake x i) (idrop x i))

```
(ilast ipair) \rightarrow object
(last-ipair ipair) \rightarrow ipair
```

ilist library procedure

ilist library procedure

Returns the last element of the non-empty, possibly dotted, ilist ipair. last-ipair returns the last ipair in the non-empty ilist pair.

```
(ilast (iq a b c)) => c
(last-ipair (iq a b c)) => (c)
```

Miscellaneous: length, append, concatenate, reverse, zip & count

 $(ilength ilist) \rightarrow integer$ 

ilist library procedure

Returns the length of its argument. It is an error to pass a value to ilength which is not a proper ilist (()-terminated). The length of a proper ilist is a non-negative integer n such that icdr applied n times to the ilist produces the empty list.

```
(iappend ilist_1 ...) \rightarrow ilist
```

ilist library procedure

Returns an ilist consisting of the elements of ilist<sub>1</sub> followed by the elements of the other ilist parameters.

```
(iappend (iq x) (iq y)) => (x y)
(iappend (iq a) (iq b c d)) => (a b c d)
(iappend (iq a (b)) (iq (c))) => (a (b) (c))
```

The resulting ilist is always newly allocated, except that it shares structure with the final ilist<sub>i</sub> argument. This last argument may be any value at all; an improper ilist results if it is not a proper ilist. All other arguments must be proper ilists.

```
(iappend (iq a b) (ipair 'c 'd)) => (a b c . d)
(iappend '() 'a) => a
(iappend (iq x y)) => (x y)
(iappend) => ()
```

(iconcatenate ilist-of-ilists)  $\rightarrow value$ 

ilist library procedure

Appends the elements of its argument together. That is, iconcatenate returns

```
(iapply iappend ilist-of-ilists)
```

or, equivalently,

```
(ireduce-right iappend '() ilist-of-ilists)
```

Note that some Scheme implementations do not support passing more than a certain number (e.g., 64) of arguments to an n-ary procedure. In these implementations, the (iapply iappend ...) idiom would fail when applied to long lists, but iconcatenate would continue to function properly.

As with iappend, the last element of the input list may be any value at all.

```
(ireverse ilist) \rightarrow ilist
                                                                                                                             ilist library procedure
```

Returns a newly allocated ilist consisting of the elements of ilist in reverse order.

```
(ireverse (iq a b c)) \Rightarrow (c b a)
(ireverse (iq a (b c) d (e (f))))
    => ((e (f)) d (b c) a)
```

```
(iappend-reverse rev-head tail) \rightarrow ilist
```

ilist library procedure

iappend-reverse returns (iappend (ireverse rev-head) tail). It is provided because it is a common operation—a common list-processing style calls for this exact operation to transfer values accumulated in reverse order onto the front of another ilist, and because the implementation is significantly more efficient than the simple composition it replaces. (But note that this pattern of iterative computation followed by a reverse can frequently be rewritten as a recursion, dispensing with the reverse and iappend-reverse steps, and shifting temporary, intermediate storage from the heap to the stack, which is typically a win for reasons of cache locality and eager storage reclamation.)

```
(izip ilist_1 ilist_2 ...) \rightarrow ilist
(lambda ilists (iapply imap ilist ilists))
```

ilist library procedure

If izip is passed n ilists, it returns an ilist as long as the shortest of these ilists, each element of which is an n-element ilist comprised of the corresponding elements from the parameter ilists.

```
(izip (iq one two three)
      (iq 1 2 3)
      (iq odd even odd even odd even))
     => ((one 1 odd) (two 2 even) (three 3 odd))
(izip (iq 1 2 3)) \Rightarrow ((1) (2) (3))
(iunzip1 ilist) \rightarrow ilist
                                                                                                            ilist library procedure
(iunzip2 ilist) \rightarrow ilist ilist
                                                                                                            ilist library procedure
(iunzip3 ilist) \rightarrow ilist ilist ilist
                                                                                                            ilist library procedure
(iunzip4 ilist) \rightarrow ilist ilist ilist ilist
                                                                                                            ilist library procedure
(iunzip5 ilist) \rightarrow ilist ilist ilist ilistilist
                                                                                                            ilist library procedure
```

iunzip1 takes an ilist of ilists, where every ilist must contain at least one element, and returns an ilist containing the initial element of each such ilist. That is, it returns (imap icar ilists). iunzip2 takes an ilist of ilists, where every ilist must contain at least two elements, and returns two values: an ilist of the first elements, and an ilist of the second elements. iunzip3 does the same for the first three elements of the ilists, and so forth.

```
(iunzip2 (iq (1 one) (2 two) (3 three))) =>
    (1 \ 2 \ 3)
    (one two three)
```

```
(icount pred\ ilist_1\ ilist_2\ ...) \rightarrow integer
```

ilist library procedure

pred is a procedure taking as many arguments as there are ilists and returning a single value. It is applied element-wise to the elements of the ilists, and a count is tallied of the number of elements that produce a true value. This count is returned. count is "iterative" in that it is guaranteed to apply pred to the ilist elements in a left-to-right order. The counting stops when the shortest ilist expires.

```
(count even? (iq 3 1 4 1 5 9 2 5 6)) \Rightarrow 3
(count < (iq 1 2 4 8) (iq 2 4 6 8 10 12 14 16)) => 3
```

```
(ifold kons \ knil \ ilist_1 \ ilist_2 \ ...) \rightarrow value
                                                                                              ilist library procedure
The fundamental ilist iterator.
First, consider the single ilist-parameter case. If ilist_1 = (e_1 \ e_2 \ ... e_n), then this procedure returns
(kons en ... (kons e2 (kons e1 knil)) ...)
That is, it obeys the (tail) recursion
(ifold kons knil lis) = (ifold kons (kons (icar lis) knil) (icdr lis))
(ifold kons knil '()) = knil
Examples:
(ifold + 0 lis)
                              ; Add up the elements of LIS.
(ifold ipair '() lis)
                                ; Reverse LIS.
(ifold ipair tail rev-head); See APPEND-REVERSE.
;; How many symbols in LIS?
(ifold (lambda (x count) (if (symbol? x) (+ count 1) count))
       lis)
;; Length of the longest string in LIS:
(ifold (lambda (s max-len) (max max-len (string-length s)))
       0
       lis)
If n ilist arguments are provided, then the kons function must take n+1 parameters: one element from each ilist, and
the "seed" or fold state, which is initially knil. The fold operation terminates when the shortest ilist runs out of values:
(ifold ipair* '() (iq a b c) (iq 1 2 3 4 5)) => (c 3 b 2 a 1)
(ifold-right kons knil ilist<sub>1</sub> ilist<sub>2</sub> ...) \rightarrow value
                                                                                              ilist library procedure
The fundamental ilist recursion operator.
First, consider the single ilist-parameter case. If ilist_1 = (e1 \ e2 \ ... \ en), then this procedure returns
 (kons e1 (kons e2 ... (kons en knil)))
That is, it obeys the recursion
(ifold-right kons knil lis) = (kons (icar lis) (ifold-right kons knil (icdr lis)))
(ifold-right kons knil '()) = knil
Examples:
(ifold-right ipair '() lis)
                                       ; Copy LIS.
;; Filter the even numbers out of LIS.
(ifold-right (lambda (x l) (if (even? x) (ipair x l) l)) '() lis))
If n ilist arguments are provided, then the kons procedure must take n+1 parameters: one element from each ilist, and
the "seed" or fold state, which is initially knil. The fold operation terminates when the shortest ilist runs out of values:
(ifold-right ipair* '() (iq a b c) (iq 1 2 3 4 5)) => (a 1 b 2 c 3)
```

```
(ipair-fold kons \ knil \ ilist_1 \ ilist_2 \ ...) \rightarrow value
```

ilist library procedure

ilist library procedure

Analogous to fold, but kons is applied to successive sub-ilists of the ilists, rather than successive elements—that is, kons is applied to the ipairs making up the lists, giving this (tail) recursion:

```
(ipair-fold kons knil lis) = (let ((tail (icdr lis)))
                                   (ipair-fold kons (kons lis knil) tail))
(ipair-fold kons knil '()) = knil
Example:
(ipair-fold ipair '() (iq a b c)) \Rightarrow ((c) (b c) (a b c))
(ipair-fold-right kons knil ilist<sub>1</sub> ilist<sub>2</sub> ...) \rightarrow value
                                                                                                ilist library procedure
Holds the same relationship with ifold-right that ipair-fold holds with ifold. Obeys the recursion
(ipair-fold-right kons knil lis) =
     (kons lis (ipair-fold-right kons knil (icdr lis)))
(ipair-fold-right kons knil '()) = knil
Example:
(ipair-fold-right ipair '() (iq a b c)) => ((a b c) (b c) (c))
(ireduce f ridentity ilist) \rightarrow value
                                                                                                ilist library procedure
ireduce is a variant of ifold.
ridentity should be a "right identity" of the procedure f—that is, for any value x acceptable to f,
(f \times ridentity) = x
ireduce has the following definition:
If ilist = (), return ridentity;
Otherwise, return (ifold f (icar ilist) (icdr ilist)).
...in other words, we compute (ifold f ridentity ilist).
```

Note that ridentity is used *only* in the empty-list case. You typically use ireduce when applying f is expensive and you'd like to avoid the extra application incurred when ifold applies f to the head of ilist and the identity value, redundantly producing the same value passed in to f. For example, if f involves searching a file directory or performing a database query, this can be significant. In general, however, ifold is useful in many contexts where ireduce is not (consider the examples given in the ifold definition—only one of the five folds uses a function with a right identity. The other four may not be performed with ireduce).

```
;; take the max of an ilist of non-negative integers.
(ireduce max 0 nums); i.e., (iapply max 0 nums)
(ireduce-right f ridentity ilist) \rightarrow value
ireduce-right is the fold-right variant of ireduce. It obeys the following definition:
(ireduce-right f ridentity '()) = ridentity
(ireduce-right f ridentity (iq e1)) = (f e1 ridentity) = e1
(ireduce-right f ridentity (iq e1 e2 ...)) =
    (f e1 (ireduce f ridentity (e2 ...)))
...in other words, we compute (ifold-right f ridentity ilist).
;; Append a bunch of ilists together.
;; I.e., (iapply iappend ilist-of-ilists)
(ireduce-right iappend '() ilist-of-ilists)
```

(iunfold  $p \ f \ g \ seed \ [tail-gen]) \rightarrow ilist$ 

iunfold is best described by its basic recursion:

```
(iunfold p f g seed) =
    (if (p seed) (tail-gen seed)
        (ipair (f seed)
              (iunfold p f g (g seed))))
```

- **p** Determines when to stop unfolding.
- f Maps each seed value to the corresponding ilist element.
- g Maps each seed value to next seed value.

**seed** The "state" value for the unfold.

tail-gen Creates the tail of the ilist; defaults to (lambda (x) '())

In other words, we use g to generate a sequence of seed values

```
seed, g(seed), g<sup>2</sup>(seed), g<sup>3</sup>(seed), ...
```

These seed values are mapped to ilist elements by f, producing the elements of the result ilist in a left-to-right order. P says when to stop.

iunfold is the fundamental recursive ilist constructor, just as ifold-right is the fundamental recursive ilist consumer. While iunfold may seem a bit abstract to novice functional programmers, it can be used in a number of ways:

```
;; Ilist of squares: 1^2 ... 10^2
(iunfold (lambda (x) (> x 10))
        (lambda (x) (* x x))
   (lambda (x) (+ x 1))
   1)
(iunfold null-ilist? icar icdr lis); Copy a proper ilist.
;; Read current input port into an ilist of values.
(iunfold eof-object? values (lambda (x) (read)) (read))
;; Copy a possibly non-proper ilist:
(iunfold not-ipair? icar icdr lis
              values)
;; Append HEAD onto TAIL:
(iunfold null-ilist? icar icdr head
              (lambda (x) tail))
```

Interested functional programmers may enjoy noting that ifold-right and iunfold are in some sense inverses. That is, given operations knull?, kar, kdr, kons, and knil satisfying

```
(kons (kar x) (kdr x)) = x and (knull? knil) = #t
then
(ifold-right kons knil (iunfold knull? kar kdr x)) = x
and
(iunfold knull? kar kdr (ifold-right kons knil x)) = x.
```

This combinator sometimes is called an "anamorphism;" when an explicit tail-gen procedure is supplied, it is called an "apomorphism."

```
(iunfold-right p \ f \ g \ seed \ tail) \rightarrow ilist
(iunfold-right p \ f \ g \ seed) \rightarrow ilist
iunfold-right constructs an ilist with the following loop:
```

ilist library procedure ilist library procedure

ilist library procedure

- **p** Determines when to stop unfolding.
- f Maps each seed value to the corresponding ilist element.
- g Maps each seed value to next seed value.

**seed** The "state" value for the unfold.

tail ilist terminator; defaults to '().

In other words, we use g to generate a sequence of seed values

```
seed, g(seed), g^2(seed), g^3(seed), ...
```

These seed values are mapped to ilist elements by f, producing the elements of the result ilist in a right-to-left order. P says when to stop.

iunfold-right is the fundamental iterative ilist constructor, just as ifold is the fundamental iterative ilist consumer. While iunfold-right may seem a bit abstract to novice functional programmers, it can be used in a number of ways:

Interested functional programmers may enjoy noting that ifold and iunfold-right are in some sense inverses. That is, given operations knull?, kar, kdr, kons, and knil satisfying

```
(kons (kar x) (kdr x)) = x and (knull? knil) = #t then (ifold kons knil (iunfold-right knull? kar kdr x)) = x and
```

(iunfold-right knull? kar kdr (ifold kons knil x)) = x.

(iunfold-right null-ilist? icar icdr rev-head tail)

This combinator presumably has some pretentious mathematical name; interested readers are invited to communicate it to the author.

```
(imap proc ilist_1 ilist_2 ...) \rightarrow ilist
```

ilist library procedure

proc is a procedure taking as many arguments as there are ilist arguments and returning a single value. imap applies proc element-wise to the elements of the ilists and returns an ilist of the results, in order. The dynamic order in which proc is applied to the elements of the ilists is unspecified.

(ifor-each proc ilist<sub>1</sub> ilist<sub>2</sub> ...)  $\rightarrow$  unspecified

ilist library procedure

ilist library procedure

The arguments to ifor-each are like the arguments to imap, but ifor-each calls proc for its side effects rather than for its values. Unlike imap, ifor-each is guaranteed to call proc on the elements of the ilists in order from the first element(s) to the last, and the value returned by ifor-each is unspecified.

Map f over the elements of the ilists, just as in the imap function. However, the results of the applications are appended together (using iappend) to make the final result.

The dynamic order in which the various applications of f are made is not specified.

Example:

```
(iappend-map (lambda (x) (ilist x (- x))) (iq 1 3 8))
=> (1 -1 3 -3 8 -8)
```

```
(imap-in-order f ilist_1 ilist_2 ...) \rightarrow ilist_1
```

ilist library procedure

A variant of the imap procedure that guarantees to apply f across the elements of the ilist<sub>i</sub> arguments in a left-to-right order. This is useful for mapping procedures that both have side effects and return useful values.

```
(ipair-for-each filist_1 ilist_2 ...) \rightarrow unspecific
```

ilist library procedure

Like ifor-each, but f is applied to successive sub-ilists of the argument ilists. That is, f is applied to the cells of the ilists, rather than the ilists' elements. These applications occur in left-to-right order.

```
(ipair-for-each (lambda (ipair) (display ipair) (newline)) (iq a b c)) ==>
  (a b c)
  (b c)
  (c)
```

```
(ifilter-map f ilist_1 ilist_2 ...) \rightarrow ilist
```

ilist library procedure

Like imap, but only true values are saved.

```
(ifilter-map (lambda (x) (and (number? x) (* x x))) (iq a 1 b 3 c 7))
=> (1 9 49)
```

The dynamic order in which the various applications of f are made is not specified.

# Filtering and partitioning

```
(ifilter pred\ ilist) \rightarrow ilist
```

ilist library procedure

Return all the elements of ilist that satisfy predicate pred. The ilist is not disordered—elements that appear in the result ilist occur in the same order as they occur in the argument ilist. The returned ilist may share a common tail with the argument ilist. The dynamic order in which the various applications of pred are made is not specified.

```
(ifilter even? (iq 0 7 8 8 43 -4)) \Rightarrow (0 8 8 -4)
```

```
(ipartition pred\ ilist) \rightarrow ilist\ ilist
```

ilist library procedure

Partitions the elements of ilist with predicate pred, and returns two values: the ilist of in-elements and the ilist of outelements. The ilist is not disordered—elements occur in the result ilists in the same order as they occur in the argument ilist. The dynamic order in which the various applications of pred are made is not specified. One of the returned ilists may share a common tail with the argument ilist.

```
(ipartition symbol? (iq one 2 3 four five 6)) =>
   (one four five)
   (236)
```

(iremove  $pred\ ilist$ )  $\rightarrow ilist$ 

ilist library procedure

Returns ilist without the elements that satisfy predicate pred:

```
(lambda (pred ilist) (ifilter (lambda (x) (not (pred x))) ilist))
```

The ilist is not disordered—elements that appear in the result ilist occur in the same order as they occur in the argument ilist. The returned ilist may share a common tail with the argument ilist. The dynamic order in which the various applications of pred are made is not specified.

```
(iremove even? (iq 0 7 8 8 43 -4)) \Rightarrow (7 43)
```

# Searching

The following procedures all search ilists for a leftmost element satisfying some criteria. This means they do not always examine the entire ilist; thus, there is no efficient way for them to reliably detect and signal an error when passed a dotted ilist. Here are the general rules describing how these procedures work when applied to different kinds of ilists:

**Proper ilists:** The standard, canonical behavior happens in this case.

**Dotted ilists:** It is an error to pass these procedures a dotted ilist that does not contain an element satisfying the search criteria. That is, it is an error if the procedure has to search all the way to the end of the dotted ilist. However, this SRFI does not specify anything at all about the behavior of these procedures when passed a dotted ilist containing an element satisfying the search criteria. It may finish successfully, signal an error, or perform some third action. Different implementations may provide different functionality in this case; code which is compliant with this SRFI may not rely on any particular behavior. Future SRFIs may refine this SRFI to define specific behavior in this case.

In brief, compliant code may not pass a dotted ilist argument to these procedures.

Here are some examples, using the ifind and iany procedures as canonical representatives:

```
;; Proper ilist - success
(ifind even? (iq 1 2 3))
                           => 2
                           => #t
(iany even? (iq 1 2 3))
;; proper ilist - failure
(ifind even? (iq 1 7 3))
                           => #f
(iany even? (iq 1 7 3))
                           => #f
;; Failure is error on a dotted ilist.
(ifind even? (ipair 1 (ipair 3 'x)))
                                       => error
(iany even? (ipair 1 (ipair 3 'x)))
                                       => error
;; The dotted ilist contains an element satisfying the search.
;; This case is not specified - it could be success, an error,
;; or some third possibility.
(ifind even? (ipair 1 (ipair 2 'x)))
                                       => error/undefined
(iany even? (ipair 1 (ipair 2 'x)))
                                     => error/undefined; success, error or other.
```

(ifind  $pred\ ilist$ )  $\rightarrow value$ 

ilist library procedure

Return the first element of ilist that satisfies predicate pred; #f if no element does.

```
(ifind even? (iq 3 1 4 1 5 9)) \Rightarrow 4
```

Note that ifind has an ambiguity in its lookup semantics—if ifind returns #f, you cannot tell (in general) if it found a #f element that satisfied pred, or if it did not find any element at all. In many situations, this ambiguity cannot arise—either the ilist being searched is known not to contain any #f elements, or the ilist is guaranteed to have an element satisfying pred. However, in cases where this ambiguity can arise, you should use ifind—tail instead of ifind—ifind—tail has no such ambiguity:

(ifind-tail  $pred\ ilist$ )  $\rightarrow ipair\ or\ \#f$ 

ilist library procedure

Return the first ipair of ilist whose icar satisfies pred. If no ipair does, return #f.

ifind-tail can be viewed as a general-predicate variant of the imember function.

#### Examples:

```
(ifind-tail even? (iq 3 1 37 -8 -5 0 0)) => (-8 -5 0 0)
(ifind-tail even? (iq 3 1 37 -5)) => #f

;; IMEMBER X LIS:
(ifind-tail (lambda (elt) (equal? x elt)) lis)
```

Ifind-tail is essentially idrop-while, where the sense of the predicate is inverted: Ifind-tail searches until it finds an element satisfying the predicate; idrop-while searches until it finds an element that *doesn't* satisfy the predicate.

(itake-while  $pred\ ilist$ )  $\rightarrow ilist$ 

ilist library procedure

Returns the longest initial prefix of ilist whose elements all satisfy the predicate pred.

```
(itake-while even? (iq 2 18 3 10 22 9)) \Rightarrow (2 18)
```

(idrop-while  $pred\ ilist$ )  $\rightarrow ilist$ 

ilist library procedure

idrops the longest initial prefix of ilist whose elements all satisfy the predicate pred, and returns the rest of the ilist.

 $(idrop-while even? (iq 2 18 3 10 22 9)) \Rightarrow (3 10 22 9)$ 

```
(ispan pred ilist) \rightarrow ilist ilist
(ibreak pred\ ilist) \rightarrow ilist\ ilist
```

ilist library procedure ilist library procedure

ispan splits the ilist into the longest initial prefix whose elements all satisfy pred, and the remaining tail. ibreak inverts the sense of the predicate: the tail commences with the first element of the input ilist that satisfies the predicate.

In other words: ispan finds the initial span of elements satisfying pred, and ibreak breaks the ilist at the first element satisfying pred.

ispan is equivalent to

```
(values (itake-while pred ilist)
        (idrop-while pred ilist))
(ispan even? (iq 2 18 3 10 22 9)) =>
 (218)
 (3 10 22 9)
(ibreak even? (iq 3 1 4 1 5 9)) =>
 (3\ 1)
 (4159)
```

(iany pred  $ilist_1$   $ilist_2$  ...)  $\rightarrow value$ 

ilist library procedure

Applies the predicate across the ilists, returning true if the predicate returns true on any application.

If there are n ilist arguments ilist<sub>1</sub> ... ilist<sub>n</sub>, then pred must be a procedure taking n arguments and returning a boolean result.

iany applies pred to the first elements of the ilist<sub>i</sub> parameters. If this application returns a true value, iany immediately returns that value. Otherwise, it iterates, applying pred to the second elements of the ilist, parameters, then the third, and so forth. The iteration stops when a true value is produced or one of the ilists runs out of values; in the latter case, iany returns #f. The application of pred to the last element of the ilists is a tail call.

Note the difference between ifind and iany—ifind returns the element that satisfied the predicate; iany returns the true value that the predicate produced.

Like ievery, iany's name does not end with a question mark—this is to indicate that it does not return a simple boolean (#t or #f), but a general value.

```
(iany integer? (iq a 3 b 2.7)) => #t
(iany integer? (iq a 3.1 b 2.7)) \Rightarrow #f
(iany < (iq 3 1 4 1 5)
        (iq 2 7 1 8 2)) \Rightarrow #t
```

(ievery  $pred\ ilist_1\ ilist_2\ ...) \rightarrow value$ 

ilist library procedure

Applies the predicate across the ilists, returning true if the predicate returns true on every application.

If there are n ilist arguments ilist<sub>1</sub> ...ilist<sub>n</sub>, then pred must be a procedure taking n arguments and returning a boolean result.

ievery applies pred to the first elements of the ilist<sub>i</sub> parameters. If this application returns #f, ievery immediately returns #f. Otherwise, it iterates, applying pred to the second elements of the ilist; parameters, then the third, and so forth. The iteration stops when a #f value is produced or one of the ilists runs out of values. In the latter case, ievery returns the true value produced by its final application of pred. The application of pred to the last element of the ilists is a tail call.

If one of the ilist $_i$  has no elements, ievery simply returns #t.

Like iany, ievery's name does not end with a question mark—this is to indicate that it does not return a simple boolean (#t or #f), but a general value.

```
(ilist-index pred\ ilist_1\ ilist_2\ ...) \rightarrow integer\ or\ \#f
```

ilist library procedure

Return the index of the leftmost element that satisfies pred.

If there are n ilist arguments ilist<sub>1</sub> ...ilist<sub>n</sub>, then pred must be a function taking n arguments and returning a boolean

ilist-index applies pred to the first elements of the ilist, parameters. If this application returns true, ilist-index immediately returns zero. Otherwise, it iterates, applying pred to the second elements of the ilisti parameters, then the third, and so forth. When it finds a tuple of ilist elements that cause pred to return true, it stops and returns the zero-based index of that position in the ilists.

The iteration stops when one of the ilists runs out of values; in this case, ilist-index returns #f.

```
(ilist-index even? (iq 3 1 4 1 5 9)) => 2
(ilist-index < (iq 3 1 4 1 5 9 2 5 6) (iq 2 7 1 8 2)) => 1
(ilist-index = (iq 3 1 4 1 5 9 2 5 6) (iq 2 7 1 8 2)) => #f
```

```
(imember x ilist =) \rightarrow ilist
                                                                                                                             ilist library procedure
(imember x ilist) \rightarrow ilist
                                                                                                                             ilist library procedure
(imemq x ilist) \rightarrow ilist
                                                                                                                             ilist library procedure
(imemv x ilist) \rightarrow ilist
                                                                                                                             ilist library procedure
```

These procedures return the first sub-ilist of ilist whose icar is x, where the sub-ilists of ilist are the non-empty ilists returned by (idrop ilist i) for i less than the length of ilist. If x does not occur in ilist, then #f is returned. imemq uses eq? to compare x with the elements of ilist, while imemv uses eqv?, and imember uses equal?.

```
(a b c)
(imemq 'a (iq a b c))
(imemq 'b (iq a b c))
                                     (b c)
(imemq 'a (iq b c d))
                                     #f
(imemq (list 'a)
        (ilist 'b '(a) 'c))
(imember (list 'a)
        (ilist 'b '(a) 'c)))
                                     ((a) c)
                                 =>
(imemq 101 (iq 100 101 102))
                                 =>
                                     *unspecified*
(imemv 101 (iq 100 101 102))
                                     (101 102)
                                 =>
```

The comparison procedure is used to compare the elements  $e_i$  of ilist to the key x in this way:

```
(= x ei)
               ; ilist is (E1 ... En)
```

That is, the first argument is always x, and the second argument is one of the ilist elements. Thus one can reliably find the first element of ilist that is greater than five with (imember 5 ilist <)

Note that fully general ilist searching may be performed with the ifind-tail and ifind procedures, e.q.

```
(ifind-tail even? ilist); Find the first elt with an even key.
```

#### Deletion

```
(ideletex ilist /=/) \rightarrow ilist
```

ilist library procedure

idelete uses the comparison procedure =, which defaults to equal?, to find all elements of ilist that are equal to x, and deletes them from ilist. The dynamic order in which the various applications of = are made is not specified.

The ilist is not disordered—elements that appear in the result ilist occur in the same order as they occur in the argument ilist. The result may share a common tail with the argument ilist.

Note that fully general element deletion can be performed with the iremove procedures, e.g.:

```
;; idelete all the even elements from LIS:
(iremove even? lis)
```

The comparison procedure is used in this way: (= x ei). That is, x is always the first argument, and an ilist element is always the second argument. The comparison procedure will be used to compare each element of ilist exactly once; the order in which it is applied to the various e<sub>i</sub> is not specified. Thus, one can reliably remove all the numbers greater than five from an ilist with (idelete 5 ilist <)

```
(idelete-duplicates ilist = ) \rightarrow ilist
                                                                                                                      ilist library procedure
(idelete-duplicates ilist) \rightarrow ilist
                                                                                                                      ilist library procedure
```

idelete-duplicates removes duplicate elements from the ilist argument. If there are multiple equal elements in the argument ilist, the result ilist only contains the first or leftmost of these elements in the result. The order of these surviving elements is the same as in the original ilist—idelete-duplicates does not disorder the ilist (hence it is useful for "cleaning up" immutable association lists).

The = parameter is used to compare the elements of the ilist; it defaults to equal?. If x comes before y in ilist, then the comparison is performed (= x y). The comparison procedure will be used to compare each pair of elements in ilist no more than once; the order in which it is applied to the various pairs is not specified.

Implementations of idelete-duplicates are allowed to share common tails between argument and result ilists—for example, if the ilist argument contains only unique elements, it may simply return exactly this ilist.

Be aware that, in general, idelete-duplicates runs in time  $O(n^2)$  for n-element ilists. Uniquifying long ilists can be accomplished in  $O(n \lg n)$  time by sorting the ilist to bring equal elements together, then using a linear-time algorithm to remove equal elements. Alternatively, one can use algorithms based on element-marking, with linear-time results.

```
(idelete-duplicates (iq a b a c a b c z)) => (a b c z)
;; Clean up an ialist:
(idelete-duplicates (iq (a . 3) (b . 7) (a . 9) (c . 1))
                   (lambda (x y) (eq? (icar x) (icar y))))
   => ((a . 3) (b . 7) (c . 1))
```

#### Immutable association lists

An "immutable association list" (or "ialist") is an ilist of ipairs. The icar of each ipair contains a key value, and the icdr contains the associated data value. They can be used to construct simple look-up tables in Scheme. Note that ialists are probably inappropriate for performance-critical use on large data; in these cases, immutable maps or some other alternative should be employed.

```
(iassoc key\ ialist\ =) \rightarrow ipair\ or\ \#f
                                                                                                                            ilist library procedure
(iassoc key\ ialist) \rightarrow ipair\ or\ \#f
                                                                                                                            ilist library procedure
(iassq key\ ialist) \rightarrow ipair\ or\ \#f
                                                                                                                            ilist library procedure
(iassv key\ ialist) \rightarrow ipair\ or\ \#f
                                                                                                                            ilist library procedure
```

ialist must be an immutable association list—an ilist of ipairs. These procedures find the first ipair in ialist whose icar field is key, and returns that ipair. If no ipair in ialist has key as its icar, then #f is returned. iassq uses eq? to compare key with the icar fields of the ipairs in ialist, while iassv uses eqv? and iassoc uses equal?.

```
(define e (iq (a 1) (b 2) (c 3)))
(iassq 'a e)
                                                  (a 1)
(iassq 'b e)
                                                 (b 2)
                                             =>
(iassq 'd e)
                                                 #f
(iassq (ilist 'a) (iq ((a)) ((b)) ((c))))
(iassoc '(a) (ilist '((a)) '((b)) '((c)))) \Rightarrow ((a))
(iassq 5 (iq (2 3) (5 7) (11 13)))
                                             *unspecified*
                                         =>
(iassv 5 (iq (2 3) (5 7) (11 13)))
                                             (57)
```

The comparison procedure is used to compare the elements  $e_i$  of ilist to the key parameter in this way:

```
(= key (icar ei)); ilist is (E1 ... En)
```

That is, the first argument is always key, and the second argument is one of the ilist elements. Thus one can reliably find the first entry of ialist whose key is greater than five with (iassoc 5 ialist <)

Note that fully general islist searching may be performed with the ifind-tail and ifind procedures, e.g.

```
;; Look up the first association in ialist with an even key: (ifind (lambda (a) (even? (icar a))) ialist)
```

```
(ialist-cons key\ datum\ ialist) \rightarrow ialist
```

ilist library procedure

```
(lambda (key datum ialist) (ipair (ipair key datum) ialist))
```

Construct a new ialist entry mapping key -> datum onto ialist. (ialist-deletekey ialist =)  $\rightarrow ialist$ 

ilist library procedure ilist library procedure

 $(ialist-deletekey ialist) \rightarrow ialist$ 

ialist-delete deletes all associations from ialist with the given key, using key-comparison procedure =, which defaults to equal?. The dynamic order in which the various applications of = are made is not specified.

Return values may share common tails with the ialist argument. The ialist is not disordered—elements that appear in the result ialist occur in the same order as they occur in the argument ialist.

The comparison procedure is used to compare the element keys  $k_i$  of ialist's entries to the key parameter in this way: (= key ki). Thus, one can reliably remove all entries of ialist whose key is greater than five with (ialist-delete 5 ialist <)

# Replacement

These two procedures are analogues of the primitive side-effect operations on pairs, set-car! and set-cdr!.

```
(replace-icar ipair\ object) \rightarrow ipair
```

ilist library procedure

This procedure returns an ipair with object in the icar field and the icdr of ipair in the icdr field.

```
(replace-icdr ipair\ object) \rightarrow ipair
```

ilist library procedure

This procedure returns an ipair with object in the icdr field and the icar of ipair in the icar field.

#### Conversion

These procedures convert between mutable and immutable pair structures.

```
(pair->ipair pair) \rightarrow ipair ilist library procedure (ipair->pair ipair) \rightarrow pair ilist library procedure
```

These procedures, which are inverses, return an ipair and a pair respectively that have the same (i)car and (i)cdr fields as the argument.

```
(list->ilist flist) \rightarrow dilist ilist library procedure (ilist->list dilist) \rightarrow flist ilist library procedure
```

These procedures return an ilist and a list respectively that have the same elements as the argument. The tails of dotted (i)lists are preserved in the result, which makes the procedures not inverses when the tail of a dotted ilist is a list or vice versa. The empty list is converted to itself.

It is an error to apply list->ilist to a circular list.

```
(tree->itree object) \rightarrow object
(itree->tree object) \rightarrow object
```

ilist library procedure ilist library procedure

These procedures walk a tree of pairs or ipairs respectively and make a deep copy of it, returning an isomorphic tree containing ipairs or pairs respectively. The result may share structure with the argument. If the argument is not of the expected type, it is returned.

These procedures are not inverses in the general case. For example, a pair of ipairs would be converted by tree->itree to an ipair of ipairs, which if converted by itree->tree would produce a pair of pairs.

```
(gtree->itree \ object) \rightarrow object
(gtree->tree \ object) \rightarrow object
```

ilist library procedure ilist library procedure

These procedures walk a generalized tree consisting of pairs, ipairs, or a combination of both, and make a deep copy of it, returning an isomorphic tree containing only ipairs or pairs respectively. The result may share structure with the argument. If the argument is neither a pair nor an ipair, it is returned.

# **Procedure Application**

This procedure allows a procedure to be applied to an ilist.

(iapply procedure object ...ilist)  $\rightarrow$  object

ilist library procedure

The iapply procedure is an analogue of apply whose last argument is an ilist rather than a list. It is equivalent to (apply procedure object ... (ilist->list ilist)), but may be implemented more efficiently.

### Comparators

ilistobject ipair-comparator

The ipair-comparator object is a SRFI-114 comparator suitable for comparing ipairs. Note that it is not a procedure. It compares pairs using default-comparator on their cars. If the cars are not equal, that value is returned. If they are equal, default-comparator is used on their cdrs and that value is returned.

ilist-comparator ilistobject

The ilist-comparator object is a SRFI-114 comparator suitable for comparing ilists. Note that it is not a procedure. It compares ilists lexicographically, as follows:

- The empty ilist compares equal to itself.
- The empty ilist compares less than any non-empty ilist.
- Two non-empty ilists are compared by comparing their icars. If the icars are not equal when compared using default-comparator, then the result is the result of that comparison. Otherwise, the icdrs are compared using ilist-comparator.

 $(make-ilist-comparator comparator) \rightarrow comparator$ 

ilist library procedure

The make-ilist-comparator procedure returns a comparator suitable for comparing ilists using element-comparator to compare the elements.

 $(make-improper-ilist-comparator comparator) \rightarrow comparator$ 

ilist library procedure

The make-improper-ilist-comparator procedure returns a comparator that compares arbitrary objects as follows: the empty list precedes all ipairs, which precede all other objects. Ipairs are compared as if with (make-ipair-comparator comparator). All other objects are compared using comparator.

 $(make-icar-comparator comparator) \rightarrow comparator$ 

ilist library procedure

The make-icar-comparator procedure returns a comparator that compares ipairs on their icars alone using comparator.

 $(make-icdr-comparator \ comparator) \rightarrow comparator$ 

ilist library procedure

The make-icdr-comparator procedure returns a comparator that compares ipairs on their icdrs alone using comparator.

#### References & links

This document, in HTML: <a href="http://srfi.schemers.org/srfi-116/srfi-116.html">http://srfi.schemers.org/srfi-116/srfi-116.html</a>
Source code for the reference implementation: <a href="http://srfi.schemers.org/srfi-116/ilists.tar.gz">http://srfi.schemers.org/srfi-116/ilists.tar.gz</a>
Archive of SRFI-116 discussion-list email: <a href="http://srfi.schemers.org/srfi-116/mail-archive/maillist.html">http://srfi.schemers.org/srfi-116/mail-archive/maillist.html</a>
SRFI web site: <a href="http://srfi.schemers.org/">http://srfi.schemers.org/</a>

Editor: Mike Sperber

# Random access pairs and lists

[Red Edition item 9] What random access pair/list library should R7RS-large provide?

SRFI 101 is a library for purely functional pairs and lists with O(log n) access time. To avoid conflicts, procedure names will be modified for R7RS-large purposes as follows:

- make-list to become make-rlist
- random-access-list->linear-access-list to become rlist->list
- linear-access-list->random-access-list to become list->rlist
- all other identifiers to be prefixed with r (rcons, rpair?, rcar, rmap, etc.)

Random-access lists [1] are a purely functional data structure for representing lists of values. A random-access list may act as a drop in replacement for the usual linear-access pair and list data structures (pair?, cons, car, cdr), which additionally supports fast index-based addressing and updating (list-ref, list-set). The impact is a whole class of purely-functional algorithms expressed in terms of index-based list addressing become feasible compared with their linear-access list counterparts.

This document proposes a library API for purely functional random-access lists consistent with the R<sup>6</sup>RS [2] base library and list utility standard library [3].

The names described in this section comprise the (scheme rlist) library.

TODO The name changes given above have not yet been incorporated into this document.

TODO This library somehow redefines features found in R<sup>7</sup>RS small. I'm not sure how to describe that here. I'm leaving this SRFI for the next iteration.

#### Random-access pairs and lists

A random-access pair (or just pair) is a compound structure with two fields called the car and the cdr fields (consistent with the historical naming of pair fields in Scheme). Pairs are created by the procedure cons. The car and cdr fields are accessed by the procedures car and cdr.

Pairs are used primarily to represents lists. A list can be defined recursively as either the empty list or a pair whose cdr is a list. More precisely, the set of lists is defined as the smallest set X such that

- The empty list is in X.
- If *list* is in X, then any pair whose cdr field contains *list* is also in X.

The objects in the car fields of successive pairs of a list are the elements of the list. For example, a two-element list is a pair whose car is the first element and whose cdr is a pair whose car is the second element and whose cdr is the empty list. The length of a list is the number of elements, which is the same as the number of pairs.

The empty list is a special object of its own type. It is not a pair. It has no elements and its length is zero.

Note: The above definitions imply that all lists have finite length and are terminated by the empty list.

A chain of pairs is defined recursively as either a non-pair object or a pair whose cdr is a chain of pairs (Note: every value is a chain of pairs). A chain of pairs ending in the empty list is a list. A chain of pairs not ending in the empty list is called an improper list. Note that an improper list is not a list. Whether a given pair is a list depends upon what is stored in the cdr field.

The external representation of pairs is not specified by this SRFI, however the examples below do use the typical notation for writing pair and list values.

Random-access pairs and lists are specified to be fully functional, or, to use the term from the academic literature, fully persistent [1]. Full persistence means that all operations on random-access lists, notably including cons, list-ref, list-set, and list-ref/update, are specified

- 1. not to mutate any of their arguments; perforce
- 2. to be safe to execute concurrently on shared arguments; and
- 3. to suffer no degradation of performance as a consequence of the history of operations carried out to produce their arguments (except as it is reflected in the lengths of those arguments); but permitted
- 4. to produce results that share structure with their arguments.

It is usually taken for granted that standard Scheme lists have these properties. This SRFI explicitly specifies that random-access lists share them.

```
syntax: (quote datum)
```

Syntax: < Datum> should be a syntactic datum.

Semantics: (quote <datum>) evaluates to the datum value represented by <datum> (see section 4.3 of R6RS). This notation is used to include constants.

When the datum value represented by <atum> contains pair structure, quote produces random-access pairs.

```
(quote a)
(quote #(a b c))
                                                   #(a b c)
(quote (+ 1 2))
                                                   (+12)
```

As noted in section 4.3.5 of R6RS, (quote <datum>) may be abbreviated as '<datum>:

```
"abc"
                                                     "abc"
145932
                                                     145932
'a
'#(a b c)
                                                     #(a b c)
'()
                                                     ()
'(+ 1 2)
                                                     (+12)
'(quote a)
                                                     (quote a)
''a
                                                     (quote a)
```

As noted in section 5.10 of R6RS, constants are immutable.

Note: Different constants that are the value of quote expression may share the same locations.

```
procedure: (equal? obj1 obj2) → bool
```

The equal? predicate returns #t if and only if the (possibly infinite) unfoldings of its arguments into regular trees are equal as ordered trees.

The equal? predicate treats pairs and vectors as nodes with outgoing edges, uses string=? to compare strings, uses bytevector=? to compare bytevectors, and uses eqv? to compare other nodes.

```
(equal? 'a 'a)
                                                   #t
(equal? '(a) '(a))
                                                   #t
(equal? '(a (b) c)
        '(a (b) c))
                                                   #t
(equal? "abc" "abc")
                                                   #t
(equal? 2 2)
                                                   #t
(equal? (make-vector 5 'a)
        (make-vector 5 'a))
                                                   #t
(equal? '#vu8(1 2 3 4 5)
        (u8-list->bytevector
         '(1 2 3 4 5))
                                                   #t
(equal? (lambda (x) x)
        (lambda (y) y))
                                                   unspecified
(let* ((x (list 'a))
       (y (list 'a))
       (z (list x y)))
 (list (equal? z (list y x))
        (equal? z (list x x))))
                                                   (#t #t)
```

procedure: (pair? obj) → bool

Returns #t if obj is a pair, and otherwise returns #f. This operation must take O(1) time.

```
(pair? '(a . b))  #t
(pair? '(a b c))  #t
(pair? '())  #f
(pair? '#(a b))  #f
```

procedure: (cons obj1 obj2) → pair

Returns a newly allocated pair whose car is  $obj_1$  and whose cdr is  $obj_2$ . The pair is guaranteed to be different (in the sense of eqv?) from every existing object. This operation must take O(1) time.

```
      (cons 'a '())
      (a)

      (cons '(a) '(b c d))
      ((a) b c d)

      (cons "a" '(b c))
      ("a" b c)

      (cons 'a 3)
      (a . 3)

      (cons '(a b) 'c)
      ((a b) . c)
```

procedure: (car pair) → obj

Returns the contents of the car field of pair. This operation must take O(1) time.

```
      (car '(a b c))
      a

      (car '((a) b c d))
      (a)

      (car '(1 . 2))
      1

      (car '())
      &assertion exception
```

procedure: (cdr pair) → obj

Returns the contents of the cdr field of pair. This operation must take O(1) time.

These procedures are compositions of car and cdr, where for example caddr could be defined by  $(define\ caddr\ (lambda\ (x)\ (cdr\ (cdr\ x)))))$ .

Arbitrary compositions, up to four deep, are provided. There are twenty-eight of these procedures in all. These operations must take O(1) time.

procedure: (null? obj) → bool

Returns #t if obj is the empty list, #f otherwise. This procedure is equivalent to the null? procedure of the R6RS base library.

procedure: (list? obj) → bool

Returns #t if obj is a list, #f otherwise. By definition, all lists are chains of pairs that have finite length and are terminated by the empty list. This operation must take time bounded by O(log(n)), where n is the number of pairs in the chain forming the potential list.

```
(list? '(a b c)) #t
(list? '()) #t
(list? '(a . b)) #f
```

procedure: (list obj ...) → list

Returns a newly allocated list of its arguments. This operation must take time bounded by O(n), where n is the number of arguments to list.

```
(list 'a (+ 3 4) 'c) (a 7 c)
(list) ()
```

```
procedure: (make-list k) \rightarrow list
procedure: (make-list k obj) \rightarrow list
```

Returns a newly allocated list of k elements. If a second argument is given, then each element is initialized to obj. Otherwise the initial contents of each element is unspecified. This operation must take time and space bounded by O(log(k)).

```
(make-list 5 0) (0 0 0 0 0)
```

procedure: (length list) → k

Returns the length of list. This operation must take time bounded by  $O(\log(n))$ , where n is the length of the list.

procedure: (length<=? obj k) → bool

Returns true if obj is a chain of at least k pairs and false otherwise. This operation must take time bounded by O(log(min(k,n))), where n is the length of the chain of pairs.

```
procedure: (append list ... obj) → obj
```

Returns a chain of pairs consisting of the elements of the first *list* followed by the elements of the other lists, with *obj* as the cdr of the final pair. An improper list results if *obj* is not a list. This operation must take time bounded by O(log(n)), where n is the total number of elements in the given lists.

```
      (append '(x) '(y))
      (x y)

      (append '(a) '(b c d))
      (a b c d)

      (append '(a (b)) '((c)))
      (a (b) (c))

      (append '(a b) '(c . d))
      (a b c . d)

      (append '() 'a)
      a
```

```
procedure: (reverse list) → list
```

Returns a newly allocated list consisting of the element of *list* in reverse order. This operation must take time bounded by O(n) where n is the length of the list.

Obj should be a chain of pairs with a count of at least k. The list-tail procedure returns the object obtained by omitting the first k elements in obj. This operation must take time bounded by O(log(min(k,n))), where n is the length of the chain of pairs.

```
      (list-tail '(a b c d) 0)
      (a b c d)

      (list-tail '(a b c d) 2)
      (c d)

      (list-tail 'not-a-list 0)
      not-a-list
```

Implementation responsibilities: The implementation must check that obj is a chain of pairs whose count is at least k.

```
procedure: (list-ref pair k) → obj
```

Pair must be a chain of pairs whose count is at least k + 1. The list-ref procedure returns the kth element of pair. This operation must take time bounded by O(min(k,log(n))), where n is the length of the chain of pairs.

```
(list-ref '(a b c d) 2)
```

Implementation responsibilities: The implementation must check that pair is a chain of pairs whose count is at least k + 1.

```
procedure: (list-set pair k obj) → obj
```

Pair must be a chain of pairs whose count is at least k + 1. The list-set procedure returns the chain of pairs obtained by replacing the kth element with obj. This operation must take time bounded by  $O(\min(k, \log(n)))$ , where n is the length of the chain of pairs.

```
(list-set '(a b c d) 2 'x) (a b x d)
```

Implementation responsibilities: The implementation must check that pair is a chain of pairs whose count is at least k + 1.

```
procedure: (list-ref/update pair k proc) → obj1 obj2
```

Returns the same results as:

but it may be implemented more efficiently.

```
procedure: (map proc list1 list2 ...) → list
```

The *lists* should all have the same length. *Proc* should accept as many arguments as there are *lists* and return a single value.

The map procedure applies *proc* element-wise to the elements of the *lists* and returns a list of the results, in order. *Proc* is always called in the same dynamic environment as map itself. The order in which *proc* is applied to the elements of the *lists* is unspecified.

Implementation responsibilities: The implementation should check that the *lists* all have the same length. The implementation must check the restrictions on *proc* to the extent performed by applying it as described. An implementation may check whether *proc* is an appropriate argument before applying it.

```
procedure: (for-each proc list1 list2 ...) → unspecified
```

The lists should all have the same length. Proc should accept as many arguments as there are lists.

The for-each procedure applies *proc* element-wise to the elements of the *lists* for its side effects, in order from the first element to the last. *Proc* is always called in the same dynamic environment as for-each itself. The return values of for-each are unspecified.

Implementation responsibilities: The implementation should check that the *lists* all have the same length. The implementation must check the restrictions on *proc* to the extent performed by applying it as described. An implementation may check whether *proc* is an appropriate argument before applying it.

Note: Implementations of for-each may or may not tail-call proc on the last element.

# Representation conversion

```
procedure: (random-access-list->linear-access-list ra-list) \rightarrow la-list procedure: (linear-access-list->random-access-list la-list) \rightarrow ra-list
```

These procedures convert between (potentially) distinct representations of lists. To avoid confusion, parameters named ra-list range over lists represented with random-access lists, i.e. objects satisfying the list? predicate described above, while parameters named la-list range over lists represented with the more traditional linear-access lists, i.e. objects satisfying the list? predicate of R6RS. In systems that represent all lists as random-access lists, these conversions may simply be list identity procedures.

Random-access pairs must be disjoint from all other base types with the possible exception of (linear-access) pairs.

The external representation of random-access pairs is unspecified. The behavior of equal? when given a random-access pair and a sequential-access pair is unspecified in implementations with disjoint representations.

The behavior of eq? and eqv? on random-access pairs must be the same as that for pairs, vectors, or records. Namely, two random-access pair objects are eq? if and only if they are eqv?, and they are eqv? if and only if they refer to the same location in the store.

All argument checking for each operation must be done within the time bounds given for that operation.

Implementations are encouraged, but not required, to support random-access pairs and lists as their primary pair and list representation. In such an implementation, the external representation of random-access pairs and list should be as described in section 4.3.2 (Pairs and lists) of R<sup>6</sup>RS, the behavior of equivalence predicates on random-access pairs should be as described in section 11.5 (Equivalence predicates) of R<sup>6</sup>RS, and so on. In short, all pairs should be random-access

Implementations supporting SRFI Libraries [4] and SRFI 101 must provide the following libraries:

```
(srfi :101)
                                             ; Composite libraries
(srfi :101 random-access-lists)
(srfi :101 random-access-lists procedures) ; Procedures only
(srfi :101 random-access-lists syntax)
                                             ; Syntax only
```

### References

[1] Purely Functional Random-Access Lists Chris Okasaki, Functional Programming Languages and Computer Architecture, June 1995, pages 86-95.

http://www.eecs.usma.edu/webs/people/okasaki/pubs.html#fpca95

- [2] Revised<sup>6</sup> Report on the Algorithmic Language Scheme Michael Sperber, et al. (Editors) http://www.r6rs.org/
- [3] Revised<sup>6</sup> Report on the Algorithmic Language Scheme, Standard Libraries Michael Sperber, et al. (Editors)

http://www.r6rs.org/

[4] SRFI 97: SRFI Libraries David Van Horn

http://srfi.schemers.org/srfi-97/

[5] PLaneT: Purely Functional Random-Access Lists David Van Horn

http://planet.plt-scheme.org/display.ss?package=ralist.plt&owner=dvanhorn

Editor: Donovan Kolbly

# Deques

[Red Edition item 10] What immutable deque library should R7RS-large provide?

SRFI 134 is a library for immutable double-ended queues, with O(1) addition and removal time at both ends.

This SRFI defines immutable deques. A deque is a double-ended queue, a sequence which allows elements to be added or removed efficiently from either end. A structure is immutable when all its operations leave the structure unchanged. Note that none of the TODO names of the procedures specified here ends with an exclamation point.

The names described in this section comprise the (scheme ideque) library.

## Procedure index

Constructors: ideque, ideque-tabulate, ideque-unfold, ideque-unfold-right

Predicates: ideque?, ideque-empty?, ideque-, ideque-any, ideque-every

 $\label{eq:Queue} Queue\ operations: \verb"ideque-front", ideque-front", ideque-remove-back", ideque-add-front", ideque-add-back \\$ 

Other accessors: ideque-ref, ideque-take, ideque-take-right, ideque-drop, ideque-drop-right, ideque-split-at

The whole ideque: ideque-length, ideque-append, ideque-reverse, ideque-count, ideque-zip

Mapping: ideque-map, ideque-filter-map, ideque-for-each, ideque-for-each-right, ideque-fold, ideque-fold-right ideque-append-map

Filtering: ideque-filter, ideque-remove, ideque-partition

Searching: ideque-find, ideque-find-right, ideque-take-while, ideque-take-while-right, ideque-drop-while, ideque-drop-while-right, ideque-span, ideque-break

Conversion: list->ideque, ideque->list, generator->ideque, ideque->generator

We specify required time efficiency upper bounds using big-O notation. We note when, in some cases, there is "slack" between the required bound and the theoretically optimal bound for an operation. Implementations may use data structures with amortized time bounds, but should document which bounds hold in only an amortized sense.

Degues are disjoint from all other Scheme types.

# Constructors

(ideque element ...)  $\rightarrow ideque???$ ?

ideque library procedure

Returns an ideque containing the *elements*. The first element (if any) will be at the front of the ideque and the last element (if any) will be at the back. Takes O(n) time, where n is the number of elements.

(ideque-tabulate  $n \ proc$ )  $\rightarrow ideque???$ 

ideque library procedure

Invokes the predicate proc on every exact integer from 0 (inclusive) to n (exclusive). Returns an ideque containing the results in order of generation. Takes O(n) time.

(ideque-unfold stop? mapper successor seed)  $\rightarrow ideque????$ 

ideque library procedure

Invokes the predicate stop? on seed. If it returns false, generate the next result by applying mapper to seed, generate the next seed by applying successor to seed, and repeat this algorithm with the new seed. If stop? returns true, return an ideque containing the results in order of accumulation. Takes O(n) time.

(ideque-unfold-right stop? mapper successor seed)  $\rightarrow ideque????$ 

ideque library procedure

Invokes the predicate stop? on seed. If it returns false, generate the next result by applying mapper to seed, generate the next seed by applying successor to seed, and repeat the algorithm with the new seed. If stop? returns true, return an ideque containing the results in reverse order of accumulation. Takes O(n) time.

### **Predicates**

(ideque? x)  $\rightarrow boolean$ ???

ideque library procedure

Returns #t if x is an ideque, and #f otherwise. Takes O(1) time.

(ideque-empty? ideque)  $\rightarrow boolean$ ???

ideque library procedure

Returns #t if *ideque* contains zero elements, and #f otherwise. Takes O(1) time.

(ideque=  $elt= ideque \dots$ )  $\rightarrow boolean ????$ 

ideque library procedure

Determines ideque equality, given an element-equality procedure. Ideque A equals ideque B if they are of the same length, and their corresponding elements are equal, as determined by elt=. If the element-comparison procedure's first argument is from  $ideque_i$ , then its second argument is from  $ideque_{i+1}$ , i.e. it is always called as  $(elt=a\ b)$  for a an element of ideque A, and b an element of ideque B.

In the n-ary case, every  $ideque_i$  is compared to  $ideque_{i+1}$  (as opposed, for example, to comparing  $ideque_1$  to every  $ideque_i$ , for i > 1). If there are zero or one ideque arguments, ideque = simply returns true. The name does not end in a question mark for compatibility with the SRFI-1 procedure list=.

Note that the dynamic order in which the *elt*= procedure is applied to pairs of elements is not specified. For example, if ideque= is applied to three ideques, A, B, and C, it may first completely compare A to B, then compare B to C, or it may compare the first elements of A and B, then the first elements of B and C, then the second elements of A and B, and so forth.

The equality procedure must be consistent with eq?. Note that this implies that two ideques which are eq? are always ideque=, as well; implementations may exploit this fact to "short-cut" the element-by-element comparisons.

(ideque-any  $pred\ ideque$ )  $\rightarrow value\ or\ boolean$ ??? (ideque-every  $pred\ ideque$ )  $\rightarrow ideque$ ???

ideque library procedure ideque library procedure

Invokes pred on the elements of the ideque in order until one call returns a true/false value, which is then returned. If there are no elements, returns #f/#t. Takes O(n) time.

# Queue operations

(ideque-front ideque)  $\rightarrow value????$  (ideque-back ideque)  $\rightarrow value????$ 

ideque library procedure ideque library procedure

Returns the front/back element of *ideque*. It is an error for *ideque* to be empty. Takes O(1) time.

(ideque-remove-front ideque)  $\rightarrow$  ideque???? (ideque-remove-back ideque)  $\rightarrow$  ideque???

ideque library procedure ideque library procedure

Returns an ideque with the front/back element of *ideque* removed. It is an error for *ideque* to be empty. Takes O(1) time.

(ideque-add-front  $ideque\ obj$ )  $\rightarrow ideque$ ??? (ideque-add-back  $ideque\ obj$ )  $\rightarrow ideque$ ???

ideque library procedure ideque library procedure

Returns an ideque with obj pushed to the front/back of ideque. Takes O(1) time.

## Other accessors

(ideque-ref ideque n)  $\rightarrow value???$ 

ideque library procedure

Returns the *nth* element of *ideque*. It is an error unless n is less than the length of *ideque*. Takes O(n) time.

(ideque-take  $ideque\ n$ )  $\rightarrow ideque$ ??? (ideque-take-right  $ideque\ n$ )  $\rightarrow ideque$ ??? ideque library procedure ideque library procedure

Returns an ideque containing the first/last n elements of *ideque*. It is an error if n is greater than the length of *ideque*. Takes O(n) time.

(ideque-drop  $ideque\ n$ )  $\rightarrow ideque$ ??? (ideque-drop-right  $ideque\ n$ )  $\rightarrow ideque$ ??? ideque library procedure ideque library procedure

Returns an ideque containing all but the first/last n elements of *ideque*. It is an error if n is greater than the length of *ideque*. Takes O(n) time.

(ideque-split-at  $ideque\ n$ )  $\rightarrow ideque????\ ideque???$ 

ideque library procedure

Returns two values, the results of (ideque-take  $ideque\ n$ ) and (ideque-drop  $ideque\ n$ ) respectively, but may be more efficient. Takes O(n) time.

### The whole ideque

(ideque-length ideque)  $\rightarrow integer$ ???

ideque library procedure

Returns the length of *ideque* as an exact integer. May take O(n) time, though O(1) is optimal. TODO "may take O(1) in the best case"??? I thought we were giving average cases.

(ideque-append ideque ...)  $\rightarrow ideque????$ 

ideque library procedure

Returns an ideque with the contents of the *ideque* followed by the others, or an empty ideque if there are none. Takes O(kn) time, where k is the number of ideques and n is the number of elements involved, though  $O(k \log n)$  is possible. some implementations may only require  $O(k \log n)$ . TODO I assume that's "lg", not that it really matters.

(ideque-reverse ideque)  $\rightarrow ideque$ ???

ideque library procedure

Returns an ideque containing the elements of *ideque* in reverse order. Takes O(1) time.

(ideque-count  $pred\ ideque$ )  $\rightarrow integer$ ???

ideque library procedure

Pred is a procedure taking a single value and returning a single value. It is applied element-wise to the elements of ideque, and a count is tallied of the number of elements that produce a true value. This count is returned. Takes O(n) time. The dynamic order of calls to pred is unspecified.

(ideque-zip  $ideque_1$   $ideque_2$  ...)  $\rightarrow ideque???$ 

ideque library procedure

Returns an ideque of lists (not ideques) each of which contains the corresponding elements of ideques in the order specified. Terminates when all the elements of any of the ideques have been processed. Takes O(kn) time, where k is the number of ideques and n is the number of elements in the shortest ideque.

# DRAFT

## **Mapping**

(ideque-map  $proc\ ideque$ )  $\rightarrow ideque$ ???

ideque library procedure

Applies proc to the elements of ideque and returns an ideque containing the results in order. The dynamic order of calls to proc is unspecified. Takes O(n) time.

(ideque-filter-map  $proc\ ideque$ )  $\rightarrow ideque$ ???

ideque library procedure

Applies proc to the elements of ideque and returns an ideque containing the true (i.e. non-#f) results in order. The dynamic order of calls to proc is unspecified. Takes O(n) time.

(ideque-for-each  $proc\ ideque$ )  $\rightarrow unspecified$ ??? (ideque-for-each-right  $proc\ ideque$ )  $\rightarrow unspecified$ ??? ideque library procedure ideque library procedure

Applies proc to the elements of ideque in forward/reverse order and returns an unspecified result. Takes O(n) time.

(ideque-fold  $proc\ nil\ ideque$ )  $\rightarrow value$ ??? (ideque-fold-right  $proc\ nil\ ideque$ )  $\rightarrow value$ ???

ideque library procedure ideque library procedure

Invokes proc on the elements of ideque in forward/reverse order, passing the result of the previous invocation as a second argument. For the first invocation, nil is used as the second argument. Returns the result of the last invocation, or nil if there was no invocation. Takes O(n) time.

(ideque-append-map  $proc\ ideque$ )  $\rightarrow ideque$ ???

ideque library procedure

Applies proc to the elements of ideque. It is an error if the result is not a list. Returns an ideque containing the elements of the lists in order. Takes O(n) time, where n is the number of elements in all the lists returned.

## **Filtering**

(ideque-filter  $pred\ ideque$ )  $\rightarrow ideque$ ??? (ideque-remove  $pred\ ideque$ )  $\rightarrow ideque$ ??? ideque library procedure ideque library procedure

Returns an ideque containing the elements of ideque that do/do not satisfy pred. Takes O(n) time.

TODO In the same order?

(ideque-partition  $proc\ ideque$ )  $\rightarrow ideque$ ??? ideque???

ideque library procedure

Returns two values, the results of (ideque-filter pred ideque) and (ideque-remove pred ideque) respectively, but may be more efficient. Takes O(n) time.

# Searching

(ideque-find  $pred\ ideque\ failure$ )  $\rightarrow value$ ??? ideque library procedure (ideque-find  $pred\ ideque$ )  $\rightarrow value???$ ideque library procedure (ideque-find-right  $pred\ ideque\ failure$ )  $\rightarrow value$ ??? ideque library procedure (ideque-find-right  $pred\ ideque$ )  $\rightarrow value???$ ideque library procedure

Returns the first/last element of ideque that satisfies pred. If there is no such element, returns the result of invoking the thunk failure; the default thunk is (lambda () #f). Takes O(n) time.

(ideque-take-while  $pred\ ideque$ )  $\rightarrow$  ideque??? (ideque-take-while-right  $pred\ ideque$ )  $\rightarrow$  ideque???

ideque library procedure ideque library procedure

Returns an ideque containing the longest initial/final prefix of elements in ideque all of which satisfy pred. Takes O(n) time

(ideque-drop-while  $pred\ ideque$ )  $\rightarrow ideque$ ??? (ideque-drop-while-right  $pred\ ideque$ )  $\rightarrow ideque$ ???

ideque library procedure ideque library procedure

Returns an ideque which omits the longest initial/final prefix of elements in *ideque* all of which satisfy pred, but includes all other elements of *ideque*. Takes O(n) time.

(ideque-span  $pred\ ideque$ )  $\rightarrow$  ideque???? ideque??? ideque??? ideque??? ideque??? ideque???

ideque library procedure ideque library procedure

Returns two values, the initial prefix of the elements of *ideque* which do/do not satisfy *pred*, and the remaining elements. Takes O(n) time.

TODO Explain why the 2 names.

#### Conversion

(list->ideque list)  $\rightarrow ideque????$  (ideque->list ideque)  $\rightarrow list???$ 

ideque library procedure ideque library procedure

Conversion between ideque and list structures. FIFO order is preserved, so the front of a list corresponds to the front of an ideque. Each operation takes O(n) time.

(generator->ideque generator)  $\rightarrow ideque$ ??? (ideque->generator ideque)  $\rightarrow generator$ ???

ideque library procedure ideque library procedure

Conversion between SRFI 121 generators and ideques. Each operation takes O(n) time. A generator is a procedure that is called repeatedly with no arguments to generate consecutive values, and returns an end-of-file object when it has no more values to return.

Editor: Arthur A. Gleckler

## Immutable texts

[Red Edition item 11] What immutable text library should R7RS-large provide?

SRFI 135 is a library for immutable character sequences with O(1) access time. Its procedures accept strings as well as texts, so that a separate string library may not be as useful.

TODO This material and the "Basic Concepts" stuff further down should be reorganized. Some material will go to the Rationale, but much of it should stay.

In Scheme, strings are a mutable data type. Although it "is an error" (R5RS and R7RS) to use string-set! on literal strings or on strings returned by symbol->string, and any attempt to do so "should raise an exception" (R6RS), all other strings are mutable.

Although many mutable strings are never actually mutated, the mere possibility of mutation complicates specifications of libraries that use strings, encourages precautionary copying of strings, and precludes structure sharing that could otherwise be used to make procedures such as substring and string-append faster and more space-efficient.

This SRFI specifies a new data type of immutable texts. It comes with efficient and portable sample implementations that guarantee O(1) indexing for both sequential and random access, even in systems whose **string-ref** procedure takes linear time.

The operations of this new data type include analogues for all of the non-mutating operations on strings specified by the R7RS and most of those specified by SRFI 130, but the immutability of texts and uniformity of character-based indexing simplify the specification of those operations while avoiding several inefficiencies associated with the mutability of Scheme's strings.

### **Issues**

None.

## **Procedure Index**

Here is a list of the procedures provided by this SRFI:

Predicates text? textual?

textual-null?

textual-every textual-any

Constructors make-text text

text-tabulate

text-unfold text-unfold-right

Conversion textual->text

textual->string textual->vector textual->list
string->text vector->text list->text

reverse-list->text

textual->utf8 textual->utf16be textual->utf16 textual->utf16le utf8->text utf16be->text utf16->text utf16le->text

Selection text-length textual-length

text-ref textual-ref subtext subtextual

textual-copy

textual-take textual-take-right textual-drop textual-drop-right textual-pad textual-pad-right

textual-trim textual-trim-right textual-trim-both

Replacement textual-replace

Comparison textual=? textual-ci=?

textual<? textual-ci<?
textual>? textual-ci>?
textual<=? textual-ci<=?
textual>=? textual-ci>=?

Prefixes & suffixes textual-prefix-length textual-suffix-length

textual-prefix? textual-suffix?

Searching textual-index textual-index-right

textual-skip textual-skip-right textual-contains textual-contains-right

Case conversion textual-upcase textual-downcase

 ${\tt textual-foldcase} \qquad {\tt textual-titlecase}$ 

Concatenation textual-append textual-concatenate textual-concatenate-reverse

textual-join

Fold & map & friends textual-fold textual-fold-right

textual-map textual-for-each textual-map-index textual-for-each-index

textual-count

textual-filter textual-remove

# Replication & splitting textual-replicate textual-split

#### Immutable texts

### Basic concepts

The names described in this section comprise the (scheme text) library.

### Conceptual model

Immutable texts are like strings except they can't be mutated.

Immutability makes it easier to use space-efficient representations such as UTF-8 and UTF-16 without incurring the cost of scanning from the beginning when character indexes are used (as with string-ref).

When mutation is not needed, immutable texts are likely to be more efficient than strings with respect to space or time. In some implementations, immutable texts may be more efficient than strings with respect to both space and time.

# Subtypes

This SRFI defines two new types:

- text is a type consisting of the immutable texts for which text? returns true.
- textual is a union type consisting of the texts and strings for which textual? returns true.

The subtypes of the new textual type include the new text type and Scheme's traditional string type, which consists of the values for which string? returns true. The string type includes both mutable strings and the (conceptually) immutable strings that are the values of string literals and calls to symbol->string.

Implementations of this SRFI are free to extend the *textual* type by adding new subtypes, provided all procedures whose names begin with textual- are extended to accept values of those new subtypes. Implementations of this SRFI should not extend the *text* type unless its extended values are immutable, are accepted as texts by all procedures of this SRFI (including the text? predicate), and achieve the performance required by this SRFI with respect to both time and space.

# External representation

This SRFI does not require any particular external representation for immutable texts, but recommends immutable texts have almost the same external representation as strings, substituting Unicode's left-pointing and right-pointing double angle quotation marks (« and », code points #xab and #xbb) for the double quotes that delimit strings, and allowing those double angle quotation marks to be escaped within the external representations of both texts and strings. That external representation is used by this SRFI's examples.

TODO This requires adding the guillemets « and » to Scheme's character set. How is this going to be done?

When feasible, implementations of this SRFI should also consider:

- extending the equal? procedure to regard two immutable texts t1 and t2 as equal if and only if (textual=? t1 t2), while regarding an immutable text as unequal to anything that isn't an immutable text.
- extending the display procedure to accept immutable texts, treating them the same as strings;
- extending the write procedure to generate the external syntax recommended for immutable texts;
- extending the read procedure to accept the external syntax recommended for immutable texts;
- extending interpreters and compilers to accept quoted literals expressed using the external syntax recommended for immutable texts; R7RS section 4.1.2 mandates this extension if read is extended to accept the external syntax for texts.

Note: Those extensions cannot be implemented portably, so portable code should not rely on them. TODO As I see it, this SRFI as part of the large language means that the above features must be redefined in R7RS-Small. Same with the guillemets above. Either that, or the recommendations given here should be removed.

## Textual input and output ports

Textual input and output ports analogous to string input and output ports would be nice, but they too cannot be implemented portably. Leaving them for another SRFI allows all of this SRFI to be implemented portably with reasonable

TODO Replace with "implementations are encouraged, but not required, to provide textual I/O ports analogous to string I/O ports"?

## Shared storage

All strings and other mutable objects returned by the procedures specified within this SRFI are newly allocated and may be mutated with abandon.

No externally visible string ever shares storage with any text. All strings and other mutable objects passed to the procedures specified within this SRFI may be mutated without affecting the behavior of any text.

The immutability of texts allows sharing of substructure, so subtext, textual-append, and similar operations can be faster and more space-efficient than Scheme's substring and string-append operations.

Although distinct texts may share storage internally, this is undetectable because texts are immutable and the procedures that operate on texts do not directly expose any of their internal components.

Implementations that share storage between texts must satisfy the following requirement: There is some reasonably small fixed bound on the ratio of storage used by the shared representation divided by the storage that would be used by an unshared representation.

Example: For the sample implementations with their default configurations, the worst case arises with UTF-8, when a 1-character ASCII text retains up to 127 characters of a text that is no longer reachable, and all 127 of those retained characters lie outside Unicode's Basic Multilingual Plane (BMP). Making reasonable assumptions about the representations of records, vectors, bytevectors, and strings on a 64-bit machine, that shared text would occupy no more than about 16 times the space occupied by an unshared representation. If the retained characters were in the BMP, the shared text would occupy no more than about 8 times the space occupied by an unshared representation. If the retained characters were ASCII, the shared text would occupy no more than about 4 times the space occupied by an unshared representation. The sample implementations can be configured to reduce those worst-case bounds, most obviously by reducing the maximum number of characters that can be shared with a very short text.

# Naming conventions

The procedures of this SRFI follow a consistent naming scheme, and are consistent with the conventions developed in SRFI 1 and used in SRFI 13 and SRFI 130. Indeed, most of the names specified here were derived from SRFI 130's names by replacing string with text or textual. As in SRFI 130, procedures that have left/right directional variants use no suffix to specify left-to-right operation, -right to specify right-to-left operation, and -both to specify both.

Note, however, that textual-index, textual-index-right, textual-skip, and textual-skip-right, return #f when no match is found. In SRFI 130, their analogues always return cursors.

The order of common arguments is consistent across the different procedures.

For convenience, most procedures that accept a text as argument will also accept a string. When given a string, those procedures behave as though the string is first converted to a text, so passing a text is likely to be more efficient than passing a string.

# Performance requirements

A few procedures are required to execute in O(1) time: text?, textual?, text-length, and text-ref.

If the first two arguments passed to textual-contains and textual-contains-right are texts, then those procedures must run in O(m n) time, where m and n are the lengths of the two subtexts specified by their arguments. If either of the first two arguments is a string, there is no such requirement.

The other procedures specified by this SRFI should run in amortized linear time, not counting time spent in procedures and predicates that were passed as arguments. That is not an absolute requirement, but the sample implementations are designed to deliver that level of performance for most procedures provided none of their textual arguments are strings. When strings are passed as arguments, the running time is unlikely to be linear unless string-ref runs in constant time, and that is not required by any of the Scheme standards.

Indeed, this SRFI was designed to make efficient text processing easier in systems whose string-ref procedure does not run in constant time. For efficiency, portable code should use strings only for fairly short sequences of characters. Representations with guaranteed efficiency (such as the immutable texts of this SRFI) should be used for longer texts.

*Note:* A procedure that runs in O(1) time does not necessarily take the same time for all inputs. Furthermore O(1)O(1000), so procedures that run in O(1) time can still be quite slow. The text-ref procedure, for example, may have worst cases for which it is hundreds of times slower than text?. Even the average case for text-ref is likely to be several times as slow as the worst case for text?.

#### Unicode

TODO This section is about UTF specifically, rather than Unicode. I think this could be substantially condensed, with a paragraph on the various UTF formats, followed by the recommendation to use the portable solution below.

During the early development of Unicode, its designers believed a 16-bit character set would suffice, which is why Java's char type has only 16 bits. When Unicode expanded to 1114112 code points, 16 bits were no longer enough to encode all Unicode characters.

The Unicode standard defines three encoding forms for arbitrary sequences of Unicode characters:

- UTF-32 is a fixed-width encoding in which every character is represented by a straightforward 32-bit representation of its code point.
- UTF-16 is a variable-width encoding in which the most common characters are represented by 16-bit representations of their code points, but characters outside the Basic Multilingual Plane (BMP) are represented by a surrogate pair consisting of two consecutive 16-bit code units.
- UTF-8 is a variable-width encoding in which ASCII characters are represented by 8-bit representations of their code points, but other characters are encoded by a sequence of two, three, or four 8-bit code units.

UTF-32 is a convenient internal representation and is used as such by several string libraries for C, C++, and Python, but it is the least compact of the three representations and is seldom used in files. UTF-16 is convenient for applications that use only the BMP, and supports fast sequential processing of arbitrary Unicode; variants of UTF-16 are used by Windows for files and by Java and C# as an internal representation. UTF-8 is upwardly compatible with the ASCII encoding and supports fast sequential processing of arbitrary Unicode; it is widely used for files on non-Windows machines and is also used by some C libraries.

The Scheme programming language does not expose the internal representation of strings. Some implementations of Scheme use UTF-32 or a similar encoding, which makes string-length, string-ref, and string-set! run in O(1) time. Some implementations of Scheme use UTF-16, which saves space at the expense of making string-ref take time proportional to the length of a string. Some implementations of Scheme use UTF-8, which saves even more space for ASCII strings while making string-ref run in linear time.

Although Scheme's string data type allows portable code to use strings independently of their internal representation, the variation in performance between implementations has created a problem for programs that use long strings. In some systems, long strings are inefficient with respect to space; in other systems, long strings are inefficient with respect to time.

The portable solution to this dilemma is to use Scheme's mutable strings only for buffers and other relatively short sequences of characters, while using the immutable texts defined by this SRFI for long sequences of characters.

Note: SRFI 130 suggests an alternative solution: Portable code should process strings sequentially using cursors instead of indexes, and should avoid mutation of strings by using vectors of characters instead, while hoping all major implementations of Scheme will soon convert their strings to use compact internal representations such as UTF-8 or UTF-16. That hope is unlikely to be realized, because a lot of legacy code assumes string-ref runs in O(1) time, as recommended by the R6RS, and mutable strings represented in UTF-32 or similar are more efficient than vectors of characters with respect to both time and space. At present, several implementations of Scheme support Unicode while providing string-ref and string-set! procedures that run in O(1) time; making those operations run asymptotically slower would displease some users of those systems.

#### Notation

In the following procedure specifications:

- A text argument is an immutable text.
- A textual argument is an immutable text or a string.
- A char argument is a character.
- An idx argument is an exact non-negative integer specifying a valid character index into a text or string. The valid character indexes of a text or string textual of length n are the exact integers idx satisfying  $0 \le idx < n$ .
- A k argument or result is a *position*: an exact non-negative integer that is either a valid character index for one of the textual arguments or is the length of a textual argument.
- start and end arguments are positions specifying a half-open interval of indexes for a subtext or substring. When omitted, start defaults to 0 and end to the length of the corresponding textual argument. It is an error unless 0 <= start <= end <= (textual-length textual); the sample implementations detect that error and raise an exception.
- A len or nchars argument is an exact non-negative integer specifying some number of characters, usually the length
  of a text or string.
- A pred argument is a unary character predicate, taking a character as its one argument and returning a value that will be interpreted as true or false. Unless noted otherwise, as with textual-every and textual-any, all predicates passed to procedures specified in this SRFI may be called in any order and any number of times. It is an error if pred has side effects or does not behave functionally (returning the same result whenever it is called with the same character); the sample implementations do not detect those errors.
- An obj argument may be any value at all.

It is an error to pass values that violate the specification above.

Arguments given in square brackets are optional. Unless otherwise noted in the text describing the procedure, any prefix of these optional arguments may be supplied, from zero arguments to the full list. When a procedure returns multiple values, this is shown by listing the return values in square brackets, as well. So, for example, the procedure with signature

```
halts? f [x init-store] → [boolean integer]
```

would take one (f), two (f, x) or three (f, x, init-store) input arguments, and return two values, a boolean and an integer.

An argument followed by "..." means zero or more elements. So the procedure with the signature

```
sum-squares x ... → number
```

takes zero or more arguments (x ...), while the procedure with signature

```
spell-check doc dict1 dict2 ... → string-list
```

takes two required arguments (doc and dict<sub>1</sub>) and zero or more optional arguments (dict<sub>2</sub> ...).

If a procedure's return value is said to be "unspecified," the procedure returns a single result whose value is unconstrained and might even vary from call to call.

### **Predicates**

 $(\text{text? } obj) \rightarrow boolean$  text library procedure

Is obj an immutable text? In particular, (text? obj) returns false if (string? obj) returns true, which implies string? returns false if text? returns true. Must execute in O(1) time. (textual? obj)  $\rightarrow boolean$  text library procedure

Returns true if and only obj is an immutable text or a string. Must execute in O(1) time.

(textual-null? text)  $\rightarrow boolean$ 

text library procedure

Is text the empty text? Must execute in O(1) time.

(textual-every pred textual start end)  $\rightarrow$  value (textual-every pred textual)  $\rightarrow$  value (textual-any pred textual start end)  $\rightarrow$  value (textual-any pred textual)  $\rightarrow$  value text library procedure text library procedure text library procedure text library procedure

Checks to see if every/any character in textual satisfies pred, proceeding from left (index start) to right (index end). textual-every These procedures are short-circuiting: if pred returns false, textual-every does not call pred on subsequent characters; if pred returns true, textual-any does not call pred on subsequent characters; Both procedures are "witness-generating":

- If textual-every is given an empty interval (with start = end), it returns #t.
- If textual-every returns true for a non-empty interval (with start < end), the returned true value is the one returned by the final call to the predicate on (text-ref (textual-copy text) (- end 1)).
- If textual-any returns true, the returned true value is the one returned by the predicate.

*Note:* The names of these procedures do not end with a question mark. This indicates a general value is returned instead of a simple boolean (#t or #f).

## Constructors

 $(make-text len char) \rightarrow text$ 

text library procedure

Returns a text of the given length filled with the given character.

(text  $char \dots$ )  $\rightarrow text$ 

text library procedure

Returns a text consisting of the given characters.

(text-tabulate  $proc\ len$ )  $\rightarrow text$ 

text library procedure

Proc is a procedure that accepts an exact integer as its argument and returns a character. Constructs a text of size len by calling proc on each value from 0 (inclusive) to len (exclusive) to produce the corresponding element of the text. The order in which proc is called on those indexes is not specified.

Rationale: Although text-unfold is more general, text-tabulate is likely to run faster for the common special case it implements.

(text-unfold stop? mapper successor seed base make-final)  $\rightarrow text$  (text-unfold stop? mapper successor seed)  $\rightarrow text$ 

text library procedure text library procedure

This is a fundamental constructor for texts.

- successor is used to generate a series of "seed" values from the initial seed: seed, (successor seed), (successor² seed), (successor³ seed), ...
- stop? tells us when to stop when it returns true when applied to one of these seed values.
- mapper maps each seed value to the corresponding character(s) in the result text, which are assembled into that text in left-to-right order. It is an error for mapper to return anything other than a character, string, or text.
- base is the optional initial/leftmost portion of the constructed text, which defaults to the empty text (text). It is an error if base is anything other than a character, string, or text.

(port->text p) = (text-unfold eof-object?

• make-final is applied to the terminal seed value (on which stop? returns true) to produce the final/rightmost portion of the constructed text. It defaults to (lambda (x) (text)). It is an error for make-final to return anything other than a character, string, or text.

text-unfold is a fairly powerful text constructor. You can use it to convert a list to a text, read a port into a text, reverse a text, copy a text, and so forth. Examples:

(textual-fold-right kons knil (text-unfold knull? kar kdr x)) = x

and

(text-unfold knull? kar kdr (textual-fold-right kons knil text)) = text.

This combinator pattern is sometimes called an "anamorphism."

Note: Implementations should not allow the size of texts created by text-unfold to be limited by limits on stack size.

```
(text-unfold-right stop? mapper successor seed base make-final) \rightarrow texttext library procedure(text-unfold-right stop? mapper successor seed) \rightarrow texttext library procedure
```

This is a fundamental constructor for texts. It is the same as text-unfold except the results of mapper are assembled into the text in right-to-left order, base is the optional rightmost portion of the constructed text, and make-final produces the leftmost portion of the constructed text.

### Conversion

```
(textual -> text \ textual) \rightarrow text
```

text library procedure

When given a text, textual->text just returns that text. When given a string, textual->text returns the result of calling string->text on that string. Signals an error when its argument is neither string nor text.

```
(textual->string textual \ start \ end) \rightarrow string
                                                                                                                   text library procedure
(textual->string textual) \rightarrow string
                                                                                                                   text library procedure
(textual->vector textual \ start \ end) \rightarrow char-vector
                                                                                                                   text library procedure
(textual - vector textual) \rightarrow char-vector
                                                                                                                   text library procedure
(textual->list textual \ start \ end) \rightarrow char-list
                                                                                                                   text library procedure
(textual \rightarrow list textual) \rightarrow char-list
                                                                                                                   text library procedure
```

textual->string, textual->vector, and textual->list return a newly allocated (unless empty) mutable string, vector, or list of the characters that make up the given subtext or substring.

```
(string->text string\ start\ end) \rightarrow text
                                                                                                                  text library procedure
(string->text string) \rightarrow text
                                                                                                                  text library procedure
(vector->text char-vector\ start\ end) \rightarrow text
                                                                                                                  text library procedure
(vector->text char\text{-}vector) \rightarrow text
                                                                                                                  text library procedure
(list->text char-list start end) \rightarrow text
                                                                                                                  text library procedure
                                                                                                                  text library procedure
(list->text char-list) \rightarrow text
```

These procedures return a text containing the characters of the given substring, subvector, or sublist. The behavior of the text will not be affected by subsequent mutation of the given string, vector, or list.

```
(reverse-list->text char	ext{-list}) 	o text
```

text library procedure

An efficient implementation of (compose list->text reverse):

```
(reverse-list->text '(#\a #\B #\c))}{procedure}{«cBa»
```

This is a common idiom in the epilogue of text-processing loops that accumulate their result using a list in reverse order. (See also textual-concatenate-reverse for the "chunked" variant.)

```
(textual->utf8 textual \ start \ end) \rightarrow bytevector
                                                                                                               text library procedure
(textual->utf8 textual) \rightarrow bytevector
                                                                                                               text library procedure
                                                                                                               text library procedure
(textual->utf16 textual \ start \ end) \rightarrow bytevector
(textual->utf16 textual) \rightarrow bytevector
                                                                                                               text library procedure
                                                                                                               text library procedure
(textual->utf16be textual \ start \ end) \rightarrow bytevector
(textual->utf16be textual) \rightarrow bytevector
                                                                                                               text library procedure
(textual->utf16le textual \ start \ end) \rightarrow bytevector
                                                                                                               text library procedure
(textual->utf16le textual) \rightarrow bytevector
                                                                                                               text library procedure
```

These procedures return a newly allocated (unless empty) bytevector containing a UTF-8 or UTF-16 encoding of the given subtext or substring.

The bytevectors returned by textual->utf8, textual->utf16be, and textual->utf16le do not contain a byte-order mark (BOM). textual->utf16be returns a big-endian encoding, while textual->utf16le returns a little-endian encoding.

The bytevectors returned by textual->utf16 begin with a BOM that declares an implementation-dependent endianness, and the bytevector elements following that BOM encode the given subtext or substring using that endianness.

Rationale: These procedures are consistent with the Unicode standard. Unicode suggests UTF-16 should default to big-endian, but Microsoft prefers little-endian.

(utf8->text bytevector start end)  $\rightarrow text$ text library procedure  $(utf8->text\ bytevector) \rightarrow text$ text library procedure (utf16->text bytevector start end)  $\rightarrow$  text text library procedure  $(utf16->text\ bytevector) \rightarrow text$ text library procedure (utf16be->text bytevector start end)  $\rightarrow$  text text library procedure  $(utf16be->text\ bytevector) \rightarrow text$ text library procedure  $(utf16le->text\ butevector\ start\ end) \rightarrow text$ text library procedure  $(utf16le->text\ bytevector) \rightarrow text$ text library procedure

These procedures interpret their bytevector argument as a UTF-8 or UTF-16 encoding of a sequence of characters, and return a text containing that sequence.

The bytevector subrange given to utf16->text may begin with a byte order mark (BOM); if so, that BOM determines whether the rest of the subrange is to be interpreted as big-endian or little-endian; in either case, the BOM will not become a character in the returned text. If the subrange does not begin with a BOM, it is decoded using the same implementation-dependent endianness used by textual->utf16.

The utf16be->text and utf16le->text procedures interpret their inputs as big-endian or little-endian, respectively. If a BOM is present, it is treated as a normal character and will become part of the result.

It is an error if the bytevector subrange given to utf8->text contains invalid UTF-8 byte sequences. For the other three procedures, it is an error if start or end are odd, or if the bytevector subrange contains invalid UTF-16 byte sequences.

### Selection

(text-length text)  $\rightarrow len$ 

text library procedure

Returns the number of characters within the given text. Must execute in O(1) time.

(text-ref text idx)  $\rightarrow char$ 

text library procedure

Returns character text(@idx@), using 0-origin indexing. Must execute in O(1) time.

(textual-length textual)  $\rightarrow len$ (textual-ref textual idx)  $\rightarrow char$  text library procedure text library procedure

textual-length returns the number of characters in textual, and textual-ref returns the character at character index idx, using 0-origin indexing. These procedures are the generalizations of text-length and text-ref to accept strings as well as texts. If textual is a text, they must execute in O(1) time, but there is no such requirement if textual is a string.

Rationale: These procedures may be more convenient than the text-only versions, but compilers may generate faster code for calls to the text-only versions.

(subtext  $text \ start \ end$ )  $\rightarrow text$ (subtextual  $textual \ start \ end$ )  $\rightarrow text$  text library procedure text library procedure

These procedures return a text containing the characters of text or textual beginning with index start (inclusive) and ending with index end (exclusive).

If textual is a string, then that string does not share any storage with the result, so subsequent mutation of that string will not affect the text returned by subtextual. When the first argument is a text, as is required by subtext, implementations are encouraged to return a result that shares storage with that text, to whatever extent sharing is possible while maintaining some small fixed bound on the ratio of storage used by the shared representation divided by the storage that would be used by an unshared representation. In particular, these procedures should just return their first argument when that argument is a text, start is 0, and end is the length of that text.

```
(textual-copy textual (@start end@)) \rightarrow text
```

text library procedure

Returns a text containing the characters of textual beginning with index start (inclusive) and ending with index end (exclusive).

Unlike subtext and subtextual, the result of textual-copy never shares substructures that would retain characters or sequences of characters that are substructures of its first argument or previously allocated objects.

If textual-copy returns an empty text, that empty text may be eq? or eqv? to the text returned by (text). If the text returned by textual-copy is non-empty, then it is not eqv? to any previously extant object.

```
\begin{array}{lll} (\text{textual-take} \ \ textual \ \ nchars) \rightarrow text & \text{text library procedure} \\ (\text{textual-drop} \ \ textual \ \ nchars) \rightarrow text & \text{text library procedure} \\ (\text{textual-take-right} \ \ \ textual \ \ nchars) \rightarrow text & \text{text library procedure} \\ (\text{textual-drop-right} \ \ \ textual \ \ nchars) \rightarrow text & \text{text library procedure} \\ \end{array}
```

textual-take returns a text containing the first nchars of textual; textual-drop returns a text containing all but the first nchars of textual. textual-take-right returns a text containing the last nchars of textual; textual-drop-right returns a text containing all but the last nchars of textual.

If textual is a string, then that string does not share any storage with the result, so subsequent mutation of that string will not affect the text returned by these procedures. If textual is a text, implementations are encouraged to return a result that shares storage with that text (which is easily accomplished by using subtext to create the result).

```
(textual-take "Pete Szilagyi" 6) => «Pete S»
(textual-drop "Pete Szilagyi" 6) => «zilagyi»

(textual-take-right "Beta rules" 5) => «rules»
(textual-drop-right "Beta rules" 5) => «Beta »
```

It is an error to take or drop more characters than are in the text:

"325" 5) => « 325»

```
(textual-take "foo" 37) => error
```

(textual-pad

```
(textual-pad textual len char start end) \rightarrow texttext library procedure(textual-pad textual len) \rightarrow texttext library procedure(textual-pad-right textual len char start end) \rightarrow texttext library procedure(textual-pad-right textual len) \rightarrow texttext library procedure
```

Returns a text of length len comprised of the characters drawn from the given subrange of textual, padded on the left (right) by as many occurrences of the character char as needed. If textual has more than len chars, it is truncated on the left (right) to length len. char defaults to #\space.

If textual is a string, then that string does not share any storage with the result, so subsequent mutation of that string will not affect the text returned by these procedures. If textual is a text, implementations are encouraged to return a result that shares storage with that text whenever sharing would be space-efficient.

Returns a text obtained from the given subrange of textual by skipping over all characters on the left / on the right / on both sides that satisfy the second argument pred: pred defaults to char-whitespace?.

If textual is a string, then that string does not share any storage with the result, so subsequent mutation of that string will not affect the text returned by these procedures. If textual is a text, implementations are encouraged to return a result that shares storage with that text whenever sharing would be space-efficient.

```
(textual-trim-both " The outlook wasn't brilliant, \n\r")
=> «The outlook wasn't brilliant,»
```

# Replacement

```
(textual-replace textual1 textual2 start1 end1 start2 end2) \rightarrow text text library procedure (textual-replace textual1 textual2 start1 end1) \rightarrow text text library procedureReturns (textual-append (subtextual textual1 0 start1) (subtextual textual2 start2 end2) (subtextual textual1 end1 (textual-length textual1)))
```

That is, the segment of characters in textual 1 from start 1 to end 1 is replaced by the segment of characters in textual 2 from start 2 to end 2. If start 1=end 1, this simply splices the characters drawn from textual 2 into textual 1 at that position.

Examples:

# Comparison

```
(textual=? textual1 \ textual2 \ textual3 \dots ) \rightarrow boolean
```

text library procedure

Returns #t if all the texts have the same length and contain exactly the same characters in the same positions; otherwise returns #f.

```
(textual<? textual1 textual2 textual3 ...) \rightarrow booleantext library procedure(textual>? textual1 textual2 textual3 ...) \rightarrow booleantext library procedure(textual<=? textual1 textual2 textual3 ...) \rightarrow booleantext library procedure(textual>=? textual1 textual2 textual3 ...) \rightarrow booleantext library procedure
```

These procedures return #t if their arguments are (respectively): monotonically increasing, monotonically decreasing, monotonically non-decreasing, or monotonically non-increasing.

These comparison predicates are required to be transitive.

These procedures compare texts in an implementation-defined way. One approach is to make them the lexicographic extensions to texts of the corresponding orderings on characters. In that case, text<? would be the lexicographic ordering on texts induced by the ordering char<? on characters, and if two texts differ in length but are the same up to the length of the shorter text, the shorter text would be considered to be lexicographically less than the longer string. However, implementations are also allowed to use more sophisticated locale-specific orderings.

In all cases, a pair of texts must satisfy exactly one of textual<?, textual=?, and textual>?, must satisfy textual<=? if and only if they do not satisfy textual>?, and must satisfy textual>=? if and only if they do not satisfy textual<?.

Note: Implementations are encouraged to use the same orderings for texts as are used by the corresponding comparisons on strings, but are allowed to use different orderings.

Rationale: The only portable way to ensure these comparison predicates use the same orderings used by the corresponding comparisons on strings is to convert all texts to strings, which would be unacceptably inefficient.

```
(textual-ci=? textual1 \ textual2 \ textual3 \dots) \rightarrow boolean
```

text library procedure

Returns #t if, after calling textual-foldcase on each of the arguments, all of the case-folded texts would have the same length and contain the same characters in the same positions; otherwise returns #f.

```
(textual-ci<? textual1 \ textual2 \ textual3 \ ...) \rightarrow boolean
                                                                                                                    text library procedure
(textual-ci>? textual1 \ textual2 \ textual3 \ ...) \rightarrow boolean
                                                                                                                    text library procedure
(textual-ci<=? textual1 \ textual2 \ textual3 \dots) \rightarrow boolean
                                                                                                                    text library procedure
(textual-ci>=? textual1 \ textual2 \ textual3 \dots) \rightarrow boolean
                                                                                                                    text library procedure
```

These procedures behave as though they had called textual-foldcase on their arguments before applying the corresponding procedures without "-ci".

#### Prefixes & suffixes

(textual-prefix-length	textual 1	$textual2 \ start1 \ end1 \ start2 \ end2) \rightarrow integer$	text library procedure
(textual-prefix-length	textual 1	$textual2) \rightarrow integer$	text library procedure
(textual-suffix-length	textual 1	$textual2 \ start1 \ end1 \ start2 \ end2) \rightarrow integer$	text library procedure
(textual-suffix-length	textual 1	$textual2) \rightarrow integer$	text library procedure

Return the length of the longest common prefix/suffix of textual1 and textual2. For prefixes, this is equivalent to their "mismatch index" (relative to the start indexes).

The optional start/end indexes restrict the comparison to the indicated subtexts of textual and textual 2.

```
(textual-prefix? textual1 textual2 start1 end1 start2 end2) \rightarrow boolean
                                                                                                          text library procedure
(textual-prefix? textual1 \ textual2) \rightarrow boolean
                                                                                                          text library procedure
(textual-suffix? textual1 textual2 start1 end1 start2 end2) \rightarrow boolean
                                                                                                          text library procedure
(textual-suffix? textual1 \ textual2) \rightarrow boolean
                                                                                                          text library procedure
```

Is textual1 a prefix/suffix of textual2?

The optional start/end indexes restrict the comparison to the indicated subtexts of textual and textual 2.

# Searching

```
(textual-index textual pred start end) \rightarrow idx-or-false
                                                                                                            text library procedure
                                                                                                            text library procedure
(textual-index textual pred) \rightarrow idx-or-false
(textual-index-right textual pred start end) \rightarrow idx-or-false
                                                                                                            text library procedure
(textual-index-right textual\ pred) \rightarrow idx-or-false
                                                                                                            text library procedure
(textual-skip textual pred start end) \rightarrow idx-or-false
                                                                                                            text library procedure
(textual-skip textual\ pred) \rightarrow idx-or-false
                                                                                                            text library procedure
(textual-skip-right textual pred start end) \rightarrow idx-or-false
                                                                                                            text library procedure
(textual-skip-right textual\ pred) \rightarrow idx-or-false
                                                                                                           text library procedure
```

textual-index searches through the given subtext or substring from the left, returning the index of the leftmost character satisfying the predicate pred. textual-index-right searches from the right, returning the index of the rightmost character satisfying the predicate pred. If no match is found, these procedures return #f.

Rationale: The SRFI 130 analogues of these procedures return cursors, even when no match is found, and SRFI 130's string-index-right returns the successor of the cursor for the first character that satisfies the predicate. As there are no cursors in this SRFI, it seems best to follow the more intuitive and long-standing precedent set by SRFI 13.

The start and end arguments specify the beginning and end of the search; the valid indexes relevant to the search include start but exclude end. Beware of "fencepost" errors: when searching right-to-left, the first index considered is (- end 1), whereas when searching left-to-right, the first index considered is start. That is, the start/end indexes describe the same half-open interval (@start,end) in these procedures that they do in all other procedures specified by this SRFI.

The skip functions are similar, but use the complement of the criterion: they search for the first char that *doesn't* satisfy pred. To skip over initial whitespace, for example, say

These functions can be trivially composed with textual-take and textual-drop to produce take-while, drop-while, span, and break procedures without loss of efficiency.

```
\begin{array}{lll} (\texttt{textual-contains} \ \ \textit{textual1} \ \ \textit{textual2} \ \ \textit{start1} \ \ \textit{end2}) \rightarrow \textit{idx-or-false} & \texttt{text library procedure} \\ (\texttt{textual-contains} \ \ \textit{textual1} \ \ \textit{textual2}) \rightarrow \textit{idx-or-false} & \texttt{text library procedure} \\ (\texttt{textual-contains-right} \ \ \ \textit{textual2} \ \ \textit{start1} \ \ \textit{end2}) \rightarrow \textit{idx-or-false} & \texttt{text library procedure} \\ (\texttt{textual-contains-right} \ \ \ \textit{textual2}) \rightarrow \textit{idx-or-false} & \texttt{text library procedure} \\ (\texttt{textual-contains-right} \ \ \ \textit{textual2}) \rightarrow \textit{idx-or-false} & \texttt{text library procedure} \\ \end{array}
```

Does the subtext of textual specified by start1 and end1 contain the sequence of characters given by the subtext of textual2 specified by start2 and end2?

Returns #f if there is no match. If start2 = end2, textual-contains returns start1 but textual-contains-right returns end1. Otherwise returns the index in textual1 for the first character of the first/last match; that index lies within the half-open interval (@start1,end1), and the match lies entirely within the (@start1,end1) range of textual1.

```
(textual-contains "eek -- what a geek." "ee" 12 18); Searches "a geek"
=> 15
```

Note: The names of these procedures do not end with a question mark. This indicates a useful value is returned when there is a match.

#### Case conversion

```
(textual-upcase textual) \rightarrow texttext library procedure(textual-downcase textual) \rightarrow texttext library procedure(textual-foldcase textual) \rightarrow texttext library procedure(textual-titlecase textual) \rightarrow texttext library procedure
```

These procedures return the text obtained by applying Unicode's full uppercasing, lowercasing, case-folding, or title-casing algorithms to their argument. In some cases, the length of the result may be different from the length of the argument. Note that language-sensitive mappings and foldings are not used.

### Concatenation

```
(textual-append textual \dots) \rightarrow text
```

text library procedure

Returns a text whose sequence of characters is the concatenation of the sequences of characters in the given arguments.

```
(textual-concatenate textual-list) \rightarrow text
```

text library procedure

Concatenates the elements of textual-list together into a single text.

If any elements of textual-list are strings, then those strings do not share any storage with the result, so subsequent mutation of those string will not affect the text returned by this procedure. Implementations are encouraged to return a result that shares storage with some of the texts in the list if that sharing would be space-efficient.

Rationale: Some implementations of Scheme limit the number of arguments that may be passed to an n-ary procedure, so the (apply textual-append textual-list) idiom, which is otherwise equivalent to using this procedure, is not as portable.

```
(textual-concatenate-reverse textual-list final-textual end) \rightarrow text
(textual-concatenate-reverse textual-list) \rightarrow text
```

text library procedure text library procedure

With no optional arguments, calling this procedure is equivalent to

```
(textual-concatenate (reverse textual-list))
```

If the optional argument final-textual is specified, it is effectively consed onto the beginning of textual-list before performing the list-reverse and textual-concatenate operations.

If the optional argument end is given, only the characters up to but not including end in final-textual are added to the result, thus producing

```
(textual-concatenate
 (reverse (cons (subtext final-textual 0 end)
                textual-list)))
```

For example:

```
(textual-concatenate-reverse '(" must be" "Hello, I") " going.XXXX" 7)
 => «Hello, I must be going.»
```

Rationale: This procedure is useful when constructing procedures that accumulate character data into lists of textual buffers, and wish to convert the accumulated data into a single text when done. The optional end argument accommodates that use case when final-textual is a mutable string, and is allowed (for uniformity) when final-textual is an immutable text.

```
(textual-join textual-list delimiter\ grammar) \rightarrow text
(textual-join \ textual-list) \rightarrow text
```

text library procedure text library procedure

This procedure is a simple unparser; it pastes texts together using the delimiter text.

textual-list is a list of texts and/or strings. delimiter is a text or a string. The grammar argument is a symbol that determines how the delimiter is used, and defaults to 'infix. It is an error for grammar to be any symbol other than these four:

- 'infix means an infix or separator grammar: insert the delimiter between list elements. An empty list will produce
- 'strict-infix means the same as 'infix if the textual-list is non-empty, but will signal an error if given an empty list. (This avoids an ambiguity shown in the examples below.)
- 'suffix means a suffix or terminator grammar: insert the delimiter after every list element.
- 'prefix means a prefix grammar: insert the delimiter before every list element.

The delimiter is the text used to delimit elements; it defaults to a single space "".

```
(textual-join '("foo" "bar" "baz"))
        => «foo bar baz»
(textual-join '("foo" "bar" "baz") "")
        => «foobarbaz»
(textual-join '("foo" "bar" "baz") «:»)
        => <foo:bar:baz>
(textual-join '("foo" "bar" "baz") ":" 'suffix)
```

```
=> <foo:bar:baz:>
;; Infix grammar is ambiguous wrt empty list vs. empty text:
(textual-join '()
                    ":") => «»
(textual-join '("") ":") => «»
;; Suffix and prefix grammars are not:
(textual-join '() ":" 'suffix)) => «»
(textual-join '("") ":" 'suffix)) => «:»
Fold & map & friends
(textual-fold kons knil textual start end) \rightarrow value
                                                                                          text library procedure
(textual-fold kons \ knil \ textual) \rightarrow value
                                                                                          text library procedure
(textual-fold-right kons knil textual start end) \rightarrow value
                                                                                          text library procedure
(textual-fold-right kons \ knil \ textual) \rightarrow value
                                                                                          text library procedure
These are the fundamental iterators for texts.
The textual-fold procedure maps the kons procedure across the given text or string from left to right:
(... (kons textual[2] (kons textual[1] (kons textual[0] knil))))
In other words, textual-fold obeys the (tail) recursion
  (textual-fold kons knil textual start end)
= (textual-fold kons (kons textual[start] knil) start+1 end)
The textual-fold-right procedure maps kons across the given text or string from right to left:
(kons textual[0]
       (... (kons textual[end-3]
                   (kons textual[end-2]
                         (kons textual[end-1]
                                knil)))))
obeying the (tail) recursion
  (textual-fold-right kons knil textual start end)
= (textual-fold-right kons (kons textual[end-1] knil) start end-1)
Examples:
;;; Convert a text or string to a list of chars.
(textual-fold-right cons '() textual)
;;; Count the number of lower-case characters in a text or string.
(textual-fold (lambda (c count)
                  (if (char-lower-case? c)
                      (+ count 1)
                      count))
               0
               textual)
```

(textual-map proc textual1 textual2 ...)  $\rightarrow$  text

The textual-fold-right combinator is sometimes called a "catamorphism."

text library procedure

It is an error if proc does not accept as many arguments as the number of textual arguments passed to textual-map, does not accept characters as arguments, or returns a value that is not a character, string, or text.

The textual-map procedure applies proc element-wise to the characters of the textual arguments, converts each value returned by proc to a text, and returns the concatenation of those texts. If more than one textual argument is given and not all have the same length, then textual-map terminates when the shortest textual argument runs out. The dynamic order in which proc is called on the characters of the textual arguments is unspecified, as is the dynamic order in which the coercions are performed. If any strings returned by proc are mutated after they have been returned and before the call to textual-map has returned, then textual-map returns a text with unspecified contents; the textual-map procedure itself does not mutate those strings.

## Example:

```
(textual-map (lambda (c0 c1 c2)
               (case c0
                ((#\1) c1)
                ((\#\2) (string c2))
                ((#\-) (text #\- c1))))
             (string->text "1222-1111-2222")
             (string->text "Hi There!")
             (string->text "Dear John"))
    => «Hear-here!»
```

(textual-for-each proc textual1 textual2 ...)  $\rightarrow$  unspecified

text library procedure

It is an error if proc does not accept as many arguments as the number of textual arguments passed to textual-map or does not accept characters as arguments.

The textual-for-each procedure applies proc element-wise to the characters of the textual arguments, going from left to right. If more than one textual argument is given and not all have the same length, then textual-for-each terminates when the shortest textual argument runs out.

```
(textual-map-index proc textual start end) \rightarrow text
                                                                                                            text library procedure
(textual-map-index proc\ textual) \rightarrow text
                                                                                                            text library procedure
```

Calls proc on each valid index of the specified subtext or substring, converts the results of those calls into texts, and returns the concatenation of those texts. It is an error for proc to return anything other than a character, string, or text. The dynamic order in which proc is called on the indexes is unspecified, as is the dynamic order in which the coercions are performed. If any strings returned by proc are mutated after they have been returned and before the call to textual-map-index has returned, then textual-map-index returns a text with unspecified contents; the textual-map-index procedure itself does not mutate those strings.

```
(textual-for-each-index proc textual start end) \rightarrow unspecified
                                                                                                         text library procedure
(textual-for-each-index proc\ textual) \rightarrow unspecified
                                                                                                         text library procedure
```

Calls proc on each valid index of the specified subtext or substring, in increasing order, discarding the results of those calls. This is simply a safe and correct way to loop over a subtext or substring.

# Example:

```
(let ((txt (string->text "abcde"))
       (v '()))
  (textual-for-each-index
    (lambda (cur) (set! v (cons (char->integer (text-ref txt cur)) v)))
    txt)
 v) \Rightarrow (101\ 100\ 99\ 98\ 97)
(textual-count textual pred start end) \rightarrow integer
                                                                                                 text library procedure
(textual-count textual pred) \rightarrow integer
                                                                                                 text library procedure
```

Returns a count of the number of characters in the specified subtext of textual that satisfy the given predicate.

text library procedure text library procedure text library procedure text library procedure

Filter the given subtext of textual, retaining only those characters that satisfy / do not satisfy pred.

If textual is a string, then that string does not share any storage with the result, so subsequent mutation of that string will not affect the text returned by these procedures. If textual is a text, implementations are encouraged to return a result that shares storage with that text whenever sharing would be space-efficient.

# Replication & splitting

```
(textual-replicate textual from to start end) \rightarrow text (textual-replicate textual from to) \rightarrow text
```

text library procedure text library procedure

This is an "extended subtext" procedure that implements replicated copying of a subtext or substring.

textual is a text or string; start and end are optional arguments that specify a subtext of textual, defaulting to 0 and the length of textual. This subtext is conceptually replicated both up and down the index space, in both the positive and negative directions. For example, if textual is "abcdefg", start is 3, and end is6, then we have the conceptual bidirectionally-infinite text

```
... d e f d e f d e f d e f d e f d e f d + +2 +3 +4 +5 +6 +7 +8 +9
```

textual-replicate returns the subtext of this text beginning at index from, and ending at to. It is an error if from is greater than to.

You can use textual-replicate to perform a variety of tasks:

- To rotate a text left: (textual-replicate "abcdef" 2 8) => «cdefab»
- To rotate a text right: (textual-replicate "abcdef" -2 4) => «efabcd»
- To replicate a text: (textual-replicate "abc" 0 7) => «abcabca»

Note that

- The from/to arguments give a half-open range containing the characters from index from up to, but not including, index to
- The from/to indexes are not expressed in the index space of textual. They refer instead to the replicated index space of the subtext defined by textual, start, and end.

It is an error if start=end, unless from=to, which is allowed as a special case.

```
(textual-split textual delimiter grammar limit start end) \rightarrow list textual-split textual delimiter) \rightarrow list textual
```

text library procedure text library procedure

Returns a list of texts representing the words contained in the subtext of textual from start (inclusive) to end (exclusive). The delimiter is a text or string to be used as the word separator. This will often be a single character, but multiple characters are allowed for use cases such as splitting on "\r\n". The returned list will have one more item than the number of non-overlapping occurrences of the delimiter in the text. If delimiter is an empty text, then the returned list contains a list of texts, each of which contains a single character.

The grammar is a symbol with the same meaning as in the textual-join procedure. If it is infix, which is the default, processing is done as described above, except an empty textual produces the empty list; if grammar is strict-infix, then an empty textual signals an error. The values prefix and suffix cause a leading/trailing empty text in the result to be suppressed.

If limit is a non-negative exact integer, at most that many splits occur, and the remainder of textual is returned as the final element of the list (so the result will have at most limit+1 elements). If limit is not specified or is #f, then as many splits as possible are made. It is an error if limit is any other value.

To split on a regular expression re, use SRFI 115's regexp-split procedure:

```
(map string->text (regexp-split re (textual->string txt)))
```

Rationale: Although it would be more efficient to have a version of regexp-split that operates on texts directly, the scope of this SRFI is limited to specifying operations on texts analogous to those specified for strings by R7RS and SRFI 130.

## References & links

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[MIT-Scheme] http://www.swiss.ai.mit.edu/projects/scheme/

[R5RS] Revised<sup>5</sup> report on the algorithmic language Scheme.

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[R6RSlibraries] Revised<sup>6</sup> report on the algorithmic language Scheme — Standard Libraries.

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[R6RS-Rationale] Revised<sup>6</sup> report on the algorithmic language Scheme — Rationale.

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[R7RS] Revised<sup>7</sup> report on the algorithmic language Scheme.

A. Shinn, J. Cowan, A. Gleckler (editors).

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[SRFI] The SRFI web site.

http://srfi.schemers.org/

[SRFI-13] O. Shivers.

SRFI-13: String libraries.

http://srfi.schemers.org/srfi-13/

[**SRFI-130**] J. Cowan.

SRFI-130: Cursor-based string library.

http://srfi.schemers.org/srfi-130/

[**DesignNotes**] W. D. Clinger.

Immutable texts.

(This reference consists of rough design notes for the sample implementations. This reference should be removed before the SRFI is finalized.)

[Unicode] The Unicode Consortium. Unicode. http://unicode.org/

## 6. Laziness

### Generators

[Red Edition item 12] What generator library should R7RS-large provide?

SRFI 121 is a collection of routines for manipulating generators, which are nullary procedures that are invoked repeatedly to generate a sequence of values. They provide lightweight laziness.

This SRFI defines utility procedures that create, transform, and consume generators. A generator is simply a procedure with no arguments that works as a source of a series of values. Every time it is called, it yields a value. Generators may be finite or infinite; a finite generator returns an end-of-file object to indicate that it is exhausted. For example, read-char, read-line, and read are generators that generate characters, lines, and objects from the current input port. Generators provide lightweight laziness.

The names described in this section comprise the (scheme generator) library.

Generators can be divided into two classes, finite and infinite. Both kinds of generators can be invoked an indefinite number of times. After a finite generator has generated all its values, it will return an end-of-file object for all subsequent calls. A generator is said to be *exhausted* if calling it will return an end-of-file object. By definition, infinite generators can never be exhausted.

A generator is said to be in an *undefined state* if it cannot be determined exactly how many values it has generated. This arises because it is impossible to tell by inspecting a generator whether it is exhausted or not. For example, (generator-fold + 0 (generator 1 2 3) (generator 1 2)) will compute 0 + 1 + 1 + 2 + 2 = 6, at which time the second generator will be exhausted. If the first generator is invoked, however, it may return either 3 or an end-of-file object, depending on whether the implementation of generator-fold has invoked it or not. Therefore, the first generator is said to be in an undefined state.

#### Generator constructors

The result of a generator constructor is just a procedure, so printing it doesn't show much. In the examples in this section we use generator->list to convert the generator to a list.

These procedures have names ending with generator.

(generator->list (make-iota-generator 3 8))

```
(generator arg \dots) \rightarrow generator
```

generator library procedure

The simplest finite generator. Generates each of its arguments in turn. When no arguments are provided, it returns an empty generator that generates no values.

```
\begin{array}{ll} (\texttt{make-iota-generator} & \texttt{count} & \texttt{start} & \texttt{step}) \rightarrow \texttt{generator} \\ (\texttt{make-iota-generator} & \texttt{count} & \texttt{start}) \rightarrow \texttt{generator} \\ (\texttt{make-iota-generator} & \texttt{count}) \rightarrow \texttt{generator} \\ \end{array}
```

Creates a finite generator of a sequence of count numbers. The sequence begins with start (which defaults to 0) and increases by step (which defaults to 1). If both start and step are exact, it generates exact numbers; otherwise it generates inexact numbers. The exactness of count doesn't affect the exactness of the results.

```
(8 9 10)

(generator->list (make-iota-generator 3 8 2))

(8 10 12)

(make-range-generator start end step) → generator

(make-range-generator start end) → generator

(make-range-generator start) → generator

(make-range-generator start) → generator

(make-range-generator start) → generator
```

Creates a generator of a sequence of numbers. The sequence begins with start, increases by step (default 1), and continues while the number is less than end, or forever if end is omitted. If both start and step are exact, it generates exact numbers; otherwise it generates inexact numbers. The exactness of end doesn't affect the exactness of the results.

```
(generator->list (make-range-generator 3) 4)
    (3 4 5 6)
(generator->list (make-range-generator 3 8))
    (3 4 5 6 7)
(generator->list (make-range-generator 3 8 2))
    (3 5 7)
```

 $(make-coroutine-generator proc) \rightarrow generator$ 

generator library procedure

Creates a generator from a coroutine.

The proc argument is a procedure that takes one argument, yield. When called, make-coroutine-generator immediately returns a generator g. When g is called, proc runs until it calls yield. Calling yield causes the execution of proc to be suspended, and g returns the value passed to yield.

Whether this generator is finite or infinite depends on the behavior of proc. If proc returns, it is the end of the sequence — g returns an end-of-file object from then on. The return value of proc is ignored.

The following code creates a generator that produces a series 0, 1, and 2 (effectively the same as (make-range-generator 0 3) and binds it to g.

```
(define g
  (make-coroutine-generator
   (lambda (yield) (let loop ((i 0))
                  (when (< i 3) (yield i) (loop (+ i 1)))))))
(generator->list g) (0 1 2)
(list>generator lis) \rightarrow generator
                                                                                               generator library procedure
(vector>generator vec\ start\ end) \rightarrow generator
                                                                                               generator library procedure
(vector>generator vec\ start) \rightarrow generator
                                                                                               generator library procedure
                                                                                               generator library procedure
(vector>generator vec) \rightarrow generator
                                                                                               generator library procedure
(reverse-vector>generator vec\ start\ end) \rightarrow generator
(reverse-vector>generator vec\ start) \rightarrow generator
                                                                                               generator library procedure
(reverse-vector>generator vec) \rightarrow generator
                                                                                               generator library procedure
(string>generator str\ start\ end) \rightarrow generator
                                                                                               generator library procedure
(string>generator str\ start) \rightarrow generator
                                                                                               generator library procedure
(string>generator str) \rightarrow generator
                                                                                               generator library procedure
(bytevector>generator bytevector start end) \rightarrow generator
                                                                                               generator library procedure
(bytevector>generator bytevector start) \rightarrow generator
                                                                                               generator library procedure
(bytevector)\rightarrow generator
                                                                                               generator library procedure
```

These procedures return generators that yield each element of the given argument. Mutating the underlying object will affect the results of the generator.

```
(generator->list (list->generator '(1 2 3 4 5)))
    (1 2 3 4 5)
(generator->list (vector->generator '#(1 2 3 4 5)))
    (1 2 3 4 5)
(generator->list (reverse-vector->generator '#(1 2 3 4 5)))
    (5 4 3 2 1)
(generator->list (string->generator "abcde"))
    (#\a #\b #\c #\d #\e)
```

The generators returned by the constructors are exhausted once all elements are retrieved; the optional start-th and end-th arguments can limit the range the generator walks across.

For reverse-vector->generator, the first value is the element right before the end-th element, and the last value is the start-th element. For all the other constructors, the first value the generator yields is the start-th element, and it ends right before the end-th element.

```
(generator->list (vector->generator '#(a b c d e) 2))
    (c d e)
(generator->list (vector->generator '#(a b c d e) 2 4))
    (c d)
(generator->list (reverse-vector->generator '#(a b c d e) 2))
    (e d c)
(generator->list (reverse-vector->generator '#(a b c d e) 2 4))
    (d c)
(generator->list (reverse-vector->generator '#(a b c d e) 2 4))
    (d c)
(generator->list (reverse-vector->generator '#(a b c d e) 0 2))
    (b a)
```

```
(make-for-each-generator for-each obj) \rightarrow generator
```

generator library procedure

A generator constructor that converts any collection obj to a generator that returns its elements using a for-each procedure appropriate for obj. This must be a procedure that when called as (for-each proc obj) calls proc on each element of obj. Examples of such procedures are for-each, string-for-each, and vector-for-each from R7RS. The value returned by for-each is ignored. The generator is finite if the collection is finite, which would typically be the case.

The collections need not be conventional ones (lists, strings, etc.) as long as *for-each* can invoke a procedure on everything that counts as a member. For example, the following procedure allows for-each-generator to generate the digits of an integer from least to most significant:

```
(define (for-each-digit proc n)
  (when (> n 0)
    (let-values (((div rem) (truncate/ n 10)))
        (proc rem)
        (for-each-digit proc div))))
```

(make-unfold-generator stop? mapper successor seed) →

generator library procedure

A generator constructor similar to SRFI 1's unfold.

The stop? predicate takes a seed value and determines whether to stop. The mapper procedure calculates a value to be returned by the generator from a seed value. The successor procedure calculates the next seed value from the current seed value.

For each call of the resulting generator, stop? is called with the current seed value. If it returns true, then the generator returns an end-of-file object. Otherwise, it applies mapper to the current seed value to get the value to return, and uses successor to update the seed value.

This generator is finite unless stop? never returns true.

### Generator operations

The following procedures accept one or more generators and return a new generator without consuming any elements from the source generator(s). In general, the result will be a finite generator if the arguments are.

The names of these procedures are prefixed with g.

```
(gcons* item ... gen) \rightarrow generator
```

generator library procedure

Returns a generator that adds items in front of gen. Once the items have been consumed, the generator is guaranteed to tail-call gen.

```
(generator->list (gcons* 'a 'b (make-range-generator 0 2)))
  (a b 0 1)
```

```
(gappend gen \dots) \rightarrow generator
```

generator library procedure

Returns a generator that yields the items from the first given generator, and once it is exhausted, from the second generator, and so on.

(gcombine  $proc \ seed \ gen \ gen_2 \ ...) \rightarrow$ 

generator library procedure

# TODO clarify this

A generator for mapping with state. It yields a sequence of sub-folds over proc.

The proc argument is a procedure that takes as many arguments as the input generators plus one. It is called as (proc  $v_1$   $v_2$  ...seed), where  $v_1$ ,  $v_2$ , ...are the values yielded from the input generators, and seed is the current seed value. It must return two values, the yielding value and the next seed. The result generator is exhausted when any of the  $gen_n$  generators is exhausted, at which time all the others are in an undefined state.

```
(gfilter pred\ gen) \rightarrow generator
(gremove pred\ gen) \rightarrow generator
```

generator library procedure generator library procedure

Return generators that yield the items from the source generator, except those on which pred answers false or true respectively.

```
(gtake gen \ k \ padding) \rightarrow generator
(gtake gen \ k) \rightarrow generator
(gdrop gen \ k) \rightarrow generator
```

generator library procedure generator library procedure generator library procedure

These are generator analogues of SRFI 1 take and drop. Gtake returns a generator that yields (at most) the first k items of the source generator, while gdrop returns a generator that skips the first k items of the source generator.

These won't complain if the source generator is exhausted before generating k items. By default, the generator returned by **gtake** terminates when the source generator does, but if you provide the padding argument, then the returned generator will yield exactly k items, using the padding value as needed to provide sufficient additional values.

```
(gtake-while pred\ gen) \rightarrow generator (gdrop-while pred\ gen) \rightarrow generator
```

generator library procedure generator library procedure

The generator analogues of SRFI-1 take-while and drop-while. The generator returned from gtake-while yields items from the source generator as long as pred returns true for each. The generator returned from gdrop-while first reads and discards values from the source generator while pred returns true for them, then starts yielding items returned by the source.

```
(gdelete item \ gen =) \rightarrow generator
(gdelete item \ gen) \rightarrow generator
```

generator library procedure generator library procedure

Creates a generator that returns whatever gen returns, except for any items that are the same as item in the sense of =, which defaults to equal?. The = predicate is passed exactly two arguments, of which the first was generated by gen before the second.

```
(generator->list (gdelete 3 (generator 1 2 3 4 5 3 6 7)))
(1 2 4 5 6 7)
```

```
(gdelete-neighbor-dups gen = ) \rightarrow generator
(gdelete-neighbor-dups gen) \rightarrow generator
```

generator library procedure generator library procedure

Creates a generator that returns whatever gen returns, except for any items that are equal to the preceding item in the sense of =, which defaults to equal?. The = predicate is passed exactly two arguments, of which the first was generated by gen before the second.

```
(generator->list
  (gdelete-neighbor-dups
    (list->generator '(a a b c a a a d c))))
    (a b c a d c)
```

```
(gindex value-gen index-gen) \rightarrow generator
```

generator library procedure

Creates a generator that returns elements of value-gen specified by the indices (non-negative exact integers) generated by index-gen. It is an error if the indices are not strictly increasing, or if any index exceeds the number of elements generated by value-gen. The result generator is exhausted when either generator is exhausted, at which time the other is in an undefined state.

```
(generator->list
  (gindex
    (list->generator '(a b c d e f))
    (list->generator '(0 2 4))))
    (a c e)
```

```
(gselect value-gen truth-gen) \rightarrow generator
```

generator library procedure

Creates a generator that returns elements of value-gen that correspond to the values generated by truth-gen. If the current value of truth-gen is true, the current value of value-gen is generated, but otherwise not. The result generator is exhausted when either generator is exhausted, at which time the other is in an undefined state.

```
(generator->list
  (gselect
    (list->generator '(a b c d e f))
    (list->generator '(#t #f #f #t #t #f))))
  (a d e)
```

# Consuming generated values

Unless otherwise noted, these procedures consume all the values available from the generator that is passed to them, and therefore will not return if one or more generator arguments are infinite. They have names prefixed with generator.

```
 \begin{array}{ll} (\texttt{generator} \to \texttt{list} & \texttt{generator} \ k) \to \textit{list} \\ (\texttt{generator} \to \texttt{list} & \texttt{generator}) \to \textit{list} \end{array}
```

Reads items from generator and returns a newly allocated list of them. By default, it reads until the generator is exhausted.

If an optional argument k is given, it must be a non-negative integer, and the list ends when either k items are consumed, or *generator* is exhausted; therefore *generator* can be infinite in this case.

```
 \begin{array}{ll} \text{(generator->reverse-list} \ \ \textit{generator} \ k) \rightarrow \textit{list} & \text{generator library procedure} \\ \text{(generator->reverse-list} \ \ \textit{generator}) \rightarrow \textit{list} & \text{generator library procedure} \\ \end{array}
```

Reads items from generator and returns a newly allocated list of them in reverse order. By default, this reads until the generator is exhausted.

If an optional argument k is given, it must be a non-negative integer, and the list ends when either k items are read, or generator is exhausted; therefore generator can be infinite in this case.

```
(generator->vector generator k) \rightarrow vector
(generator->vector generator) \rightarrow vector
```

generator library procedure generator library procedure

Reads items from generator and returns a newly allocated vector of them. By default, it reads until the generator is exhausted.

If an optional argument k is given, it must be a non-negative integer, and the list ends when either k items are consumed, or *generator* is exhausted; therefore *generator* can be infinite in this case.

```
(generator->vector! vector \ at \ generator) \rightarrow integer
```

generator library procedure

Reads items from generator and puts them into vector starting at index at, until vector is full or generator is exhausted. Generator can be infinite. The number of elements generated is returned.

```
(generator->string generator k) \rightarrow string (generator->string generator) \rightarrow string
```

generator library procedure generator library procedure

Reads items from generator and returns a newly allocated string of them. It is an error if the items are not characters. By default, it reads until the generator is exhausted.

If an optional argument k is given, it must be a non-negative integer, and the string ends when either k items are consumed, or *generator* is exhausted; therefore *generator* can be infinite in this case.

```
(generator-fold proc seed gen<sub>1</sub> gen<sub>2</sub> ...) \rightarrow value
```

generator library procedure

Works like SRFI 1 fold on the values generated by the generator arguments.

When one generator is given, for each value v generated by gen, proc is called as (proc v r), where r is the current accumulated result; the initial value of the accumulated result is seed, and the return value from proc becomes the next accumulated result. When gen is exhausted, the accumulated result at that time is returned from generator-fold.

When more than one generator is given, proc is invoked on the values returned by all the generator arguments followed by the current accumulated result. The procedure terminates when any of the  $gen_n$  generators is exhausted, at which time all the others are in an undefined state.

```
(with-input-from-string "a b c d e"
  (lambda () (generator-fold cons 'z read)))
  (e d c b a . z)
```

```
(generator-for-each proc gen gen<sub>2</sub> ...) \rightarrow unspecified
```

generator library procedure

A generator analogue of for-each that consumes generated values using side effects. Repeatedly applies proc on the values yielded by gen, gen<sub>2</sub> ... until any one of the generators is exhausted. The values returned from proc are discarded. The procedure terminates when any of the  $gen_n$  generators is exhausted, at which time all the others are in an undefined state. Returns an unspecified value.

```
(generator-find pred\ qen) \rightarrow value
```

generator library procedure

Returns the first item from the generator gen that satisfies the predicate pred, or #f if no such item is found before gen is exhausted. If gen is infinite, generator-find will not return if it cannot find an appropriate item.

```
(generator-count pred\ gen) \rightarrow integer
```

generator library procedure

Returns the number of items available from the generator gen that satisfy the predicate pred.

(generator-any pred qen)  $\rightarrow value$ 

generator library procedure

TODO This returns either a value from the generator, or false. However, as a return type, value or #f looks redundant.

Applies *pred* to each item from *gen*. As soon as it yields a true value, the value is returned without consuming the rest of *gen*. If *gen* is exhausted, returns #f.

(generator-every  $pred\ gen$ )  $\rightarrow value$ 

generator library procedure

TODO value or #t?

Applies *pred* to each item from *gen*. As soon as it yields a false value, the value is returned without consuming the rest of *gen*. If *gen* is exhausted, returns the last value returned by *pred*, or #t if *pred* was never called.

(generator-unfold gen unfold arg ...)  $\rightarrow$  ???

generator library procedure

Equivalent to (unfold eof-object? (lambda (x) x) (lambda (x) (gen)) (gen) arg ...). The values of gen are unfolded into the collection that unfold creates.

The signature of the unfold procedure is (unfold stop? mapper successor seed args ...). Note that the vector-unfold and vector-unfold-right of SRFI 43 and SRFI 133 do not have this signature and cannot be used with this procedure. To unfold into a vector, use SRFI 1's unfold and then apply list->vector to the result.

```
;; Iterates over string and unfolds into
;; a list using SRFI 1 unfold
(generator-unfold
  (make-for-each-generator string-for-each "abc")
  unfold)
   (#\a #\b #\c)
```

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# Lazy sequences

[Red Edition item 13] What lazy sequence library should R7RS-large provide?

SRFI 127 is a variant of SRFI 1 for lazy sequences, which are either proper lists or lists with a generator in the tail. They provide medium-weight laziness.

Lazy sequences (or lseqs, pronounced "ell-seeks") are a generalization of lists. In particular, an lseq is either a proper list or a dotted list whose last cdr is a SRFI 121 generator. A generator is a procedure that can be invoked with no arguments in order to lazily supply additional elements of the lseq. When a generator has no more elements to return, it returns an end-of-file object. Consequently, lazy sequences cannot reliably contain end-of-file objects.

This SRFI provides a set of procedures suitable for operating on lazy sequences based on SRFI 1.

The names described in this section comprise the (scheme lseq) library.

### Procedure Index

Here is a short list of the procedures provided by this SRFI.

```
Constructors generator->lseq
```

Predicates lseq? lseq=?

Selectors lseq-car lseq-cdr lseq-first lseq-rest lseq-ref

lseq-take lseq-drop

The whole lazy sequence | lseq-realize | lseq->generator

lseq-length

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Mapping and filtering lseq-map lseq-for-each

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Searching lseq-find lseq-find-tail

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lseq-index

lseq-take-while lseq-drop-while

lseq-member lseq-memv lseq-memv

## **Specification**

The templates given below obey the following conventions for procedure formals:

lseq A lazy sequence x, y, a, b Any value object, value Any value

n, i A natural number (an integer  $\geq 0$ )

proc A procedure

pred A procedure whose return value is treated as a boolean

generator A procedure with no arguments that returns a sequence of values

= A boolean procedure taking two arguments

To interpret the examples, pretend that they are executed on a Scheme that prints lazy sequences with the syntax of lists, truncating them when they get too long.

## Constructors

Every list constructor procedure is also an lseq constructor procedure. The procedure generator->lseq constructs an lseq based on the values of a generator. In order to prepend a value to an lseq, simply use cons; to prepend more than one value, use SRFI 1's cons\*.

(generator->lseq generator)  $\rightarrow lseq$ 

lseq library procedure

Returns an Iseq whose elements are the values generated by generator. The exact behavior is as follows:

- Generator is invoked with no arguments to produce an object obj.
- If obj is an end-of-file object, the empty list is returned.
- Otherwise, a newly allocated pair whose car is obj and whose cdr is generator is returned.

(generator->lseq (make-iota-generator +inf.0 1)) => (1 2 3 ...)

# Predicates

(lseq? x)  $\rightarrow boolean$ 

lseq library procedure

Returns #t if x is an Iseq. This procedure may also return #t if x is an improper list whose last cdr is a procedure that requires arguments, since there is no portable way to examine a procedure to determine how many arguments it requires. Otherwise it returns #f.

(lseq=? 
$$elt=? lseq_1 lseq_2$$
)  $\rightarrow boolean$ 

lseq library procedure

Determines lseq equality, given an element-equality procedure. Two lseqs are equal if they are of the same length, and their corresponding elements are equal, as determined by elt=?. When elt=? is called, its first argument is always from lseq<sub>1</sub> and its second argument is from lseq<sub>2</sub>.

The dynamic order in which the elt=? procedure is applied to pairs of elements is not specified.

The elt=? procedure must be consistent with eq?. This implies that two lseqs which are eq? are always lseq=?, as well; implementations may exploit this fact to "short-cut" the element-by-element equality tests.

### Selectors

(lseq-car 
$$lseq$$
)  $\rightarrow object$   
(lseq-first  $lseq$ )  $\rightarrow object$ 

lseq library procedure lseq library procedure

These procedures are synonymous. They return the first element of Iseq. They are included for completeness, as they are the same as car. It is an error to apply them to an empty Iseq.

(lseq-cdr 
$$lseq$$
)  $\rightarrow lseq$   
(lseq-rest  $lseq$ )  $\rightarrow lseq$ 

lseq library procedure lseq library procedure

These procedures are synonymous. They return an Iseq with the contents of Iseq except for the first element. The exact behavior is as follows:

If lseq is a pair whose cdr is a procedure, then the procedure is invoked with no arguments to produce an object obj.

- If obj is an end-of-file object, then the cdr of lseq is set to the empty list, which is returned.
- If obj is any other object, then a new pair is allocated whose car is *obj* and whose cdr is the cdr of lseq (i.e. the procedure). The cdr of lseq is set to the newly allocated pair, which is returned.

If lseq is a pair whose cdr is not a procedure, then the cdr is returned.

If lseq is not a pair, it is an error.

```
(lseq-ref lseq\ i) \rightarrow value
```

lseq library procedure

Returns the ith element of lseq. (This is the same as (lseq-first (lseq-drop lseq i)).) It is an error if i >= n, where n is the length of lseq.

 $(lseq-ref '(a b c d) 2) \Rightarrow c$ 

```
(lseq-take lseq\ i) \rightarrow lseq
(lseq-drop lseq\ i) \rightarrow lseq
```

lseq library procedure lseq library procedure

lseq-take lazily returns the first i elements of lseq. lseq-drop returns all but the first i elements of lseq.

```
(lseq-take '(a b c d e) 2) \Rightarrow (a b) (lseq-drop '(a b c d e) 2) \Rightarrow (c d e)
```

lseq-drop is exactly equivalent to performing i lseq-rest operations on lseq.

### The whole lazy sequence

```
(lseq-realize lseq) \rightarrow list
```

lseq library procedure

Repeatedly applies lseq-cdr to lseq until its generator (if there is one) has been exhausted, and returns lseq, which is now guaranteed to be a proper list. This procedure can be called on an arbitrary lseq before passing it to a procedure which only accepts lists. However, if the generator never returns an end-of-file object, lseq-realize will never return.

 $(lseq->generator lseq) \rightarrow generator$ 

lseq library procedure

Returns a generator which when invoked will return all the elements of Iseq, including any that have not yet been realized.

(lseq-length olseq)  $\rightarrow integer$ 

lseq library procedure

Returns the length of its argument, which is the non-negative integer n such that lseq-rest applied n times to the lseq produces an empty lseq. lseq must be finite, or this procedure will not return.

(lseq-append  $lseq \dots$ )  $\rightarrow lseq$ 

lseq library procedure

Returns an Iseq that lazily contains all the elements of all the Iseqs in order.

(lseq-zip  $lseq_1 \ lseq_2 \ ...$ )  $\rightarrow lseq$ 

lseq library procedure

If lseq-zip is passed n lseqs, it lazily returns an lseq each element of which is an n-element list comprised of the corresponding elements from the lseqs. If any of the lseqs are finite in length, the result is as long as the shortest lseq.

```
(lseq-zip '(one two three)
     (generator->lseq (make-iota-generator +inf.0 1 1))
     (generator->lseq (make-repeating-generator) '(odd even))))
     => ((one 1 odd) (two 2 even) (three 3 odd))
(lseq-zip '(1 2 3)) => ((1) (2) (3))
```

## Mapping and filtering

(lseq-map  $proc\ lseq_1\ lseq_2\ ...) \rightarrow lseq$ 

lseq library procedure

The lseq-map procedure lazily applies proc element-wise to the corresponding elements of the lseqs, where proc is a procedure taking as many arguments as there are lseqs and returning a single value, and returns an lseq of the results in order. The dynamic order in which proc is applied to the elements of the lseqs is unspecified.

```
(lseq-for-each proc lseq_1 \ lseq_2 \ ...) \rightarrow unspecified
```

lseq library procedure

The arguments to lseq-for-each are like the arguments to lseq-map, but lseq-for-each calls proc for its side effects rather than for its values. Unlike lseq-map, lseq-for-each is guaranteed to call proc on the elements of the lseqs in order from the first element(s) to the last, and the value returned by lseq-for-each is unspecified.

If none of the lseqs are finite, lseq-for-each never returns.

```
(lseq-filter pred\ lseq) \rightarrow lseq
(lseq-remove pred\ lseq) \rightarrow lseq
```

lseq library procedure lseq library procedure

The procedure lseq-filter lazily returns an lseq that contains only the elements of lseq that satisfy pred.

The procedure lseq-remove is the same as lseq-filter, except that it returns elements that do not satisfy pred. These procedures are guaranteed to call pred on the elements of the lseqs in sequence order.

```
(lseq-filter odd? (generator->lseq (make-range-generator 1 5)))
    => (1 3)
(lseq-remove odd? (generator->lseq (make-range-generator 1 5)))
    => (2 4)
```

### Searching

The following procedures all search lseqs for the leftmost element satisfying some criterion.

```
(lseq-find pred lseq) \rightarrow value
```

lseq library procedure

Return the first element of lseq that satisfies predicate pred, or **#f** if no element does. It cannot reliably be applied to lseqs that include **#f** as an element; use **lseq-find-tail** instead. The predicate is guaranteed to be evaluated on the elements of lseq in sequence order, and only as often as necessary.

```
(lseq-find even? '(3 1 4 1 5 9 2 6)) \Rightarrow 4
```

```
(lseq-find-tail pred lseq) \rightarrow lseq or #f
```

lseq library procedure

Returns the longest tail of lseq whose first element satisfies pred, or #f if no element does. The predicate is guaranteed to be evaluated on the elements of lseq in sequence order, and only as often as necessary.

lseq-find-tail can be viewed as a general-predicate variant of the lseq-member function.

Examples:

```
(lseq-find-tail even? '(3 1 37 -8 -5 0 0)) => (-8 -5 0 0)
(lseq-find-tail even? '(3 1 37 -5)) => #f

;; equivalent to (lseq-member elt lseq)
(lseq-find-tail (lambda (elt) (equal? x elt)) lseq)
```

```
(lseq-take-while pred lseq) \rightarrow lseq
```

lseq library procedure

Lazily returns the longest initial prefix of lseq whose elements all satisfy the predicate pred.

(lseq-take-while even? '(2 18 3 10 22 9)) => (2 18)

(lseq-drop-while pred lseq)  $\rightarrow lseq$ 

lseq library procedure

Drops the longest initial prefix of lseq whose elements all satisfy the predicate pred, and returns the rest of the lseq.

```
(lseq-drop-while even? '(2 18 3 10 22 9)) => (3 10 22 9)
```

Note that lseq-drop-while is essentially lseq-find-tail where the sense of the predicate is inverted: lseq-find-tail searches until it finds an element satisfying the predicate; lseq-drop-while searches until it finds an element that doesn't satisfy the predicate.

(lseq-any  $pred\ lseq_1\ lseq_2\ ...) \rightarrow value$ 

lseq library procedure

Applies pred to successive elements of the lseqs, returning true if pred returns true on any application. If an application returns a true value, lseq-any immediately returns that value. Otherwise, it iterates until a true value is produced or one of the lseqs runs out of values; in the latter case, lseq-any returns #f. It is an error if pred does not accept the same number of arguments as there are lseqs and return a boolean result.

Note the difference between lseq-find and lseq-any—lseq-find returns the element that satisfied the predicate; lseq-any returns the true value that the predicate produced.

Like lseq-every, lseq-any's name does not end with a question mark—this is to indicate that it does not return a simple boolean (#t or #f), but a general value.

```
(lseq-any integer? '(a 3 b 2.7)) => #t
(lseq-any integer? '(a 3.1 b 2.7)) => #f
(lseq-any < '(3 1 4 1 5)
        '(2 7 1 8 2)) => #t

(define (factorial n)
  (cond
      ((< n 0) #f)
      ((= n 0) 1)
      (else (* n (factorial (- n 1))))))
(lseq-any factorial '(-1 -2 3 4))
        => 6
```

(lseq-every pred  $lseq_1 \ lseq_2 \ ...) \rightarrow value$ 

lseq library procedure

Applies pred to successive elements of the lseqs, returning true if the predicate returns true on every application. If an application returns a false value, lseq-every immediately returns that value. Otherwise, it iterates until a false value is produced or one of the lseqs runs out of values; in the latter case, lseq-every returns the last value returned by pred, or #t if pred was never invoked. It is an error if pred does not accept the same number of arguments as there are lseqs and return a boolean result.

Like lseq-any, lseq-every's name does not end with a question mark—this is to indicate that it does not return a simple boolean (#t or #f), but a general value.

```
(lseq-every factorial '(1 2 3 4))
=> 24
```

(lseq-index  $pred\ lseq_1\ lseq_2\ ...$ )  $\rightarrow integer\ or\ \#f$ 

lseq library procedure

Return the index of the leftmost element that satisfies pred.

Applies pred to successive elements of the lseqs, returning an index usable with lseq-ref if the predicate returns true. Otherwise, it iterates until one of the lseqs runs out of values, in which case #f is returned.

It is an error if pred does not accept the same number of arguments as there are lseqs and return a boolean result.

The iteration stops when one of the lseqs runs out of values; in this case, lseq-index returns #f.

```
(lseq-index even? '(3 1 4 1 5 9)) => 2
(lseq-index < '(3 1 4 1 5 9 2 5 6) '(2 7 1 8 2)) => 1
(lseq-index = '(3 1 4 1 5 9 2 5 6) '(2 7 1 8 2)) => #f
```

```
\begin{array}{ll} (\texttt{lseq-member} \ x \ \textit{lseq} \ \textit{pred}) \rightarrow \textit{lseq} & \texttt{lseq} \ \textit{library} \ \textit{procedure} \\ (\texttt{lseq-member} \ x \ \textit{lseq}) \rightarrow \textit{lseq} & \texttt{lseq} \ \textit{library} \ \textit{procedure} \\ (\texttt{lseq-mem} \ x \ \textit{lseq}) \rightarrow \textit{lseq} & \texttt{lseq} \ \textit{library} \ \textit{procedure} \\ (\texttt{lseq-memv} \ x \ \textit{lseq}) \rightarrow \textit{lseq} & \texttt{lseq} \ \textit{library} \ \textit{procedure} \\ \end{array}
```

These procedures return the longest tail of lseq whose first element is x, where the tails of lseq are the non-empty lseqs returned by (lseq-drop lseq i) for i less than the length of lseq. If x does not occur in lseq, then #f is returned. lseq-memq uses eq? to compare x with the elements of lseq, while lseq-memv uses eqv?, and lseq-member uses pred, which defaults to equal?.

The equality procedure is used to compare the elements  $e_i$  of lseq to the key x in this way: the first argument is always x, and the second argument is one of the lseq elements. Thus one can reliably find the first element of lseq that is greater than five with (lseq-member 5 lseq <)

Note that fully general lseq searching may be performed with the lseq-find-tail procedure, e.g.

(lseq-find-tail even? lseq); Find the first elt with an even key.

## Streams

[Red Edition item 14] What stream library should R7RS-large provide?

SRFI 41 provides classical streams based on delay/force. They provide heavyweight laziness. It specifies two libraries, but will be treated as just one for R7RS purposes.

TODO This SRFI uses a lot of good examples, which certainly help us to understand the library. That said, it doesn't match the style of most of the others, which tend to have few or no extended examples. I wonder if some of them should be moved to an appendix? (Of course, any example appendices must follow ALGOL 60 tradition, and include Runge-Kutta integration:).)

TODO Similarly, all of the material from **Utilities** onward is examples, performance notes, etc. Should it too be reorganized?

TODO This SRFI includes separated type signatures for the procedures. I've integrated the types into the prototypes, as per the other SRFIs, but left them in for checking. They will(?) be removed later.

TODO Terminology here is a bit different from some of the other SRFIs. How much do we want to do in smoothing things out?

Streams, sometimes called lazy lists, are a sequential data structure containing elements computed only on demand. A stream is either null or is a pair with a stream in its cdr. Since elements of a stream are computed only when accessed, streams can be infinite. Once computed, the value of a stream element is cached in case it is needed again.

TODO Delete? or move to rationale? Streams without memoization were first described by Peter Landin in 1965. Memoization became accepted as an essential feature of streams about a decade later. Today, streams are the signature data type of functional programming languages such as Haskell.

TODO Reword This Scheme Request for Implementation describes two libraries for operating on streams: a canonical set of stream primitives and a set of procedures and syntax derived from those primitives that permits convenient expression of stream operations. They rely on facilities provided by R6RS, including libraries, records, and error reporting. To load both stream libraries, say: (import (streams))

The names described in this section comprise the (scheme stream) library.

The (streams primitive) This library provides two mutually-recursive abstract data types: An object of the stream abstract data type is a promise that, when forced, is either stream-null or is an object of type stream-pair. An object of the stream-pair abstract data type contains a stream-car and a stream-cdr, which must be a stream. The essential feature of streams is the systematic suspensions of the recursive promises between the two data types.

TODO The Red Edition document says these are to be one library, so probably all evidence of there being two libraries in this version must be removed.

```
stream
:: (promise stream-null)
| (promise ( stream-pair))
stream-pair
:: (promise ) × (promise ( stream))
```

The object stored in the stream-car of a stream-pair is a promise that is forced the first time the stream-car is accessed; its value is cached in case it is needed again. The object may have any type, and different stream elements may have different types. If the stream-car is never accessed, the object stored there is never evaluated. Likewise, the stream-cdr is a promise to return a stream, and is only forced on demand.

This library provides eight operators: constructors for stream-null and stream-pairs, type recognizers for streams and the two kinds of streams, accessors for both fields of a stream-pair, and a lambda that creates procedures that return streams.

Constructors

 $(stream-null) \rightarrow stream$ 

stream library procedure

Stream-null is a promise that, when forced, is a single object, distinguishable from all other objects, that represents the null stream. Stream-null is immutable and unique.

(stream-cons object stream)  $\rightarrow$  stream

stream library syntax

Stream-cons is a macro that accepts an *object* and a *stream* and creates a newly-allocated stream containing a promise that, when forced, is a stream-pair with the *object* in its stream-car and the *stream* in its stream-cdr. Stream-cons must be syntactic, not procedural, because neither *object* nor *stream* is evaluated when stream-cons is called. Since *stream* is not evaluated, when the stream-pair is created, it is not an error to call stream-cons with a *stream* that is not of type stream; however, doing so will cause an error later when the stream-cdr of the stream-pair is accessed. Once created, a stream-pair is immutable; there is no stream-set-car! or stream-set-cdr! that modifies an existing stream-pair. There is no dotted-pair or improper stream as with lists.

Recognizers **TODO** aka predicates?

(stream?  $object) \rightarrow boolean$ 

stream library procedure

Stream? is a procedure that takes an *object* and returns #t if the *object* is a stream and #f otherwise. If *object* is a stream, stream? does not force its promise. If (stream? obj) is #t, then one of (stream-null? obj) and (stream-pair? obj) will be #t and the other will be #f; if (stream? obj) is #f, both (stream-null? obj) and (stream-pair? obj) will be #f.

## (stream-null? object) $\rightarrow boolean$

stream library procedure

Stream-null? is a procedure that takes an *object* and returns #t if the *object* is the distinguished null stream and #f otherwise. If *object* is a stream, stream-null? must force its promise in order to distinguish stream-null from stream-pair.

# (stream-pair? object) $\rightarrow boolean$

stream library procedure

Stream-pair? is a procedure that takes an *object* and returns #t if the *object* is a stream-pair constructed by stream-cons and #f otherwise. If *object* is a stream, stream-pair? must force its promise in order to distinguish stream-null from stream-pair.

Accessors

```
(stream-car stream) \rightarrow value
```

stream library procedure

Stream-car is a procedure that takes a *stream* and returns the object stored in the stream-car of the *stream*. Stream-car signals an error if the object passed to it is not a stream-pair. Calling stream-car causes the object stored there to be evaluated if it has not yet been; the object's value is cached in case it is needed again.

```
(stream-cdr stream) \rightarrow stream
```

stream library procedure

Stream-cdr is a procedure that takes a *stream* and returns the stream stored in the stream-cdr of the *stream*. Stream-cdr signals an error if the object passed to it is not a stream-pair. Calling stream-cdr does not force the promise containing the stream stored in the stream-cdr of the *stream*.

Syntactic form

```
(stream-lambda args\ body) \rightarrow procedure
```

stream library syntax

Stream-lambda creates a procedure that returns a promise to evaluate the body of the procedure. The last body expression to be evaluated must yield a stream. As with normal lambda, args may be a single variable name, in which case all the formal arguments are collected into a single list, or a list of variable names, which may be null if there are no arguments, proper if there are an exact number of arguments, or dotted if a fixed number of arguments is to be followed by zero or more arguments collected into a list. Body must contain at least one expression, and may contain internal definitions preceding any expressions to be evaluated.

### The (streams derived) library

TODO Reword to reflect it's all one lib.

The (streams derived) library provides useful procedures and syntax that depend on the primitives defined above. In the operator templates given below, an ellipsis ... indicates zero or more repetitions of the preceding subexpression and square brackets [...] indicate optional elements. In the type annotations given below, square brackets [...] refer to lists, curly braces {...} refer to streams, and nat refers to exact non-negative integers.

```
(define-stream name args body) \rightarrow unspecified???
```

stream library syntax

Define-stream creates a procedure that returns a stream, and may appear anywhere a normal define may appear, including as an internal definition, and may have internal definitions of its own, including other define-streams. The defined procedure takes arguments in the same way as stream-lambda. Define-stream is syntactic sugar on stream-lambda; see also stream-let, which is also a sugaring of stream-lambda.

A simple version of stream-map that takes only a single input stream calls itself recursively:

(define strm123 (list->stream '(1 2 3)))
; fails with divide-by-zero error
(define s (list->stream (list 1 (/ 1 0) -1)))

```
(port->stream port) \rightarrow stream (port->stream) \rightarrow stream
```

stream library procedure stream library procedure

 $port \rightarrow \{char\}$ 

Port->stream takes a *port* and returns a newly-allocated stream containing in its elements the characters on the port. If *port* is not given it defaults to the current input port. The returned stream has finite length and is terminated by stream-null.

It looks like one use of port->stream would be this:

```
(define s ;wrong!
  (with-input-from-file filename
        (lambda () (port->stream))))
```

But that fails, because with-input-from-file is eager, and closes the input port prematurely, before the first character is read. To read a file into a stream, say:

# syntax: (stream object ...)

Stream is syntax that takes zero or more *objects* and creates a newly-allocated stream containing in its elements the *objects*, in order. Since stream is syntactic, the *objects* are evaluated when they are accessed, not when the stream is created. If no *objects* are given, as in (stream), the null stream is returned. See also list->stream.

```
(define strm123 (stream 1 2 3))
```

```
; (/ 1 0) not evaluated when stream is created (define s (stream 1 (/ 1 0) -1))
```

```
 (\texttt{stream->list} \ n \ stream) \rightarrow list \\ (\texttt{stream->list} \ stream) \rightarrow list
```

stream library procedure stream library procedure

Stream->list takes a natural number n and a stream and returns a newly-allocated list containing in its elements the first n items in the stream. If the stream has less than n items all the items in the stream will be included in the returned list. If n is not given it defaults to infinity, which means that unless stream is finite stream->list will never return.

```
(stream->list 10
(stream-map (lambda (x) (* x x))
(stream-from 0)))
(0 1 4 9 16 25 36 49 64 81)
(stream-append stream ...) → stream
```

stream library procedure

```
\{\ \} \dots \rightarrow \{\ \}
```

 $\text{nat} \times \{\} \rightarrow []$ 

Stream-append returns a newly-allocated stream containing in its elements those elements contained in its input *streams*, in order of input. If any of the input *streams* is infinite, no elements of any of the succeeding input *streams* will appear in the output stream; thus, if x is infinite, (stream-append x y) x. See also stream-concat.

Quicksort can be used to sort a stream, using stream-append to build the output; the sort is lazy; so if only the beginning of the output stream is needed, the end of the stream is never sorted.

Note also that, when used in tail position as in qsort, stream-append does not suffer the poor performance of append on lists. The list version of append requires re-traversal of all its list arguments except the last each time it is called. But stream-append is different. Each recursive call to stream-append is suspended; when it is later forced, the preceding elements of the result have already been traversed, so tail-recursive loops that produce streams are efficient even when each element is appended to the end of the result stream. This also implies that during traversal of the result only one promise needs to be kept in memory at a time.

```
(stream-concat stream) \rightarrow stream
```

stream library procedure

```
\{\{\}\} \dots \to \{\}
```

Stream-concat takes a *stream* consisting of one or more streams and returns a newly-allocated stream containing all the elements of the input streams. If any of the streams in the input *stream* is infinite, any remaining streams in the input *stream* will never appear in the output stream. See also stream-append.

```
(stream->list
  (stream-concat
    (stream
          (stream 1 2) (stream) (stream 3 2 1))))
  (1 2 3 2 1)
```

The permutations of a finite stream can be determined by interleaving each element of the stream in all possible positions within each permutation of the other elements of the stream. Interleave returns a stream of streams with x inserted in each possible position of yy:

```
(define-stream (interleave x yy)
 (stream-match yy
    (() (stream (stream x)))
    ((y . ys)
      (stream-append
        (stream (stream-cons x yy))
        (stream-map
          (lambda (z) (stream-cons y z))
          (interleave x ys))))))
(define-stream (perms xs)
 (if (stream-null? xs)
      (stream (stream))
      (stream-concat
        (stream-map
          (lambda (ys)
            (interleave (stream-car xs) ys))
          (perms (stream-cdr xs))))))
```

```
(\texttt{stream-constant}\ object\ ...) \rightarrow procedure
```

stream library procedure

```
... \rightarrow \{ \}
```

Stream-constant takes one or more *objects* and returns a newly-allocated stream containing in its elements the *objects*, repeating the *objects* in succession forever.

```
 \begin{array}{ll} \mbox{(stream-constant 1)} & 1 \ 1 \ 1 \ \dots \\ \mbox{(stream-constant $\# t$ $\# f$)} & \mbox{\# t $\# f$ $\# t$ $\# f$ $\# t$ $\# f$ $\dots$} \\ \end{array}
```

```
(stream-drop n \ stream) \rightarrow procedure
```

stream library procedure

```
\mathrm{nat} \times \{\ \} \to \{\ \}
```

Stream-drop returns the suffix of the input stream that starts at the next element after the first n elements. The output stream shares structure with the input stream; thus, promises forced in one instance of the stream are also forced in the other instance of the stream. If the input stream has less than n elements, stream-drop returns the null stream. See also stream-take.

(stream-drop-while  $pred?\ stream$ )  $\rightarrow stream$ 

stream library procedure

```
(\rightarrow boolean) \times \{\} \rightarrow \{\}
```

Stream-drop-while returns the suffix of the input *stream* that starts at the first element x for which (pred? x) is #f. The output stream shares structure with the input *stream*. See also stream-take-while.

Stream-unique creates a new stream that retains only the first of any sub-sequences of repeated elements.

```
((stream-filter pred? stream) \rightarrow stream
```

stream library procedure

```
(\rightarrow boolean) \times \{\} \rightarrow \{\}
```

Stream-filter returns a newly-allocated stream that contains only those elements x of the input stream for which (pred? x) is non-#f.

```
(stream-filter odd? (stream-from 0))
    1 3 5 7 9 ...
```

```
(stream-fold proc\ base\ stream) \rightarrow value
```

stream library procedure

```
( \ \times \ \rightarrow \ ) \times \ \times \{ \ \} \rightarrow
```

Stream-fold applies a binary procedure to base and the first element of stream to compute a new base, then applies the procedure to the new base and the next element of stream to compute a succeeding base, and so on, accumulating a value that is finally returned as the value of stream-fold when the end of the stream is reached. Stream must be finite, or stream-fold will enter an infinite loop. See also stream-scan, which is similar to stream-fold, but useful for infinite streams. For readers familiar with other functional languages, this is a left-fold; there is no corresponding right-fold, since right-fold relies on finite streams that are fully-evaluated, at which time they may as well be converted to a list.

Stream-fold is often used to summarize a stream in a single value, for instance, to compute the maximum element of a stream.

```
(define (stream-maximum lt? strm)
  (stream-fold
    (lambda (x y) (if (lt? x y) y x))
    (stream-car strm)
    (stream-cdr strm)))
Sometimes, it is useful to have stream-fold defined only on non-null streams:
(define (stream-fold-one proc strm)
  (stream-fold proc
    (stream-car strm)
    (stream-cdr strm)))
Stream-minimum can then be defined as:
(define (stream-minimum lt? strm)
  (stream-fold-one
    (lambda (x y) (if (lt? x y) x y))
    strm))
Stream-fold can also be used to build a stream:
(define-stream (isort lt? strm)
    (define-stream (insert strm x)
       (stream-match strm
         (() (stream x))
         ((y . ys)
            (if (lt? y x)
                (stream-cons y (insert ys x))
                (stream-cons x strm)))))
    (stream-fold insert stream-null strm))
(stream-for-each proc stream ...) \rightarrow unspecified???
                                                                                            stream library procedure
(\times\times\times...)\times\{\}\times\{\}...
Stream-for-each applies a procedure element-wise to corresponding elements of the input streams for its side-effects; it
returns nothing. Stream-for-each stops as soon as any of its input streams is exhausted.
TODO I made the return type in the prototype "unspecified", the above ¶ should probably match that.
The following procedure displays the contents of a file:
(define (display-file filename)
  (stream-for-each display
    (file->stream filename)))
(stream-from first \ step) \rightarrow stream
                                                                                            stream library procedure
(stream-from first) \rightarrow stream
                                                                                            stream library procedure
number \times number \rightarrow \{number\}
Stream-from creates a newly-allocated stream that contains first as its first element and increments each succeeding
element by step. If step is not given it defaults to 1. First and step may be of any numeric type. Stream-from is
frequently useful as a generator in stream-of expressions. See also stream-range for a similar procedure that creates finite
```

Stream-from could be implemented as (stream-iterate (lambda (x) (+ x step)) first).

streams.

(define nats (stream-from 0))  $0\ 1\ 2$  ... (define odds (stream-from 1 2))  $1\ 3\ 5$  ...

stream library procedure

$$( \rightarrow ) \times \rightarrow \{ \}$$

Stream-iterate creates a newly-allocated stream containing base in its first element and applies proc to each element in turn to determine the succeeding element. See also stream-unfold and stream-unfolds.

```
(stream-iterate (lambda (x) (+ x 1)) 0)
    0 1 2 3 4 ...
(stream-iterate (lambda (x) (* x 2)) 1)
    1 2 4 8 16 ...
```

Given a seed between 0 and  $2^{32}$ , exclusive, the following expression creates a stream of pseudo-random integers between 0 and  $2^{32}$ , exclusive, beginning with seed, using the method described by Stephen Park and Keith Miller:

```
(stream-iterate
(lambda (x) (modulo (* x 16807) 2147483647))
seed)
```

Successive values of the continued fraction shown below approach the value of the "golden ratio" 1.618:

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \dots}}}}}$$

TODO Check that this matches the original SRFI.

The fractions can be calculated by the stream

```
(stream-iterate (lambda (x) (+1 (/x))) 1)
```

```
(stream-length stream) \rightarrow integer
```

stream library procedure

```
\{ \} \to \mathrm{nat}
```

Stream-length takes an input stream and returns the number of elements in the stream; it does not evaluate its elements. Stream-length may only be used on finite streams; it enters an infinite loop with infinite streams.

(stream-length strm123) 3

```
(stream-let tag\ ((var\ expr)\ ...)\ body) \rightarrow stream???
```

stream library syntax

TODO I'm not sure just now whether a stream-pair is a stream...so not quite sure on the return type.

Stream-let creates a local scope that binds each variable to the value of its corresponding expression. It additionally binds tag to a procedure which takes the bound variables as arguments and body as its defining expressions, binding the tag with stream-lambda. Tag is in scope within body, and may be called recursively. When the expanded expression defined by the stream-let is evaluated, stream-let evaluates the expressions in its body in an environment containing the newly-bound variables, returning the value of the last expression evaluated, which must yield a stream.

Stream-let provides syntactic sugar on stream-lambda, in the same manner as normal let provides syntactic sugar on normal lambda. However, unlike normal let, the tag is required, not optional, because unnamed stream-let is meaningless.

Stream-member returns the first stream-pair of the input strm with a stream-car x that satisfies (eql? obj x), or the null stream if x is not present in strm.

```
(stream-map proc\ stream\ ...) \rightarrow stream
```

stream library procedure

```
(\times ... \rightarrow) \times \{\} \times \{\} ... \rightarrow \{\}
```

Stream-map applies a *procedure* element-wise to corresponding elements of the input *streams*, returning a newly-allocated stream containing elements that are the results of those *procedure* applications. The output stream has as many elements as the minimum-length input *stream*, and may be infinite.

```
(define (square x) (* x x))
(stream-map square (stream 9 3)) 81 9
(define (sigma f m n)
  (stream-fold + 0
        (stream-map f (stream-range m (+ n 1)))))
(sigma square 1 100) 338350
```

In some functional languages, stream-map takes only a single input stream, and stream-zipwith provides a companion function that takes multiple input streams.

```
(stream-match stream clause ...) \rightarrow ???
```

stream library syntax

Stream-match provides the syntax of pattern-matching for streams. The input *stream* is an expression that evaluates to a stream. Clauses are of the form (*pattern* [*fender*] *expr*), consisting of a *pattern* that matches a stream of a particular shape, an optional *fender* that must succeed if the pattern is to match, and an *expression* that is evaluated if the *pattern* matches. There are four types of *patterns*:

- () Matches the null stream.
- $(pat_0 \ pat_1 \dots)$  Matches a finite stream with length exactly equal to the number of pattern elements.
- $(pat_0 \ pat_1 \dots pat_{rest})$  Matches an infinite stream, or a finite stream with length at least as great as the number of pattern elements before the literal dot.
- pat Matches an entire stream. Should always appear last in the list of clauses; it's not an error to appear elsewhere, but subsequent clauses could never match.

Each pattern element  $pat_i$  may be either:

- An identifier Matches any stream element. Additionally, the value of the stream element is bound to the variable named by the identifier, which is in scope in the *fender* and *expression* of the corresponding *clause*. Each identifier in a single pattern must be unique.
- A literal underscore Matches any stream element, but creates no bindings.

The patterns are tested in order, left-to-right, until a matching pattern is found; if fender is present, it must evaluate as non-#f for the match to be successful. Pattern variables are bound in the corresponding fender and expression. Once the matching pattern is found, the corresponding expression is evaluated and returned as the result of the match. An error is signaled if no pattern matches the input stream.

Stream-match is often used to distinguish null streams from non-null streams, binding head and tail:

```
(define (len strm)
  (stream-match strm
     (() 0)
     ((head . tail) (+ 1 (len tail)))))
```

Fenders can test the common case where two stream elements must be identical; the else pattern is an identifier bound to the entire stream, not a keyword as in cond.

```
(stream-match strm
  ((x y . _) (equal? x y) 'ok)
  (else 'error))
```

A more complex example uses two nested matchers to match two different stream arguments; (stream-merge lt? . strms) stably merges two or more streams ordered by the lt? predicate:

(stream-of  $expr\ clause\ ...$ )  $\rightarrow$  ???

stream library syntax

Stream-of provides the syntax of stream comprehensions, which generate streams by means of looping expressions. The result is a stream of objects of the type returned by expr. There are four types of clauses:

- (var in stream-expr) Loop over the elements of stream-expr, in order from the start of the stream, binding each element of the stream in turn to var. Stream-from and stream-range are frequently useful as generators for stream-expr.
- (var is expr) Bind var to the value obtained by evaluating expr.
- (pred? expr) Include in the output stream only those elements x for which (pred? x) is non-#f.

The scope of *variables* bound in the stream comprehension is the clauses to the right of the binding clause (but not the binding clause itself) plus the result expression.

When two or more generators are present, the loops are processed as if they are nested from left to right; that is, the rightmost generator varies fastest. A consequence of this is that only the first generator may be infinite and all subsequent generators must be finite. If no generators are present, the result of a stream comprehension is a stream containing the result expression; thus, (stream-of 1) produces a finite stream containing only the element 1.

```
(stream-of (* x x)
  (x in (stream-range 0 10))
  (even? x))
    0 4 16 36 64

(stream-of (list a b)
    (a in (stream-range 1 4))
    (b in (stream-range 1 3)))
        (1 1) (1 2) (2 1) (2 2) (3 1) (3 2)

(stream-of (list i j)
    (i in (stream-range 1 5))
    (j in (stream-range (+ i 1) 5)))
        (1 2) (1 3) (1 4) (2 3) (2 4) (3 4)
```

(stream-range first past step)  $\rightarrow$  stream (stream-range first past)  $\rightarrow$  stream stream library procedure stream library procedure

number  $\times$  number  $\times$  number  $\rightarrow$  {number}

Stream-range creates a newly-allocated stream that contains *first* as its first element and increments each succeeding element by *step*. The stream is finite and ends before *past*, which is not an element of the stream. If *step* is not given it

defaults to 1 if *first* is less than *past* and -1 otherwise. *First*, *past* and *step* may be of any numeric type. Stream-range is frequently useful as a generator in stream-of expressions. See also stream-from for a similar procedure that creates infinite streams.

```
(stream-range 0 10) 0 1 2 3 4 5 6 7 8 9 (stream-range 0 10 2) \rightarrow 0 2 4 6 8
```

Successive elements of the stream are calculated by adding *step* to *first*, so if any of *first*, *past* or *step* are inexact, the length of the output stream may differ from (ceiling (- (/ (- past first) step) 1).

```
(stream-ref stream n) \rightarrow value
```

stream library procedure

```
\{ \} \times \text{nat} \rightarrow
```

Stream-ref returns the nth element of stream, counting from zero. An error is signaled if n is greater than or equal to the length of stream.

```
(define (fact n)
  (stream-ref
    (stream-scan * 1 (stream-from 1))
    n))
```

```
(stream-reverse stream) \rightarrow stream
```

stream library procedure

```
\{\ \} \rightarrow \{\ \}
```

Stream-reverse returns a newly-allocated stream containing the elements of the input *stream* but in reverse order. Stream-reverse may only be used with finite streams; it enters an infinite loop with infinite streams. Stream-reverse does not force evaluation of the elements of the stream.

```
> (define s (stream 1 (/ 1 0) -1))
> (define r (stream-reverse s))
> (stream-ref r 0)
> (stream-ref r 2)
1
> (stream-ref r 1)
error: division by zero
```

```
(stream-scan proc\ base\ stream) \rightarrow stream
```

stream library procedure

```
(\times \to) \times \times \{\} \to \{\}
```

Stream-scan accumulates the partial folds of an input stream into a newly-allocated output stream. The output stream is the base followed by (stream-fold proc base (stream-take i stream)) for each of the first i elements of stream.

```
(stream-scan + 0 (stream-from 1))
  (stream 0 1 3 6 10 15 ...)
(stream-scan * 1 (stream-from 1))
  (stream 1 1 2 6 24 120 ...)
```

```
(stream-take n \ stream) \rightarrow stream
```

stream library procedure

```
\text{nat} \times \{\} \rightarrow \{\}
```

Stream-take takes a non-negative integer n and a stream and returns a newly-allocated stream containing the first n elements of the input stream. If the input stream has less than n elements, so does the output stream. See also stream-drop.

Mergesort splits a stream into two equal-length pieces, sorts them recursively and merges the results:

(stream-take-while pred? stream)  $\rightarrow stream$ 

stream library procedure

```
(\rightarrow boolean) \times \{\} \rightarrow \{\}
```

Stream-take-while takes a predicate and a *stream* and returns a newly-allocated stream containing those elements x that form the maximal prefix of the input *stream* for which (pred? x) is non-#f. See also stream-drop-while.

```
(stream-car
  (stream-reverse
    (stream-take-while
        (lambda (x) (< x 1000))
        primes))) 997</pre>
```

(stream-unfold map pred? gen base)  $\rightarrow$  stream

stream library procedure

```
(\rightarrow) \times (\rightarrow boolean) \times (\rightarrow) \times \rightarrow \{\}
```

Stream-unfold is the fundamental recursive stream constructor. It constructs a stream by repeatedly applying gen to successive values of base, in the manner of stream-iterate, then applying map to each of the values so generated, appending each of the mapped values to the output stream as long as  $(pred?\ base)$  is non-#f. See also stream-iterate and stream-unfolds.

The expression below creates the finite stream 0 1 4 9 16 25 36 49 64 81. Initially the base is 0, which is less than 10, so map squares the base and the mapped value becomes the first element of the output stream. Then gen increments the base by 1, so it becomes 1; this is less than 10, so map squares the new base and 1 becomes the second element of the output stream. And so on, until the base becomes 10, when pred? stops the recursion and stream-null ends the output stream.

```
(stream-unfold
```

```
(lambda (x) (expt x 2)) ; map
(lambda (x) (< x 10)) ; pred?
(lambda (x) (+ x 1)) ; gen
0) ; base</pre>
```

```
(stream-unfolds proc seed) \rightarrow stream ...
```

stream library procedure

```
(\rightarrow (\text{values} \times ...)) \times \rightarrow (\text{values} \{\}...)
```

Stream-unfolds returns n newly-allocated streams containing those elements produced by successive calls to the generator proc, which takes the current seed as its argument and returns n+1 values

```
(proc\ seed \rightarrow seed\ result_0\ ...\ result_{n-1})
```

where the returned seed is the input seed to the next call to the generator and  $result_i$  indicates how to produce the next element of the  $i^{th}$  result stream:

- (value) value is the next car of the result stream
- #f no value produced by this iteration of the generator proc for the result stream
- () the end of the result stream

It may require multiple calls of *proc* to produce the next element of any particular result stream. See also stream-iterate and stream-unfold.

Stream-unfolds is especially useful when writing expressions that return multiple streams. For instance, (stream-partition pred? strm) is equivalent to

```
(values
  (stream-filter pred? strm)
  (stream-filter
    (lambda (x) (not (pred? x))) strm))
but only tests pred? once for each element of strm.
(define (stream-partition pred? strm)
  (stream-unfolds
    (lambda (s)
       (if (stream-null? s)
           (values s '() '())
            (let ((a (stream-car s))
                  (d (stream-cdr s)))
              (if (pred? a)
                  (values d (list a) #f)
                  (values d #f (list a))))))
    strm))
(call-with-values
  (lambda ()
    (stream-partition odd?
       (stream-range 1 6)))
  (lambda (odds evens)
     (list (stream->list odds)
           (stream->list evens))))
    ((1 \ 3 \ 5) \ (2 \ 4))
(stream-zip stream \dots) \rightarrow stream
                                                                                            stream library procedure
\{\} \times \{\} \times ... \rightarrow \{[\quad ...]\}
```

Stream-zip takes one or more input *streams* and returns a newly-allocated stream in which each element is a list (not a stream) of the corresponding elements of the input *streams*. The output stream is as long as the shortest input *stream*, if any of the input *streams* is finite, or is infinite if all the input *streams* are infinite.

A common use of stream-zip is to add an index to a stream, as in (stream-finds  $eql?\ obj\ strm$ ), which returns all the zero-based indices in strm at which obj appears; (stream-find  $eql?\ obj\ strm$ ) returns the first such index, or #f if obj is not in strm.

```
(define-stream (stream-finds eql? obj strm)
  (stream-of (car x)
        (x in (stream-zip (stream-from 0) strm))
      (eql? obj (cadr x))))
(define (stream-find eql? obj strm)
      (stream-car
        (stream-append
            (stream-finds eql? obj strm)
            (stream #f))))
(stream-find char=? #\l
      (list->stream
        (string->list "hello"))) 2
```

```
(stream-find char=? #\l
  (list->stream
    (string->list "goodbye"))) #f
```

Stream-find is not as inefficient as it looks; although it calls stream-finds, which finds all matching indices, the matches are computed lazily, and only the first match is needed for stream-find.

### Utilities

Streams, being the signature structured data type of functional programming languages, find useful expression in conjunction with higher-order functions. Some of these higher-order functions, and their relationship to streams, are described below.

The identity and constant procedures are frequently useful as the recursive base for maps and folds; (identity obj) always returns obj, and (const obj) creates a procedure that takes any number of arguments and always returns the same obj, no matter its arguments:

```
(define (identity obj) obj)
(define (const obj) (lambda x obj))
```

Many of the stream procedures take a unary predicate that accepts an element of a stream and returns a boolean. Procedure (**negate** *pred?*) takes a unary predicate and returns a new unary predicate that, when called, returns the opposite boolean value as the original predicate.

```
(define (negate pred?)
  (lambda (x) (not (pred? x))))
```

Negate is useful for procedures like stream-take-while that take a predicate, allowing them to be used in the opposite direction from which they were written; for instance, with the predicate reversed, stream-take-while becomes stream-take-until. Stream-remove is the opposite of stream-filter:

```
(define-stream (stream-remove pred? strm)
  (stream-filter (negate pred?) strm))
```

A section is a procedure which has been partially applied to some of its arguments; for instance, (double x), which returns twice its argument, is a partial application of the multiply operator to the number 2. Sections come in two kinds: left sections partially apply arguments starting from the left, and right sections partially apply arguments starting from the right. Procedure (lsec proc args ...) takes a procedure and some prefix of its arguments and returns a new procedure in which those arguments are partially applied. Procedure (rsec proc args ...) takes a procedure and some reversed suffix of its arguments and returns a new procedure in which those arguments are partially applied.

Since most of the stream procedures take a stream as their last (right-most) argument, left sections are particularly useful in conjunction with streams.

```
(define stream-sum (lsec stream-fold + 0))
```

Function composition creates a new function by partially applying multiple functions, one after the other. In the simplest case there are only two functions, f and g, composed as ((compose f g) x); the composition can be bound to create a new function, as in (define fg (compose f g)). Procedure (compose proc ...) takes one or more procedures and returns a new procedure that performs the same action as the individual procedures would if called in succession.

Compose works with sections to create succinct but highly expressive procedure definitions. The expression to compute the squares of the integers from 1 to 10 given above at stream-unfold could be written by composing stream-map, stream-take-while, and stream-iterate:

```
((compose
  (lsec stream-map (rsec expt 2))
  (lsec stream-take-while (negate (rsec > 10)))
  (lsec stream-iterate (rsec + 1)))
1)
```

# Examples

The examples below show a few of the myriad ways streams can be exploited, as well as a few ways they can trip the unwary user. All the examples are drawn from published sources; it is instructive to compare the Scheme versions to the originals in other languages.

### Infinite streams

As a simple illustration of infinite streams, consider this definition of the natural numbers:

```
(define nats
  (stream-cons 0
      (stream-map add1 nats)))
```

The recursion works because it is offset by one from the initial stream-cons. Another sequence that uses the offset trick is this definition of the fibonacci numbers:

```
(define fibs
  (stream-cons 1
      (stream-map +
         fibs
        (stream-cdr fibs)))))
```

Yet another sequence that uses the same offset trick is the Hamming numbers, named for the mathematician and computer scientist Richard Hamming, defined as all numbers that have no prime factors greater than 5; in other words, Hamming numbers are all numbers expressible as  $2^i \cdot 3^j \cdot 5^k$ , where i, j and k are non-negative integers. The Hamming sequence starts with 1 2 3 4 5 6 8 9 10 12 and is computed starting with 1, taking 2, 3 and 5 times all the previous elements with stream-map, then merging sub-streams and eliminating duplicates.

```
(define hamming
  (stream-cons 1
        (stream-unique =
```

```
(stream-merge <
  (stream-map (lsec * 2) hamming)
  (stream-map (lsec * 3) hamming)
  (stream-map (lsec * 5) hamming)))))
```

It is possible to have an infinite stream of infinite streams. Consider the definition of power-table:

```
(define power-table
 (stream-of
    (stream-of (expt m n)
      (m in (stream-from 1)))
      (n in (stream-from 2))))
```

which evaluates to an infinite stream of infinite streams:

```
(stream
 (stream 1 4 9 16 25 ...)
 (stream 1 8 27 64 125 ...)
 (stream 1 16 81 256 625 ...)
 ...)
```

But even though it is impossible to display power-table in its entirety, it is possible to select just part of it:

```
(stream->list 10 (stream-ref power-table 1))
   (1 8 27 64 125 216 343 512 729 1000)
```

This example clearly shows that the elements of a stream are computed lazily, as they are needed; (stream-ref power-table 0) is not computed, even when its successor is displayed, since computing it would enter an infinite loop.

Chris Reade shows how to calculate the stream of prime numbers according to the sieve of Eratosthenes, using a method that eliminates multiples of the sifting base with addition rather than division:

```
(define primes (let ()
 (define-stream (next base mult strm)
    (let ((first (stream-car strm))
          (rest (stream-cdr strm)))
      (cond ((< first mult)</pre>
              (stream-cons first
                (next base mult rest)))
            ((< mult first)
              (next base (+ base mult) strm))
            (else (next base
                    (+ base mult) rest)))))
 (define-stream (sift base strm)
    (next base (+ base base) strm))
 (define-stream (sieve strm)
    (let ((first (stream-car strm))>
          (rest (stream-cdr strm)))
      (stream-cons first
        (sieve (sift first rest)))))
 (sieve (stream-from 2))))
```

A final example of infinite streams is a functional pearl from Jeremy Gibbons, David Lester and Richard Bird that enumerates the positive rational numbers without duplicates:

```
(define rats
 (stream-iterate
    (lambda (x)
      (let* ((n (floor x)) (y (- x n)))
        (/ (- n -1 y)))
   1))
```

### Backtracking via the stream of successes

Philip Wadler describes the *stream of successes* technique that uses streams to perform backtracking search. The basic idea is that each procedure returns a stream of possible results, so that its caller can decide which result it wants; an empty stream signals failure, and causes backtracking to a previous choice point. The stream of successes technique is useful because the program is written as if to simply enumerate all possible solutions; no backtracking is explicit in the code.

The Eight Queens puzzle, which asks for a placement of eight queens on a chessboard so that none of them attack any other, is an example of a problem that can be solved using the stream of successes technique. The algorithm is to place a queen in the first column of a chessboard; any column is satisfactory. Then a queen is placed in the second column, in any position not held in check by the queen in the first column. Then a queen is placed in the third column, in any position not held in check by the queens in the first two columns. And so on, until all eight queens have been placed. If at any point there is no legal placement for the next queen, backtrack to a different legal position for the previous queens, and try again.

The chessboard is represented as a stream of length m, where there are queens in the first m columns, each position in the stream representing the rank on which the queen appears in that column. For example, stream 4 6 1 5 2 8 3 7 represents the following chessboard:

### Included graphics: streams2.jpg

Two queens at column i row j and column m row n check each other if their columns i and m are the same, or if their rows j and n are the same, or if they are on the same diagonal with i + j = m + n or i - j = m - n. There is no need to test the columns, because the placement algorithm enforces that they differ, so the check? procedure tests if two queens hold each other in check.

The algorithm walks through the columns, extending position p by adding a new queen in row n with (stream-append p (stream n)). Safe? tests if it is safe to do so, using the utility procedure stream-and.

Procedure (queens m) returns all the ways that queens can safely be placed in the first m columns.

```
(define (queens m)
  (if (zero? m)
        (stream (stream))
        (stream-of (stream-append p (stream n))
            (p in (queens (- m 1)))
            (n in (stream-range 1 9))
            (safe? p n))))
```

To see the first solution to the Eight Queens problem, say

```
(stream->list (stream-car (queens 8)))
To see all 92 solutions, say
(stream->list
  (stream-map stream->list
        (queens 8)))
```

There is no explicit backtracking in the code. The stream-of expression in queens returns all possible streams that satisfy safe?; implicit backtracking occurs in the recursive call to queens.

### Generators and co-routines

It is possible to model generators and co-routines using streams. Consider the task, due to Carl Hewitt, of determining if two trees have the same sequence of leaves:

```
(same-fringe? = '(1 (2 3))'((1 2) 3)) #t
(same-fringe? = '(1 2 3)'(1 (3 2))) #f
```

The simplest solution is to flatten both trees into lists and compare them element-by-element:

That works, but requires time to flatten both trees and space to store the flattened versions; if the trees are large, that can be a lot of time and space, and if the fringes differ, much of that time and space is wasted.

Hewitt used a generator to flatten the trees one element at a time, storing only the current elements of the trees and the machines needed to continue flattening them, so same-fringe? could stop early if the trees differ. Dorai Sitaram presents both the generator solution and a co-routine solution, which both involve tricky calls to call-with-current-continuation and careful coding to keep them synchronized.

An alternate solution flattens the two trees to streams instead of lists, which accomplishes the same savings of time and space, and involves code that looks little different than the list solution presented above:

Note that streams, a data structure, replace generators or co-routines, which are control structures, providing a fine example of how lazy streams enhance modularity.

### A pipeline of procedures

Another way in which streams promote modularity is enabling the use of many small procedures that are easily composed into larger programs, in the style of unix pipelines, where streams are important because they allow a large dataset to be processed one item at a time. Bird and Wadler provide the example of a text formatter. Their example uses right-folds:

Bird and Wadler define text as a stream of characters, and develop a standard package for operating on text, which they derive mathematically (this assumes the line-separator character is a single #\newline):

```
(define (breakon a)
 (stream-lambda (x xss)
    (if (equal? a x)
        (stream-append (stream (stream)) xss)
        (stream-append
          (stream (stream-append
              (stream x) (stream-car xss)))
          (stream-cdr xss)))))
(define-stream (lines strm)
 (stream-fold-right
    (breakon #\newline)
    (stream (stream))
   strm))
(define-stream (words strm)
 (stream-filter stream-pair?
    (stream-fold-right
      (breakon #\space)
      (stream (stream))
      strm)))
```

```
(define-stream (paras strm)
  (stream-filter stream-pair?
    (stream-fold-right
      (breakon stream-null)
      (stream (stream))
      strm)))
(define (insert a)
  (stream-lambda (xs ys)
    (stream-append xs (stream a) ys)))
(define unlines
  (lsec stream-fold-right-one
    (insert #\newline)))
(define unwords
  (lsec stream-fold-right-one
    (insert #\space)))
(define unparas
  (lsec stream-fold-right-one
    (insert stream-null)))
These versatile procedures can be composed to count words, lines and paragraphs; the normalize procedure squeezes out
multiple spaces and blank lines:
(define countlines
  (compose stream-length lines))
(define countwords
  (compose stream-length
            stream-concat
            (lsec stream-map words)
           lines))
(define countparas
  (compose stream-length paras lines))
(define parse
  (compose (lsec stream-map
              (lsec stream-map words))
           paras
           lines))
(define unparse
  (compose unlines
            unparas
            (lsec stream-map
              (lsec stream-map unwords))))
(define normalize (compose unparse parse))
More useful than normalization is text-filling, which packs as many words onto each line as will fit.
(define (greedy m ws)
  (- (stream-length
       (stream-take-while (rsec <= m)
          (stream-scan
            (lambda (n word)
              (+ n (stream-length word) 1))
            -1
            ws))) 1))
```

```
(define-stream (fill m ws)
  (if (stream-null? ws)
      stream-null
      (let* ((n (greedy m ws))
             (fstline (stream-take n ws))
             (rstwrds (stream-drop n ws)))
        (stream-append
          (stream fstline)
          (fill m rstwrds)))))
(define linewords
  (compose stream-concat
           (lsec stream-map words)))
(define textparas
  (compose (lsec stream-map linewords)
           lines))
(define (filltext m strm)
  (unparse (stream-map (lsec fill m) (textparas strm))))
To display filename in lines of n characters, say:
(stream-for-each display
  (filltext n (file->stream filename)))
```

Though each operator performs only a single task, they can be composed powerfully and expressively. The alternative is to build a single monolithic procedure for each task, which would be harder and involve repetitive code. Streams ensure procedures are called as needed.

### Persistent data

Queues are one of the fundamental data structures of computer science. In functional languages, queues are commonly implemented using two lists, with the front half of the queue in one list, where the head of the queue can be accessed easily, and the rear half of the queue in reverse order in another list, where new items can easily be added to the end of a queue. The standard form of such a queue holds that the front list can only be null if the rear list is also null:

```
(define queue-null (cons '() '())
(define (queue-null? obj)
  (and (pair? obj) (null? (car obj))))
(define (queue-check f r)
  (if (null? f)
      (cons (reverse r) '())
      (cons f r)))
(define (queue-snoc q x)
  (queue-check (car q) (cons x (cdr q))))
(define (queue-head q)
  (if (null? (car q))
      (error "empty queue: head")
      (car (car q))))
(define (queue-tail q)
  (if (null? (car q))
      (error "empty-head: tail")
      (queue-check (cdr (car q)) (cdr q))))
```

Chris Okasaki points out that, if the queue is used persistently, its time-complexity rises from linear to quadratic since each persistent copy of the queue requires its own linear-time access. The problem can be fixed by implementing the front and rear parts of the queue as streams, rather than lists, and rotating one element from rear to front whenever the rear list is larger than the front list:

```
(define queue-null
 (cons stream-null stream-null))
(define (queue-null? x)
 (and (pair? x) (stream-null (car x))))
(define (queue-check f r)
 (if (< (stream-length r) (stream-length f))</pre>
      (cons f r)
      (cons (stream-append f (stream-reverse r))
            stream-null)))
(define (queue-snoc q x)
 (queue-check (car q) (stream-cons x (cdr q))))
(define (queue-head q)
 (if (stream-null? (car q))
      (error "empty queue: head")
      (stream-car (car q))))
(define (queue-tail q)
 (if (stream-null? (car q))
      (error "empty queue: tail")
      (queue-check (stream-cdr (car q))
                   (cdr q))))
```

Memoization solves the persistence problem; once a queue element has moved from rear to front, it need never be moved again in subsequent traversals of the queue. Thus, the linear time-complexity to access all elements in the queue, persistently, is restored.

### Reducing two passes to one

The final example is a lazy dictionary, where definitions and uses may occur in any order; in particular, uses may precede their corresponding definitions. This is a common problem. Many programming languages allow procedures to be used before they are defined. Macro processors must collect definitions and emit uses of text in order. An assembler needs to know the address that a linker will subsequently give to variables. The usual method is to make two passes over the data, collecting the definitions on the first pass and emitting the uses on the second pass. But Chris Reade shows how streams allow the dictionary to be built lazily, so that only a single pass is needed. Consider a stream of requests:

```
(define requests
  (stream
   '(get 3)
   '(put 1 "a") ; use follows definition
   '(put 3 "c") ; use precedes definition
   '(get 1)
   '(get 2)
   '(put 2 "b") ; use precedes definition
   '(put 4 "d"))) ; unused definition
```

We want a procedure that will display cab, which is the result of (get 3), (get 1), and (get 2), in order. We first separate the request stream into gets and puts:

```
(define (get? obj) (eq? (car obj) 'get))
(define-stream (gets strm)
  (stream-map cadr (stream-filter get? strm)))
(define-stream (puts strm)
  (stream-map cdr (stream-remove get? strm)))
```

Now, run-dict inserts each element of the puts stream into a lazy dictionary, represented as a stream of key/value pairs (an association stream), then looks up each element of the gets stream with stream-assoc:

Dict is created in the let, but nothing is initially added to it. Each time stream-assoc performs a lookup, enough of dict is built to satisfy the lookup, but no more. We are assuming that each item is defined once and only once. All that is left is to define the procedure that inserts new items into the dictionary, lazily:

```
(define-stream (build-dict puts)
  (if (stream-null? puts)
    stream-null
    (stream-cons
        (stream-car puts)
        (build-dict (stream-cdr puts)))))
```

Now we can run the requests and print the result:

```
(stream-for-each display
  (stream-map cadr (run-dict requests)))
```

The (put 4 "d") definition is never added to the dictionary because it is never needed.

#### **Pitfalls**

Programming with streams, or any lazy evaluator, can be tricky, even for programmers experienced in the genre. Programming with streams is even worse in Scheme than in a purely functional language, because, though the streams are lazy, the surrounding Scheme expressions in which they are embedded are eager. The impedance between lazy and eager can occasionally lead to astonishing results. Thirty-two years ago, William Burge warned:

For example, a simple version of stream-map that returns a stream built by applying a unary procedure to the elements of an input stream could be defined like this:

That looks right. It properly wraps the procedure in stream-lambda, and the two legs of the if both return streams, so it type-checks. But it fails because the named let binds loop to a procedure using normal lambda rather than streamlambda, so even though the first element of the result stream is lazy, subsequent elements are eager. Stream-map can be written using stream-let:

```
(define-stream (stream-map proc strm)
 (stream-let loop ((strm strm))
    (if (stream-null? strm)
       stream-null
        (stream-cons
          (proc (stream-car strm))
          (loop (stream-cdr strm))))))
```

Here, stream-let assures that each element of the result stream is properly delayed, because each is subject to the streamlambda that is implicit in stream-let, so the result is truly a stream, not a "list in disguise." Another version of this procedure was given previously at the description of define-stream.

Another common problem occurs when a stream-valued procedure requires the next stream element in its definition. Consider this definition of stream-unique:

```
(define-stream (stream-unique eql? strm); wrong!
 (stream-match strm
    (() strm)
    (( ) strm)
    ((a b . _)
      (if (eql? a b)
          (stream-unique eql?
            (stream-cdr strm))
          (stream-cons a
            (stream-unique eql?
              (stream-cdr strm)))))))
```

The (a b . \_) pattern requires the value of the next stream element after the one being considered. Thus, to compute the  $n^{\text{th}}$  element of the stream, one must know the  $n+1^{\text{st}}$  element, and to compute the  $n+1^{\text{st}}$  element, one must know the  $n+2^{\text{nd}}$  element, and to compute.... The correct version, given above in the description of stream-drop-while, only needs the current stream element.

A similar problem occurs when the stream expression uses the previous element to compute the current element:

```
(define (nat n)
 (stream-ref
    (stream-let loop ((s (stream 0)))
      (stream-cons (stream-car s)
        (loop (stream (add1 (stream-car s))))))
   n))
```

This program traverses the stream of natural numbers, building the stream as it goes. The definition is correct; (nat 15) evaluates to 15. But it needlessly uses unbounded space because each stream element holds the value of the prior stream element in the binding to s.

When traversing a stream, it is easy to write the expression in such a way that evaluation requires unbounded space, even when that is not strictly necessary. During the discussion of SRFI-40, Joe Marshall created this infamous procedure:

```
(define (times3 n)
 (stream-ref
    (stream-filter
      (lambda (x)
        (zero? (modulo x n)))
      (stream-from 0))
   3))
```

(times 3 5) evaluates to 15 and (times 3 #e1e9) evaluates to three billion, though it takes a while. In either case, times 3 should operate in bounded space, since each iteration mutates the promise that holds the next value. But it is easy to write times 3 so that it does not operate in bounded space, as the follies of SRFI-40 showed. The common problem is that some element of the stream (often the first element) is bound outside the expression that is computing the stream, so it holds the head of the stream, which holds the second element, and so on. In addition to testing the programmer, this procedure tests the stream primitives (it caught several errors during development) and also tests the underlying Scheme system (it found a bug in one implementation).

Laziness is no defense against an infinite loop; for instance, the expression below never returns, because the odd? predicate never finds an odd stream element.

```
(stream-null?
  (stream-filter odd?
        (stream-from 0 2)))
```

Ultimately, streams are defined as promises, which are implemented as thunks (lambda with no arguments). Since a stream is a procedure, comparisons such as eq?, eqv? and equal? are not meaningful when applied to streams. For instance, the expression (define s ((stream-lambda () stream-null))) defines s as the null stream, and (stream-null? s) is #t, but (eq? s stream-null) is #f. To determine if two streams are equal, it is necessary to evaluate the elements in their common prefixes, reporting #f if two elements ever differ and #t if both streams are exhausted at the same time.

It is generally not a good idea to mix lazy streams with eager side-effects, because the order in which stream elements are evaluated determines the order in which the side-effects occur. For a simple example, consider this side-effecting version of strm123:

```
(define strm123-with-side-effects
  (stream-cons (begin (display "one") 1)
      (stream-cons (begin (display "two") 2)
        (stream-cons (begin (display "three") 3)
        stream-null))))
```

The stream has elements 1 2 3. But depending on the order in which stream elements are accessed, "one", "two" and "three" could be printed in any order.

Since the performance of streams can be very poor, normal (eager) lists should be preferred to streams unless there is some compelling reason to the contrary. For instance, computing pythagorean triples with streams

```
(stream-of (list a b c)
  (n in (stream-from 1))
  (a in (stream-range 1 n))
  (b in (stream-range a n))
  (c is (- n a b))
  (= (+ (* a a) (* b b)) (* c c)))
```

(stream-ref

50)

is about two orders of magnitude slower than the equivalent expression using loops. **TODO** Explain why...what features of an implementation can make streams perform better.

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### Miscellaneous

### **Boxes**

[Red Edition item 15] What box library should R7RS-large provide? \*

SRFI 111 is a trivial library for boxes (single-slot records).

A box is a container for an object of any Scheme type, including another box. It is like a single-element vector, or half of a pair, or a direct representation of state. Boxes are normally used as minimal mutable storage, and can inject a controlled amount of mutability into an otherwise immutable data structure (or one that is conventionally treated as immutable). They can be used to implement call-by-reference semantics by passing a boxed value to a procedure and expecting the procedure to mutate the box before returning.

Boxes are objects with a single mutable state. Several Schemes have them, sometimes called *cells*. A constructor, predicate, accessor, and mutator are provided. TODO keep this  $\P$ ?

The names described in this section comprise the (scheme box) library.

### **Procedures**

The following procedures implement the box type (which is disjoint from all other Scheme types)., and are exported by the (srfi 111) library (or (srfi :111) on R6RS).

 $(box value) \rightarrow box$  box library procedure

Constructor. Returns a newly allocated box initialized to value.

((box? object)  $\rightarrow boolean$  box library procedure

Predicate. Returns #t if object is a box, and #f otherwise.

(unbox box)  $\rightarrow value$  box library procedure

Accessor. Returns the current value of box.

(set-box! box value)  $\rightarrow$  unspecified? box library procedure

Mutator. Changes box to hold value.

The behavior of boxes with the equivalence predicates eq?, eqv?, and equal? is the same as if they were implemented with records. That is, two boxes are both eq? and eqv? iff they are the product of the same call to box and not otherwise, and while they must be equal? if they are eqv?, the converse is implementation-dependent.

# Autoboxing (optional)

The following provisions of this SRFI are optional: TODO Are they optional in R7RS-Large?

- A procedure, whether system-provided or user-written, that expects a box as an argument but receives a non-box may, if appropriate, allocate a box itself that holds the value, thus providing autoboxing.
- A procedure that accepts arguments only of specified types (such as +) but receives a box instead may, if appropriate, unbox the box. Procedures that accept arguments of any type (such as cons) must not unbox their arguments.
- Calling unbox on a non-box may simply return the non-box.

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# List queues

[Red Edition item 16] What list queue library should R7RS-large provide?

SRFI 117 provides mutable half-deques with O(1) addition at both ends and O(1) deletion from the front. They are based directly on ordinary Scheme lists, and are known in other Lisps as "toonc structures".

List queues are mutable ordered collections that can contain any Scheme object. Each list queue is based on an ordinary Scheme list containing the elements of the list queue by maintaining pointers to the first and last pairs of the list. It's cheap to add or remove elements from the front of the list or to add elements to the back, but not to remove elements from the back. List queues are disjoint from other types of Scheme objects.

The names described in this section comprise the (scheme list-queue) library.

# Constructors

 $(make-list-queue\ list\ last) \rightarrow list-queue$  $(make-list-queue\ list) \rightarrow list-queue$ 

list-queue library procedure list-queue library procedure

Returns a newly allocated list queue containing the elements of list in order. The result shares storage with list. If the last argument is not provided, this operation is O(n) where n is the length of list.

However, if last is provided, make-list-queue returns a newly allocated list queue containing the elements of the list whose first pair is first and whose last pair is last. It is an error if the pairs do not belong to the same list. Alternatively, both first and last can be the empty list. In either case, the operation is O(1).

Note: To apply a non-destructive list procedure to a list queue and return a new list queue, use (make-list-queue (proc (list-queue-list list-queue))).

(list-queue element ...)  $\rightarrow$ 

list-queue library list-queue

Returns a newly allocated list queue containing the elements. This operation is O(n) where n is the number of elements.

(list-queue-copy list-queue)  $\rightarrow list$ -queue

list-queue library procedure

Returns a newly allocated list queue containing the elements of list-queue. This operation is O(n) where n is the length of list-queue.

(list-queue-unfold stop? mapper successor seed queue)  $\rightarrow list-queue$  (list-queue-unfold stop? mapper successor seed)  $\rightarrow$ 

list-queue library procedure list-queue library list-queue

Performs the following algorithm:

If the result of applying the predicate stop? to seed is true, return queue. Otherwise, apply the procedure mapper to seed, returning a value which is added to the front of queue. Then get a new seed by applying the procedure successor to seed, and repeat this algorithm.

If queue is omitted, a newly allocated list queue is used.

(list-queue-unfold-right stop? mapper successor seed queue) →

list-queue library list-queue

Performs the following algorithm:

If the result of applying the predicate stop? to seed is true, return the list queue. Otherwise, apply the procedure mapper to seed, returning a value which is added to the back of the list queue. Then get a new seed by applying the procedure successor to seed, and repeat this algorithm.

If queue is omitted, a newly allocated list queue is used.

#### **Predicates**

(list-queue? obj)  $\rightarrow boolean$ 

list-queue library procedure

Returns #t if obj is a list queue, and #f otherwise. This operation is O(1).

(list-queue-empty? list-queue)  $\rightarrow boolean$ 

list-queue library procedure

Returns #t if list-queue has no elements, and #f otherwise. This operation is O(1).

#### Accessors

(list-queue-front list-queue)  $\rightarrow v$  alue

list-queue library procedure

Returns the first element of list-queue. If the list queue is empty, it is an error. This operation is O(1).

(list-queue-back list-queue)  $\rightarrow value$ 

list-queue library procedure

Returns the last element of list-queue. If the list queue is empty, it is an error. This operation is O(1).

(list-queue-list list-queue)  $\rightarrow list$ 

list-queue library procedure

Returns the list that contains the members of list-queue in order. The result shares storage with list-queue. This operation is O(1).

(list-queue-first-last list-queue)  $\rightarrow value \ value$ 

list-queue library procedure

Returns two values, the first and last pairs of the list that contains the members of list-queue in order. If list-queue is empty, returns two empty lists. The results share storage with list-queue. This operation is O(1).

### Mutators

(list-queue-add-front! list-queue element)  $\rightarrow unspecified$ 

list-queue library procedure

Adds element to the beginning of list-queue. Returns an unspecified value. This operation is O(1).

(list-queue-add-back! list-queue element)  $\rightarrow unspecified$ 

list-queue library procedure

Adds element to the end of list-queue. Returns an unspecified value. This operation is O(1).

(list-queue-remove-front! list-queue)  $\rightarrow value$ 

list-queue library procedure

Removes the first element of list-queue and returns it. If the list queue is empty, it is an error. This operation is O(1).

(list-queue-remove-back! list-queue)  $\rightarrow value$ 

list-queue library procedure

Removes the last element of list-queue and returns it. If the list queue is empty, it is an error. This operation is O(n) where n is the length of list-queue, because queues do not not have backward links.

(list-queue-remove-all! list-queue)  $\rightarrow list$ 

list-queue library procedure

Removes all the elements of list-queue and returns them in order as a list. This operation is O(1).

(list-queue-set-list! list-queue list last)  $\rightarrow$  unspecified (list-queue-set-list! list-queue list)  $\rightarrow$  unspecified

list-queue library procedure list-queue library procedure

Replaces the list associated with list-queue with list, effectively discarding all the elements of list-queue in favor of those in list. Returns an unspecified value. This operation is O(n) where n is the length of list. If last is provided, it is treated in the same way as in make-list-queue, and the operation is O(1).

Note: To apply a destructive list procedure to a list queue, use (list-queue-set-list! (proc (list-queue-list list-queue))).

(list-queue-append list-queue ...)  $\rightarrow list$ -queue

list-queue library procedure

Returns a list queue which contains all the elements in front-to-back order from all the list-queues in front-to-back order. The result does not share storage with any of the arguments. This operation is O(n) in the total number of elements in all queues.

TODO Does this belong in a subsection entitled "Mutators"?

(list-queue-append! list-queue ...)  $\rightarrow list$ -queue

list-queue library procedure

Returns a list queue which contains all the elements in front-to-back order from all the list-queues in front-to-back order. It is an error to assume anything about the contents of the list-queues after the procedure returns. This operation is O(n) in the total number of queues, not elements. It is not part of the R7RS-small list API, but is included here for efficiency when pure functional append is not required.

(list-queue-concatenate list-of-list-queues)  $\rightarrow list-queue$ 

list-queue library procedure

Returns a list queue which contains all the elements in front-to-back order from all the list queues which are members of list-of-list-queues in front-to-back order. The result does not share storage with any of the arguments. This operation is O(n) in the total number of elements in all queues. It is not part of the R7RS-small list API, but is included here to make appending a large number of queues possible in Schemes that limit the number of arguments to apply.

### Mapping

(list-queue-map  $proc\ list-queue$ )  $\rightarrow list-queue$ 

list-queue library procedure

Applies proc to each element of list-queue in unspecified order and returns a newly allocated list queue containing the results. This operation is O(n) where n is the length of list-queue.

(list-queue-map!  $proc\ list-queue$ )  $\rightarrow list-queue$ 

list-queue library procedure

Applies proc to each element of list-queue in front-to-back order and modifies list-queue to contain the results. This operation is O(n) in the length of list-queue. It is not part of the R7RS-small list API, but is included here to make transformation of a list queue by mutation more efficient.

(list-queue-for-each  $proc\ list-queue$ )  $\rightarrow unspecified$ 

list-queue library procedure

Applies proc to each element of list-queue in front-to-back order, discarding the returned values. Returns an unspecified value. This operation is O(n) where n is the length of list-queue.

Editor: Michael Sperber

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# **Ephemerons**

[Red Edition item 17] What ephemeron library should R7RS-large provide?

SRFI 124 provides ephemerons compatible with MIT Scheme except that they are immutable. A dummy implementation for systems without GC support is also provided.

An ephemeron is an object with two components called its *key* and its *datum*. It differs from an ordinary pair as follows: if the garbage collector (GC) can prove that there are no references to the key except from the ephemeron itself and possibly from the datum, then it is free to *break* the ephemeron, dropping its reference to both key and datum. In other words, an ephemeron can be broken when nobody else cares about its key. Ephemerons can be used to construct weak vectors or lists and (possibly in combination with finalizers) weak hash tables.

Much of this specification is derived with thanks from the MIT Scheme Reference Manual.

The names described in this section comprise the (scheme ephemeron) library.

# Specification

(ephemeron?  $object) \rightarrow boolean$ 

ephemeron library procedure

Returns #t if object is an ephemeron; otherwise returns #f.

 $(make-ephemeron \ key \ datum) \rightarrow ephemeron$ 

ephemeron library procedure

Returns a newly allocated ephemeron, with components key and datum. Note that if key and datum are the same in the sense of eq?, the ephemeron is effectively a weak reference to the object.

(ephemeron-broken? ephemeron)  $\rightarrow boolean$ 

ephemeron library procedure

Returns #t if ephemeron has been broken; otherwise returns #f.

This procedure must be used with care. If it returns #f, that guarantees only that prior evaluations of ephemeron-key or ephemeron-datum yielded the key or datum that was stored in *ephemeron*. However, it makes no guarantees about subsequent calls to ephemeron-key or ephemeron-datum, because the GC may run and break the ephemeron immediately after ephemeron-broken? returns. Thus, the correct idiom to fetch an ephemeron's key and datum and use them if the ephemeron is not broken is:

```
(let ((key (ephemeron-key ephemeron))
      (datum (ephemeron-datum ephemeron)))
  (if (ephemeron-broken? ephemeron)
      ... broken case ...
      ... code using key and datum ...))
```

```
(ephemeron-key ephemeron) \rightarrow value (ephemeron-datum ephemeron) \rightarrow value
```

ephemeron library procedure ephemeron library procedure

These return the key or datum component, respectively, of *ephemeron*. If *ephemeron* has been broken, these operations return #f, but they can also return #f if that is what was stored as the key or datum.

```
(reference-barrier key) \rightarrow ???
```

ephemeron library procedure

This procedure is optional.

This procedure ensures that the garbage collector does not break an ephemeron containing an unreferenced key before a certain point in a program. The program can invoke a *reference barrier* on the key by calling this procedure, which guarantees that even if the program does not use the key, it will be considered strongly reachable until after reference-barrier returns.

TODO What does "optional" mean here? Can a conforming implementation just not export it? Or always generate an error? Is there a cond-expand feature for this?

### References

The original paper on ephemerons is Barry Hayes, "Ephemerons: a New Finalization Mechanism", Object-Oriented Languages, Programming, Systems, and Applications, 1997.

A useful implementation paper is Bruno Haible, "Weak References: Data Types and Implementation" posted 2005-04-24.

"Eliminating Cycles in Weak Tables" is about the addition of ephemeron tables to Lua 5.2. It explains how Lua's tricolor mark-sweep GC is extended to handle them, unfortunately using the  $O(N^2)$  algorithm of Hayes 1997.

"Extending Garbage Collection to Complex Data Structures" extends ephemerons, which have a fixed GC strategy, to a new data structure called blobs that explain to the GC how they are to be processed, thus allowing an arbitrary number of key-like and value-like pointers.

### Verse

TODO With all respect to gls, does this stay in the final report?

Reclaimer, spare that tree!
Take not a single bit!
It used to point to me,
Now I'm protecting it.
It was the reader's cons
That made it, paired by dot;
Now, GC, for the nonce,
Thou shalt reclaim it not.

That old familiar tree, Whose cdrs and whose cars Are spread o'er memory — And wouldst thou it unparse? GC, cease and desist! In it no free list store; Oh spare that moby list Now pointing throughout core!

It was my parent tree
When it was circular;
It pointed then to me:
I was its cadadr.
My cdr was a list,
My car a dotted pair —
That tree will sore be missed
If it remains not there.

And now I to thee point, A saving root, old friend! Thou shalt remain disjoint From free lists to the end. Old tree! The sweep still brave! And, GC, mark this well: While I exist to save, Thou shan't reclaim one cell.

The Great Quux (with apologies to George Pope Morris)

(Pedantic note: In Scheme, pairs constructed by read are officially immutable, so this scenario is technically impossible.)

Editor: Arthur A. Gleckler

# Titlecase library

[Red Edition item 18] The vote was for no titlecase library.

This section is left in as a placeholder, and will be removed later in the editing process.

# Comparators

[Red Edition item 19] What comparator library should R7RS-large provide?

SRFI 128 is a comparator library whose interface is used by SRFI 113 and SRFI 125. It was not formally balloted but was voted in based on the votes for those libraries, as (scheme comparator).

**Post-finalization note**: Because of the extremely high cost of conforming to the first and third conditions of default-hash, implementers may disregard those conditions and examine only a bounded portion of the argument.

This SRFI provides *comparators*, which bundle a type test predicate, an equality predicate, an ordering predicate, and a hash function (the last two are optional) into a single Scheme object. By packaging these procedures together, they can be treated as a single item for use in the implementation of data structures.

The names described in this section comprise the (scheme comparator) library.

The procedures in this SRFI are in the (srfi 128) library (or (srfi :128) on R6RS), but the sample implementation currently places them in the (comparators) library. This means it can't be used alongside SRFI 114, but there's no reason for anyone to do that.

### **Definitions**

A *comparator* is an object of a disjoint type. It is a bundle of procedures that are useful for comparing two objects in a total order. It is an error if any of the procedures have side effects. There are four procedures in the bundle:

- The *type test predicate* returns #t if its argument has the correct type to be passed as an argument to the other three procedures, and #f otherwise.
- The *equality predicate* returns #t if the two objects are the same in the sense of the comparator, and #f otherwise. It is the programmer's responsibility to ensure that it is reflexive, symmetric, transitive, and can handle any arguments that satisfy the type test predicate.
- The *ordering predicate* returns #t if the first object precedes the second in a total order, and #f otherwise. Note that if it is true, the equality predicate must be false. It is the programmer's responsibility to ensure that it is irreflexive, antisymmetric, transitive, and can handle any arguments that satisfy the type test predicate.
- The *hash function* takes an object and returns an exact non-negative integer. It is the programmer's responsibility to ensure that it can handle any argument that satisfies the type test predicate, and that it returns the same value on two objects if the equality predicate says they are the same (but not necessarily the converse).

It is also the programmer's responsibility to ensure that all four procedures provide the same result whenever they are applied to the same object(s) (in the sense of eqv?), unless the object(s) have been mutated since the last invocation. In particular, they must not depend in any way on memory addresses in implementations where the garbage collector can move objects in memory.

### Limitations

The comparator objects defined in this SRFI are not applicable to circular structure or to NaNs, or to objects containing any of these. Attempts to pass any such objects to any procedure defined here, or to any procedure that is part of a comparator defined here, is an error except as otherwise noted.

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• Standard hash functions:

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• Bounds and salt:

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### **Predicates**

(comparator? obj)  $\rightarrow boolean$ 

comparator library procedure

Returns #t if obj is a comparator, and #f otherwise.

(comparator-ordered? comparator)  $\rightarrow boolean$ 

comparator library procedure

Returns #t if *comparator* has a supplied ordering predicate, and #f otherwise.

(comparator-hashable? comparator)  $\rightarrow boolean$ 

comparator library procedure

Returns #t if *comparator* has a supplied hash function, and #f otherwise.

### Constructors

The following comparator constructors all supply appropriate type test predicates, equality predicates, ordering predicates, and hash functions based on the supplied arguments. They are allowed to cache their results: they need not return a newly allocated object, since comparators are pure and functional. In addition, the procedures in a comparator are likewise pure and functional.

 $(make-comparator\ type-test\ equality\ ordering\ hash) \rightarrow comparator$ 

comparator library procedure

Returns a comparator which bundles the *type-test*, *equality*, *ordering*, and *hash* procedures provided. However, if *ordering* or *hash* is #f, a procedure is provided that signals an error on application. The predicates comparator-ordered? and/or comparator-hashable?, respectively, will return #f in these cases.

Here are calls on make-comparator that will return useful comparators for standard Scheme types:

- (make-comparator boolean? boolean? (lambda (x y) (and (not x) y)) boolean-hash) will return a comparator for booleans, expressing the ordering #f < #t and the standard hash function for booleans.
- (make-comparator real? = < (lambda (x) (exact (abs x)))) will return a comparator expressing the natural ordering of real numbers and a plausible (but not optimal) hash function.
- (make-comparator string? string=? string<? string-hash) will return a comparator expressing the implementation's ordering of strings and the standard hash function.
- (make-comparator string? string-ci=? string-ci<? string-ci-hash will return a comparator expressing the implementation's case-insensitive ordering of strings and the standard case-insensitive hash function.

 $(make-pair-comparator\ car-comparator\ cdr-comparator) \rightarrow comparator$ 

comparator library procedure

This procedure returns comparators whose functions behave as follows. TODO why plural?

- The type test returns #t if its argument is a pair, if the car satisfies the type test predicate of car-comparator, and the cdr satisfies the type test predicate of cdr-comparator.
- The equality function returns #t if the cars are equal according to car-comparator and the cdrs are equal according to cdr-comparator, and #f otherwise.
- The ordering function first compares the cars of its pairs using the equality predicate of car-comparator. If they are equal, then the ordering predicate of car-comparator is applied to the cars and its value is returned. Otherwise, the predicate compares the cdrs using the equality predicate of cdr-comparator. If they are not equal, then the ordering predicate of cdr-comparator is applied to the cdrs and its value is returned.

• The hash function computes the hash values of the car and the cdr using the hash functions of car-comparator and cdr-comparator respectively and then hashes them together in an implementation-defined way.

(make-list-comparator element-comparator type-test empty? head tail)  $\rightarrow$  comparator comparator library procedure. This procedure returns comparators whose functions behave as follows: TODO plural?

- The type test returns #t if its argument satisfies type-test and the elements satisfy the type test predicate of element-comparator.
- The total order defined by the equality and ordering functions is as follows (known as lexicographic order):
  - The empty sequence, as determined by calling empty?, compares equal to itself.
  - The empty sequence compares less than any non-empty sequence.
  - Two non-empty sequences are compared by calling the head procedure on each. If the heads are not equal when compared using element-comparator, the result is the result of that comparison. Otherwise, the results of calling the tail procedure are compared recursively.
- The hash function computes the hash values of the elements using the hash function of element-comparator and then hashes them together in an implementation-defined way.

(make-vector-comparator element-comparator type-test length ref)  $\rightarrow$  comparator comparator comparator procedure This procedure returns comparators whose functions behave as follows: TODO plural?

- The type test returns #t if its argument satisfies type-test and the elements satisfy the type test predicate of element-comparator.
- The equality predicate returns #t if both of the following tests are satisfied in order: the lengths of the vectors are the same in the sense of =, and the elements of the vectors are the same in the sense of the equality predicate of element-comparator.
- The ordering predicate returns #t if the results of applying length to the first vector is less than the result of applying length to the second vector. If the lengths are equal, then the elements are examined pairwise using the ordering predicate of element-comparator. If any pair of elements returns #t, then that is the result of the list comparator's ordering predicate; otherwise the result is #f
- The hash function computes the hash values of the elements using the hash function of element-comparator and then hashes them together in an implementation-defined way.

Here is an example, which returns a comparator for byte vectors:

```
(make-vector-comparator
  (make-comparator exact-integer? = < number-hash)
  bytevector?
  bytevector-length
  bytevector-u8-ref)

(make-eq-comparator) → comparator
  (make-eqv-comparator) → comparator
  (make-equal-comparator) → comparator</pre>
```

comparator library procedure comparator library procedure comparator library procedure

These procedures return comparators whose functions behave as follows:

• The type test returns #t in all cases.

- The equality functions are eq?, eqv?, and equal? respectively.
- The ordering function is implementation-defined, except that it must conform to the rules for ordering functions. It may signal an error instead.
- The hash function is default-hash.

These comparators accept circular structure (in the case of equal-comparator, provided the implementation's equal? predicate does so) and NaNs.

### Standard hash functions

These are hash functions for some standard Scheme types, suitable for passing to make-comparator. Users may write their own hash functions with the same signature. However, if programmers wish their hash functions to be backward compatible with the reference implementation of SRFI 69, they are advised to write their hash functions to accept a second argument and ignore it.

```
\begin{array}{lll} (\mathsf{boolean-hash}\mathit{obj}) \to \mathit{integer} & \mathsf{comparator\ library\ procedure} \\ (\mathsf{char-hash}\mathit{obj}) \to \mathit{integer} & \mathsf{comparator\ library\ procedure} \\ (\mathsf{char-ci-hash}\mathit{obj}) \to \mathit{integer} & \mathsf{comparator\ library\ procedure} \\ (\mathsf{string-hash}\mathit{obj}) \to \mathit{integer} & \mathsf{comparator\ library\ procedure} \\ (\mathsf{string-ci-hash}\mathit{obj}) \to \mathit{integer} & \mathsf{comparator\ library\ procedure} \\ (\mathsf{symbol-hash}\mathit{obj}) \to \mathit{integer} & \mathsf{comparator\ library\ procedure} \\ (\mathsf{number-hash}\mathit{obj}) \to \mathit{integer} & \mathsf{comparator\ library\ procedure} \\ & \mathsf{comparator\ library\ procedure
```

These are suitable hash functions for the specified types. The hash functions char-ci-hash and string-ci-hash treat their argument case-insensitively. Note that while symbol-hash may return the hashed value of applying symbol->string and then string-hash to the symbol, this is not a requirement.

#### Bounds and salt

The following macros allow the callers of hash functions to affect their behavior without interfering with the calling signature of a hash function, which accepts a single argument (the object to be hashed) and returns its hash value. They are provided as macros so that they may be implemented in different ways: as a global variable, a SRFI 39 or R7RS parameter, or an ordinary procedure, whatever is most efficient in a particular implementation.

### $(hash-bound) \rightarrow integer$

comparator library syntax

Hash functions should be written so as to return a number between 0 and the largest reasonable number of elements (such as hash buckets) a data structure in the implementation might have. What that value is depends on the implementation. This value provides the current bound as a positive exact integer, typically for use by user-written hash functions. However, they are not required to bound their results in this way.

### $(hash-salt) \rightarrow integer$

comparator library syntax

A salt is random data in the form of a non-negative exact integer used as an additional input to a hash function in order to defend against dictionary attacks, or (when used in hash tables) against denial-of-service attacks that overcrowd certain hash buckets, increasing the amortized O(1) lookup time to O(n). Salt can also be used to specify which of a family of hash functions should be used for purposes such as cuckoo hashing. This macro provides the current value of the salt, typically for use by user-written hash functions. However, they are not required to make use of the current salt.

The initial value is implementation-dependent, but must be less than the value of (hash-bound), and should be distinct for distinct runs of a program unless otherwise specified by the implementation. Implementations may provide a means to specify the salt value to be used by a particular invocation of a hash function.

# Default comparators

 $(make-default-comparator) \rightarrow integer$ 

comparator library procedure

Returns a comparator known as a default comparator that accepts Scheme values and orders them in some implementation-defined way, subject to the following conditions:

- Given disjoint types a and b, one of three conditions must hold:
  - All objects of type a compare less than all objects of type b.
  - All objects of type a compare greater than all objects of type b.
  - All objects of both type a and type b compare equal to each other. This is not permitted for any of the Scheme types mentioned below.
- The empty list must be ordered before all pairs.
- When comparing booleans, it must use the total order #f < #t.
- When comparing characters, it must use char=? and char<?.

Note: In R5RS, this is an implementation-dependent order that is typically the same as Unicode codepoint order; in R6RS and R7RS, it is Unicode codepoint order.

- When comparing pairs, it must behave the same as a comparator returned by make-pair-comparator with default comparators as arguments.
- When comparing symbols, it must use an implementation-dependent total order. One possibility is to use the order obtained by applying symbol->string to the symbols and comparing them using the total order implied by string<?.
- When comparing bytevectors, it must behave the same as a comparator created by the expression (make-vector-comparator (make-comparator < = number-hash) bytevector? bytevector-length bytevector-u8-ref).
- When comparing numbers where either number is complex, since non-real numbers cannot be compared with <, the following least-surprising ordering is defined: If the real parts are < or >, so are the numbers; otherwise, the numbers are ordered by their imaginary parts. This can still produce somewhat surprising results if one real part is exact and the other is inexact.
- When comparing real numbers, it must use = and <.
- When comparing strings, it must use string=? and string<?.

Note: In R5RS, this is lexicographic order on the implementation-dependent order defined by char<?; in R6RS it is lexicographic order on Unicode codepoint order; in R7RS it is an implementation-defined order.

- When comparing vectors, it must behave the same as a comparator returned by (make-vector-comparator (make-default-comparator) vector? vector-length vector-ref).
- When comparing members of types registered with comparator-register-default!, it must behave in the same
  way as the comparator registered using that function.

Default comparators use default-hash as their hash function.

 $(default-hash \ obj) \rightarrow value$ 

comparator library procedure

This is the hash function used by default comparators, which accepts a Scheme value and hashes it in some implementation-defined way, subject to the following conditions:

 When applied to a pair, it must return the result of hashing together the values returned by default-hash when applied to the car and the cdr.

- When applied to a boolean, character, string, symbol, or number, it must return the same result as boolean-hash, char-hash, string-hash, symbol-hash, or number-hash respectively.
- When applied to a list or vector, it must return the result of hashing together the values returned by default-hash when applied to each of the elements.

### comparator-register-default! comparatorprocedureunspecified

Registers comparator for use by default comparators, such that if the objects being compared both satisfy the type test predicate of comparator, it will be employed by default comparators to compare them. Returns an unspecified value. It is an error if any value satisfies both the type test predicate of comparator and any of the following type test predicates: boolean?, char?, null?, pair?, symbol?, bytevector?, number?, string?, vector?, or the type test predicate of a comparator that has already been registered.

This procedure is intended only to extend default comparators into territory that would otherwise be undefined, not to override their existing behavior. In general, the ordering of calls to comparator-register-default! should be irrelevant. However, implementations that support inheritance of record types may wish to ensure that default comparators always check subtypes before supertypes.

### Accessors and Invokers

(comparator-type-test-predicate comparator)  $\rightarrow$  procedure (comparator-equality-predicate comparator)  $\rightarrow$  procedure (comparator-ordering-predicate comparator)  $\rightarrow$  procedure (comparator-hash-function comparator)  $\rightarrow$  procedure

Return the four procedures of *comparator*.

comparator library procedure comparator library procedure comparator library procedure comparator library procedure

(comparator-test-type  $comparator \ obj$ )  $\rightarrow boolean$ 

comparator library procedure

Invokes the type test predicate of *comparator* on *obj* and returns what it returns. More convenient than *comparator*-type-test-predicate, but less efficient when the predicate is called repeatedly.

(comparator-check-type  $comparator \ obj$ )  $\rightarrow boolean$ 

comparator library procedure

Invokes the type test predicate of *comparator* on *obj* and returns true if it returns true, but signals an error otherwise. More convenient than comparator-type-test-predicate, but less efficient when the predicate is called repeatedly.

TODO the return type here is misleading; if it's a boolean, then it's true. We don't have a standard way, in a prototype of saying "may signal an error". I'm not sure what to do here; my instinct is just to leave it as is.

(comparator-hash comparator obj)  $\rightarrow integer$ 

comparator library procedure

Invokes the hash function of *comparator* on obj and returns what it returns. More convenient than comparator-hash-function, but less efficient when the function is called repeatedly.

Note: No invokers are required for the equality and ordering predicates, because =? and <? serve this function.

### Comparison predicates

(=? comparator object<sub>1</sub> object<sub>2</sub> object<sub>3</sub> ...)  $\rightarrow$  boolean (<? comparator object<sub>1</sub> object<sub>2</sub> object<sub>3</sub> ...)  $\rightarrow$  boolean (>? comparator object<sub>1</sub> object<sub>2</sub> object<sub>3</sub> ...)  $\rightarrow$  boolean comparator library procedure comparator library procedure comparator library procedure

```
(<=? comparator\ object_1\ object_2\ object_3\ ...) \rightarrow boolean
(>=? comparator\ object_1\ object_2\ object_3\ ...) \rightarrow boolean
```

comparator library procedure comparator library procedure

These procedures are analogous to the number, character, and string comparison predicates of Scheme. They allow the convenient use of comparators to handle variable data types.

These procedures apply the equality and ordering predicates of comparator to the objects as follows. If the specified relation returns #t for all object<sub>i</sub> and object<sub>j</sub> where n is the number of objects and 1 <= i < j <= n, then the procedures return #t, but otherwise #f. Because the relations are transitive, it suffices to compare each object with its successor. The order in which the values are compared is unspecified.

# **Syntax**

It is an error unless <comparator> evaluates to a comparator and <object<sub>1</sub>> and <object<sub>2</sub>> evaluate to objects that the comparator can handle. If the ordering predicate returns true when applied to the values of <object<sub>1</sub>> and <object<sub>2</sub>> in that order, then <less-than> is evaluated and its value returned. If the equality predicate returns true when applied in the same way, then <equal-to> is evaluated and its value returned. If neither returns true, <greater-than> is evaluated and its value returned.

If <comparator> is omitted, a default comparator is used.

TODO remove angle brackets, use std param notation

Editor: Arthur A. Gleckler