

LightGBM:A Highly Efficient Gradient Boosting Decision Tree

王太峰 [徐静 整理]

2018/10/05



微软亚洲研究院AI头条分享

Introduction to LightGBM

Taifeng Wang (王太峰)

主管研究员

微软亚洲研究院机器学习组



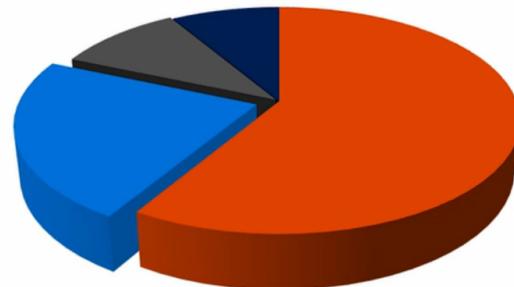
<http://dmtk.io>





LightGBM

最近微软 DMTK 团队在github上开源了性能超越其他boosting decision tree工具LightGBM，三天之内star了1000+次，fork了200+次。知乎上有近千人关注“如何看待微软开源的LightGBM？”问题，被评价为“速度惊人”，“非常有启发”，“支持分布式”，“代码清晰易懂”，“占用内存小”等。



且听来自MSRA开发团队的解读





Outline

有关GBDT的基础介绍

与已有系统的实验对比(e.g. XGBoost)

LightGBM中的优化

LightGBM的并行

动手指导与实践经验





Recall of supervised learning

- Component of supervised learning
 - Data: $[X, Y]$
 - $X = [x_1, x_2, \dots, x_n]^T, Y = [y_1, y_2, \dots, y_n]^T, x_i = [x_{i1}, x_{i2}, \dots, x_{im}]$
 - x_i is i-th training record, its label is y_i
 - x_{ij} is the j-th feature value of i-th training record.
 - Model/Function: $F(X)$
 - E.g. Linear model $F(x_i) = \sum_j w_j x_{ij}$
 - Loss Function: $L(F(X), Y) = \sum_i l(F(x_i), y_i)$
 - E.g. L2 loss: $l(F(x_i), y_i) = (F(x_i) - y_i)^2$
 - Regularization: $R(F(X))$, optional
 - E.g. L1 regularization on linear model: $R(F(X)) = \sum_j |w_j|$
- Goal of supervised learning
 - $F^*(X) = \arg \min_{F(X)} (L(F(X), Y) + R(F(x)))$

Loss function
measures how well
model fit on training
data

Regularization
measures complexity
of model





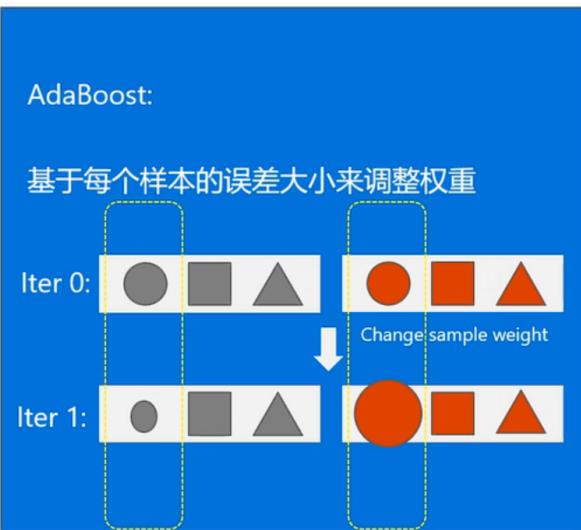
Boosting

- You can view boosting as a linear combination of many models
 - $F_m(X) = \alpha_0 f_0(X) + \alpha_1 f_1(X) + \dots + \alpha_m f_m(x)$
- It is stage-wise optimized algorithm
 - Learn F_0 , then F_1, F_2, \dots
 - Emphasizes error on each iteration
 - $L(F_m(X), Y) < L(F_{m-1}(X), Y)$
- AdaBoost
 - Emphasizes error by changing the distribution of samples
- Gradient Boosting
 - Emphasizes error by changing training targets.

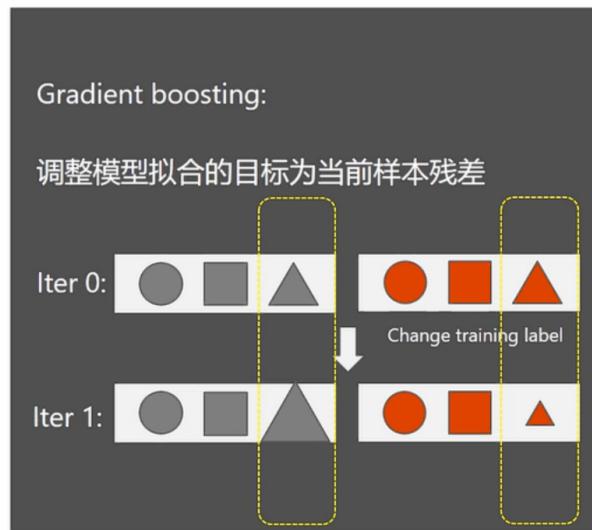




Boosting



○ :weight □ :feature △ :label





Gradient Boosting

- Basic formulation

- $F(X) = \sum_{m=0}^M f_m(X)$
- $f(X)$ is "base learner", and we use decision tree in GBDT

- How to learn?

- Greedy way

- $F_m(X) = F_{m-1}(X) + f_m(X)$
- Let $L(y, F_m(X)) < L(y, F_{m-1}(X))$

- Gradient descent:

- Get the negative gradient firstly

- $\hat{y}_i = -\partial_{F_{m-1}(x_i)} l(F_{m-1}(x_i), y_i)$

- Learn $f_m(X)$ to fit \hat{Y} by using L2 loss

- $f_m(X) = \arg \min_{f(X)} \sum_{i=1}^n (f(x_i) - \hat{y}_i)^2$

Thinking about L2 loss, $L = (y_i - F_{m-1}(x_i))^2$
then $\hat{y}_i = y_i - F_{m-1}(x_i)$





GBDT

- GBDT = Gradient Boosting + Decision Tree
- Use decision tree learner to fit gradients
- Supported tasks
 - Regression
 - Binary classification
 - pCTR task
 - Multi classification
 - Ranking
 - Lambdarank

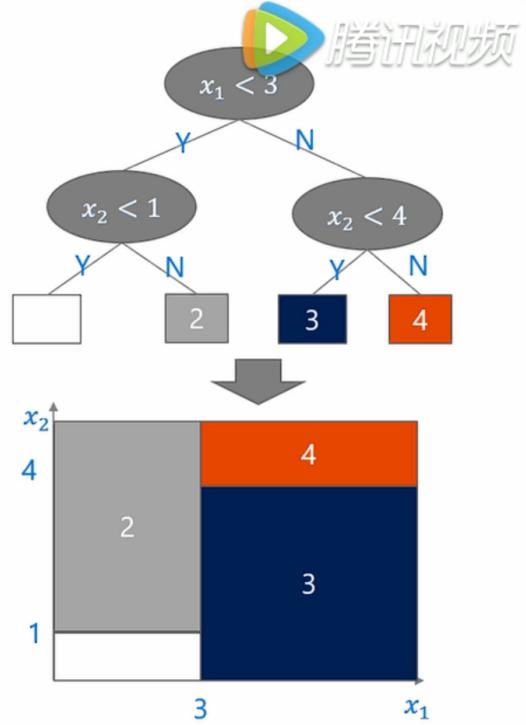
Algorithm: **GBDT**

Input: Training data (X, Y) , Iteration M ,
Loss function l , number of leaf C
 $F_0(X) = 0$
For m in $(1, M)$:
 ▷ get the training targets
 For all $(x_i, y_i) \in (X, Y)$:
 $y_i^m = -\partial_{F_{m-1}(x_i)} l(y_i, F_{m-1}(x_i))$
 ▷ use decision tree to fit targets
 $f_m(X) = \text{DecisionTree}(X, Y^m, C, L2Loss)$
 $F_m(X) = F_{m-1}(X) + f_m(X)$



Decision Tree

- Decision tree divided data into many non-overlapping regions
- Binary tree
- Components
 - Non-leaf node
 - Contain a simple decision rule(split), $\{feature, threshold\}$
 - Partition current region into two regions
 - Leaf node
 - Each x_i belongs one leaf
 - The data is same leaf means that data have similar label
 - Each leaf r_j has a output value
 - Generally, leaf output $w(r_j) = \text{Average}(\{y_i | i \in r_j\})$
- Formulation
 - $r_j = \text{loc}(x_i)$, get x_i 's leaf index (x_i is a sample)
 - $T(X) = w(\text{loc}(X))$, the output of the tree.

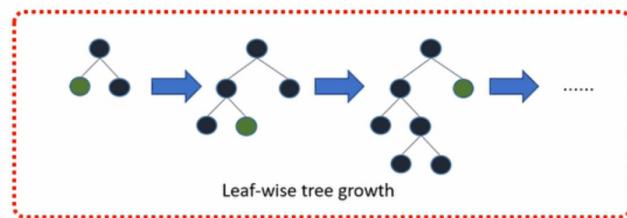




How to learn decision Tree

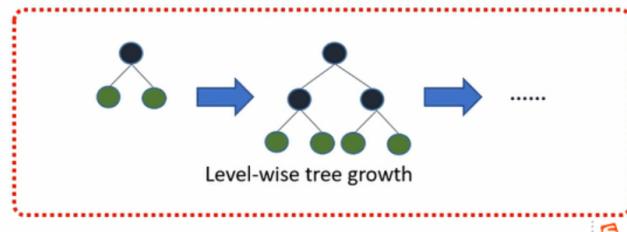
- Leaf-wise learning

- Choose a leaf (with max delta loss)
- split it into 2 leaves
- $(p_m, f_m, v_m) = \arg \min_{(p, f, v)} L(T_{m-1}(X).split(p, f, v), Y)$
- $T_m(X) = T_{m-1}(X).split(p_m, f_m, v_m)$



- Level-wise learning

- split all leaves into 2 leaves





Decision Tree Learning Algorithm

Algorithm: **DecisionTree**

Input: Training data (X, Y) , number of leaf C ,
Loss function l

▷ put all data on root

$T_1(X) = X$

For m in $(2, C)$:

▷ find best split

$(p_m, f_m, v_m) = \text{FindBestSplit}(X, Y, T_{m-1}, l)$

▷ perform split

$T_m(X) = T_{m-1}(X).split(p_m, f_m, v_m)$

Algorithm: **FindBestSplit**

Input: Training data (X, Y) , Loss function l , Current
Model $T_{m-1}(X)$

For all Leaf p in $T_{m-1}(X)$:

For all f in $X.\text{Features}$:

For all v in $f.\text{Thresholds}$:

$(left, right) = \text{partition}(p, f, v)$

$\Delta loss = L(X_p, Y_p) - L(X_{left}, Y_{left}) - L(X_{right}, Y_{right})$

if $\Delta loss > \Delta loss(p_m, f_m, v_m)$:

$(p_m, f_m, v_m) = (p, f, v)$

Main computation cost in decision
tree learning, can be further
optimized





Existing Boosted Tree Tools

- XGBoost, pGBRT, Sklearn, R.GBM
 - XGBoost beat other tools on both training speed and accuracy^[1]

Table 3: Comparison of Exact Greedy Methods with 500 trees on Higgs-1M data.

Method	Time per Tree (sec)	Test AUC
XGBoost	0.6841	0.8304
XGBoost (colsample=0.5)	0.6401	0.8245
scikit-learn	28.51	0.8302
R.gbm	1.032	0.6224

Table 4: Comparison of Learning to Rank with 500 trees on Yahoo! LTRC Dataset

Method	Time per Tree (sec)	NDCG@10
XGBoost	0.826	0.7892
XGBoost (colsample=0.5)	0.506	0.7913
pGBRT [22]	2.576	0.7915

[1] Chen, Tianqi, and Carlos Guestrin. "Xgboost: A scalable tree boosting system." *arXiv preprint arXiv:1603.02754* (2016).





Implementation of XGBoost

- Pre-sorted(exact) algorithm
 - Pros:
 - Can find exact split point
 - Cons:
 - High computation cost
 - High memory usage
 - Exact split point may cause over-fitting
- Level-wise tree growth
 - Pros:
 - Easy for multi-threading optimization
 - Can speed up pre-sorted algorithm
 - Cons:
 - Not efficient, may grow unnecessary leaf





LightGBM

- LightGBM is a gradient boosting framework. It is designed to be distributed and efficient with following advantages:
 - Fast training speed and high efficiency
 - Lower memory usage
 - Better accuracy
 - Parallel learning supported
 - Capability of handling large-scaling data
 - Support categorical feature directly
- <https://github.com/Microsoft/LightGBM>





What we do in LightGBM ?

	XGBoost	LightGBM
Tree growth algorithm	Level-wise good for engineering optimization but not efficient to learn model	Leaf-wise with max depth limitation get better trees with smaller computation cost, also can avoid overfitting
Split search algorithm	Pre-sorted algorithm	Histogram algorithm
memory cost	$2 * \#feature * \#data * 4\text{Bytes}$	$\#feature * \#data * 1\text{Bytes}$ (8x smaller)
Calculation of split gain	$O(\#data * \#features)$	$O(\#bin * \#features)$
Cache-line aware optimization	n/a	40% speed-up on Higgs data
Categorical feature support	n/a	8x speed-up on Expo data





Comparison

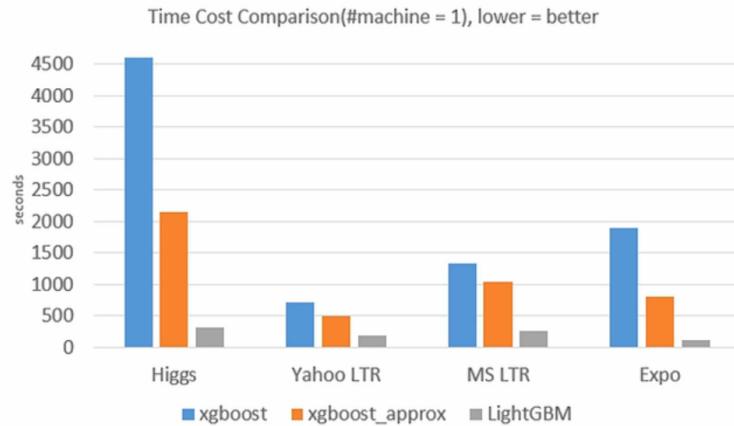
Accuracy:

Data	Metric	xgboost	xgboost_approx	LightGBM
Higgs	AUC	0.839528	0.840533	0.845123
Yahoo LTR	NDCG@5	0.740316	0.739363	0.756369
MSLTR	NDCG@5	0.476245	0.474441	0.510153
Expo	AUC	0.75548	0.757071	0.781061

Memory consumption:

Data	xgboost	xgboost_approx	LightGBM
Higgs	4.853GB	4.875GB	0.822GB
Yahoo LTR	1.907GB	2.221GB	0.831GB
MS LTR	5.469GB	5.600GB	0.745GB
Expo	1.553GB	1.560GB	0.450GB

Speed:





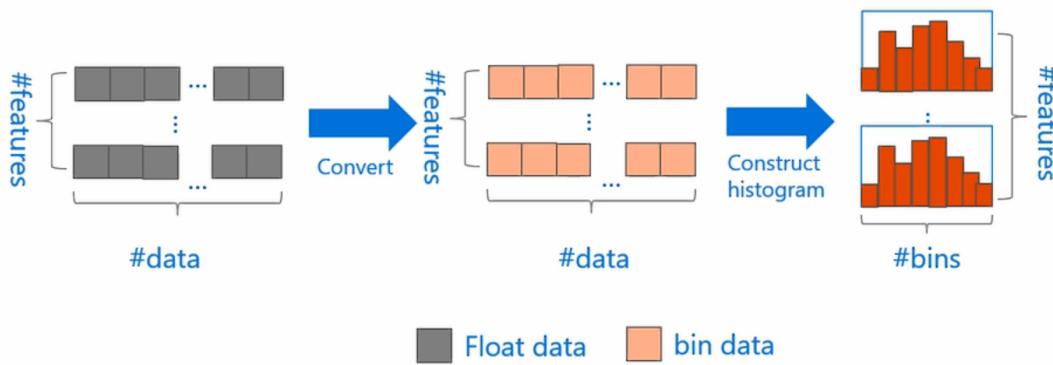
Detail Optimizations





Histogram optimization

- Compression of feature
- Map continues values to discrete values(called "bin")
 - E.g. [0,0.1) -> 0, [0.1,0.3)->1, ...





Histogram optimization

Convert feature value to bin
before training

Use bin to index histogram, not
need to sort

Reduce computation cost of
split gain

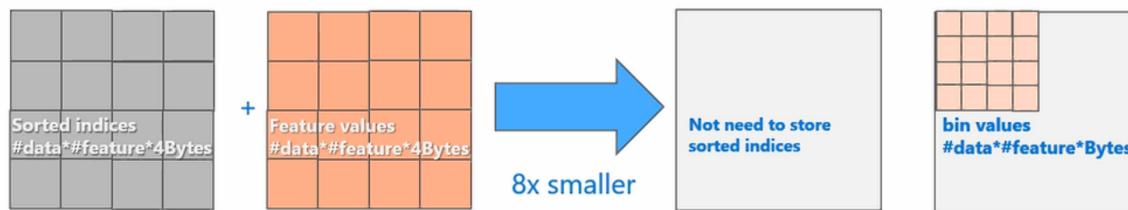
```
Algorithm: FindBestSplitByHistogram
Input: Training data X , Current Model  $T_{c-1}(X)$ 
       First order gradient G, second order gradient H
For all Leaf p in  $T_{c-1}(X)$ :
  For all f in X.Features:
    ▷ construct histogram
    H = new Histogram()
    For i in (0, num_of_row) //go through all the data row
      H[f.bins[i]].g += g_i; H[f.bins[i]].n += 1
    ▷ find best split from histogram
    For i in (0, len(H)): //go through all the bins
      S_L += H[i].g; n_L += H[i].n
      S_R = S_P - S_L; n_R = n_P - n_L
      Δloss =  $\frac{S_L^2}{n_L} + \frac{S_R^2}{n_R} - \frac{S_P^2}{n_P}$ 
      if Δloss > Δloss(p_m, f_m, v_m):
        (p_m, f_m, v_m) = (p, f, H[i].value)
```





Memory usage optimization

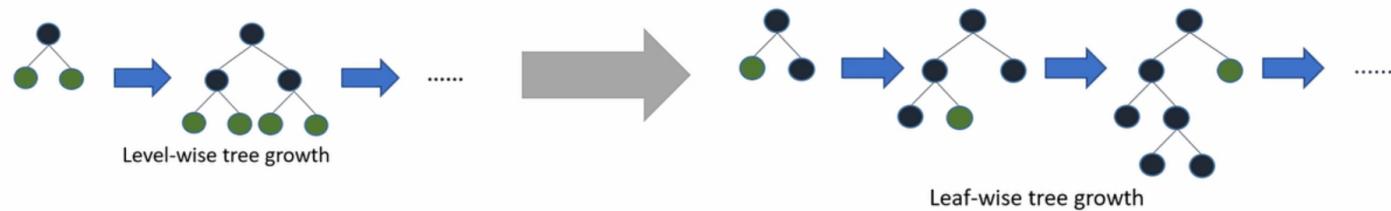
- Only need to save bin values.
- If #bins is small, can use small data type, e.g. uint8_t, to store training data





Leaf-wise with max depth limitation

- Use leaf-wise to grow trees efficiently
 - Can reduce more loss when growing same #leaves
- Use max depth to avoid growing too deep tree and overfitting





Histogram subtraction

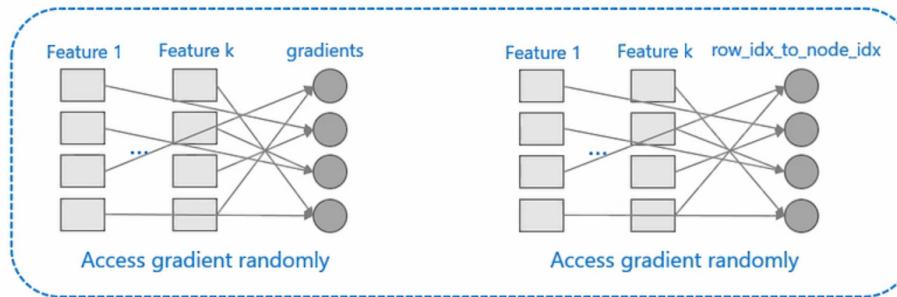
- To get one leaf's histograms in a binary tree, can use the histogram subtraction of its parent and its neighbor
- Construct histograms for one leaf (with smaller #data than its neighbor), then can get histograms of its neighbor by histogram subtraction with small cost($O(\#bins)$)
- 2x speed-up





Increase cache hit chance

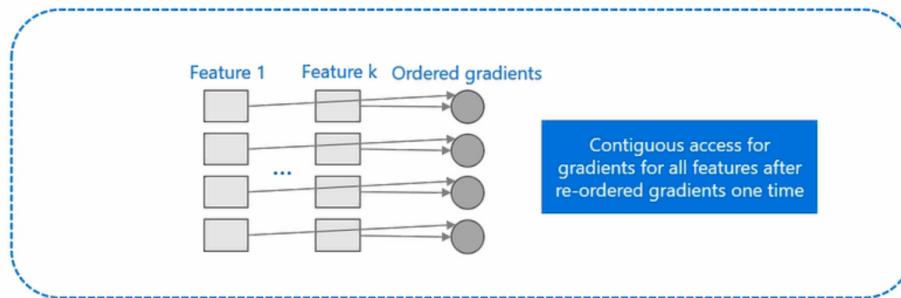
- Pre-sorted algorithm will suffer from cache-miss
 - Access gradients randomly, $O(\#data * \#feature)$
 - Different feature will access gradients by different order
 - Access `row_idx_to_node_idx` randomly, $O(\#data * \#feature)$
 - Pre-sorted algorithm use `row_idx_to_node_idx` to speed up "split" procedure
 - But it access this array randomly
- These random access cause many cache miss





Increase cache hit chance

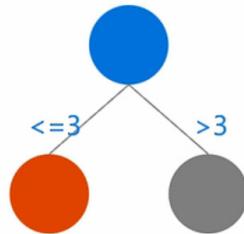
- Histogram based algorithm is easy to increase cache hit chance
 - Access gradient continuous
 - Different features access gradients by same order
 - re-order gradients one time, and every feature can access gradients contiguously
 - Not need to use row_idx_to_node_idx array



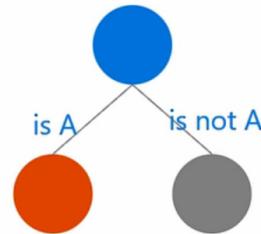


Categorical feature support

- Existing tools use one-hot coding to support categorical feature
 - Need expand feature dimension. Cost much on time and space
- LightGBM can direct use categorical feature as input
 - Change decision rule for categorical features



Numerical feature decision rule



Categorical feature decision rule





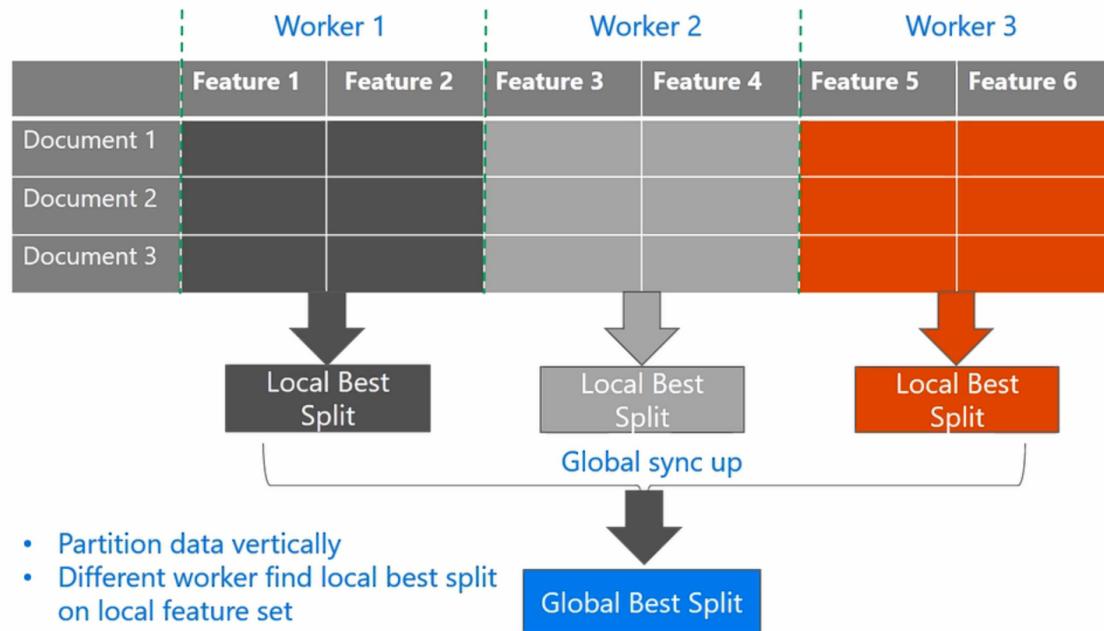
Parallel Learning Support

- Feature Parallelization
 - Cost of computation and communication are depending on #data
- Data Parallelization
 - Communication cost is depending on #features
- Voting Parallelization
 - Reduce the communication in data parallelization
 - Constant communication cost
 - Accepted by NIPS 2016





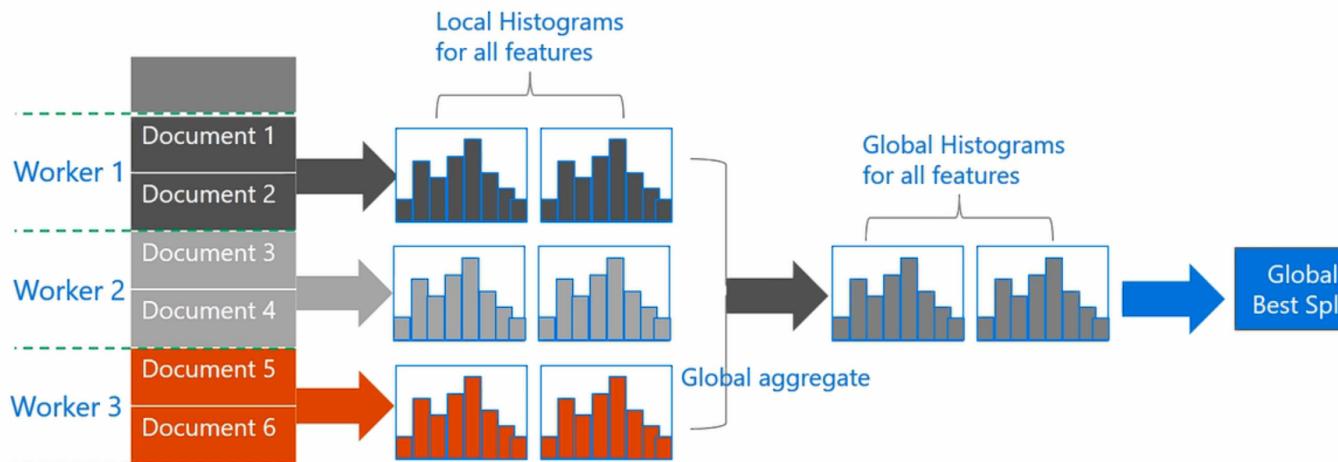
Feature/Attribute Parallelization



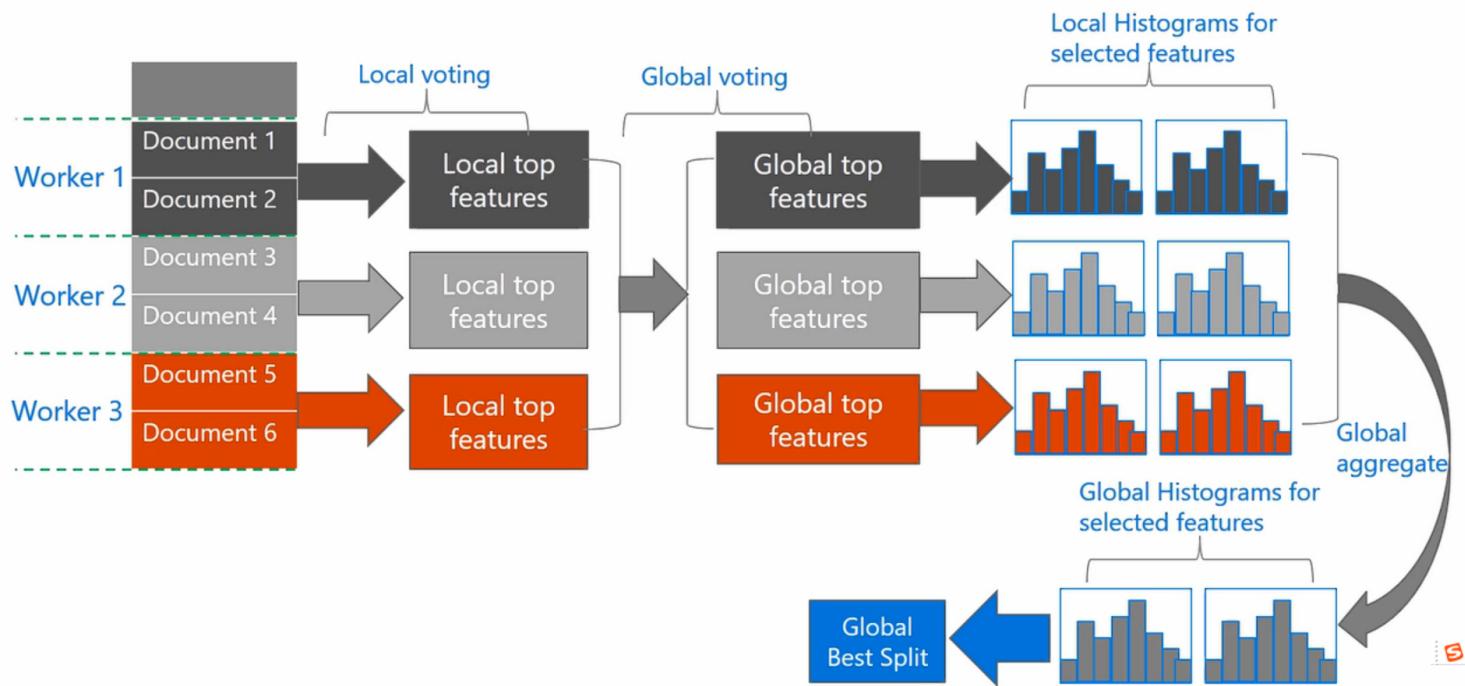


Data Parallelization

- Partition data horizontally
- Each worker construct local histograms, then aggregate global histograms from all local histograms



Parallel optimization – voting based parallel





Parallel Experiments

- learning to rank task, about 11M training data

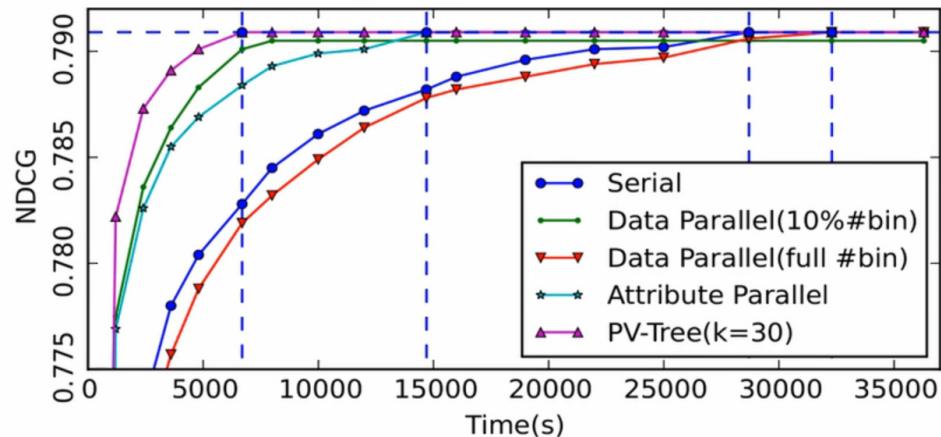


Figure 1. Performances of different algorithms (LTR, 8 machines)





Parallel Experiments

- pCTR task, about 235M training data

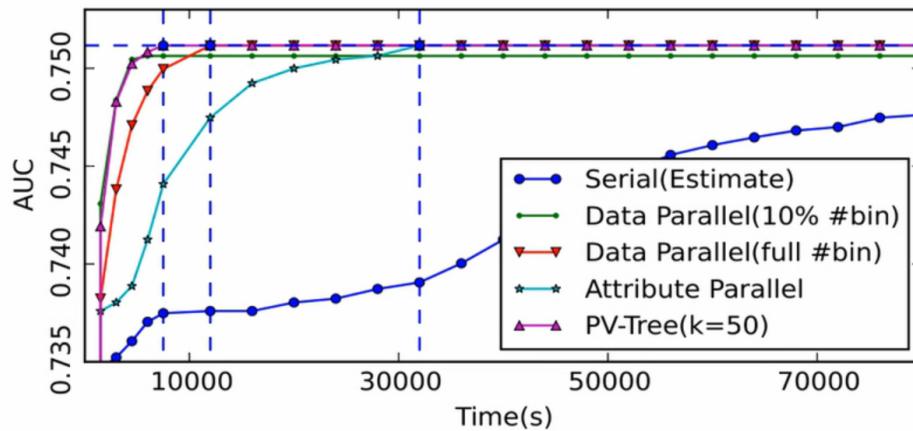


Figure 2. Performances of different algorithms (CTR, 32 machines)





Others Features

Model training tricks

Efficiency

User-friendly functions

- Regularization methods
- DART(drop out) support
- Weighted training
- Sub-samples (Bagging and sub-feature)

- Optimize for sparse features
- Multi-threading optimization

- Continued train
- Early stopping
- Cross Validation
- Python support





Command line quick start

- Prepare your data in Libsvm, csv or tsv format
- train it with lightgbm

```
lightgbm.exe data=train.svm valid=valid.svm num_trees=50 num_leaves=100 output_model=model.txt
```

- Parallel training

```
mpiexec lightgbm.exe num_machine=2 tree_learner=voting data=train.svm  
valid=valid.svm num_trees=50 num_leaves=100 output_model=model.txt
```

- After trained, you can get the model file: "model.txt", use it to predict

```
lightgbm.exe task=prediction data=test.svm input_model=model.txt
```





```
1 import lightgbm as lgb
2 import pandas as pd
3 from sklearn.metrics import mean_squared_error
4 from sklearn.model_selection import GridSearchCV
5
6 # load or create your dataset
7 print('Load data...')
8 df_train = pd.read_csv('../regression/regression.train', header=None, sep='\t')
9 df_test = pd.read_csv('../regression/regression.test', header=None, sep='\t')
10
11 y_train = df_train[0]
12 y_test = df_test[0]
13 X_train = df_train.drop(0, axis=1)
14 X_test = df_test.drop(0, axis=1)
15
16 # train
17 gbm = lgb.LGBMRegressor(objective='regression',
18                         num_leaves=31,
19                         learning_rate=0.05,
20                         n_estimators=20)
21 gbm.fit(X_train, y_train,
22          eval_set=[(X_test, y_test)],
23          eval_metric='l1',
24          early_stopping_rounds=5)
25
26 # predict
27 y_pred = gbm.predict(X_test, num_iteration=gbm.best_iteration)
28 # eval
29 print('The rmse of prediction is:', mean_squared_error(y_test, y_pred) ** 0.5)
```

Python Quick start guide





Convert max_depth to num_leaves

- $\text{num_leaves} = 2^{\text{(max_depth)}}$

max_depth	num_leaves
1	2
2	4
3	8
7	128
10	1024





Faster learning speed

- Bagging (data sub-sampling)
- Feature sub-sampling
- Use categorical feature directly
- Save data file to binary file to speed up data loading in future learning
- Use parallel learning





For better accuracy

- Small learning_rate with large num_iterations
- Large num_leave(may over-fitting)
- Cross validation
- Bigger training data
- Try DART – use drop out during the training





Deal with overfitting

- small max_bin – feature - 分桶略微粗一些
- small num_leaves – 不要在单棵树上分的太细
- Control min_data_in_leaf and min_sum_hessian_in_leaf – 确保叶子节点还有足够多的数据
- Sub-sample – 在构建每棵树的时候，在data上做一些sample
- Sub-feature – 在构建每棵树的时候，在feature上做一些sample
- bigger training data – 更多的训练数据
- lambda_l1, lambda_l2 and min_gain_to_split to regularization - 正则
- max_depth to avoid growing deep tree – 控制树深度





- Star LightGBM in Github:
<https://github.com/Microsoft/LightGBM>
- Open issues when met problems:
<https://github.com/Microsoft/LightGBM/issues>
- Welcome to contribute:
<https://github.com/Microsoft/LightGBM/issues?q=is%3Aissue+is%3Aopen+label%3Acall-for-contribution>





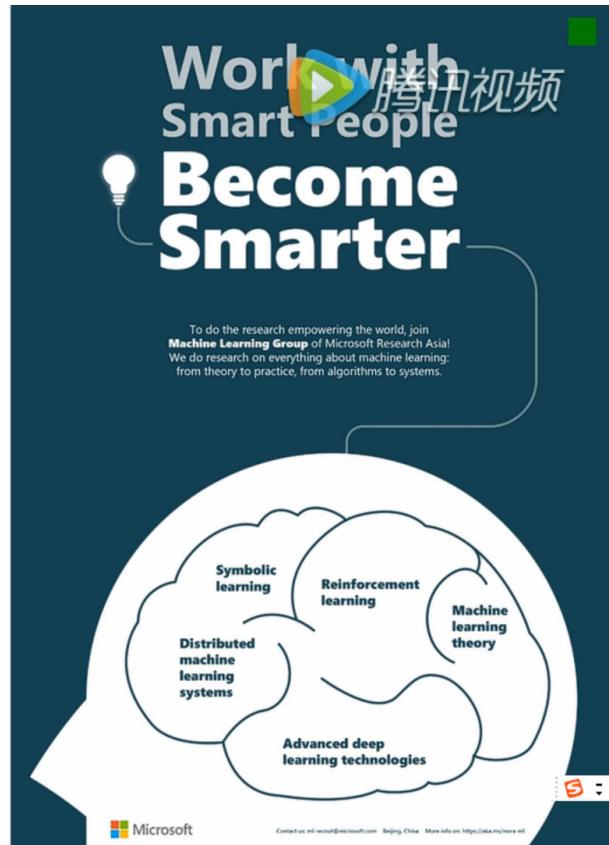
Looking forward

- Speed up with GPU
- More language support – R/Scala/Julia
- More platform support – Hadoop/Spark
- Online version – learn from infinite data
- Integration/Fusion with DNN



We are hiring!

Contact us by: tyliu@microsoft.com



MSRA WeMedia Platforms



WeChat: 微软研究院AI头条



- Top 10 most popular AI WeChat account



Weibo: 微软亚洲研究院



- <http://weibo.com/msra>



Toutiao.com: 微软亚洲研究院



- <http://www.toutiao.com/m6088543147/>



Yidianzixun.com: 微软研究院



- <http://www.yidianzixun.com/home?page=channel&id=m140441>



Sohu.com: 微软亚洲研究院



- <http://mp.sohu.com/profile?xpt=MTMwODIzNTg0M0BzaW5hLnNvaHuuY29t>



参考资料

- [1].LightGBM: A Highly Efficient Gradient Boosting Decision Tree
- [2].lightGBM视频教程
- [3].lightGBM-CN
- [4].论文解读1
- [5].论文解读2
- [6].论文解读3



© 2016 Microsoft Corporation. All rights reserved.

