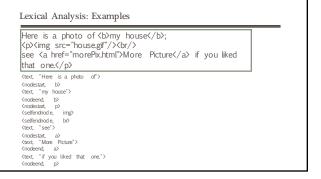


Token Class In Programming Language keywords, identifiers, LPAR, RPAR, corst, etc. In English? Noun, vetb, ...

Token Class • Each class corresponds to a set of strings • Identifier • Strings are letters or digits, starting with a letter • Eg: • Numbers: • A non-empty strings of digits • Eg: • Keywords • A fixed set of reserved words • Eg: • Whitespace • A non-empty sequence of blanks, newlines, and tabs

Lexical Analysis (Example) • Classify program substrings according to roles (token class) • Communicate tokens to parser Character stream Z = 1 Lexical Token stream - <ld, "Z"> - <Op, "="> - <Numbers, "1"> Token = ⟨Class, String⟩ "Z", "=", "1" are called lexemes (an instance of the corr. token class) $% \left(\frac{1}{2}\right) =\frac{1}{2}\left(\frac{1}{2}\right) =\frac{1$



Lexical Analysis: Examples

- Usually, given the pattern describing the lexemes of a token, it is relatively simple to recognize matching lexemes when they occur on the input.
- However, in some languages, it is not immediately apparent when we have seen an instance of a lexeme corresponding to a token.

FORTRAN RULE: White Space is insignificant: VA R1 == VAR1

DO 5 I = 1.25

DO 5 I = 1,25

- Lexical analysis may require to "look ahead" to resolve ambiguity.
 - Look ahead complicates the design of lexical analysis
 Minimize the amount of look ahead

Lookahead

- Lexical analysis tries to partition the input string into the logically units of the language. This is implemented by reading left to right. "scanning", recognizing one token at a time.
- "Lookahead" is required to decide where one token ends and the next token begins.

else

Keyword/Id en tifi er?

Lexical Analysis: Examples

- · C++ template Syntax:
 - Foo⟨Bar⟩
- C++ stream Syntax:
- cin >> var
- Ambiguity
 - Foo<Bar<Bar1>> cin >> var

Summary So Far

- The goal of Lexical Analysis
 - Partition the input string to lexeme
 Identify the token class of each lexeme
- Left-to-right scan => look ahead may require



- Lexical structure of a programming language is a set of token
- Each token class consists of some set of strings.
- How to map which set of strings belongs to which token class? Use regular languages
- Use Regular Expressions to define Regular Languages.

Regular Expressions

- Single character
- 'c' = {"c"}
- Epsilon
 ε = {""}
- Union • A + B = {a | a ∈ A} ∪ {b | b ∈ B}
- Concatenation
- AB = {ab | a ∈ A ^ b ∈ B}
- Iteration (Kleene closure)
- $A^x = \bigcup_{i \ge 0} A^i = A....A$ (i times) $A^0 = \varepsilon$ (empty string)

Regular Expressions

- \mathbf{Def} : The regular expressions over $\mathcal {E}$ are the smallest set of expressions including

```
R = \varepsilon
   | 'c', 'c' \epsilon \Sigma
    | R + R
    | RR
    | R*
```

Regular Expression Example

- $\Sigma = \{0,1\}$
 - (0+1)1 0*+1*
- There can be many ways to write an expression

Formal Languages

- ullet Def: Let ${\mathcal E}$ be a set of character (alphabet). A language over ${\mathcal E}$ is a set of strings of characters drawn from Σ.

 • Regular languages is a formal language
- Alphabet = English character, Language = English Language Is it formal language?
- Alphabet = ASCII, Language = C Language

Formal Language

```
'c' = {"c"}
  \varepsilon = \{ {}^{\omega} \}
A + B = {a | a \( \epsilon \) A} \( \text{b | b \( \epsilon \) B}
AB = {ab | a \epsilon A ^ b \epsilon B}
A^* = \bigcup_{i \ge 0} A^i
```

Formal Language

```
L('c') = \{"c"\}
\begin{array}{l} L(\varepsilon) = \{ e^{\alpha} \} \\ L(A + B) = \{ a \mid a \in L(A) \} \cup \{ b \mid b \in L(B) \} \\ L(AB) = \{ ab \mid a \in L(A) \land b \in L(B) \} \end{array}
L(A^*) = \bigcup_{i \ge 0} L(A^i)
           L: Exp -> Set of strings

• Meaning function L maps syntax to semantics

• Mapping is many to one

• Never one to many
```

Lexical Specifications

```
• Keywords: "if" or "else" or "then" or "for" ....
    Regular expression = 'i' 'f' + 'e' 'l' 's' 'e'
= 'if' + 'else' + 'then'
```

Numbers: a non-empty string of digits
 dgit = '0+1'+7+3+4+5'+6+7+8+9
 dgit*

How to enforce non-empty string?
 digit digit* = digit+

Lexical Specifications

```
\bullet Identifier: strings of letters or digits, starting with a letter
    • letter = 'a' + 'b' + 'c' + .... + 'z' + 'A' + 'B' + .... + 'Z' = [a-zA-Z]

    letter (letter + digit)*
```

• Whitespace: a non-empty sequence of blanks, newline, and tabs

PASCAL Lexical Specification

```
• digit = '0'+'1'+'2'+'3'+'4'+'5'+'6'+'7'+'8'+'9'
• digits = digit+
```

• opt_fraction = ('.' digits) +
$$\varepsilon$$
 = ('.' digits)?

• opt_exponent = ('E' ('+' + '-' +
$$\varepsilon$$
) digits) + ε
= ('E' ('+' + '-')? digits)?

• num = digits opt_fraction opt_exponent

Common Regular Expression

```
• At least one A^+ \equiv AA^*
```

• Option: A? \equiv A + ϵ

■ Range: 'a' + ... + 'z' = [a-z]

• Excluded range: complement of $[a-z] \equiv [^a-z]$

Lexical Specification of a language

```
1. Write a regex for the lexemes of each token class
   ■ Number = digit<sup>+</sup>

Keywords = 'if' + 'else' + ..
Identifiers = letter (letter + digit)*

   ■ LPAR = '('
```

Lexical Specification of a language

```
2. Construct R, matching all lexemes for all tokens
 R = Number + Keywords + Identifiers + ...
    = R_1 + R_2 + R_3 + ...
3. Let input be x1...xn.
   For 1 \le i \le n, check x_1...x_i \in L(R)
4. If successful, then we know that
    x_1...x_i \in L(R_j) for some j
5. Remove x1...xi from input and go to step 3.
```

Lexical Specification of a language

```
• How much input is used?
```

- x1...xi \in L(R) x1...xj \in L(R), i \neq j Which one do we want? (e.g., or \Rightarrow) Maximal munch: always choose the longer one

• Which token is used if more than one matches? • $x_1...x_i \in L(R)$ where $R = R_1 + R_2 + ... + R_n$

- X1...X is LUN where X = Id + Id + Id + ... + In

 X1...X is LURen)

 X1...X is LUR

Lexical Specification of a language

- What if no rule matches?
- * x1...xi ∉ L(R) ... compiler typically tries to avoid this scenario
 * Error = [all strings not in the lexical spec]
 * Put it in last in priority

Summary so far

- · Regular Expressions are concise notations for the string patterns
- Use in lexical analysis with some extensions
- To resolve ambiguities
 To handle errors
- Implementation?
 - We will study next

Finite Automata

- Regular Expression = specification
- Finite Automata = implementation
- A finite automaton consists of
 - An input Alphabet: A finite set of states: S
 - A start state: n
 - A set of accepting states: $F \subseteq S$
 - A set of transitions state: state1 \xrightarrow{input} state2

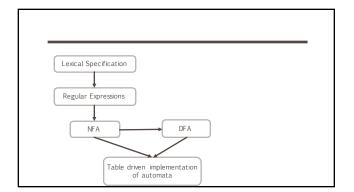


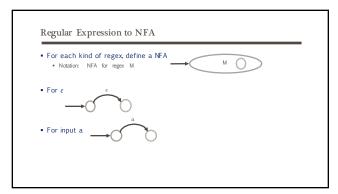
Transition

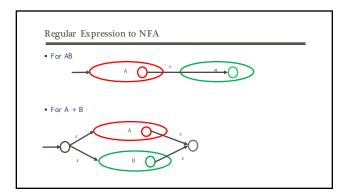
- s1 $\stackrel{a}{\rightarrow}$ s2 (state s1 on input a goes to state s2)
- If end of the input and in final state, the input is accepted
- Otherwise reject
- Language of FA = set of strings accepted by that FA

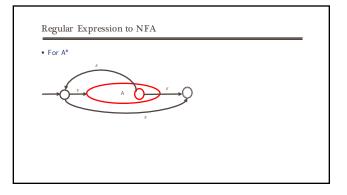
Example Automata

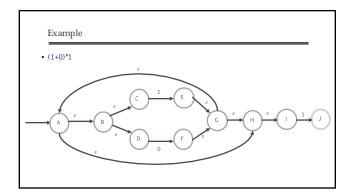
- a finite automaton that accepts only "1"
- A finite automaton that accepting any number of "1" followed by "0"

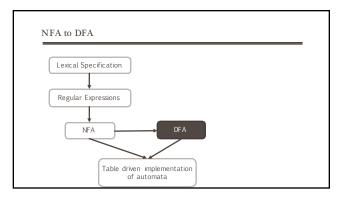


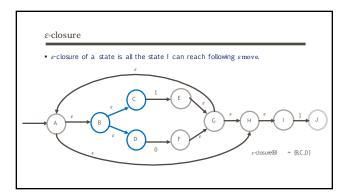


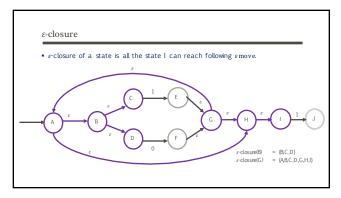












NFA

- An NFA can be in many states at any time
- How many different states? If NFA has N states, it reaches some subset of those states, say S $|S| \le N$ • There are $2^{n} 1$ possible subsets (finite number)

NFA to DFA

<u>NFA</u>

- States S
- Start s
- Final state F
- Transition state • $a(X) = \{y \mid x \in X \land x \xrightarrow{a} y\}$
- \bullet $\varepsilon-closure$

- States will be all possible subset of S except empty set
- Start state = $\varepsilon closure(s)$
- Final state $\{X \mid X \cap F = \emptyset\}$
- $X \stackrel{a}{\rightarrow} Y$ if $Y = \varepsilon closure (a(X))$

