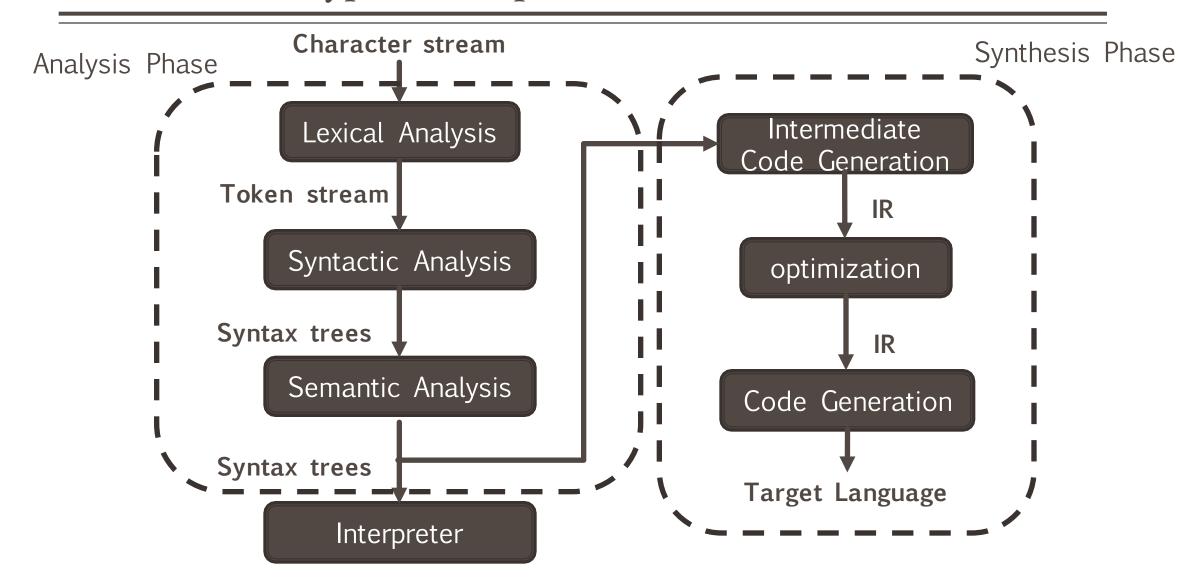
# LEXICAL ANALYSIS

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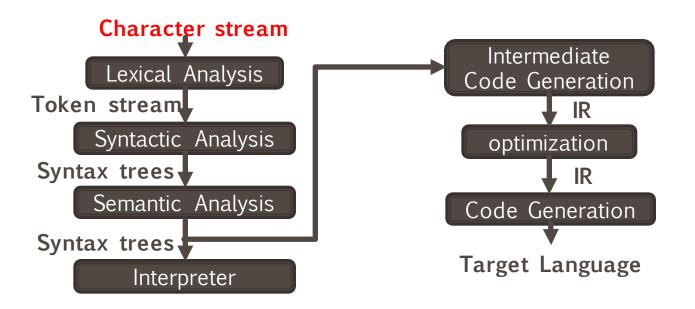
Fall 2018



### Structure of a Typical Compiler



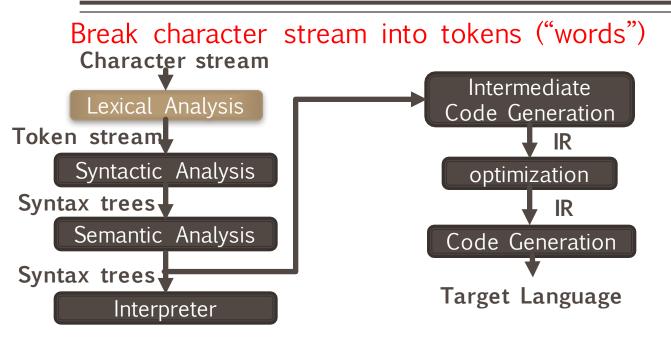
### Input to Compiler



```
if(i == j)
z = 0;
else
z = 1;
```

```
i f (i = = j) \ x = 0 ; \ x = 1 ;
```

### Lexical Analysis



```
if(i == j)

z = 0;

else

z = 1;
```

```
i f ( i = = j )\n\t z = 0 ; \n\t else z = 1 ;

'if' '(' 'i' '==' 'j' ')' '\n' '\t' 'z' '=' '0' ';' '\n' '\t' 'else' 'z' '=' '1' ';'
```

keyword $\langle if \rangle$  LPAR identifier $\langle i \rangle$  op $\langle = \rangle$  identifier $\langle j \rangle$  RPAR whitespaces identifier $\langle z \rangle$  op $\langle = \rangle$  number $\langle 0 \rangle$   $\langle ; \rangle$  whitespaces keyword $\langle else \rangle$  identifier $\langle z \rangle$  op $\langle = \rangle$  number $\langle 1 \rangle$  ';'

1. Identify the substrings

2. Identify the token classes

### Token Class

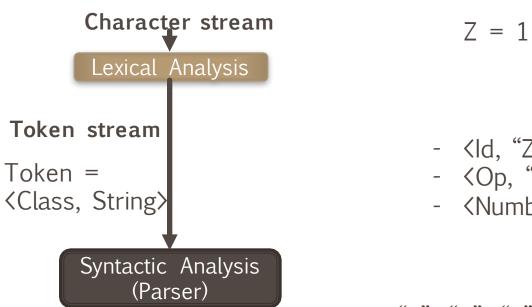
- In Programming Language
  - keywords, identifiers, LPAR, RPAR, const, etc.
- In English?
  - Noun, verb, ...

### Token Class

- Each class corresponds to a set of strings
- Identifier
  - Strings are letters or digits, starting with a letter
  - Eg:
- Numbers:
  - A non-empty strings of digits
  - Eg:
- Keywords
  - A fixed set of reserved words
  - Eg:
- Whitespace
  - A non-empty sequence of blanks, newlines, and tabs

## Lexical Analysis (Example)

- Classify program substrings according to roles (token class)
- Communicate tokens to parser



"Z", "=", "1" are called lexemes (an instance of the corr. token class)

### Lexical Analysis: Examples

```
Here is a photo of \b>my house\/b>; \chi>\limp src="house.gif"/>\br/> see \a href="morePix.html">More Picture\/a> if you liked that one.\(\lambda/p\)
```

```
<text, "Here is a photo of">
<nodestart, b>
⟨text, "my house"⟩
⟨nodeend, b⟩
<nodestart, p>
<selfendnode, img>
⟨selfendnode, br⟩
⟨text, "see"⟩
<nodestart, a>
<text, "More Picture">
⟨nodeend, a⟩
<text, "if you liked that one.">
⟨nodeend, p⟩
```

### Lexical Analysis: Examples

- Usually, given the **pattern** describing the lexemes of a token, it is relatively simple to recognize matching lexemes when they occur on the input.
- However, in some languages, it is not immediately apparent when we have seen an instance of a lexeme corresponding to a token.

FORTRAN RULE: White Space is insignificant: VA R1 == VAR1

DO 5 I = 1.25

DO 5 I = 1,25

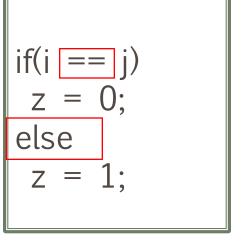
- Lexical analysis may require to "look ahead" to resolve ambiguity.
  - Look ahead complicates the design of lexical analysis
  - Minimize the amount of look ahead

### Lookahead

• Lexical analysis tries to partition the input string into the logically units of the language. This is implemented by reading left to right. "scanning", recognizing one token at a time.

"Lookahead" is required to decide where one token ends and the next token

begins.



Keyword/Identifier?

# Lexical Analysis: Examples

- C++ template Syntax:
  - Foo〈Bar〉
- C++ stream Syntax:
  - cin >> var
- Ambiguity
  - Foo〈Bar〈Bar1〉〉
  - cin >> var

## Summary So Far

- The goal of Lexical Analysis
  - Partition the input string to lexeme
  - Identify the token class of each lexeme

■ Left-to-right scan => look ahead may require

# REGULAR LANGUAGES

- Lexical structure of a programming language is a set of token classes.
- Each token class consists of some set of strings.
- How to map which set of strings belongs to which token class?
  - Use regular languages
- Use Regular Expressions to define Regular Languages.

# Regular Expressions

- Single character
  - 'c' = {"c"}
- Epsilon
  - $\bullet \quad \varepsilon = \{```\}$
- Union
  - $\bullet A + B = \{a \mid a \in A\} \cup \{b \mid b \in B\}$
- Concatenation
  - AB = {ab |  $a \in A \land b \in B$ }
- Iteration (Kleene closure)
  - $\bullet A^* = \bigcup_{i \ge 0} A^i = A....A \text{ (i times)}$
  - $A^0 = \varepsilon$  (empty string)

### Regular Expressions

ullet **Def:** The regular expressions over  $\Sigma$  are the smallest set of expressions including

```
R = \varepsilon
| 'c', 'c' \in \Sigma
| R + R
| RR
| R^*
```

# Regular Expression Example

•  $\Sigma = \{0,1\}$ -  $1^*$ - (0+1)1-  $0^*+1^*$ -  $(0+1)^*$ 

■ There can be many ways to write an expression

### Formal Languages

- **Def**: Let  $\Sigma$  be a set of character (alphabet). A language over  $\Sigma$  is a set of strings of characters drawn from  $\Sigma$ .
  - Regular languages is a formal language
- Alphabet = English character, Language = English Language
  - Is it formal language?
- Alphabet = ASCII, Language = C Language

## Formal Language

```
c' = \{\text{``c''}\}
\varepsilon = \{\text{``''}\}
A + B = \{a \mid a \in A\} \cup \{b \mid b \in B\}
AB = \{ab \mid a \in A \land b \in B\}
A^* = \bigcup_{i \geq 0} A^i
expression Set
```

## Formal Language

```
L(c) = \{c\}
L(\epsilon) = \{c\}
L(A + B) = \{a \mid a \in L(A)\} \cup \{b \mid b \in L(B)\}
L(AB) = \{ab \mid a \in L(A) \land b \in L(B)\}
L(A^*) = \bigcup_{i \ge 0} L(A^i)
expression Set
```

- L: Exp -> Set of strings
- Meaning function L maps syntax to semantics
- Mapping is many to one
- Never one to many

### Lexical Specifications

- Keywords: "if" or "else" or "then" or "for" ....
  - Regular expression = 'i' 'f' + 'e' 'l' 's' 'e'
    = 'if' + 'else' + 'then'
- Numbers: a non-empty string of digits
  - digit = (0'+'1'+'2'+'3'+'4'+'5'+'6'+'7'+'8'+'9'
  - digit\*
  - How to enforce *non-empty string*?
    - digit digit\* = digit+

### **Lexical Specifications**

- Identifier: strings of letters or digits, starting with a letter
  - letter = 'a' + 'b' + 'c' + .... + 'z' + 'A' + 'B' + .... + 'Z' = [a-zA-Z]
  - letter (letter + digit)\*
- Whitespace: a non-empty sequence of blanks, newline, and tabs
  - (' ' + '\n' + '\t')+

### PASCAL Lexical Specification

- digit = (0'+1'+2'+3'+4'+5'+6'+7'+8'+9')
- digits = digit+
- opt\_fraction = ('.' digits) +  $\varepsilon$  = ('.' digits)?
- opt\_exponent = ('E' ('+' + '-' +  $\varepsilon$ ) digits ) +  $\varepsilon$ = ('E' ('+' + '-')? digits )?
- num = digits opt\_fraction opt\_exponent

## Common Regular Expression

- At least one  $A^+ \equiv AA^*$
- Union: A  $\mid B \equiv A + B$
- Option:  $A? \equiv A + \varepsilon$
- Range: 'a' + ... + 'z' = [a-z]
- Excluded range: complement of  $[a-z] \equiv [^a-z]$

- 1. Write a regex for the lexemes of each token class
  - Number = digit+
  - Keywords = 'if' + 'else' + ...
  - Identifiers = letter (letter + digit)\*
  - LPAR = '('

2. Construct R, matching all lexemes for all tokens

```
R = Number + Keywords + Identifiers + ...
= R_1 + R_2 + R_3 + ...
```

3. Let input be  $x_1...x_n$ .

For 
$$1 \le i \le n$$
, check  $x_1...x_i \in L(R)$ 

4. If successful, then we know that

$$x_1...x_i \in L(R_j)$$
 for some j

5. Remove  $x_1...x_i$  from input and go to step 3.

- How much input is used?
  - $x_1...x_i \in L(R)$
  - $x_1...x_i \in L(R)$ ,  $i \neq j$
  - Which one do we want? (e.g., == or =)
  - Maximal munch: always choose the longer one
- Which token is used if more than one matches?
  - $x_1...x_i \in L(R)$  where  $R = R_1 + R_2 + ... + R_n$
  - $x_1...x_i \in L(R_m)$
  - $x_1...x_i \in L(R_n)$ , m  $\neq n$
  - Eg: Keywords = 'if', Identifier = letter (letter + digit)\*, if matches both
  - Keyword has higher priority
  - Rule of Thumb: Choose the one listed first

- What if no rule matches?
  - $x_1...x_i \notin L(R)$  ... compiler typically tries to avoid this scenario
  - Error = [all strings not in the lexical spec]
  - Put it in last in priority

### Summary so far

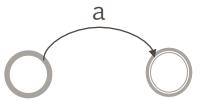
Regular Expressions are concise notations for the string patterns

- Use in lexical analysis with some extensions
  - To resolve ambiguities
  - To handle errors
- Implementation?
  - We will study next

### Finite Automata

- Regular Expression = specification
- Finite Automata = implementation

- A finite automaton consists of
  - An input Alphabet: Σ
  - A finite set of states: S
  - A start state: n
  - A set of accepting states:  $F \subseteq S$
  - A set of transitions state: state1  $\xrightarrow{input}$  state2



### Transition

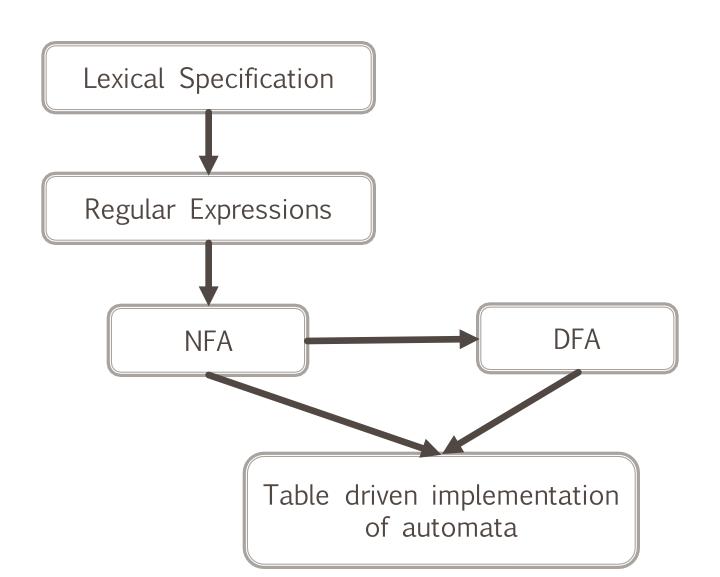
- $s1 \xrightarrow{a} s2$  (state s1 on input a goes to state s2)
- If end of the input and in final state, the input is accepted
- Otherwise reject

Language of FA = set of strings accepted by that FA

## Example Automata

a finite automaton that accepts only "1"

■ A finite automaton that accepting any number of "1" followed by "0"



# Regular Expression to NFA

- For each kind of regex, define a NFA
  - Notation: NFA for regex M





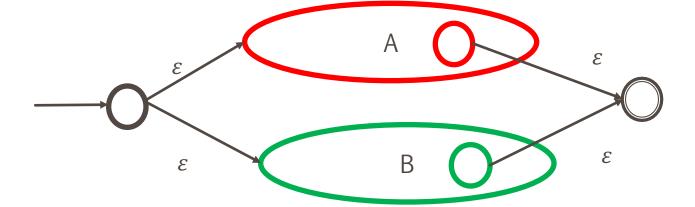


# Regular Expression to NFA



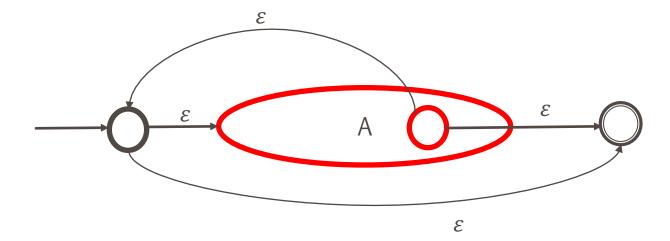


■ For A + B



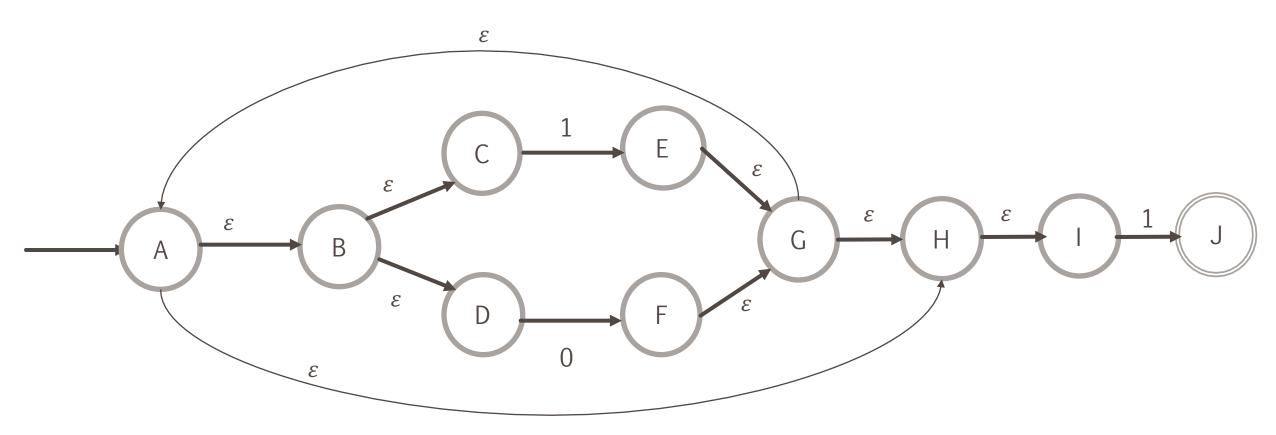
# Regular Expression to NFA

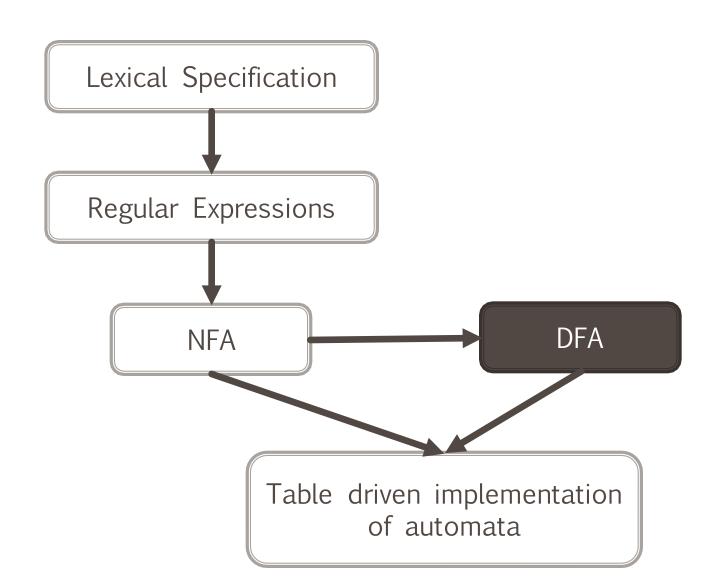
### ■ For A\*



# Example

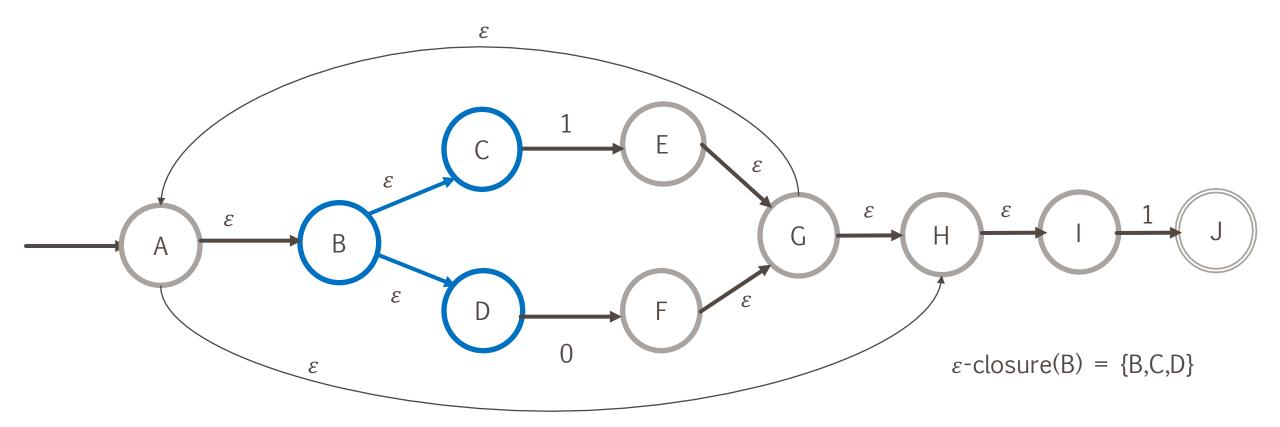
**(1+0)\*1** 





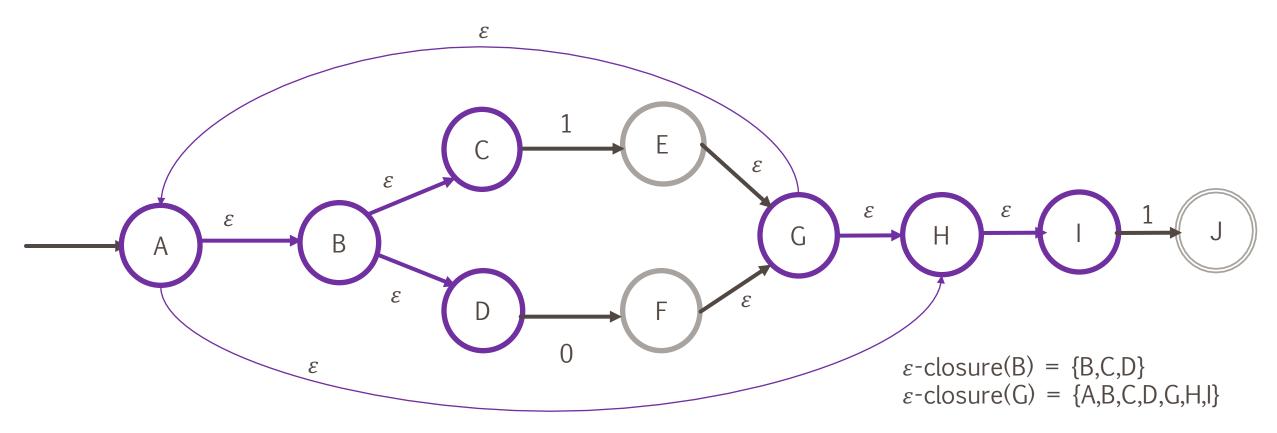
#### $\varepsilon$ -closure

•  $\varepsilon$ -closure of a state is all the state I can reach following  $\varepsilon$  move.



#### $\varepsilon$ -closure

lacktriangleright  $\epsilon$ -closure of a state is all the state I can reach following  $\epsilon$  move.



#### NFA

An NFA can be in many states at any time

- How many different states?
  - If NFA has N states, it reaches some subset of those states, say S
  - |S| ≤ N
  - There are 2<sup>N</sup> 1 possible subsets (finite number)

#### **NFA**

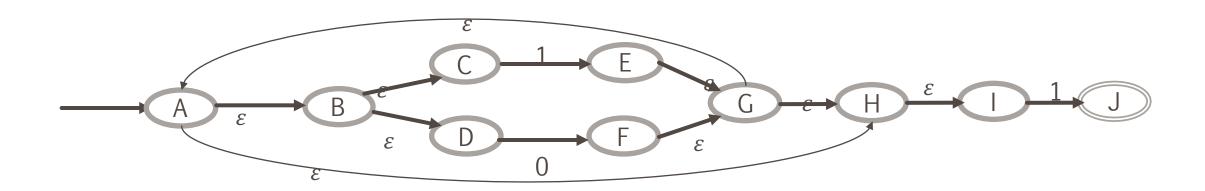
- States S
- Start s
- Final state F
- Transition state

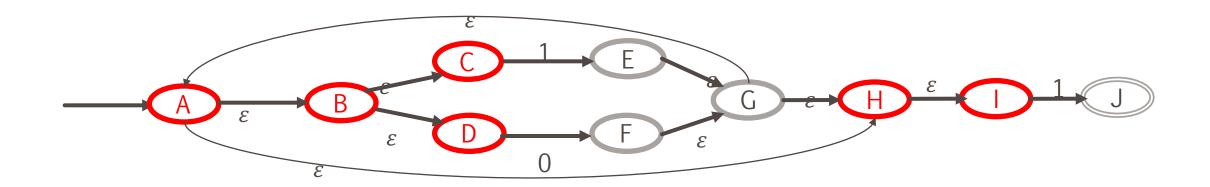
$$\bullet \ a(X) = \{ y \mid x \in X \land x \xrightarrow{a} y \}$$

•  $\varepsilon$  – closure

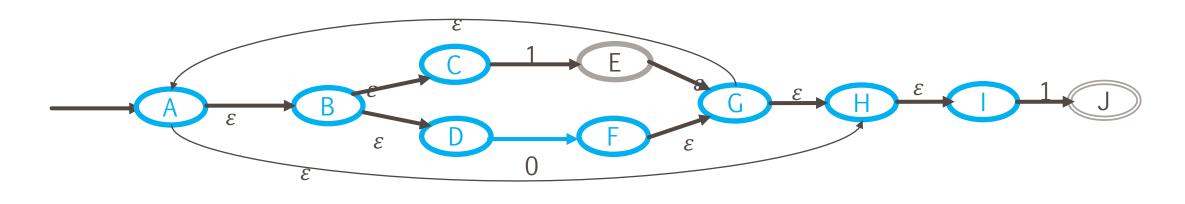
#### **DFA**

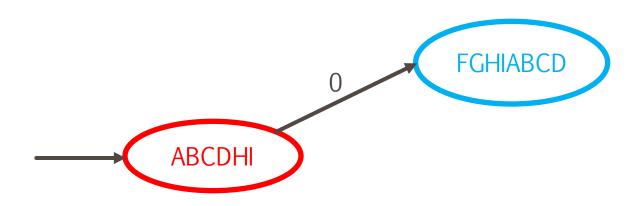
- States will be all possible subset of S except empty set
- Start state =  $\varepsilon closure(s)$
- Final state  $\{X \mid X \cap F = \emptyset\}$
- $X \xrightarrow{a} Y$  if •  $Y = \varepsilon - closure (a(X))$

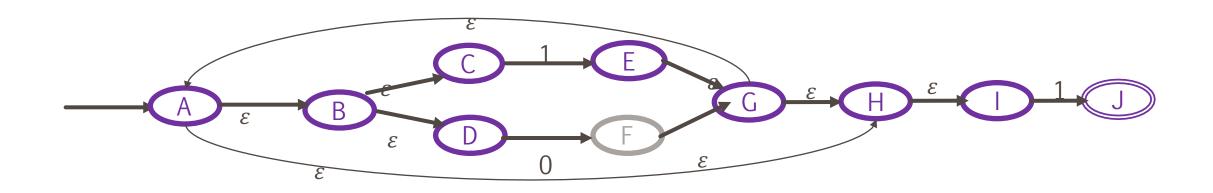


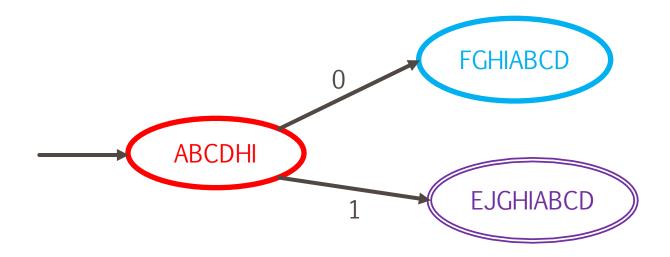


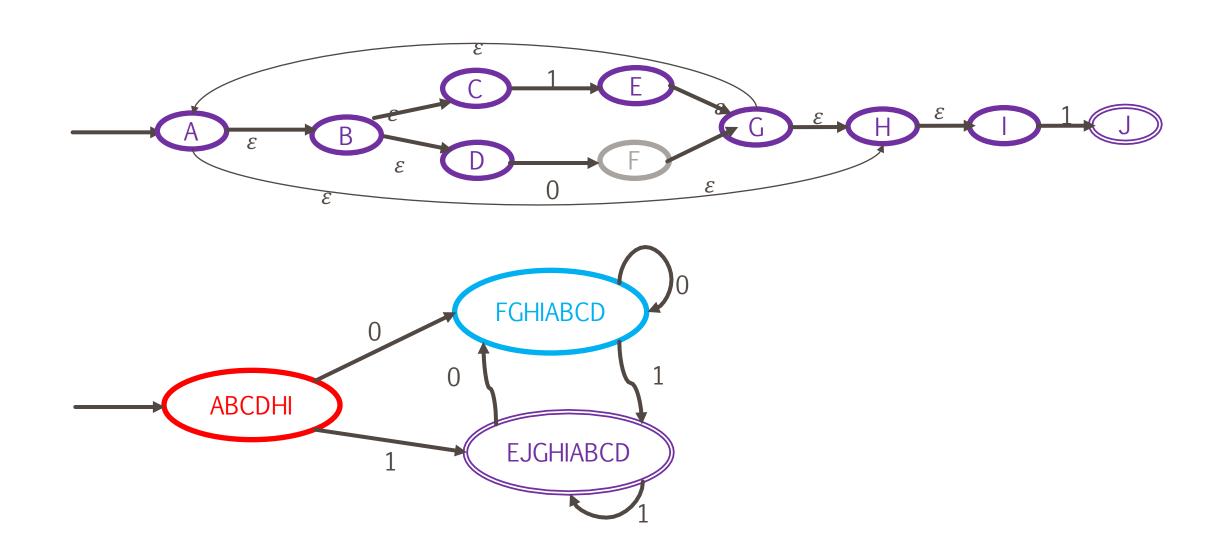


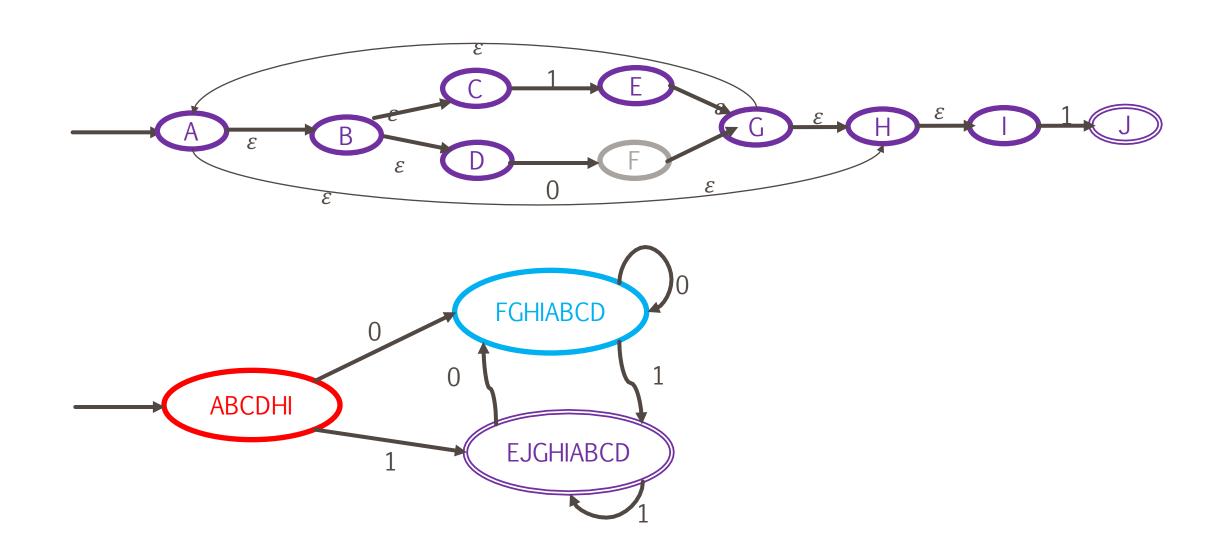








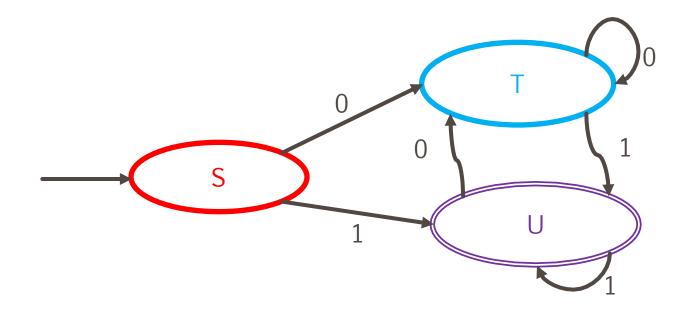




- A DFA can be implemented by a 2D table T
  - One dimension is states
  - Another dimension is input symbol
  - For every transition  $s_i a$   $s_k$ : define T[i,a] = k

Table A

	0	1
S	Τ	U
Т	Τ	U
U	Τ	U



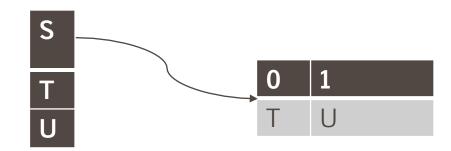
```
i = 0;
state = 0;
while(input[i])
  state = A[state,input[i]]
```

Table A

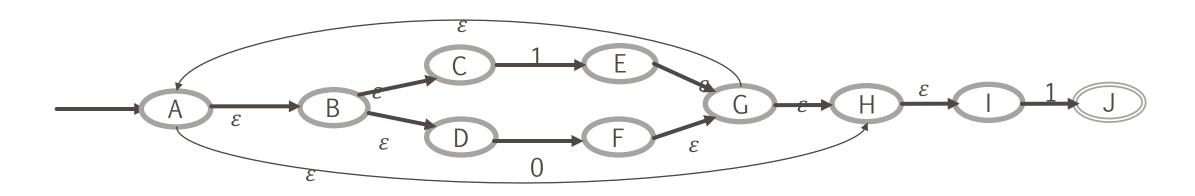
	0	1
S	Τ	U
Т	Τ	U
U	Т	U

A lot of duplicate entries

Table B



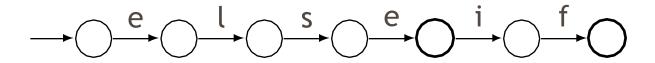
Compact but need an extra indirection - Inner loop will be slower



	0	1	ε
Α			{B,H}
В			{C,D}
С		{E}	
•••			

Deal with set of states rather than single state-→ inner loop is complicated

## Deterministic Finite Automata: Example



#### Deterministic Finite Automata

