

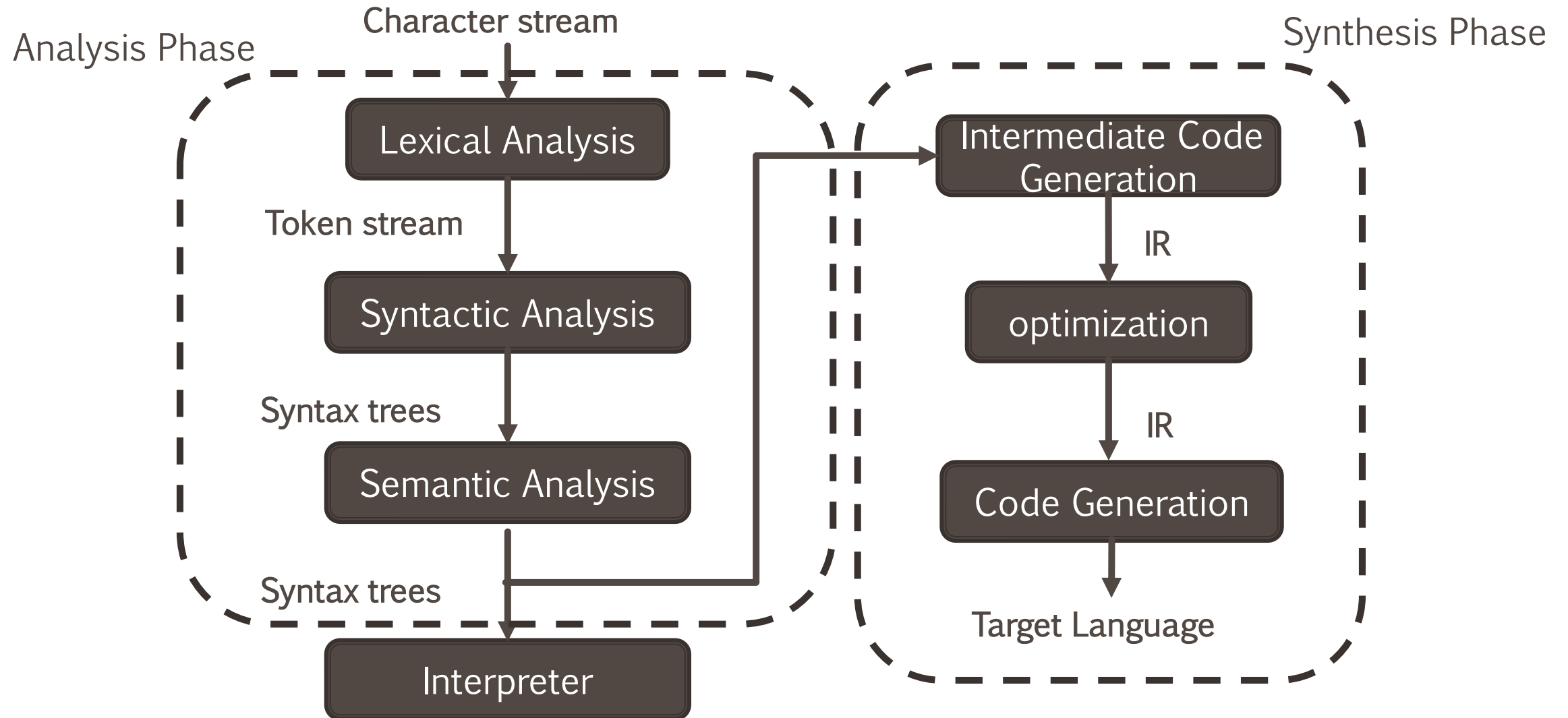
SEMANTIC ANALYSIS

Baishakhi Ray

These slides are motivated from Prof. Alex Aiken and Prof. Stephen Edward



Structure of a Typical Compiler



The Compiler So Far

- Lexical analysis
 - Detects inputs with illegal tokens
- Parsing
 - Detects inputs with ill-formed parse trees
- Semantic analysis
 - Last “front end” phase
 - Catches all remaining errors

What's Wrong With This?

$$a + f(b, c)$$

What's Wrong With This?

$a + f(b, c)$

Is a defined?

Is f defined?

Are b and c defined?

Is f a function of two arguments?

Can you add whatever a is to whatever f returns?

Does f accept whatever b and c are?

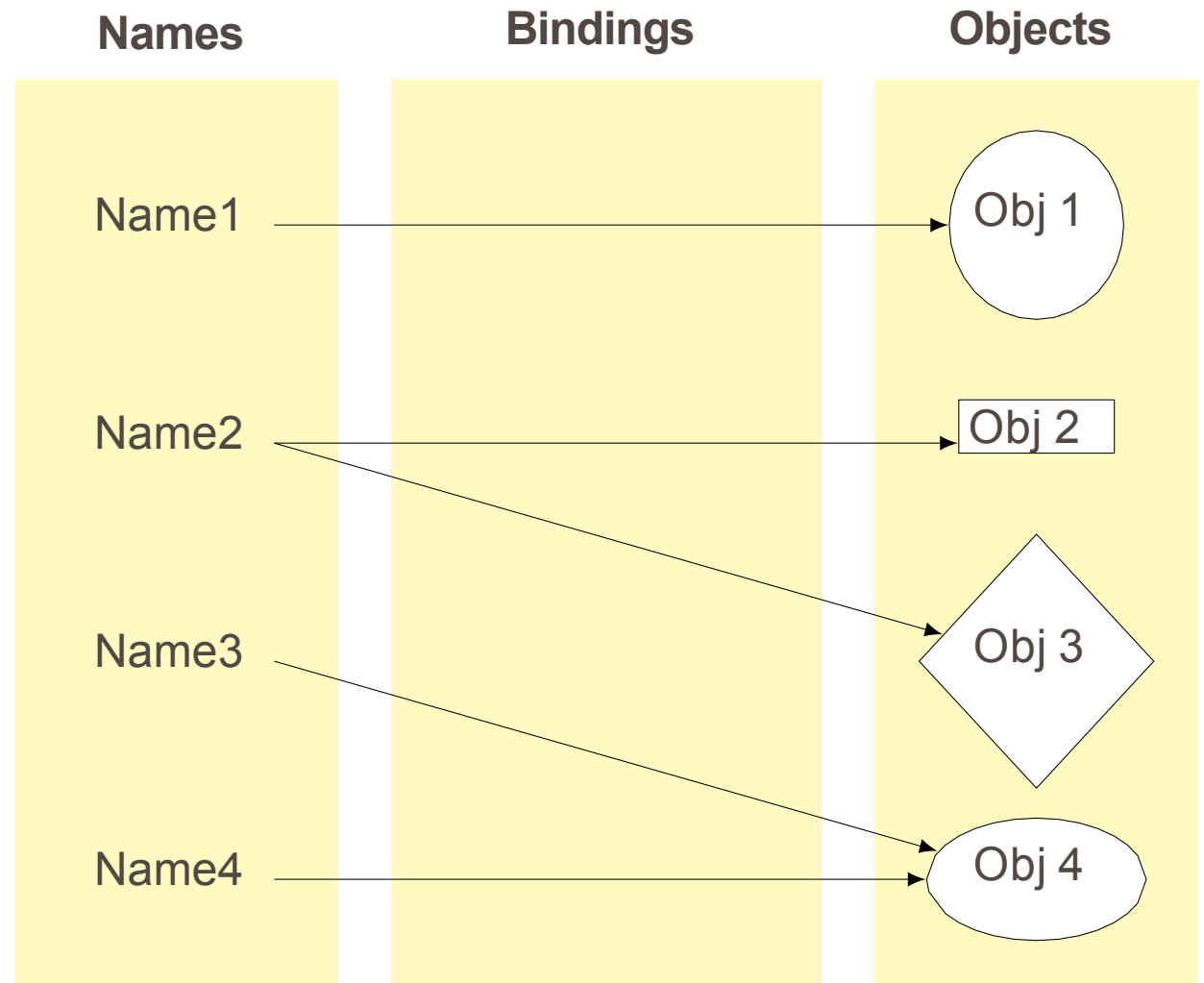
Scope questions

Type questions

parsing
alone
cannot
answer these
question.

Scope

- The scope of an identifier is the portion of a program in which that identifier is accessible.
- The same identifier may refer to different things in different parts of the program.
 - Different scopes for same name don't overlap.
- An identifier may have restricted scope.



Static Vs. Dynamic Scoping

- Most modern languages have static scope
 - Scope depends only on the program text, not runtime behavior
 - Most modern languages use static scoping. Easier to understand, harder to break programs.
- A few languages are dynamically scoped
 - Scope depends on execution of the program
 - Lisp, SNOBOL (Lisp has changed to mostly static scoping)
 - Advantage of dynamic scoping: ability to change environment.
 - A way to surreptitiously pass additional parameters.

Hiding a Definition

Nested scopes can hide earlier definitions, giving a hole.

From the CLRM, “If an identifier is explicitly declared at the head of a block, including the block constituting a function, any declaration of the identifier outside the block is suspended until the end of the block.”

```
void foo()  
{  
    int x;  
    while ( a < 10 ) {  
        int x;  
    }  
}
```

Dynamic Definitions in T_EX

```
% \x, \y undefined
{
  % \x, \y undefined
  \def \x 1
  % \x defined, \y undefined

  \ifnum \a < 5
    \def \y 2
  \fi

  % \x defined, \y may be undefined
}
% \x, \y undefined
```

Open vs. Closed Scopes

- An *open scope* begins life including the symbols in its outer scope.
- Example: blocks in Java

```
{  
  int x;  
  for (;;) {  
    /* x visible here */  
  }  
}
```

- A *closed scope* begins life devoid of symbols. Example: structures in C.

```
struct foo { int x; float y; }
```

Symbol Tables

- A symbol table is a data structure that tracks the current bindings of identifiers
- Can be implemented as a stack
- Operations
 - `add_symbol(x)` push `x` and associated info, such as `x`'s type, on the stack
 - `find_symbol(x)` search stack, starting from top, for `x`. Return first `x` found or `NULL` if none found
 - `remove_symbol()` pop the stack when out of scope
- Limitation:
 - What if two identical objects are defined in the same scope multiple times.
 - Eg: `foo(int x, int x)`

Advanced Symbol Table

- `enter_scope()` start a new nested scope
- `find_symbol(x)` finds current `x` (or null)
- `add_symbol(x)` add a symbol `x` to the table
- `check_scope(x)` true if `x` defined in current scope
- `exit_scope()` exit current scope

Types

- What is a type?
 - A set of values
 - A set of operations defined on those values
 - However, the notion may vary from language to language
- Classes are one instantiation of the modern notion of type

Why Do We Need Type Systems?

- Consider the assembly language fragment

add \$r1, \$r2, \$r3

- What are the types of \$r1, \$r2, \$r3?
- Certain operations are legal for values of each type
 - It doesn't make sense to add a function pointer and an integer in C
 - It does make sense to add two integers
 - But both have the same assembly language implementation!

Type Systems

- A language's type system specifies which operations are valid for which types
- The goal of type checking is to ensure that operations are used with the correct types
 - Enforces intended interpretation of values, because nothing else will!
- Three kinds of languages:
 - Statically typed: All or almost all checking of types is done as part of compilation (C, Java)
 - Dynamically typed: Almost all checking of types is done as part of program execution (Python)
 - Untyped: No type checking (machine code)

Static vs. Dynamic Typing

- Static typing proponents say:
 - Static checking catches many programming errors at compile time
 - Avoids overhead of runtime type checks
- Dynamic typing proponents say:
 - Static type systems are restrictive
 - Rapid prototyping difficult within a static type system
- In practice
 - code written in statically typed languages usually has an escape mechanism •
 - Unsafe casts in C, Java
 - Some dynamically typed languages support “pragmas” or “advice” • i.e., type declarations.

Type Checking and Type Inference

- Type Checking is the process of verifying fully typed programs
- Type Inference is the process of filling in missing type information
- The two are different, but the terms are often used interchangeably
- Rules of Inference
 - We have seen two examples of formal notation specifying parts of a compiler : Regular expressions, Context-free grammars
 - The appropriate formalism for type checking is logical rules of inference

Why Rules of Inference?

- Inference rules have the form If Hypothesis is true, then Conclusion is true
- Type checking computes via reasoning

If E1 and E2 have certain types, then E3 has a certain type

- Rules of inference are a compact notation for “If-Then” statements

From English to an Inference Rule

- The notation is easy to read with practice
- Start with a simplified system and gradually add features
- Building blocks
 - Symbol \wedge is “and”
 - Symbol \Rightarrow is “if-then”
 - $x:T$ is “x has type T”
- If e_1 has type Int and e_2 has type Int, then $e_1 + e_2$ has type Int
 - $(e_1 \text{ has type Int} \wedge e_2 \text{ has type Int}) \Rightarrow e_1 + e_2 \text{ has type Int}$
 - $(e_1: \text{Int} \wedge e_2: \text{Int}) \Rightarrow e_1 + e_2: \text{Int}$
 - It is a special case of $\text{Hypothesis}_1 \wedge \dots \wedge \text{Hypothesis}_n \Rightarrow \text{Conclusion}$ (This is an inference rule).

Notation for Inference Rules

- By tradition inference rules are written

$$\frac{\vdash \text{Hypothesis} \dots \vdash \text{Hypothesis}}{\vdash \text{Conclusion}}$$

$\vdash e:T$ means “it is provable that e is of type T ”

Two Rules

$$\frac{\vdash i \text{ is an integer literal}}{\vdash i: \text{Int}} \quad [\text{Int}]$$

$$\frac{\vdash e1: \text{Int} \quad \vdash e2: \text{Int}}{\vdash e1+e2: \text{Int}} \quad [\text{Add}]$$

$$\frac{\vdash e: \text{Bool}}{\vdash !e: \text{Bool}} \quad [\text{Not}]$$

- These rules give templates describing how to type integers and + expressions
- By filling in the templates, we can produce complete typings for expressions
- Example: $1 + 2$?

Type Checking Proofs

- Type checking proves facts $e: T$
 - Proof is on the structure of the AST
 - Proof has the shape of the AST
 - One type rule is used for each AST node
- In the type rule used for a node e :
 - Hypotheses are the proofs of types of e 's sub-expressions
 - Conclusion is the type of e
- Types are computed in a bottom-up pass over the AST

A Problem

- What is the type of a variable reference?

x is a variable

- $\vdash x:?$

- The local, structural rule does not carry enough information to give x a type.

A solution

- Put more information in the rules!
- A type environment gives types for free variables
 - A type environment is a function from ObjectIdentifiers to Types
 - A variable is free in an expression if it is not defined within the expression
- Type Environments
 - Let O be a function from ObjectIdentifiers to Types
 - The sentence $O \vdash e : T$
is read: Under the assumption that free variables have the types given by O , it is provable that the expression e has the type T
 - $$\frac{O(x) = T}{\vdash x : T}$$

Implementing Type Checking

$$\frac{O, M, C \vdash e1: Int \quad O, M, C \vdash e2: Int}{O, M, C \vdash e1 + e2: Int}$$

```
TypeCheck(Environment, e1 + e2) = {  
  T1 = TypeCheck(Environment, e1);  
  T2 = TypeCheck(Environment, e2);  
  Check T1 == T2 == Int;  
  return Int; }
```

Binding Time

When are bindings created and destroyed?



Binding Time

When a name is connected to an object.

Bound when	Examples
language designed	if else datatype
language implemented	widths foo bar
Program written	static addresses, code
compiled	relative addresses shared
linked	objects
loaded	heap-allocated objects
run	

Binding Time and Efficiency

Earlier binding time \Rightarrow more efficiency, less flexibility

Compiled code more efficient than interpreted because most decisions about what to execute made beforehand.

```
switch (statement) {  
  
    case add:  
        r = a + b;  
        break;  
  
    case sub:  
        r = a - b;  
        break;  
  
    /* ... */  
}
```

```
add %o1, %o2, %o3
```

Binding Time and Efficiency

Dynamic method dispatch in OOLanguages:

```
class Box : Shape {  
    public void draw() { ... }  
}  
  
class Circle : Shape {  
    public void draw() { ... }  
}  
  
Shape s;  
s.draw(); /* Bound at run time */
```

Static Semantic Analysis

How do we validate names, scope, and types?

Static Semantic Analysis

Lexical analysis: Each token is valid?

```
if i 3 "This"          /* valid Java tokens */  
#a1123                 /* not a token */
```

Syntactic analysis: Tokens appear in the correct order?

```
for ( i = 1 ; i < 5 ; i++ ) 3 + "foo"; /* valid Java syntax */  
for break                      /* invalid syntax */
```

Semantic analysis: Names used correctly? Types consistent?

```
int v = 42 + 13;          /* valid in Java (if v is new) */  
return f + f(3);          /* invalid */
```


What To Check

Examples from Java:

Verify names are defined and are of the right type.

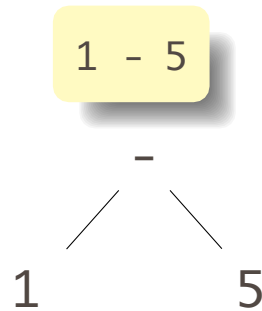
```
int i = 5;  
int a = z;      /* Error: cannot find symbol */  
int b = i[3]; /* Error: array required, but int found */
```

Verify the type of each expression is consistent.

```
int j = i + 53;  
int k = 3 + "hello"; /* Error: incompatible types */  
int l = k(42);      /* Error: k is not a method */  
if ("Hello") return 5; /* Error: incompatible types */  
String s = "Hello";  
int m = s;          /* Error: incompatible types */
```

How To Check Expressions: Depth-first AST Walk

Checking function: environment \rightarrow node \rightarrow type

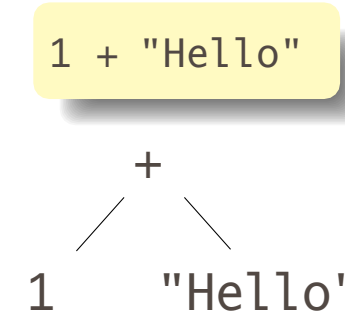


check(-)

check(1) = int

check(5) = int

Success: int - int = int



check(+)

check(1) = int

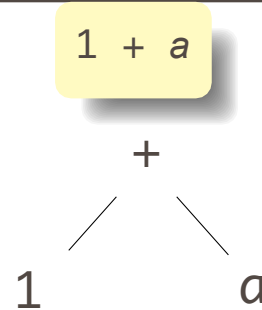
check("Hello") = string

FAIL: Can't add int and string

Ask yourself: at each kind of node, what must be true about the nodes below it? What is the type of the node?

How To Check: Symbols

Checking function: environment \rightarrow node \rightarrow type



```
check(+)  
  check(1) = int  
  check(a) = int  Success:  
  int + int = int
```

The key operation: determining the type of a symbol when it is encountered.

The environment provides a “symbol table” that holds information about each in-scope symbol.

A Static Semantic Checking Function

A big function: “check: ast \rightarrow sast”

Converts a raw AST to a “semantically checked AST”

Names and types resolved

AST
type expression =
 IntConst of int
 | Id of string
 | Call of string * expression list
 | ...



SAST
type expr_detail =
 IntConst of int
 | Id of variable_decl
 | Call of function_decl * expression list
 | ... type expression = expr_detail * Type.t