
Hard Disk Design

Table of Contents

Task 1	1
Task 2	1
Task 3a	2
Task 3b	5
Task 3C	7
Task 4	8

Task 1

The differential equation of input voltage and head position is given, so it is pretty easy to get the open loop transfer function by taking the lapalce transform of both side and can easily get

$$\frac{Y(s)}{U(s)} = \frac{1}{Js^2 + bs}$$

Task 2

open loop transfer function is given by multiplying both G1 and G2

$$G1(s)G2(s) = \frac{Km}{(Ls + R) * (Js^2 + bs)} = \frac{Km}{LJs^3 + Lbs^2 + RJs^2 + Rbs}$$

```
s = tf('s');
J = 1;
b = 20;
R = 1;
L = 0.001;
Km = 5;
G1 = Km/(L*s+R)
G2 = 1/(J*s^2+b*s)
openTF = G1*G2
t=[0:0.005:0.5];
y = step(openTF,t);
plot(t,y);
```

G1 =

$$\frac{5}{0.001 s + 1}$$

Continuous-time transfer function.

$G2 =$

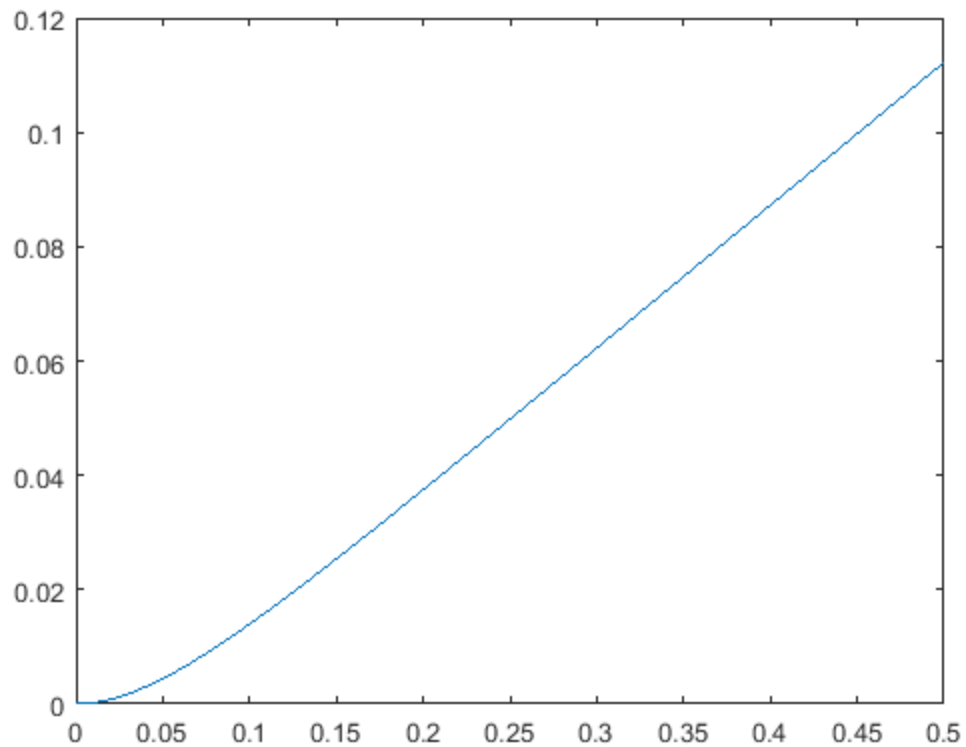
$$\frac{1}{s^2 + 20s}$$

Continuous-time transfer function.

$openTF =$

$$\frac{5}{0.001s^3 + 1.02s^2 + 20s}$$

Continuous-time transfer function.



You can see that if a constant voltage is applied, then the read head will move in a constant speed. And at the beginning when the voltage is applied, there is a curve, which indicates that the read head is accelerating under applied voltage.

Task 3a

The proportional compensator is applied, so that the open loop transfer function is given by

$$K a * G1(s) * G2(s)$$

and closed loop transfer function is given by

$$\frac{K a * G1(s) * G2(s)}{1 + K a * G1(s) * G2(s)}$$

after plug in $G1(s)G2(s)$ from previous computation, we have

$$\frac{K a * K m}{L J s^3 + (L b + R J) s^2 + R b s + K a K m}$$

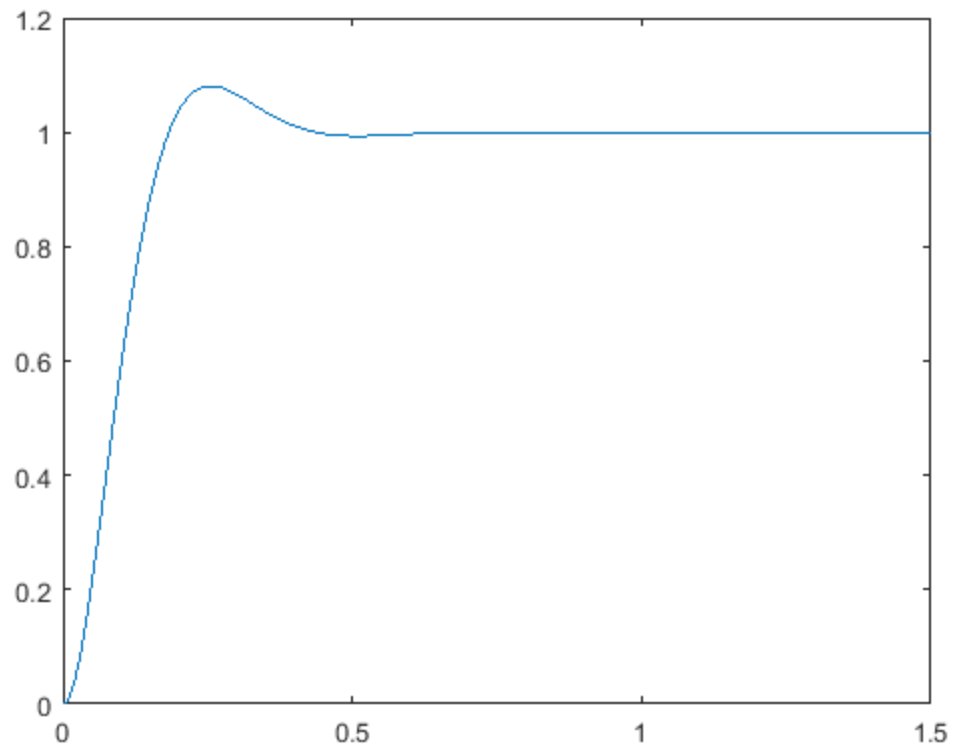
Try plugging in $K a = 50$, we can get the following plot

```
Ka = 50;
t=[0:0.005:1.5];
ProportionalTF =(Ka*G1*G2)/(1+Ka*G1*G2)
y = step(ProportionalTF, t);
plot(t,y);
```

ProportionalTF =

$$\frac{0.25 s^3 + 255 s^2 + 5000 s}{1e-06 s^6 + 0.00204 s^5 + 1.08 s^4 + 41.05 s^3 + 655 s^2 + 5000 s}$$

Continuous-time transfer function.



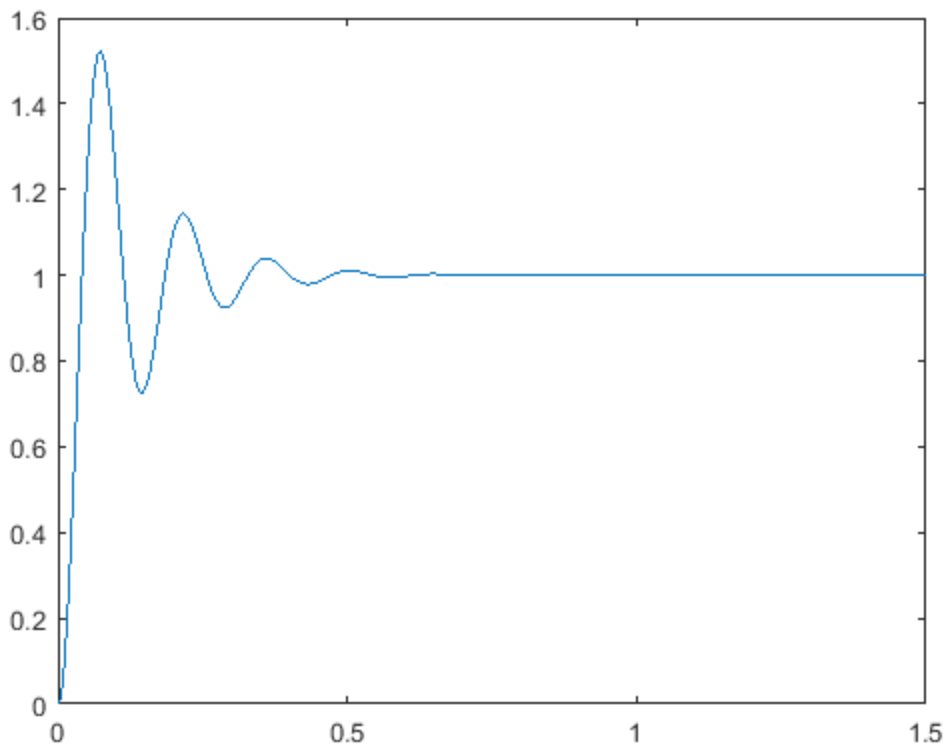
Then applied step when $K_a = 400$

```
Ka = 400;
ProportionalTF = (Ka*openTF)/(1+Ka*openTF)
y = step(ProportionalTF, t);
plot(t,y);
```

ProportionalTF =

$$\frac{2 s^3 + 2040 s^2 + 40000 s}{1e-06 s^6 + 0.00204 s^5 + 1.08 s^4 + 42.8 s^3 + 2440 s^2 + 40000 s}$$

Continuous-time transfer function.



Clearly you can see that the $K_a=50$ has less over shoot than $K_a=400$ does. This is because for $K_a=400$, the feedback amplification is too big and make system too sensitive.

Task 3b

So when disturbance is Introduced to the system, the disturbance input flows into system between G_1 and G_2 . So that we can derive the transfer function for disturbance:

$$Tw = \frac{G_2(s)}{1 + K_a * G_1(s)}$$

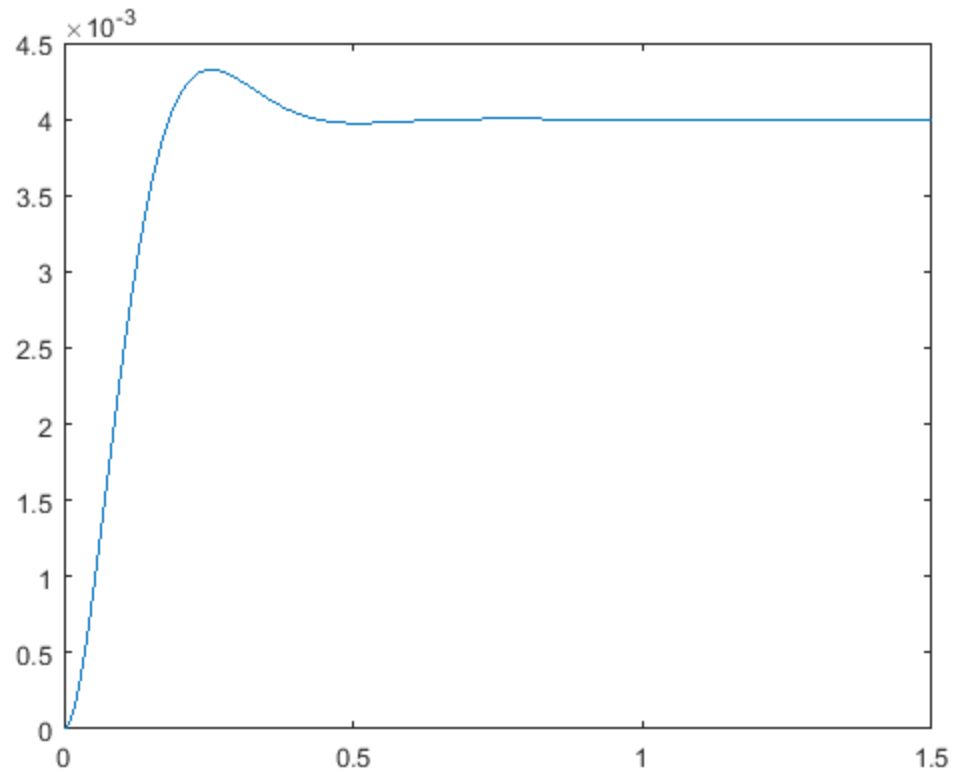
First plot the response of disturbance in case of $K_a = 50$

```
Ka = 50;
Tw = G2/(1+Ka*G1*G2)
y = step(Tw, t);
plot(t,y);
```

$Tw =$

$$\frac{0.001 s^3 + 1.02 s^2 + 20 s}{0.001 s^5 + 1.04 s^4 + 40.4 s^3 + 650 s^2 + 5000 s}$$

Continuous-time transfer function.



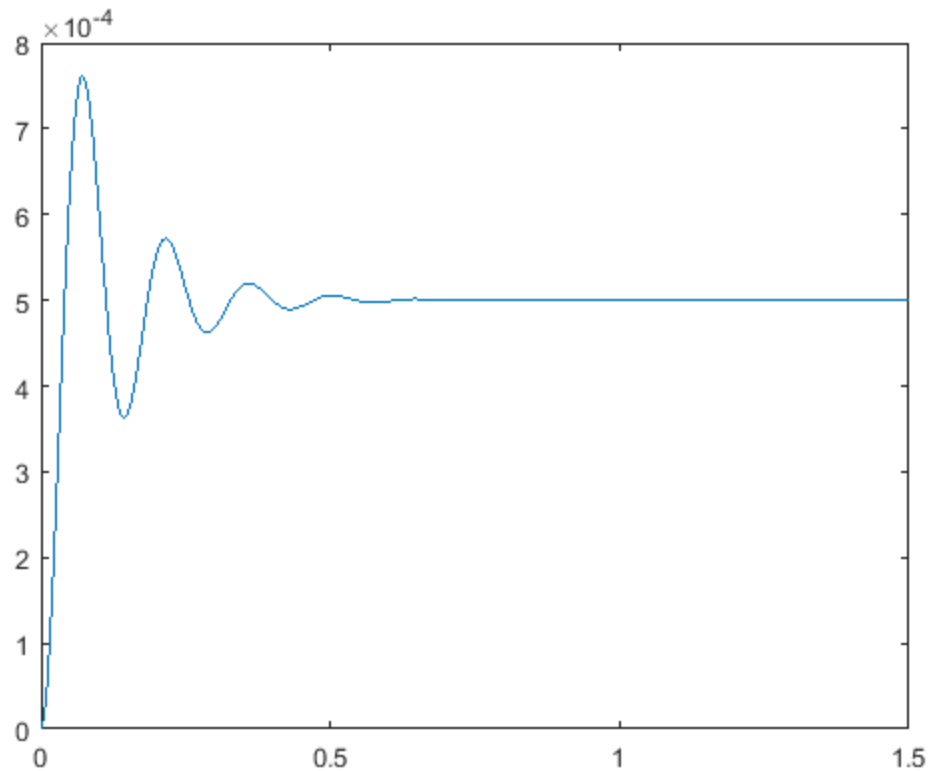
Then plot the response of disturbance in case of $K_a = 400$

```
Ka = 400;
Tw = G2/(1+Ka*G1*G2)
y = step(Tw, t);
plot(t,y);
```

$T_w =$

$$\frac{0.001 s^3 + 1.02 s^2 + 20 s}{0.001 s^5 + 1.04 s^4 + 40.4 s^3 + 2400 s^2 + 40000 s}$$

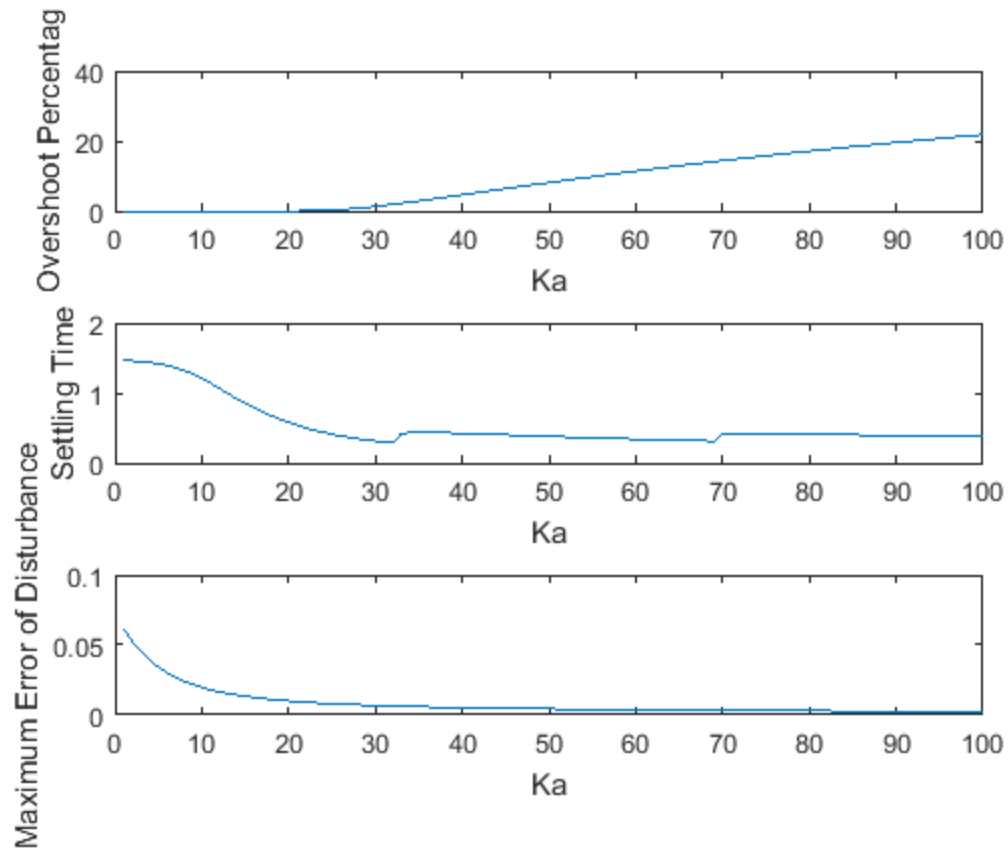
Continuous-time transfer function.



Task 3C

We can plot overshoot percentage and settling time as a function of K_a , and analyze the optimal K_a for the system

```
overshoot = [];  
settlingTime = [];  
maxError = [];  
n=[1:100];  
for Ka=n  
    ProportionalTF = (Ka*openTF)/(1+Ka*openTF);  
    y = step(ProportionalTF, t);  
    info = stepinfo(y, t, 'SettlingTimeThreshold', 0.02);  
    overshoot = [overshoot, info.Overshoot];  
    settlingTime = [settlingTime info.SettlingTime];  
  
    Tw = G2/(1+Ka*G1*G2);  
    y = step(Tw, t);  
    maxError = [maxError max(y)];  
end  
subplot(3,1,1);  
plot(n,overshoot);xlabel('Ka');ylabel('Overshoot Percentage');  
subplot(3,1,2);  
plot(n,settlingTime);xlabel('Ka');ylabel('Settling Time');  
subplot(3,1,3);  
plot(n,maxError);xlabel('Ka');ylabel('Maximum Error of Disturbance');
```



for overshoot less than 5%, Ka is required to be equal or less than 41 Ka value that satisfy settling time less than 250ms is too big and is not in the graph for disturbance less than 0.005, Ka is required to be equal or bigger than 41 Clearly, you cannot satisfy both requirement at the same time.

Task 4

The closed loop transfer function in this case would be

$$\frac{KaG1(s)G2(s)}{1 + KaH(s)G1(s)G2(s)}$$

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