

# COMP10002 Workshop Week 11

Representation of integers and floats, Ex. 13.1

File Operations: Ex13.2

1. Try your hand at Exercise 11.3, **time limit: 10 minutes**
2. Assignment 2:
  1. make progress & ask questions,
  2. submit on Gradescope

# A number can be written using different base

Base 10 (decimal system) uses 10 digits 0..9

10 is written using 2 digits: 10

Base 2 (binary) uses 2 digits 0..1

2 is written using 2 digits: 10

Base 16 (hexadecimal) uses 16 digits 0..9, A..F

16 is written using 2 digits: 10

the number

...  $d_3 \ d_2 \ d_1 \ d_0.$   $d_{-1} \ d_{-2} \dots$  (B) (in base B)

has the value

... +  $d_3 \times B^3 + d_2 \times B^2 + d_1 \times B^1 + d_0 + d_{-1} \times B^{-1} + d_{-2} \times B^{-2} \dots$

Examples:

$$1011.101_{(2)} = ?_{(10)}$$

$$3A.2_{(16)} = ?_{(10)}$$

Practical advice: for conversions, remember:

128	64	32	16	8	4	2	1	0.5	0.25	0.125
$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$	$2^{-1}$	$2^{-2}$	$2^{-3}$

# Note: Converting between bases 2 and 16 is easy!

$16=2^4 \rightarrow$  1 hexadecimal digit is equivalent to 4 binary digits.

$110101101_{(2)}$	$\Leftrightarrow$	$1\ 1010\ 1101_{(2)}$	$\Leftrightarrow$	$1AD_{(16)}$
$11111011011$	$\Leftrightarrow$		$\Leftrightarrow$	?
$111.110001$	$\Leftrightarrow$		$\Leftrightarrow$	?
?	$\Leftrightarrow$		$\Leftrightarrow$	5F.B6

Notes: hexadecimal is normally used for writing binary numbers in a shorter format

# Exercises: Converting Decimal → Binary

Recap:

To change a decimal  $x$  to binary: represent  $x$  as the sum of power of two.

Example:  $23.375 = 16 + 0 \times 8 + 4 + 2 + 1 + 0 \times 0.5 + 0.25 + 0.125$

$$2^4 + 2^2 + 2^1 + 2^0 + + 2^{-1} + 2^{-2}$$

So:  $23.375 =$

$$10111.011_{(2)}$$

Exercises:  $132 \rightarrow_{(2)}$   
 $89.375 \rightarrow_{(2)}$

# Representation of integers (in computers) using $w$ bits

- Note that we use a fixed amount of bits  $w$
- Make difference between `unsigned` and `signed` integers  
(`unsigned int` and `int` in C)

## `unsigned` integers :

Range:  $0 \dots 2^w - 1$       ( $0 \dots 255$  for  $w=8$ )

Representation: Just convert to binary, then add `0` to the front to have enough  $w$  bits.

Examples: represent `89` and `257` as `unsigned int` with  $w=8$

# Representation of signed integers using w bits

**signed integer** range:  $-2^{w-1}$  to  $2^{w-1}-1$   
 $(-128 \dots +127 \text{ for } w=8)$   
 $(-2^{31} \dots +2^{31}-1 \text{ for } w=32)$

- To represent **signed** integers  $x$ :
  - Positive numbers ( $x \geq 0$ ):
    - just like **unsigned**: the binary representation of  $x$  in  $w$  bits,
    - → the first bit will always be  $0$ .
  - Popular Method for negative numbers ( $x < 0$ ):
    - using *twos-complement* of  $|x|$  in  $w$  bit,
    - → the first bit will always be  $1$ .

## Negative int: Finding twos-complement representation in w bits in 3 steps

Suppose that we need to find the twos-complement representation for  $-x$ , where  $x$  is positive, in  $w=16$  bits. Do it in 3 steps:

- 1) Write binary representation of  $|x|$  in  $w$  bits
- 2) Find the **rightmost one-bit**
- 3) Inverse (ie. flip 1 to 0, 0 to 1) all bits on the left of that **rightmost one-bit**

<i>find the 2-comp repr of -40</i>	Bit sequence			
1) bin repr of 40 in 16 bits	0000	0000	0010	1000
2) find the <b>rightmost 1</b>	0000	0000	0010	<b>1000</b>
3) inverse its left	1111	1111	1101	<b>1000</b>

**Why?** Think about finding  $(-x)$  so that  $x + (-x) = 0$ , where  $x$  is a bit pattern.

## Ex. 13.01

Suppose that a computer uses  $w= 6$  bits to represent integers. Calculate the two-complement representations for 0, 4, 19, -1, -8, and -31; Verify that  $19-8 = 11$ ;

value	representation
0	
4	
19	
35	
-1	
-8	
-31	

verify!		
	19	
+		-8
=	11	

# Representation of floats

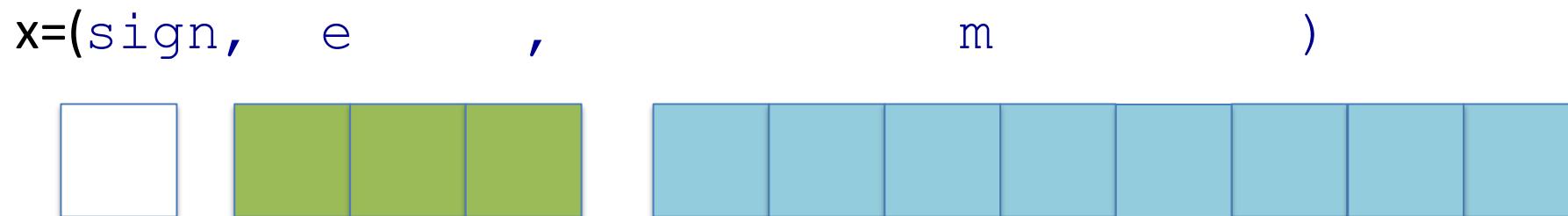
Many different ways! We learnt 2 formats:

- *format-1*: using 16 bits, as described in [lec09.pdf](#) and in the text book
- *format-2* : using 32 bits, which is an [IEEE standard](#), that
  - is employed in most of modern computers for type `int`,
  - is demonstrated in the lecture, and
  - you can experiment with using the program `floatbits.c` ([lec09.pdf](#), around page 26).

**General Principle** for representing a float  $x$ ? (for example,  $x = -20.75$ ) :

- to get rid of the sign (+ or -) and the dot (.) by replacing  $x$  with 3 integers: sign  $s$ , mantissa  $m$ , exponent  $e$  so that:
  - $s$  is 0 (for positive) or 1 (for negative)
  - $|x|$  is equivalent to  $0.m \times 2^e$  (*format-1*) or  $1.m \times 2^e$  (*format-2*)

## Representation of floats (format-1: w=16, as described in lec09.pdf)



1 bit

sign

$w_e$  bits

two-compl of  $e$

$w_m$  bits

representation of first  $n$  bits of mantissa  $m$

Convert  $|x|$  to binary form, and transform so that:

$$|x| = 0.b_0b_1b_2\dots \times 2^e \text{ where } b_0 = 1$$

$e$  is called exponent,  $m = b_0b_1b_2\dots$  is called mantissa

$x$  is represented as the triple  $(\text{sign}, e, m)$  as shown in the diagram.

$|x|$  is equivalent to  $0.m \times 2^e$

## Ex. 13.02

Suppose  $w_s=1$ ,  $w_e=3$ ,  $w_m=12$ , what's the representation of 2.0, -2.5, 7.875 ?

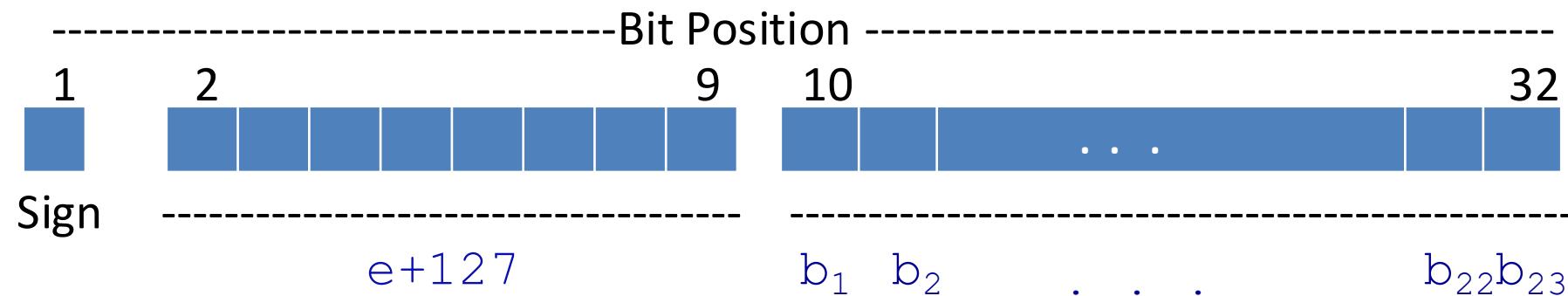
value	binary form	s= ?	m= ?	e= ?	representation
2.0	10.0				
-0.375					
7.875					

# Representation of 32-bit float: (format-2: IEEE 754, as in floatbits.c )

$w_s=1$ ,  $w_e=8$ ,  $w_m=23$

$$|x| = 1.b_1b_2\dots \times 2^e$$

$|x|$  is equivalent to  $1.m \times 2^e$



Here:

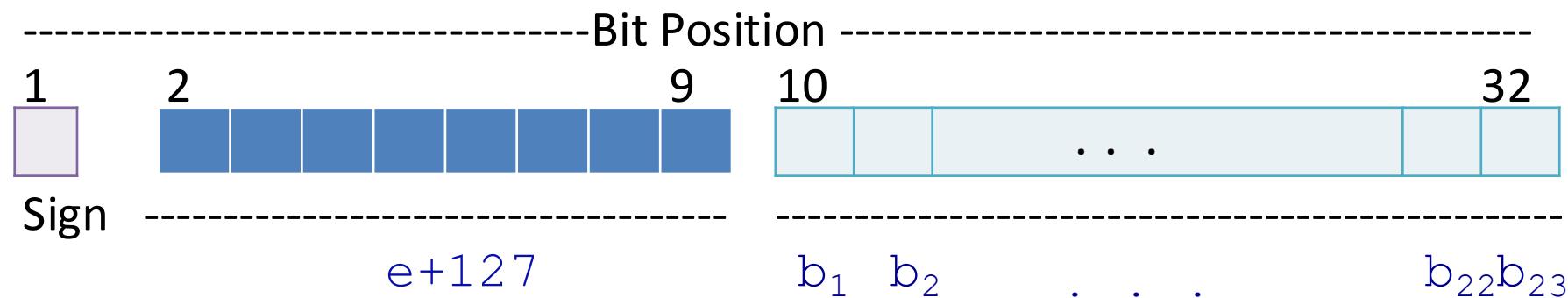
- The sign bit is 0 or 1 as in the previous case
- $e$  is represented in the excess-127 format: as the unsigned value  $e+127$  in  $w_e=8$  bits
- The integer part 1 is omitted from the representation, and the mantissa is represented as just  $b_1b_2\dots b_{23}$

**Class Exercise:** IEEE representation for -3.375, 0.125

**Note:** There are 256 possible values for  $e$ . But valid  $e$  is  $-126 \rightarrow +127$ , corresponding to bit patterns values 0000 0001  $\rightarrow$  1111 1110

# Representation of 32-bit float: (IEEE 754, as in floatbits.c )

$w_e=8$



Un-important note on the exponent part:

- Valid  $e$  is -126  $\rightarrow$  +127, corresponding to bit patterns `0000 0001`  $\rightarrow$  `1111 1110`
- Pattern `0000 0000` used for representing `0.0`,
- Pattern `1111 1111` used to represent `infinity`,
- And, `0.0` is all 32 zero-bit, and `infinity` is all 32 one-bit.

**Class Exercise:** IEEE representation for 3.5

## Representation of 32-bit float: (IEEE 754, as in floatbits.c )

- $w_s=1, w_e=8, w_m=23$
- $|x| = 1.m \times 2^e$

Example:  $x = -3.5$

In binary:  $x = -11.1 \rightarrow |x| = 1.11 \times 2^1$

→ sign bit: 1

→  $e=1$  is represented as  $e+127=128$  in 8 bits

→ e is represented as

→ m= 23-bit mantissa: 110 0000 0000 0000 0000 0000

→ Final representation:

0100 0000 0110 0000 0000 0000 0000

or 4 0 6 0 0 0 0 0 (16)

# LAB TIME: Assignment 2 + exercise 11.3

- **2b|~2b** : do exercise 11.3 in less than 10 minutes
- Work on assignment 2, ask questions

# LAB: (Do Assignment 2 || Do Ex 11.3) && Q&A for Assignment 2

**Ex 11.3:** The Unix `tee` command writes its `stdin` through to `stdout` in the same way that the `cat` command does. But it also creates an additional copy of the file into each of the filenames listed on the command-line when it is executed.

Implement a simple version of this command.

Hint: you will need an array of files all opened for writing.

```
./program file1 file2
```

```
Hello world!
```

```
[^D]
```

```
Hello world!
```

[The program will also create two files named `file1` and `file2`, both containing "Hello world!\n" as the file content.]

```
// here is an implementation of command cat
// change it to that for tee
```

```
int main(int argc, char *argv[]) {
    char c;

    while ( (c=getchar()) != EOF) {
        putchar(c);
    }

    return 0;
}
```

# Additional Slides

# Decimal $\rightarrow$ Binary: A procedure for converting Integer Part

*Changing integer  $x$  to binary: Just divide  $x$  and the subsequent quotients by 2 until getting zero. The sequence of remainders, in reverse order of appearance, is the binary form of  $x$ .*

*Example:* 23

operation	quoation	remainder
$23 : 2$	11	1
$11 : 2$	5	1
$5 : 2$	2	1
$2 : 2$	1	0
$1 : 2$	0	1

$$\text{So: } 23 = 10111_{(2)} \quad 11 = ?_{(2)} \quad 46 = ?_{(2)}$$

# Decimal → Binary: General Method for the Fraction Part

*Problem: Converting fraction could be complicated*

$$0.1 = 0 \times 0.5 + 0 \times 0.25 + 0 \times 0.125 + 0.0625 + 0.0375 (= \dots)$$

**Easy method:** Multiply it, and subsequent fractions, by 2 until getting zero.  
Result = sequence of integer parts of results, in appearance order. Examples:

0.375			0.1		
operation	int	fraction	operation	int	fraction
.375 × 2	0	.75	.1 × 2	0	.2
.75 × 2	1	.5	.2 × 2	0	.4
.5 × 2	1	.0	.4 × 2	0	.8
			.8 × 2	1	.6
			.6 × 2	1	.2

$$\text{So: } 0.375 = 0.\textcolor{red}{011}_{(2)}$$

$$0.1 = 0.\textcolor{red}{00011(0011)}_{(2)}$$