Python Basics

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Variables and Data Types

Variable Assignment

>	>	>	þ	(=	1
Ų.	2	i.			
0	~	r	e		

Calculations With Variables

>>> x+2	Sum of two variables
7	Annual and the property of the control and the
>>> x-2	Subtraction of two variables
1	1000000 00 NO LOU
>>> x*2	Multiplication of two variables
10 >>> x**2	Exponentiation of a variable
25	and recommendation of
>>> x12	Remainder of a variable
1	
>>> x/float(2)	Division of a variable
- S &	A CONTRACTOR OF THE CONTRACTOR

Types and Type Conversion

str()	'5', '3,45', 'True'	Variables to strings
int()	5, 3, 1	Variables to integers
float()	5.0, 1.0	Variables to floats
bool()	True, True, True	Variables to booleans

Asking For Help

>>> help(str)

Strings

```
>>> my string = 'thisStringIsAwesome'
>>> my string
*thinStringInAvenume*
```

String Operations

```
>>> my string * 2
 'thisStringIsAwesomethisStringIsAwesome'
>>> my string + 'Innit'
 "thinStringInAvenomeInnit"
>>> 'm' in my string
```

Lists Also see NumPy Arrays

```
>>> a = 'is'
>>> b = 'nice'
>>> my list = ['my', 'list', a, b]
>>> my list2 = [[4,5,6,7], [3,4,5,6]]
```

Selecting List Elements

Index starts at o

Subset >>> my_list[1] >>> my_list[-3] Slice	Select item at index 1 Select 3rd last item
>>> my_list[1:3] >>> my_list[1:] >>> my_list[:3] >>> my_list[:]	Select items at index 1 and 2 Select items after index 0 Select items before index 3 Copy my_list
Subset Lists of Lists >>> my_list2[1][0] >>> my_list2[1][:2]	my_list[list][itemOfList]

List Operations

```
>>> my list + my list
fleyt, "list", tiet, telest, teyt, flist, flat, telest)
>>> my list * 2
I'my', "list", 'his', 'mics', 'my', 'list', 'is', 'mics')
>>> my_list2 > 4
```

List Methods

>>> my_list.index(a)	Get the index of an item
>>> my list.count(a)	Count an item
>>> my list.append('!')	Append an item at a time
>>> my_list.remove('!')	Remove an item
>>> del(my list[0:1])	Remove an item
>>> my_list.reverse()	Reverse the list
>>> my_list.extend('!')	Append an item
>>> my_list.pop(-1)	Remove an item
>>> my_list.insert(0,'!')	Insert an item
>>> my_list.sort()	Sort the list

String Operations

Index starts at o

>>>	my_	5	t	r	i	ng	[3	1	
>>>										1

String Methods

>>> my string.upper()	String to uppercase
>>> my string.lower()	String to lowercase
>>> my string.count('w')	Count String elements
>>> my string.replace('e', 'i')	Replace String elements
>>> my_string.strip()	Strip whitespace from end

Libraries

Import libraries

>>> import numpy >>> import numpy as np Selective import

>>> from math import pi



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Data analysis

Scientific computing

* matplotlib 2D plotting

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Numpy Arrays

```
>>> my list = [1, 2, 3, 4]
>>> my array = op.array(my list)
>>> my 2darray = np.array([[1,2,3],[4,5,6]])
```

Selecting Numpy Array Elements

Index starts at o

Subset >>> my array(1)

Slice

>>> my_array[0:2] arrayt[1, 2])

array([1, 4])

Subset 2D Numpy arrays >>> my_2darray[:,0]

Select item at index 1

Select items at index o and 1

my 2darray[rows, columns]

Numpy Array Operations

```
>>> my array > 3
 array([frim, frime, frime, from), dtype-bool)
>>> my_array * 2
 array([2, 4, 6, 8])
>>> my array + np.array([5, 6, 7, 8])
 array([6, 8, 10, 12])
```

Numpy Array Functions

>>>	my array.shape	Get the dimensions of the array
>>>	np.append(other_array)	Append items to an array
>>>	np.insert(my_array, 1, 5)	Insert items in an array
>>>	np.delete(my_array,[1])	Delete items in an array
>>>	np.mean(my_array)	Mean of the array
	np.median(my array)	Median of the array
>>>	my array.corrcoef()	Correlation coefficient
>>>	np.std(my_array)	Standard deviation

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Data Science Cheat Sheet

NumPy

KEY

We'll use shorthand in this cheat sheet arr - A numpy Array object

IMPORTS

Import these to start import numpy as np

IMPORTING/EXPORTING

np.loadtxt('file.txt') - From a text file

np.genfromtxt('file.csv',delimiter=',')

- From a CSV file

np.savetxt('file.txt',arr,delimiter=' ')

- Writes to a text file

np.savetxt('file.csv',arr,delimiter=',')

- Writes to a CSV file

CREATING ARRAYS

np.array([1,2,3]) - One dimensional array np.array([(1,2,3),(4,5,6)]) - Two dimensional

np.zeros(3) - 1D array of length 3 all values 0

np.ones((3,4)) - 3x4 array with all values 1

np.eye(5) - 5x5 array of 0 with 1 on diagonal (identity matrix)

np.linspace(0,100,6) - Array of 6 evenly divided values from 0 to 100

np.arange(0,10,3) - Array of values from 0 to less than 10 with step 3 (eg [0,3,6,9])

np.full((2,3),8) - 2x3 array with all values 8 np.random.rand(4,5) - 4x5 array of random floats between 0-1

np.random.rand(6,7)*100 - 6x7 array of random floats between 0-100

np.random.randint(5,size=(2,3)) - 2x3 array with random ints between 0-4

INSPECTING PROPERTIES

arr.size - Returns number of elements in arr

arr.shape - Returns dimensions of arr (rows, columns)

arr.dtype - Returns type of elements in arr arr.astype(dtype) - Convert arr elements to

arr.tolist() - Convert arr to a Python list np.info(np.eye) - View documentation for np.eye

COPYING/SORTING/RESHAPING

np.copy(arr) - Copies arr to new memory

arr.view(dtype) - Creates view of arr elements with type dtype

arr.sort() - Sorts arr

arr.sort(axis=0) - Sorts specific axis of arr two_d_arr.flatten() - Flattens 2D array

two_d_arr to 1D

arr.T - Transposes arr (rows become columns and vice versa)

arr.reshape(3,4) - Reshapes arr to 3 rows, 4 columns without changing data

arr.resize((5,6)) - Changes arr shape to 5x6 and fills new values with 0

ADDING/REMOVING ELEMENTS

np.append(arr, values) - Appends values to end

np.insert(arr,2,values) - Inserts values into
arr before index 2

np.delete(arr,3,axis=0) - Deletes row on index 3 of arr

np.delete(arr,4,axis=1) - Deletes column on index 4 of arr

COMBINING/SPLITTING

np.concatenate((arr1,arr2),axis=0) - Adds arr2 as rows to the end of arr1

np.concatenate((arr1,arr2),axis=1) - Adds
arr2 as columns to end of arr1

np.split(arr,3) - Splits arr into 3 sub-arrays
np.hsplit(arr,5) - Splits arr horizontally on the
5th index

INDEXING/SLICING/SUBSETTING

arr[5] - Returns the element at index 5

arr[2,5] - Returns the 2D array element on index [2][5]

arr[1]=4 - Assigns array element on index 1 the value 4

arr[1,3]=10 - Assigns array element on index [1][3] the value 10

arr[0:3] - Returns the elements at indices 0,1,2 (On a 2D array: returns rows 0,1,2)

arr[0:3,4] - Returns the elements on rows 0,1,2 at column 4

arr[:2] - Returns the elements at indices 0,1 (On a 2D array: returns rows 0,1)

arr[:,1] - Returns the elements at index 1 on all

arr<5 - Returns an array with boolean values (arr1<3) & (arr2>5) - Returns an array with boolean values

~arr - Inverts a boolean array

arr[arr<5] - Returns array elements smaller than 5

SCALAR MATH

np.add(arr,1) - Add 1 to each array element

np.subtract(arr,2) - Subtract 2 from each array element

np.multiply(arr,3) - Multiply each array element by 3

np.divide(arr,4) - Divide each array element by 4 (returns np.nan for division by zero)

np.power(arr,5) - Raise each array element to the 5th power

VECTOR MATH

np.add(arr1,arr2) - Elementwise add arr2 to

np.subtract(arr1,arr2) - Elementwise subtract arr2 from arr1

np.multiply(arr1,arr2) - Elementwise multiply arr1 by arr2

np.divide(arr1, arr2) - Elementwise divide arr1 by arr2

np.power(arr1, arr2) - Elementwise raise arr1 raised to the power of arr2

np.array_equal(arr1,arr2) - Returns True if the arrays have the same elements and shape

np.sqrt(arr) - Square root of each element in the
array

np.sin(arr) - Sine of each element in the array

np.log(arr) - Natural log of each element in the array

np.abs(arr) - Absolute value of each element in the array

np.ceil(arr) - Rounds up to the nearest int

np.floor(arr) - Rounds down to the nearest int

np.round(arr) - Rounds to the nearest int

STATISTICS

np.mean(arr,axis=0) - Returns mean along
specific axis

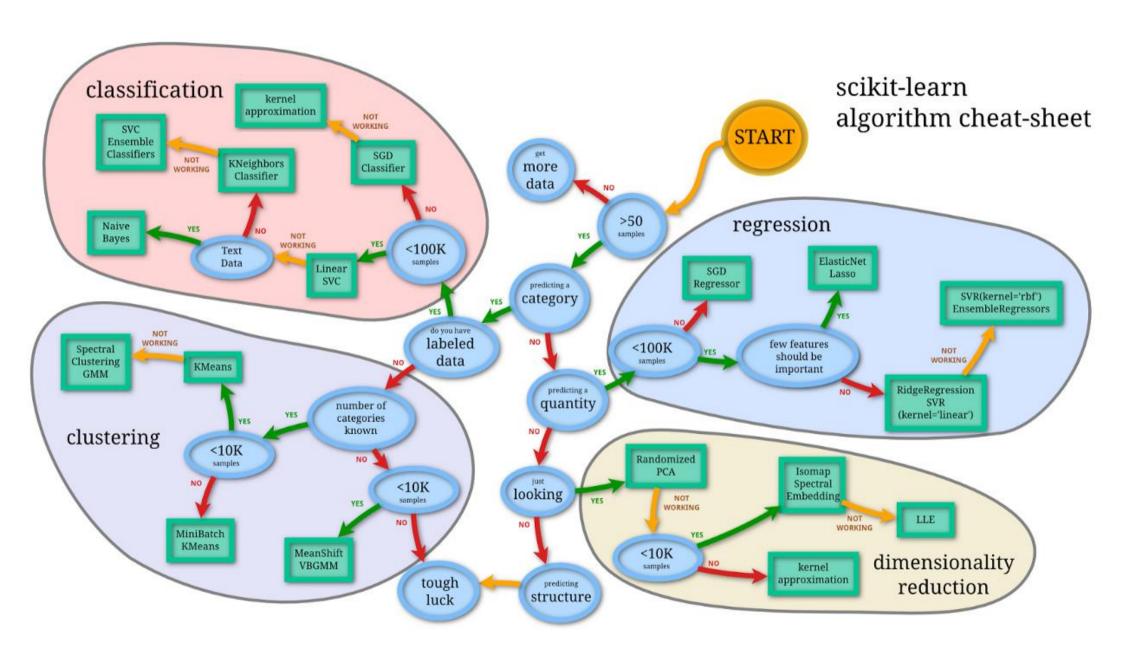
arr.sum() - Returns sum of arr

arr.min() - Returns minimum value of arr

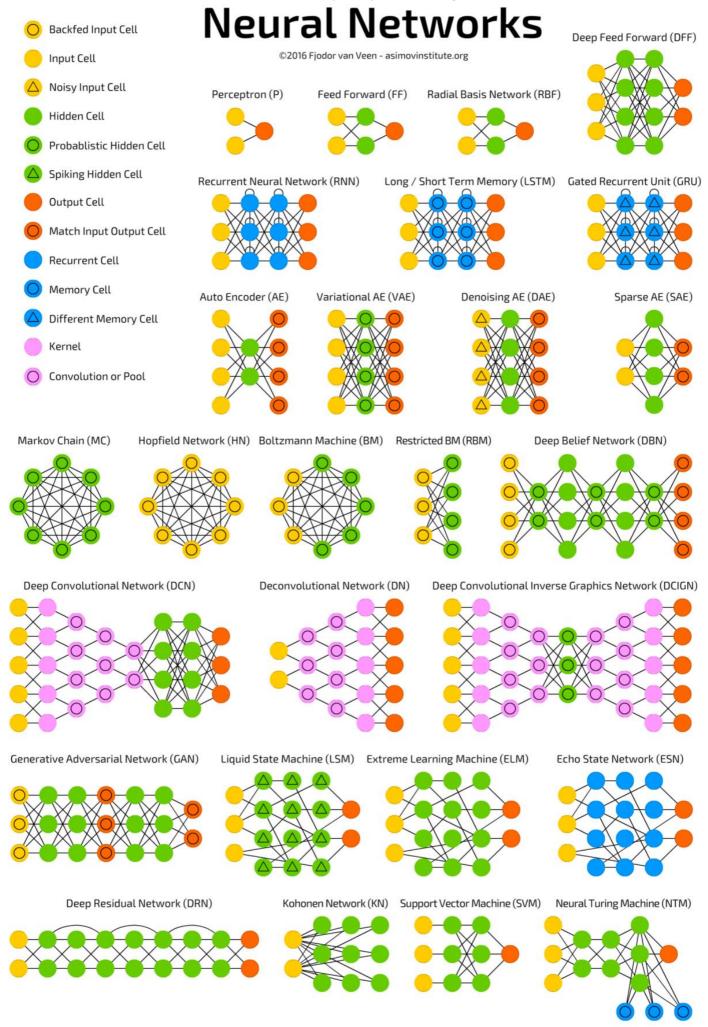
arr.max(axis=0) - Returns maximum value of specific axis

np.var(arr) - Returns the variance of array np.std(arr,axis=1) - Returns the standard deviation of specific axis

arr.corrcoef() - Returns correlation coefficient
 of array

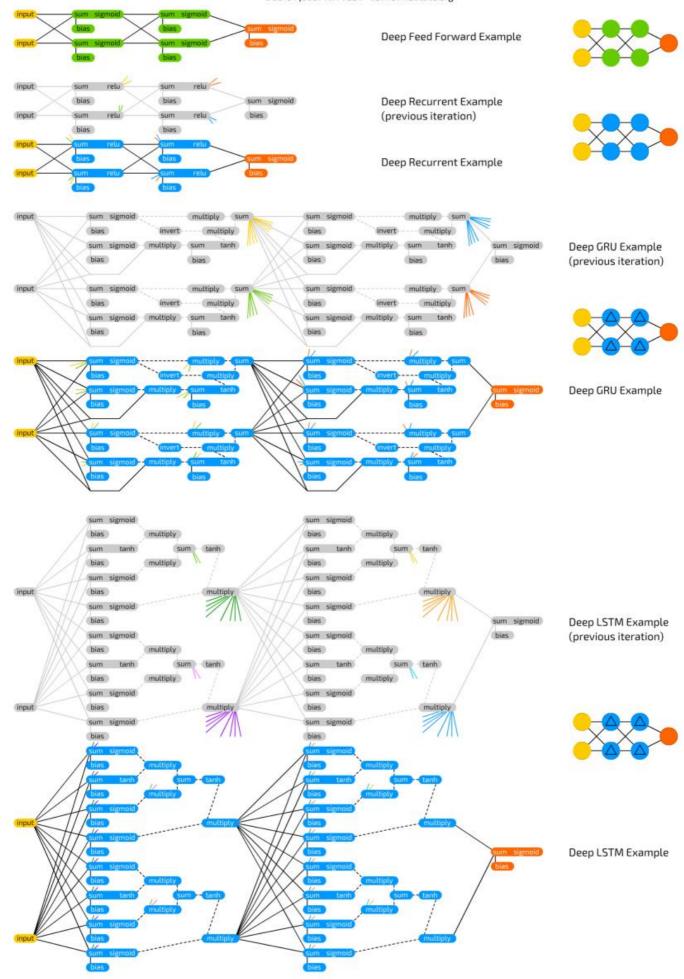


A mostly complete chart of



Neural Network Graphs

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Scikit-Learn

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Scikit-learn

Scikit-learn is an open source Python library that implements a range of machine learning, preprocessing, cross-validation and visualization algorithms using a unified interface.



A Basic Example

```
>>> from sklearn import neighbors, datasets, preprocessing
>>> from sklearn.cross validation import train test split
>>> from sklearn.metrics import accuracy score
>>> iris - datasets.load iris()
>>> X, y = iris.data[:, :2], iris.target
>>> X train, X test, y train, y test = train test split(X, y, random state=33)
>>> scaler = preprocessing.StandardScaler().fit(X train)
>>> X train = scaler.transform(X train)
>>> X test = scaler.transform(X test)
>>> knn = neighbors.KNeighborsClassifier(n neighbors=5)
>>> knn.fit(X train, y train)
>>> y pred = knn.predict(X test)
>>> accuracy score(y test, y pred)
```

Loading The Data

Also see NumPy & Pandas

Your data needs to be numeric and stored as NumPy arrays or SciPy sparse matrices. Other types that are convertible to numeric arrays, such as Pandas DataFrame, are also acceptable.

```
>>> import numpy as np
>>> X = np.random.random((10,5))
>>> X[X < 0.7] = 0
```

Training And Test Data

```
>>> from sklearn.cross validation import train test split
>>> X train, X test, y train, y test = train test split(X,
                                                  random state=0)
```

Create Your Model

Supervised Learning Estimators

Linear Regression

>>> from sklearn.linear model import LinearRegression >>> lr = LinearRegression(normalize=True)

Support Vector Machines (SVM)

>>> from sklearn.svm import SVC >>> svc = SVC(kernel='linear')

Naive Bayes

>>> from sklearn.naive bayes import GaussianNB >>> gnb = GaussianNB()

>>> from sklearn import neighbors

>>> knn = neighbors.KNeighborsClassifier(n neighbors=5)

Unsupervised Learning Estimators

Principal Component Analysis (PCA)

>>> from sklearn.decomposition import PCA

>>> pca = PCA(n components=0.95)

>>> from sklearn.cluster import KMeans

>>> k means = KMeans(n clusters=3, random state=0)

Model Fitting

Supervised learning

>>> lr.fit(X, y) >>> knn.flt(X train, y train)

>>> svc.fit(X train, y train)

Unsupervised Learning

>>> k means.fit(X train)

>>> pca model = pca.fit transform(X train) | Fit to data, then transform it

Fit the model to the data

Fit the model to the data

Prediction

Supervised Estimators

Unsupervised Estimators

>>> y pred = svc.predict(np.random.random((2,5)) >>> y pred = lr.predict(X test)

>>> y pred = knn.predict proba(X test)

Predict labels Predict labels Estimate probability of a label

>>> y pred = k means.predict(X test)

Predict labels in clustering algos

Preprocessing The Data

Standardization

- >>> from sklearn.preprocessing import StandardScaler
- >>> scaler = StandardScaler().fit(X train)
- >>> standardized X = scaler.transform(X train) >>> standardized X test = scaler.transform(X test)

Normalization

- >>> from sklearn.preprocessing import Normalizer
- >>> scaler = Normalizer().fit(X train) >>> normalized X = scaler.transform(X train)
- >>> normalized X test = scaler.transform(X test)

Binarization

- >>> from sklearn.preprocessing import Binarizer
- >>> binarizer = Binarizer(threshold=0.0).fit(X)
- >>> binary X = binarizer.transform(X)

Encoding Categorical Features

- >>> from sklearn.preprocessing import LabelEncoder
- >>> enc = LabelEncoder()
- >>> v = enc.fit transform(v)

Imputing Missing Values

- >>> from sklearn.preprocessing import Imputer
- >>> imp = Imputer(missing values=0, strategy='mean', axis=0)
- >>> imp.fit transform(X train)

Generating Polynomial Features

- >>> from sklearn.preprocessing import PolynomialFeatures
- >>> poly = PolynomialFeatures(5)
- >>> poly.fit transform(X)

Evaluate Your Model's Performance

Classification Metrics

Accuracy Score

- >>> knn.score(X test, y test)
- >>> from sklearn.metrics import accuracy score Metric scoring functions
- >>> accuracy score(y test, y pred)

Estimator score method

Classification Report

>>> from sklearn.metrics import classification report Precision, recall, fi-score >>> print(classification report (y test, y pred)) and support

Confusion Matrix

- >>> from sklearn.metrics import confusion matrix
- >>> print(confusion matrix(y test, y pred))

Regression Metrics

Mean Absolute Error

- >>> from sklearn.metrics import mean absolute error
- >>> y_true = [3, -0.5, 2]
 >>> mean absolute error(y true, y pred)

Mean Squared Error

>>> from sklearn.metrics import mean squared error >>> mean squared error(y test, y pred)

- >>> from sklearn.metrics import r2 score
- >>> r2 score(y true, y pred)

Clustering Metrics

Adjusted Rand Index

>>> from sklearn.metrics import adjusted rand score >>> adjusted rand score(y true, y pred)

Homogeneity

- >>> from sklearn.metrics import homogeneity score
- >>> homogeneity_score(y_true, y_pred)

V-measure

- >>> from sklearn.metrics import v measure score
- >> metrics.v measure score(v true, v pred)

Cross-Validation

- >>> from sklearn.cross validation import cross val score
- >>> print(cross val score(knn, % train, y train, cv=4))
- >>> print(cross val score(lr, X, y, cv=2))

Tune Your Model

Grid Search

- >> from sklearn.grid search import GridSearchCV
- >>> grid = GridSearchCV(estimator=knn,
- param grid=params) >> grid.flt(X train, y train)
- >>> print(grid.best_score) >>> print(grid.best_estimator .n neighbors)

Randomized Parameter Optimization

- >>> from sklearn.grid search import RandomizedSearchCV
- >>> params = ("n_neighbors": range(1,5), "weights": ["uniform", "distance"]} >>> rsearch = RandomizedSearchCV(estimator-knn,
 - param_distributions=params, cv=4, n iter=8, random state=5)
 - >>> rsearch.fit(X train, v train)
 - >>> print(rsearch.best score)



Python Basics

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Variables and Data Types

Variable Assignment

>>	>	X	•5
>>	>	×	

Calculations With Variables

>>> x+2	Sum of two variables
7	Sum of two variables
>>> x-2	Subtraction of two variables
1	99999 27 (27) 1397
>>> x*2	Multiplication of two variables
10 >>> x**2	Exponentiation of a variable
25	est accompanies of
>>> x12	Remainder of a variable
1	1224 242 C C C C C C C C C C C C C C C C
>>> x/float(2)	Division of a variable

Types and Type Conversion

str()	'5', '3,45', 'True'	Variables to strings
int()	5, 3, 1	Variables to integers
float()	5.0, 1.0	Variables to floats
bool()	True, True, True	Variables to booleans

Asking For Help

>>> help(str)

Strings

```
>>> my string = 'thisStringIsAwesome'
>>> my string
*thinStringInAvenome
```

String Operations

```
>>> my string * 2
 'thisStringIsAwesomethisStringIsAwesome'
>>> my string + 'Innit'
 "thinStringInAvenomeInnit"
>>> 'm' in my string
```

Also see NumPy Arrays

```
>>> a = 'is'
>>> b = 'nice'
>>> my list = ['my', 'list', a, b]
>>> my list2 = [[4,5,6,7], [3,4,5,6]]
```

Selecting List Elements

Lists

Index starts at o

Subset	Anna Carlo C
>>> my_list[1]	Select item at index 1
>>> my list[-3]	Select 3rd last item
Slice	***************************************
>>> my_list[1:3]	Select items at index 1 and 2
>>> my list[1:]	Select items after index o
>>> my list[:3]	Select items before index 3
>>> my_list[:]	Copy my_list
Subset Lists of Lists	
>>> my list2[1][0]	my_list[list][itemOfList]

List Operations

>>> my_list2[1][:2]

```
>>> my list + my list
fley', "list", the', teles", Tey', "list", that, telest)
>>> my list * 2
"my", "list", "is", "mirs", "my", "list", "is", 'mirst]
>>> my list2 > 4
```

List Methods

>>> my_list.index(a)	Get the index of an item
>>> my_list.count(a)	Count an item
>>> my_list.append('!')	Append an item at a time
>>> my list.remove('!')	Remove an item
>>> del(my list[0:1])	Remove an item
>>> my_list.reverse()	Reverse the list
>>> my_list.extend('!')	Append an item
>>> my_list.pop(-1)	Remove an item
>>> my_list.insert(0,'!')	Insert an item
>>> my_list.sort()	Sort the list

String Operations

Index starts at o

>>>	my_	st	ri	ng	[.	3	1		
>>>	my_	st	ri	ng	Į.	4	;	9	1

String Methods

>>> my string.upper()	String to uppercase
>>> my string.lower()	String to lowercase
>>> my string.count('w')	Count String elements
>>> my string.replace('e', 'i')	Replace String elements
>>> my_string.strip()	Strip whitespace from end

Libraries

Import libraries

>>> import numpy >>> import numpy as np Selective import

>>> from math import pi



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Numpy Arrays

```
>>> my list - [1, 2, 3, 4]
>>> my array = op.array(my list)
>>> my 2darray = np.array([[1,2,3],[4,5,6]])
```

Selecting Numpy Array Elements

Index starts at o

```
Subset
>>> my_array(1)
```

Slice

>>> my_array[0:2] arraytil, 21) Subset 2D Numpy arrays >>> my_2darray[:,0] array([1, 4])

Select item at index 1

Select items at index 0 and 1

my 2darray[rows, columns]

Numpy Array Operations

```
>>> my array > 3
 array([frim, frice, frim, frue), dtype-bool)
>>> my_array * 2
 array([2, 4, 6, 8])
>>> my array + np.array([5, 6, 7, 8])
 array([6, 8, 10, 12])
```

Numpy Array Functions

Tellinetonical Jellinetonic Johnson States and States a	
>>> my_array.shape >>> np.append(other_array) >>> np.insert(my_array, 1, 5) >>> np.delete(my_array,[1])	Get the dimensions of the array Append items to an array Insert items in an array Delete items in an array
>>> np.mean(my_array) >>> np.median(my_array)	Mean of the array Median of the array
>>> my_array.corrcoef() >>> np.std(my_array)	Correlation coefficient Standard deviation
>>> np.std(my_array)	Standard deviation

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Python Cheat Sheet

AND THE BANKS

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GENERAL

- · Python is case sensitive
- . Python index starts from 0
- Python uses whitespace (tabs or spaces) to indent code instead of using braces.

HELP

Help Home Page	help()	
Function Help	help(str.replace)	
Module Help	help(re)	

MODULE (AKA LIBRARY)

Python module is simply a '.py' file

List Module Contents	dir(module1)
Load Module	import module1 *
Call Function from Module	nodulel.funcl()

* import statement creates a new namescace and executes at the statements in the associated opy file within that remespace. If you want to load the module's content no cream namespace, use * Excurrence and the statement of the

SCALAR TYPES

Check data type : type (variable)

SIX COMMONLY USED DATA TYPES

- 1. Int/long* Large int automatically converts to long
- 2. float* 64 bits, there is no 'double' type
- 3. bool* True or False
- 4. str* ASCII valued in Python 2x and Unicode in Python 3
- . String can be in single/double/triple quotes
- String is a sequence of characters, thus can be treated like other sequences
- Special character can be done via \ or preface with z

strl = r'this\f?ff'

. String formatting can be done in a number of ways

template = '%.2f %s hahe 5%d'; strl = template % (4.88, 'hola', Z)

SCALAR TYPES

- str(), bool(), knt() and float() are also explicit type cest functions.
- NoneType(None) Python 'null' value (ONLY one instance of None object exists)
 - None is not a reserved keyword but rather a unique instance of "NoneType"
 - None is common default value for optional function arguments:

def funci (a, b, c = None)

· Common usage of None :

if variable is None :

- datetime built-in python 'datetime' module provides 'datetime', 'date', 'time' types.
- 'datetime' combines information stored in 'date' and 'time'

Create datetime from String	dt1 = datetime. strptime('20091031', '8Y8x8d')
Get 'date' object	dtl.date()
Get 'time' object	dtl.time()
	dtl.strftime('%n/%d/%Y %H:%M')
Change Field Value	dt2 - dt1.replace(minute - 0, second - 30)
Get Difference	diff = dtl - dt2 # diff is a 'datetime timedella' object

Note: Most objects in Python are mutable except or "strings" and "tuples"

DATA STRUCTURES

Note: All non-Get function call ie. lietl.sort() examples below are in-place (without creating a new object) operations unless noted otherwise.

TUPLE

One dimensional, fixed-length, immutable sequence of Python objects of ANY type.

DATA STRUCTURES

Create Tuple	tup1 = 4, 5, 6 or tup1 = (6,7,8)
Create Nested Tuple	tup1 - (4,5,6), (7,8)
Convert Sequence or Iterator to Tuple	tuple((1, 0, 2))
Concatenate Tuples	tupl + tup2
Ungack Tuple	a, b, c = tupl

Application of Tuple

Swap variables	b,	41.7	a.	· bi	

LIST

One dimensional, variable length, mutable (i.e. contents can be modified) sequence of Python objects of ANY type.

Create List	list1 = (1, 'a', 3) or list1 = list(tupl)
Concatenate Lists*	list1 + list2 or list1.extend(list2)
Append to End of List	list1.append('b')
Insert to Specific Position	listl.insert(posldx,
Inverse of Insert	valueAtidx = listl. pop(posidx)
Remove First Value from List	listl.remove('a')
Check Membership	3 in list! => True ***
Sort List	list1.sort()
Sort with User- Supplied Function	list1.sort(key = len) #sort by length

- List concatenation using '+' is expensive since a new list must be created and objects copied over. Thus, extend () is preferable.
- ** Insert is computationally expansive compared with append.
- *** Checking that a list contains a value is lot slowe than dicts and sets as Python makes a linear scan where others (based on hash tables) in constant line.

Built-in 'bisect module:

- Implements binary search and insertion into a sorted list
- "bisect.bisect" finds the location, where 'bisect. insort' actually inserts into that location.

WARNING: bisect module functions do not check whether the list is sorted, doing so would be computationally expensive. Thus, using them in an unsorted list will succeed without error but may lead to incorrect results.

SLICING FOR SEQUENCE TYPES

† Sequence types include 'str', 'array', 'tuple', 'list', etc.

Notation	list1(start:stop)	
	list1[start:stop:step] (fstep & used) S	

Note

- · 'starf index is included, but 'stop' index is NOT.
- startistop can be omitted in which they default to the startiend.

5 Application of 'step' :

Take every other element	list1[::2]
Reverse a string	str1[::-1]

DICT (HASH MAP)

Create Dict	dictl = ('key1' :'waluel', 2 :[3, 2])
Create Dict from Sequence	dict(zip(keylist, valueList))
Get/Set/Insert Element	dictl['keyl']" dictl['keyl'] = 'newValue'
Get with Default Value	dictl.get('keyl', defaultValue) **
Check if Key Exists	'keyl' in dictl
Delete Element	del dicti('key1']
Get Key List	dicti.keys() ***
Get Value List	dicti.values() ***
Update Values	dicti.update (dict2) # dict1 values are replaced by dict2

- * 'KeyError' exception if the key does not exist.
- " 'get()' by default (aka no 'defaultValue') will return 'None' if the key does not exist.
- *** Returns the lists of keys and values in the same order. However, the order is not any perficular order, also it is most likely not sorted.

Valid dict key types

- Keys have to be immutable like scalar types (int, float, string) or tuples (all the objects in the tuple need to be immutable too)
- The technical term here is 'hashability', check whether an object is hashable with the hash('this is string'), hash([1, 2])
 this would fail.

SET

- A set is an unordered collection of UNIQUE
- . You can think of them like dicts but keys only.

	set([3, 6, 3]) or (3, 6, 3)		
Test Subset	set1.issubset(set2)		
Test Superset	set1.issuperset(set2)		
Test sets have same content	set1 == set2		

· Set operations :

Union(aka 'or')	set1 set2
Intersection (aka 'and')	set1 & set2
Difference	set1 - set2
Symmetric Difference (aka 'xor')	set1 * set2

Numpy Cheat Sheet

NUMPY (NUMERICAL PYTHON)

What is NumPy?

Foundation package for scientific computing in Python

Why NumPy?

- Numpy 'ndarray' is a much more efficient way of storing and manipulating "numerical data" than the built-in Python data structures.
- Libraries written in lower-level languages, such as C, can operate on data stored in Numpy 'ndarray' without copying any data.

N-DIMENSIONAL ARRAY (NDARRAY)

What is NdArray?

Fast and space-efficient multidimensional array (container for homogeneous data) providing vectorized arithmetic operations

Create NdArray	np.array(seq1)			
	# seq1 - is any sequence like object, i.e. [1, 2, 3]			
Create Special NdArray	1, np.zeros(10)			
	# one dimensional ndarray with 10 elements of value 0			
	2, np.ones(2, 3)			
	# two dimensional ndamay with 6 elements of value 1			
	3, np.empty(3, 4, 5) *			
	# three dimensional ndamay of uninitialized values			
	4, np.eye(N) or np.identity(N)			
	# creates N by N identity matrix			
NdArray version of Python's mange	np.arange(1, 10)			
Get # of Dimension	ndarrayl.ndim			
Get Dimension Size	dimlsize, dim2size, = ndarrayl.shape			
Get Data Type **	ndarrayl.dtype			
Explicit Casting	ndarray2 = ndarray1. astype(np.int32) ***			

Cannot assume empty() will return all zeros. It could be garbage values.

- Default data type is 'np.float64'. This is equivalent to Python's float type which is 8 bytes (64 bits); thus the name 'float64'.
- If casting were to fail for some reason, 'TypeError' will be raised.

SLICING (INDEXING/SUBSETTING)

- Slicing (i.e. ndarray1 [2:6]) is a "view" on the original array. Data is NOT copied. Any modifications (i.e. ndarray1 [2:6] = 8) to the 'view' will be reflected in the original array.
- · Instead of a 'view', explicit copy of slicing via

```
ndarray1[2:6].copy()
```

Multidimensional array indexing notation :

ndarray1[0][2] Of ndarray1[0, 2]

* Boolean indexing

```
ndarrayl[(names -- 'Bob') | (names -- 'Will'), 2:]
```

'2.' means select from 3rd column on

- Selecting data by boolean indexing ALWAYS creates a copy of the data.
- The 'and' and 'or' keywords do NOT work with boolean arrays. Use & and |.
- Fancy indexing (aka 'indexing using integer arrays')
 Select a subset of rows in a particular order:

```
ndarray1 [ [3, 8, 4] ]
ndarray1 [ [-1, 6] ]
# negative indices select rows from the end
```

Fancy indexing ALWAYS creates a copy of the data.

NUMPY (NUMERICAL PYTHON)

Setting data with assignment:

ndarrayl(ndarrayl < 01 = 0 *

If ndamay1 is two-dimensions, ndamay1 < 0 creates a two-dimensional boolean array.

COMMON OPERATIONS

1. Transposing

 A special form of reshaping which returns a 'view' on the underlying data without copying anything.

```
ndarray1.transpose() Of
ndarray1.7 Or
ndarray1.swapaxes(0, 1)
```

Vectorized wrappers (for functions that take scalar values)

math.sqrt() works on only 8 scalar
 np.sqrt(seq1) # any sequence (list, ndarray, etc) to return a ndarray

3. Vectorized expressions

 np. where (cond, x, y) is a vectorized version of the expression 'x if condition else y'

```
np.where[[True, False], [1, 2], [2, 3]) => ndarray (1, 3)
```

Common Usages

np.where (matrixArray > 0, 1, -1)
=> a new array (same shape) of 1 or -1 values
np.where (cond, 1, 0).argmax() *
=> Find the first True element

argmax() can be used to find the index of the maximum element.
Example usage is find the first element that has a "price > number" in an array of price data.

Aggregations/Reductions Methods (i.e. mean, sum, std)

Compute mean	ndarrayl.mean() Of np.mean(ndarrayl)
Compute statistics	ndarrayl.mean(axis = 1)
over axis.*	ndarrayl.sum(axis = 0)

axis = 0 means column axis, 1 is row exis.

5. Boolean arrays methods

Count # of 'Trues' in boolean array	(ndarrayl > 0).sum()		
If at least one value is 'True'	ndacrayl.any()		
If all values are 'True'	ndarrayl.all()		

Note: These methods also work with non-boolean arrays, where non-zero elements evaluate to True.

6. Sorting

Inplace sorting	ndarray1.sort()			
Return a sorted copy instead of inplace	sorted1 = np.sort(ndarray1)			

7. Set methods

Return sorted unique values	np.unique(ndarrayi)				
Test membership of ndarray1 values in [2, 3, 6]	resultRooleanArray = np.inid(ndarray1, [2, 3, 6])				

 Other set methods: intersected(),unionld(), setdiffld(),setworld()

8. Random number generation (np.random)

 Supplements the built-in Python random * with functions for efficiently generating whole arrays of sample values from many kinds of probability distributions.

samples = rp.random.normal(size =13, 3))

Python built-in random ONLY samples

Created by Arianne Colton and Sean Chen

www.datasciencefree.com Based on content from 'Python for Data Analysis' by Wes McKinney

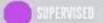
Updated: August 18, 2016

MACHINE LEARNING IN EMOJI









human builds model based on input / output

human input, machine output human utilizes if satisfactory

REINFURCEMENT

human input, machine output human reward/punish, cycle continues



K-MEANS

cluster.KMeans()

Similar datum into groups



BASIC REGRESSION



linear_model.LinearRegression()

Lots of numerical data









linear_model.LogisticRegression()

Target variable is categorical





CLASSIFICATION





neural_network.MLPClassifier()

Complex relationships. Prone to overfitting Basically magic.





neighbors.KNeighborsClassifier()

Group membership based on proximity





DECISION TREE

tree DecisionTreeClassifier()

If/then/else. Non-contiguous data Can also be regression







RANDOM FOREST

ensemble.RandomForestClassifier()

Find best split randomly Can also be regression











SVM

svm.SVC() svm.LinearSVC()

Maximum margin classifier. Fundamental Data Science algorithm





MVI BY & GaussianNB() MultinomialNB() BernoulliNB()

Updating knowledge step by step with new info



based on centroids

Finding outliers through grouping











FEATURE REDUCTION

T-BISTRIS STOCKASTIC NEIF EMBEDDING manifold.TSNE()

Visualize high dimensional data. Convert similarity to joint probabilities



PRINCIPLE COMPONENT ANALYSIS decomposition.PCA()

Distill feature space into components that describe greatest variance



CANONICAL CORRELATION ANALYSIS decomposition.CCA()

Making sense of cross-correlation matrices



LINEAR DISCRIMINANT ANALYSIS

Linear combination of features that separates classes



OTHER IMPORTANT CONCEPTS

BIAS VARIANCE TRADEOFF

UNDERFITTING / OVERFITTING



ACCURACY FUNCTION

(TP + TN)/(P + N)

PRECISION FUNCTION

TP / (TP + FP)

SPECIFICITY FUNCTION

TN / (FP + TN)

SENSITIVITY FUNCTION

TP / (TP + FN)



@emilyinamillion made this

Keras

Learn Python for data science Interactively at www.DataCamp.com



Keras

Keras is a powerful and easy-to-use deep learning library for Theano and TensorFlow that provides a high-level neural networks API to develop and evaluate deep learning models.

A Basic Example

Data

Also see NumPy, Pandas & Scikit-Learn

Your data needs to be stored as NumPy arrays or as a list of NumPy arrays. Ideally, you split the data in training and test sets, for which you can also resort to the train test split module of sklearn.cross validation.

Keras Data Sets

Other

```
>>> from urllib.request import urlopen
>>> data = np.loadtxt(urlopen("http://archive.ics.uci.edu/
ml/machine-learning-databases/pima-indians-diabetes/
pima-indians-diabetes.data"),delimiter=",")
>>> X = data[:,0:8]
>>> y = data [:,8]
```

Model Architecture

Sequential Model

```
>>> from keras.models import Sequential
>>> model = Sequential()
>>> model2 = Sequential()
>>> model3 = Sequential()
```

Multilayer Perceptron (MLP)

Binary Classification

```
>>> model.add(Dense(1,kernel_Initializer='uniform',activation='sigmoid'))
Multi-Class Classification
>>> from keras.layers import Dropout
>>> model.add(Dense(512,activation='relu',input_shape=(784,)))
>>> model.add(Dropout(0.2))
>>> model.add(Dense(512,activation='relu'))
>>> model.add(Dropout(0.2))
>>> model.add(Dropout(0.2))
>>> model.add(Dense(10,activation='softmax'))
```

egression

```
>>> model.add(Dense(64,activation='relu',input_dim=train_data.shape[1]))
>>> model.add(Dense(1))
```

Convolutional Neural Network (CNN)

```
>>> from keras.layers import Activation, Conv2D, MaxPooling2D, Flatten
>>> model2.add(Conv2D(32,(3,3),padding='same',input shape=x train.shape[1:]))
>>> model2.add(Activation('relu'))
>>> mode12.add(Conv2D(32,(3,3)))
>>> model2.add(Activation('relu'))
>>> model2.add(MaxPooling2D(pool size=(2,2)))
>>> model2.add(Dropout(0.25))
>>> model2.add(Conv2D(64,(3,3), padding='same'))
>>> model2.add(Activation('relu'))
>>> mode12.add(Conv2D(64,(3, 3)))
>>> model2.add(Activation('relu'))
>>> model2.add(MaxPooling2D(pool size=(2,2)))
>>> model2.add(Dropout(0.25))
>>> model2.add(Flatten())
>>> mode12.add(Dense(512))
>>> model2.add(Activation('relu'))
>>> mode12.add(Dropout(0.5))
>>> model2.add(Dense(num classes))
>>> model2.add(Activation('softmax'))
```

Recurrent Neural Network (RNN)

```
>>> from keras.klayers import Embedding,LSTM
>>> model3.add(Embedding(20000,128))
>>> model3.add(LSTM(128,dropout=0.2,recurrent_dropout=0.2))
>>> model3.add(Dense(1,activation='sigmoid'))
```

Preprocessing

Sequence Padding

```
>>> from keras.preprocessing import sequence
>>> x train4 = sequence.pad sequences(x train4,maxlen=80)
>>> x test4 = sequence.pad sequences(x test4,maxlen=80)
```

One-Hot Encoding

```
>>> from keras.utils import to_categorical
>>> Y_train = to_categorical(y_train, num_classes)
>>> Y_test = to_categorical(y_test, num_classes)
>>> Y_train3 = to_categorical(y_train3, num_classes)
>>> Y_test3 = to_categorical(y_test3, num_classes)
```

Train and Test Sets

Also see NumPy & Scikit-Learn

Standardization/Normalization

```
>>> from sklearn.preprocessing import StandardScaler
>>> scaler = StandardScaler().fit(x_train2)
>>> standardized X = scaler.transform(x_train2)
>>> standardized_X_test = scaler.transform(x_test2)
```

Inspect Model

```
>>> model.output_shape
>>> model.summary()
>>> model.get_config()
>>> model.get_weights()

Model output shape
Model summary representation
Model configuration
List all weight tensors in the model
```

Compile Model

metrics=['mae'])

Recurrent Neural Network

```
>>> model3.compile(loss='binary crossentropy', optimizer='adam', metrics=['accuracy'])
```

Model Training

Evaluate Your Model's Performance

Prediction

```
>>> model3.predict(x_test4, batch_size=32)
>>> model3.predict_classes(x_test4,batch_size=32)
```

Save/Reload Models

```
>>> from keras.models import load_model
>>> model3.save('model_file.h5')
>>> my_model = load_model('my_model.h5')
```

Model Fine-tuning

Optimization Parameters

Early Stopping

DataCamp



Bokeh

Learn Bokeh Interactively at www.DataCamp.com, taught by Bryan Van de Ven, core contributor



Plotting With Bokeh

The Python interactive visualization library Bokeh enables high-performance visual presentation of large datasets in modern web browsers.



Bokeh's mid-level general purpose bokeh.plotting interface is centered around two main components; data and glyphs.



The basic steps to creating plots with the bokeh. plotting interface are:

1. Prepare some data:

Python lists, NumPy arrays, Pandas DataFrames and other sequences of values

- 2. Create a new plot
- 3. Add renderers for your data, with visual customizations
- 4. Specify where to generate the output
- 5. Show or save the results

```
>>> from bokeh.plotting import figure
>>> from bokeh.io import output file, show
>>> x = [1, 2, 3, 4, 5]
>>> y = [6, 7, 2, 4, 5]
>>> p = figure(title="simple line example", < Stop 2)
             x axis label-'x',
              v axis label='v')
>>> p.line(x, y, legend-"Temp.", line width-2)
>>> output file ("lines.html") - Stop (
>>> show(p) <5tep 5
```

Data

Under the hood, your data is converted to Column Data Sources. You can also do this manually:

```
>>> import numpy as np
>>> import pandas as pd
>>> df = pd.DataFrame(np.array([[33.9,4,65, 'US'],
                                           [32.4,4,66, 'Asia'],
                           [21.4,4,109, 'Europe']]),
columns=['mpg','cyl', 'hp', 'origin'],
index=['Toyota', 'Fiat', 'Volvo'])
>>> from bokeh.models import ColumnDataSource
```

Plottina

>>> cds df = ColumnDataSource(df)

```
>>> from bokeh.plotting import figure
>>> p1 = figure(plot width=300, tools='pan,box zoom')
>>> p2 = figure(plot width=300, plot height=300,
               x range=(0, 8), y range=(0, 8))
>>> p3 = figure()
```

Renderers & Visual Customizations

```
Glyphs
          Scatter Markers
```

```
>>> pl.circle(np.array([1,2,3]), np.array([3,2,1]),
            fill color='white')
>>> p2.square(np.array([1.5,3.5,5.5]), [1,4,3],
            color='blue', size=1)
```

Line Glyphs

>>> from bokeh.layouts import gridplot

>>> layout = gridplot([[p1,p2],[p3]])

>>> tab1 = Panel(child=p1, title="tab1")

>>> tab2 = Panel(child=p2, title="tab2")

>>> layout = Tabs(tabs=[tab1, tab2])

>>> from bokeh.models.widgets import Panel, Tabs

>>> p1.line([1,2,3,4], [3,4,5,6], line width=2) >>> p2.multi line(pd.DataFrame([[1,2,3],[5,6,7]]), pd.DataFrame([[3,4,5],[3,2,1]]), color="blue")

Rows & Columns Layout

```
>>> from bokeh.layouts import row >>> from bokeh.layouts import columns
>>> layout = row(p1,p2, p3)
                                  >>> layout - column(p1,p2,p3)
Nesting Rows & Columns
>>>layout = row(column(p1,p2), p3)
```

Linked Plots

Linked Axes

>>> p2.x range - p1.x range >>> p2.y range = p1.y range

Linked Brushing

>>> p4 = figure(plot width = 100, tools='box select, lasso select') >>> p4.circle('mpg', 'cyl', source=cds df) >>> p5 = figure(plot width = 200, tools='box select,lasso select') >>> p5.circle('npg', 'hp', source-cds df) >>> layout = row(p4.p5)

>>> p.add tools(hover)

Colormapping

Customized Glyphs

Selection and Non-Selection Glyphs

>>> p.circle('mpg', 'cyl', source-cds df,

>>> color mapper = CategoricalColorMapper(

>>> p.circle('mpg', 'cyl', source=cds df,

selection color='red',

nonselection alpha=0.1)

>>> hover - HoverTool(tooltips-None, mode-'vline')

color=dict (field='origin',

factors=['Europe', 'Asia', 'US'],

palette=['red', 'green', 'blue'])

transform-color mapper),

legend='Origin'))

Legends

Grid Lavout

>>> row2 - [p3]

>>> row1 = [p1,p2]

Tabbed Layout

Inside Plot Area >>> p.legend.location = 'bottom left' Outside Plot Area

>>> r1 = p2.asterisk(np.array([1,2,3]), np.array([3,2,1])
>>> r2 = p2.line([1,2,3,4], [3,4,5,6])
>>> legend = Legend(items=[("One", [p1, r1]),("Two", [r2])], location=(0, -30)) >>> p.add_layout(legend, 'right')

Legend Orientation

>>> p.legend.orientation = "horizontal" >>> p.legend.orientation = "vertical"

>>> p.legend.border line color = "navy" >>> p,legend,background fill color - "white"

Output

Output to HTML File

>>> from bokeh.io import output file, show >>> output file ('my bar chart.html', mode='cdn')

Notebook Output

>>> from bokeh.io import output notebook, show >>> output notebook()

Embedding

Standalone HTML

>>> from bokeh.embed import file html >>> html = file html(p, CDN, "my plot") Components >>> from bokeh.embed import components >>> script, div = components(p)

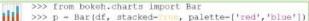
Show or Save Your Plots

>>> show(p1) >>> save (p1) >>> show(layout) >>> save(layout)

Statistical Charts With Bokeh

Bokeh's high-level bokeh. charts interface is ideal for quickly creating statistical charts

Bar Chart



Box Plot



>>> from bokeh.charts import BoxPlot >>> p = BoxPlot(df, values='vals', label='cyl', legend='bottom right')

Histogram



>>> from bokeh.charts import Histogram >>> p = Histogram(df, title='Histogram')

Scatter Plot

>>> from bokeh.charts import Scatter >>> p - Scatter(df, x-'mpg', y -'hp', marker-'square', xlabel='Miles Per Gallon', ylabel-'Horsepower')

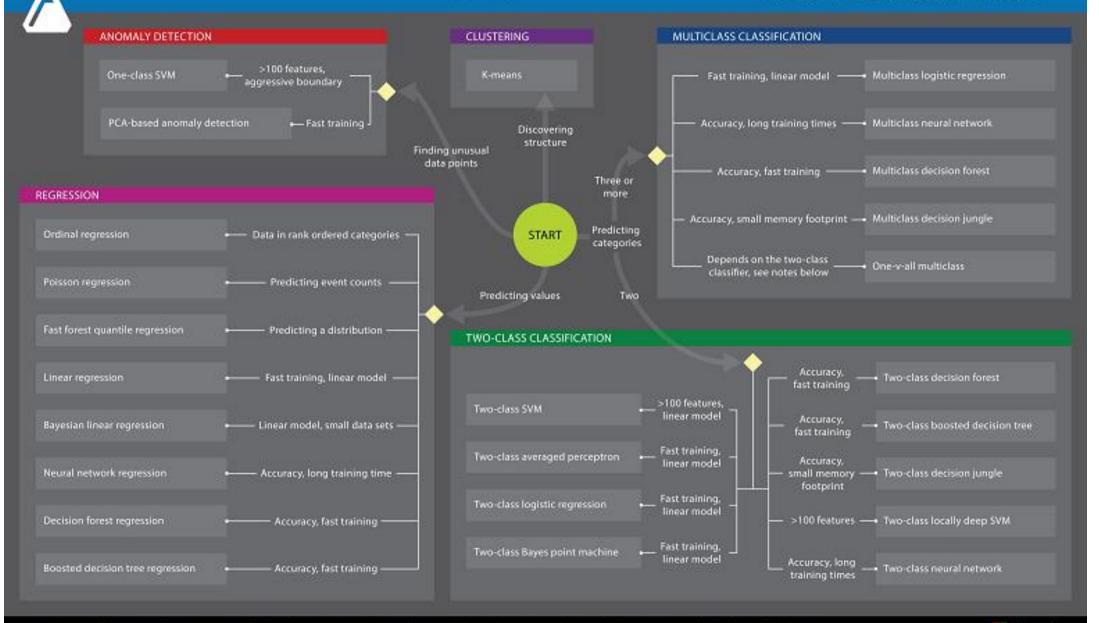
DataCamp

Learn Python for Data Science Interactively



Microsoft Azure Machine Learning: Algorithm Cheat Sheet

This cheat sheet helps you choose the best Azure Machine Learning Studio algorithm for your predictive analytics solution. Your decision is driven by both the nature of your data and the question you're trying to answer.



Data Wrangling

with pandas
Cheat Sheet
http://pandas.pydata.org

Syntax – Creating DataFrames

	1	4		7	10	
	2	5	1	В	11	
	3	6		9	12	
i	ind.Dad.Dad.[4, [5, [6,].]	{"a" "b" "c" dex = es for e taFra 7, 10 8, 11 9, 12 =[1, ns=['	: [4 : [7 : [1, ach c me(],],], a',	, 8, 0, 1 2, olum	9], 1, 12 3])	
			а	b	c	
	n	v				
	d	1	4	7	10	
		2	5	8	11	
	е	2	6	9	12	
df = p	od.Da	taFra	me(

Method Chaining

index = pd.MultiIndex.from tuples(

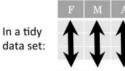
Create DataFrame with a MultiIndex

[('d',1),('d',2),('e',2)],

names=['n','v'])))

Most pandas methods return a DataFrame so that another pandas method can be applied to the result. This improves readability of code.

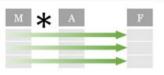
Tidy Data - A foundation for wrangling in pandas







Tidy data complements pandas's vectorized operations. pandas will automatically preserve observations as you manipulate variables. No other format works as intuitively with pandas.

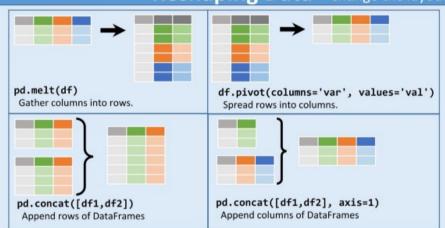


M * A

Each variable is saved in its own column

Each **observation** is saved in its own **row**

Reshaping Data – Change the layout of a data set

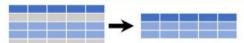


- df.sort values('mpg')
- Order rows by values of a column (low to high).
- df.sort_values('mpg',ascending=False)
 Order rows by values of a column (high to low).
- df.rename(columns = {'y':'year'})
- Rename the columns of a DataFrame
- df.sort_index()
 Sort the index of a DataFrame
- df.reset_index()

Reset index of DataFrame to row numbers, moving index to columns.

df.drop(['Length','Height'], axis=1)
Drop columns from DataFrame

Subset Observations (Rows)



df[df.Length > 7]

Extract rows that meet logical criteria.

df.drop_duplicates()
 Remove duplicate rows (only

df.head(n)
Select first n rows.

considers columns).

df.tail(n)
Select last n rows.

df.sample(frac=0.5)

Randomly select fraction of rows.

df.sample(n=10)

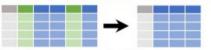
Randomly select n rows.

df.iloc[10:20]
Select rows by position.

df.nlargest(n, 'value')
 Select and order top n entries.

df.nsmallest(n, 'value')
Select and order bottom n entries.

Subset Variables (Columns)



df[['width', 'length', 'species']]
Select multiple columns with specific names.

df['width'] or df.width

Select single column with specific name.

df.filter(regex='regex')

Select columns whose name matches regular expression regex.

regex (Regular Expressions) Examples		
'\.'	Matches strings containing a period '.'	
'Length\$'	Matches strings ending with word 'Length'	
'^Sepal'	Matches strings beginning with the word 'Sepal'	
'^x[1-5]\$'	Matches strings beginning with 'x' and ending with 1,2,3,4,5	
''^(?!Species\$).*'	Matches strings except the string 'Species'	

df.loc[:,'x2':'x4']

Select all columns between x2 and x4 (inclusive).

df.iloc[:,[1,2,5]]

Select columns in positions 1, 2 and 5 (first column is 0).

df.loc[df['a'] > 10, ['a','c']]

Select rows meeting logical condition, and only the specific columns .

Logic in Python (and pandas)

Linear Vector Spaces:

Definition: A linear vector space, X is a set of elements (vectors) defined over a scalar field, F, that satisfies the following conditions:

1) if $\chi \in X$ and $y \in X$ then $\chi + y \in X$. 2) $\chi + y = y + \chi$ 3) $(\chi + y) + z = \chi + (y + z)$

There is a unique vector θ∈ X, such that x + θ = x for all x ∈ X.

 For each vector χ∈ X there is a unique vector in X, to be called ⟨¬χ⟩, such that multiplication, for all scalars a ∈ F, and all vectors x ∈ X, For any χ∈ X, 1χ-χ (for scalar 1).

8) For any two scalars $a \in F$ and $b \in F$ and any $x \in X$, a(bx) = (ab)x.

9) (a+b) x=ax+bx. 10) a(x+y)=ax+ay.

Linear Independence: Consider n vectors {x 1, x 3,..., x a }. If there exists n scalars a), a), ..., a, at least one of which is nonzero, such that $a_1x_1 + a_2x_2 + ... + a_nx_n = 0$, then the $\{x_i\}$ are linearly dependent.

Spanning a Space:

Let X be a linear vector space and let $\{u_1, u_2, ..., u_n\}$ be a subset of vectors in X. This subset spans X if and only if for every vector $x \in X$ there exist scalars x_k $x_0,...,x_n$ such that $x = x_0u_0 + x_0u_2 + ... + x_nu_n$

Inner Product: (x,y) for any scalar function of x and y.

1.(x,y) = (y,x) 2. $(x,ay_1 + by_2) = a(x,y_1) + b(x,y_2)$

(x,x) ≥ 0, where equality holds iff x is the zero vector.

Norm: Ascalar function ||x|| is called a norm if it satisfies:

 $1. \|x\| > 0$

2. ||x|| = 0 if and only if x = 0.

 $3. \|ax\| = |a| \|x\|$

 $4. \|x + y\| \le \|x\| + \|y\|$

Angle: The angle θ bet. 2 vectors x and y is defined by $\cos \theta = \frac{(xy)}{\|x\|\|y\|}$

Orthogonality: 2 vectors $x, y \in X$ are said to be orthogonal if (x,y) = 0.

Gram Schmidt Orthogonalization:

Assume that we have n independent vectors $y_0 y_0 \dots y_n$. From these vectors we will obtain n orthogonal vectors $v_{j_1} v_{j_2} ..., v_{n_n}$.

$$v_1 = y_1$$
, $v_k = y_k - \sum_{i=1}^{k-1} \frac{(v_i, y_k)}{(v_i, v_l)} v_i$,

where $\frac{(v_i, y_k)}{(v_i, v_i)} v_i$ is the projection of y_k on v_i

$$x = \sum_{i=1}^{n} x_i v_i = x_1 v_1 + x_2 v_2 + \dots + x_n v_n,$$

$$for orthogonal \ vectors, x_j = \frac{(v_j, x)}{(v_j, v_j)}$$

To compute the reciprocal basis vectors: set $\mathbf{B} = [v_1 \ v_2 \ ... \ v_n]$,

 $\mathbf{R} = [\mathbf{r}_1 \ \mathbf{r}_2 \dots \ \mathbf{r}_n], \ \mathbf{R}^T = \mathbf{B}^{-1} \quad \text{In matrix form: } \mathbf{x}^v = \mathbf{B}^{-1} \ \mathbf{x}^s$

Transformations:

A transformation consists of three parts:

domain: $X = \{x_i\}$, range: $Y = \{y_i\}$, and a rule relating each $x_i \in$ X to an element $y_i \in Y$.

Linear Transformations: transformation A is linear if:

1. for all $x_1, x_2 \in X$, $A(x_1+x_2) = A(x_1) + A(x_2)$

2. for all $x \in X$, $a \in R$, A(ax) = aA(x)

Matrix Representations:

Let $\{v_1, v_2, ..., v_n\}$ be a basis for vector space X, and let $\{u_1, u_2, ..., u_n\}$ be a basis for vector space Y. Let A be a linear transformation with domain X and range Y: A(x) = y

The coefficients of the matrix representation are obtained from

$$A(v_j) = \sum_{i=1}^{m} a_{ij}u_i$$

Change of Basis: $\mathbf{B}_t = [\mathbf{t}_1 \ \mathbf{t}_2 \ ... \ \mathbf{t}_n]$, $\mathbf{B}_w = [\mathbf{w}_1 \ \mathbf{w}_2 \ ... \ \mathbf{w}_n]$ $\mathbf{A}' = [\mathbf{B}_w^{-1} \mathbf{A} \mathbf{B}_t]$

Eigenvalues & Eigenvectors: $Az = \lambda z$, $|[A - \lambda I]| = 0$

Diagonalization: $B = [z_1 \ z_2 ... z_n]$,

where $\{z, z_2, ..., z_n\}$ are the eigenvectors of a square matrix A, $[\mathbf{B}^{-1}\mathbf{A}\mathbf{B}] = \operatorname{diag}([\lambda_1 \ \lambda_2 \dots \lambda_n])$

Perceptron Architecture:

$$\mathbf{a} = hardlim(\mathbf{W}\mathbf{p} + \mathbf{b}), \mathbf{W} = \begin{bmatrix} \mathbf{a}\mathbf{w}^T & \mathbf{w}^T & \dots & \mathbf{s}\mathbf{w}^T \end{bmatrix}^T,$$

 $a_t = hardlim(n_t) = hardlim(\mathbf{a}\mathbf{w}^T \mathbf{p} + b_t)$

Decision Boundary: $_{i}\mathbf{w}^{T}\mathbf{p} + b_{i} = 0$

The decision boundary is always orthogonal to the weight vector. Single-layer perceptrons can only classify linearly separable vectors.

$$\frac{\text{Perceptron Learning Rule}}{\mathbf{W}^{new} = \mathbf{W}^{old} + \mathbf{e}\mathbf{p}^{T}, \mathbf{b}^{new} = \mathbf{b}^{old} + \mathbf{e},$$

$$\text{where } \mathbf{e} = \mathbf{t} - \mathbf{a}$$

Hebb's Postulate: "When an axon of cell A is near enough to excite a cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A's efficiency, as one of the cells firing B, is increased."

Linear Associator: a = purelin(Wp)

The Hebb Rule: Supervised Form: $w_{ij}^{new} = w_{ij}^{old} + t_{ql}P_{ql}$

Rule: Supervised Form:
$$\mathbf{W}_{ij}^{ever} = \mathbf{W}_{ij}^{ever}$$

$$\mathbf{W} = \mathbf{t}_1 \mathbf{P}_1^T + \mathbf{t}_2 \mathbf{P}_2^T + \dots + \mathbf{t}_Q \mathbf{P}_Q^T$$

$$\mathbf{W} = \begin{bmatrix} \mathbf{t}_1 \ \mathbf{t}_2 \ \dots \mathbf{t}_Q \end{bmatrix} \begin{bmatrix} \mathbf{p}_1^T \\ \mathbf{p}_2^T \\ \vdots \\ \mathbf{p}_Q^T \end{bmatrix} = \mathbf{T} \mathbf{P}^T$$

Pseudoinverse Rule: W = TP

When the number, R, of rows of P is greater than the num ber of columns,Q, of P and the columns of P are independent, then the pseudoinverse can be computed by $\mathbf{P}^+ = (\mathbf{P}^T \mathbf{P})^{-1} \mathbf{P}^T$

Variations of Hebbian Learning:

Filtered Learning (Ch. 16): $\mathbf{W}^{new} = (1 - \gamma)\mathbf{W}^{old} + \alpha \mathbf{t}_q \mathbf{p}_q^T$

Delta Rule (Ch.10):
$$\mathbf{W}^{new} = \mathbf{W}^{old} + \alpha(\mathbf{t}_q - \mathbf{a}_q)\mathbf{p}_q^T$$

Unsupervised Hebb (Ch.13): $\mathbf{W}^{n_{GW}} = \mathbf{W}^{old} + \alpha \mathbf{a}_{g} \mathbf{p}_{g}^{T}$

$$\frac{\text{Taylor:}}{\frac{1}{2}}F(\mathbf{x}) = F(\mathbf{x}^*) + \nabla F(\mathbf{x})^T|_{\mathbf{x} = \mathbf{x}^*} (\mathbf{x} - \mathbf{x}^*) + \frac{1}{2}(\mathbf{x} - \mathbf{x}^*)\nabla^2 F(\mathbf{x})^T|_{\mathbf{x} = \mathbf{x}^*} (\mathbf{x} - \mathbf{x}^*) + \cdots$$

Grad
$$\nabla F(\mathbf{x}) = \begin{bmatrix} \frac{\partial}{\partial \mathbf{x}_1} F(\mathbf{x}) & \frac{\partial}{\partial \mathbf{x}_2} F(\mathbf{x}) & \dots & \frac{\partial}{\partial \mathbf{x}_n} F(\mathbf{x}) \end{bmatrix}^T$$

Hessian:
$$\nabla^2 F(x) =$$

$$\frac{\text{Hessian:}}{\left[\frac{\partial}{\partial x_1^2}F(\mathbf{x}) = \frac{\partial}{\partial x_1 \partial x_2}F(\mathbf{x}) \dots \frac{\partial}{\partial x_1 \partial x_n}F(\mathbf{x})\right]} = \frac{\left[\frac{\partial}{\partial x_1^2}F(\mathbf{x}) \frac{\partial}{\partial x_1 \partial x_2}F(\mathbf{x}) \dots \frac{\partial}{\partial x_1 \partial x_n}F(\mathbf{x})\right]}{\left[\frac{\partial}{\partial x_2 \partial x_1}F(\mathbf{x}) \frac{\partial}{\partial x_2^2}F(\mathbf{x}) \dots \frac{\partial}{\partial x_2^2}F(\mathbf{x})\right]} = \frac{\partial}{\partial x_n \partial x_1}F(\mathbf{x}) = \frac{\partial}{\partial x_n \partial x_2}F(\mathbf{x}) \dots = \frac{\partial}{\partial x_n^2}F(\mathbf{x})$$

$$\frac{1^{\text{st Dir.Der.:}}}{\|\mathbf{p}\|} \xrightarrow{\mathbf{p}^T \nabla F(\mathbf{x})} \frac{\mathbf{p}^T \nabla^2 F(\mathbf{x}) \mathbf{p}}{\|\mathbf{p}\|^2}$$

Minima:

Strong Minimum: if a scalar $\delta > 0$ exists, such that $F(x) < F(x + \Delta x)$ for all Δx such that $\delta > ||\Delta x|| > 0$. Global Minimum: if $F(x) \le F(x + \Delta x)$ for all $\Delta x \ne 0$ Weak Minimum: if it is not a strong minimum, and a scalar $\delta > 0$ exists, such that $F(x) \leq F(x + \Delta x)$ for all Δx such that $\delta > ||\Delta x|| > 0$.

Necessary Conditions for Optimality:

 I^{st} -Order Condition: $\nabla F(\mathbf{x})|_{\mathbf{x}=\mathbf{x}^*} = 0$ (Stationary Points) 2^{vd} -Order Condition: $\nabla^2 F(\mathbf{x})|_{\mathbf{x}=\mathbf{x}^*} \ge 0$ (Positive Semidefinite Hessian Matrix).

Quadratic fn.:
$$F(x) = \frac{1}{2}x^{T}Ax + d^{T}x + c$$

$$\nabla F(x) = \mathbf{A}\mathbf{x} + \mathbf{d}, \ \nabla^2 F(x) = \mathbf{A}, \ \lambda_{min} \le \frac{\mathbf{p}^T \mathbf{A} \mathbf{p}}{\|\mathbf{p}\|^2} \le \lambda_{max}$$