Signal combination in vibration perception

Shasha Wei^{1,2} Alex R. Wade^{1,3} Catherine E.J. Preston¹ & Daniel H. Baker¹

ORCID:

Shasha Wei: https://orcid.org/0009-0002-8975-4214 Alex Wade: https://orcid.org/0000-0003-4871-2747

Catherine Preston: https://orcid.org/0000-0001-7158-5382 Daniel Baker: https://orcid.org/0000-0002-0161-443X

Corresponding author

Shasha Wei, Email: mfv507@york.ac.uk

Present address:

¹Department of Psychology, University of York, York, UK, YO10 5DD

Author Contributions

D.H.B. designed research; S.W. performed research; S.W., A.R.W. and D.H.B. analysed data; and S.W., A.R.W., C.E.J.P. and D.H.B. wrote and revised the paper.

Competing Interests

The authors declare no competing interest.

Classification: Social Science-Psychological and Cognitive Sciences

Keywords: vibrotactile summation, suppression, somatosensory, computational modelling

This manuscript was deposited as a preprint on PsyArXiv (DOI: 10.31234/osf.io/yjv6s) under the CC-BY Attribution 4.0 International license.

¹Department of Psychology, University of York, UK, YO10 5DD

²Corresponding author, email: mfv507@york.ac.uk

³York Biomedical Research Institute, University of York, UK, YO10 5D

Abstract

While the brain's integration of auditory and visual inputs has been extensively investigated, the mechanisms underlying the combination of somatosensory signals remain less explored. Here, we investigated vibrotactile summation across fingers using psychophysical and electrophysiological methods. In Experiment 1, discrimination thresholds for 26 Hz vibrations were measured using a two-alternative forced-choice (2AFC) task. Thresholds exhibited a 'dipper' pattern when plotted against baseline intensity level. Detection thresholds decreased by approximately 1dB when all ten fingers were stimulated ('dekadactyl' condition) simultaneously compared to when each alternate finger was stimulated ('pentadactyl' condition), suggesting a process of probability summation. When a target stimulus was presented to five digits and a baseline stimulus to the remaining digits ('dichodactyl' condition) simultaneously, thresholds increased, consistent with suppression between digit representations. In Experiment 2, steady-state somatosensory evoked potential (SSSEP) signals showed approximately a 1.4-fold amplitude increase in dekadactyl compared to pentadactyl conditions, indicating a summation effect. Conversely, SSSEP amplitudes decreased when targets and masks were presented simultaneously at different frequencies, providing additional evidence of suppression. These results are consistent with a model featuring inhibition between digits and reveal that the weight of suppression is intermediate between that observed in binocular vision and binaural hearing.

Keywords:

vibrotactile summation, suppression, somatosensory, computational modelling

Significance

Suppression is known to occur both between the eyes and the ears, but how does the brain combine tactile inputs from multiple fingers? Using psychophysical threshold measurements and EEG recordings, we found that doubling the inputs led to a weak improvement in threshold and an increase in EEG amplitude, though less than double. This suggests that the combination of vibration signals involves both probability summation and suppressive processes. Computational modelling further suggests a unique mechanism of tactile integration, distinct from those observed in vision and audition.

Introduction

Signal combination is crucial for human perception and our interaction with the environment. Our sensory systems comprise a variety of receptors and neural pathways that detect and process a wide range of stimuli, including sight, hearing, touch, and smell. To construct a coherent and comprehensive representation of our surroundings and our own body, the brain must filter out overlapping or redundant information and avoid excessively strong signals to prevent sensory overload. Therefore, in addition to additive processes, suppressive processes are also involved in signal combination. This suppression during signal combination has been investigated both within (e.g., vision, hearing, touch, 1, 2–4) and between (e.g., visuo-tactile, audio-visual, 5, 6) modalities.

In visual and auditory perception, psychophysical studies have shown that detection performance for binocular or binaural presentation is typically between a factor of $\sqrt{2}$ and 2 better than for monocular or monaural presentation (2, 7, 8). This summation at threshold implies the existence of physiological mechanisms that combine signals across eyes or ears. Above threshold, detection performance improves when a weak fixed intensity ('pedestal') stimulus is added, a phenomenon known as facilitation. At higher intensity pedestals performance worsens, producing a masking effect. When plotted against baseline intensity, the discrimination thresholds exhibit a "dipper" shape (see Figure 4b). The facilitation and masking effects arise from the brain transducing physical signals into neural responses in a non-linear manner, and are observed for many sensory stimuli (reviewed by 9).

To complement psychophysical work, we can directly measure the response to stimuli of different intensities by recording brain activity. One convenient method is the steady state technique, in which periodic stimulus oscillations are reflected in electromagnetic neural responses at the same frequency, which can be recorded using EEG or MEG. For instance, some EEG studies have investigated the signal combination process in visual and auditory modalities by recording steady-state signals (1, 2). These studies found that responses increased when input channels (eyes or ears) were doubled, but by less than a factor of two. Additionally, when a mask was added to one channel instead of a signal input (i.e. oscillating at a different frequency), the signal response decreased due to suppression.

The process by which the brain combines multiple signals has attracted great interest in recent years, leading to the development of several computational models. The two stage gain control model of signal combination (10) successfully accounts for both binocular and binaural perception, positing that the signal from one channel (left or right) is inhibited by the other channel before being summed. The equations describing this model are defined as:

$$Stage1_L = \frac{I_L^m}{S + I_L + \omega I_R} \tag{1}$$

$$Stage1_{R} = \frac{I_{R}^{m}}{S + I_{R} + \omega I_{L}} \tag{2}$$

$$sum = Stage1_L + Stage1_R \tag{3}$$

$$resp = \frac{sum^p}{Z + sum^q} \tag{4}$$

In this model, sensory inputs from adjacent channels are processed in two stages. At the first stage, each input undergoes gain control, where the response from one channel is suppressed by the input from the other channel. This is described by Equations 1 and 2. For example, the left channel response $(Stage1_L)$ depends not only on its own stimulus intensity (I_L) but also on the intensity of the right channel (I_R) , modulated by the suppression weight ω . The exponent m and saturation constant S are free parameters and determine how the input is transformed nonlinearly. The outputs of the left and right channels are then summed to form sum(Equation 3), which represents the combined signal strength after inter-channel suppression. This combined signal is then passed through a nonlinear transducer function (Equation 4), which produces the final response (resp) based on the free parameters p, q and Z. These parameters govern the gain and saturation characteristics of the system. In vision, the weight of suppression is approximately $\omega=1$, whereas in auditory perception, suppression between the ears is dramatically weaker, with ω close to 0. Therefore, while suppression can be key to signal combination, its strength varies across different sensory modalities.

In tactile perception, some neuroimaging findings suggest there exist summation and suppression of vibration signals also. For instance, studies have recorded brain responses to vibration stimuli delivered to two fingers separately and simultaneously. Results indicated that at low levels of stimulation near the perceptual threshold, there was a facilitation or summation effect between two fingers. However, at higher levels of stimulation, a suppression effect was observed (4). Furthermore, the brain's response to simultaneous vibration of two fingers is less than (approximately 50% of) the sum of the responses to individual finger stimuli (3, 4). In addition, the extent of suppression is dependent on the spatial distance between the fingers (4, 11). In some psychophysical studies, researchers measured vibration detection thresholds using various contactor sizes (12, 13). Results showed that the threshold decreased as the contactor size increased, a phenomenon known as area summation. Specifically, when the contactor size was doubled, the threshold decreased by approximately 3 dB (a factor of 1.4 (12)). These findings focused on the summation rather than suppression between inputs, because suppressive processes are minimal at low intensities near threshold. In summary, although substantial evidence suggests the existence of suppression in vibration combination, there has been relatively little work measuring psychophysical threshold, and a corresponding computational model has yet to be developed.

Here, we combine psychophysical measurements (Experiment 1) with EEG recordings (Experiment 2) to assess human vibration perception, and fit a computational model to interpret the processes of vibration signal combination and suppression. In Experiment 1, we measure how thresholds vary across different conditions and pedestal levels using a two-interval forced-choice (2IFC) task. Our aim is to investigate two processes: the summation effect (by doubling the number of stimulated digits), and the masking effect (by introducing an additional mask stimulus) (see *Psychophysical procedures*). Thresholds decreased by approximately

1 dB when the number of stimulated digits was doubled, a finding consistent with probability summation rather than physiological summation. In psychophysical tasks, probability summation refers to improved detection performance resulting from multiple independent detection opportunities at the decision level (14), whereas physiological summation reflects the neural integration of sensory signals across populations of neurons. Our computational modelling indicated that this effect could potentially be explained without requiring suppression between digits. This is because psychophysical thresholds are determined primarily by the most sensitive subset of neurons relevant to the task, and suppression does not necessarily impact this 2IFC task. In comparison, EEG recordings reflect the overall activity of the entire neuronal population, where suppression between neurons is an important characteristic of sensory perception. Therefore, in our EEG Experiment, we tested these neural mechanisms directly by measuring steady-state somatosensory evoked potentials (SSSEPs). We examined summation by stimulating adjacent digits at the same frequency, and suppression by introducing a second frequency simultaneously (see *EEG procedures*). These different frequencies allowed us to isolate suppressive interactions between digits without the complicating factor of summation. The EEG modelling results indicated an inhibitory weight of suppression of $\omega \sim 0.5$, intermediate between the weights observed for vision ($\omega \sim 1$) and audition ($\omega \sim 0$).

Results

Summation and suppression effects on vibration thresholds

In Experiment 1, participants were required to report which interval included the target stimulus. Individual thresholds were measured using a 3-down-1-up staircase procedure. These data were used to fit psychometric functions, estimating thresholds at 75% correct and slope parameters via cumulative Gaussians. The average thresholds across 8 participants for each condition and baseline intensity level (equivalent to the pedestal contrast in studies of visual contrast discrimination) are shown in Figure 1a. A 4 (condition) \times 8 (baseline intensity level) repeated measures ANOVA was used to assess statistical differences between factors. We found significant main effects of condition (F = 233.52, p < 0.001, $\eta_{G_{-}}^{2} = 0.651$, Greenhouse-Geisser corrected) and baseline intensity level (F = 70.87, p < 0.001, $\eta_G^2 = 0.83$, Greenhouse-Geisser corrected), as well as a significant interaction between the two factors (F = 22.06, p < 0.001, $\eta_G^2 = 0.419$, Greenhouse-Geisser corrected). When plotting the thresholds against baseline intensity level, except for the dichodactyl condition (green diamonds), the other three conditions exhibited a dipper shape. Specifically, at low baseline intensity level (0.5 to 2%), thresholds decreased with increasing baseline intensity level, indicating a facilitation effect. When the baseline intensity level exceeded 2%, thresholds increased due to a masking effect, resulting in approximately parallel 'handles' across the pentadactyl (blue circles), dekadactyl (red squares) and half-dekadactyl (orange triangles) conditions. At detection threshold (baseline intensity level = 0%), the threshold for the dekadactyl condition was around 1 dB lower than for the pentadactyl condition, with no significant difference. This weak summation between digits is lower than that typically attributed to physiological summation (3-6 dB), suggesting a process of probability summation instead (14, 15).

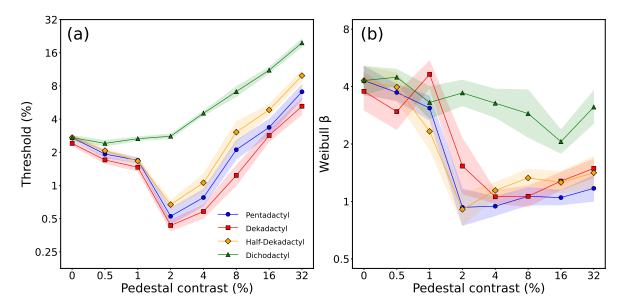


Figure 1: Thresholds (a) and psychometric slope values (b) from Experiment 1. Data are averaged across N=8 participants, with shaded regions indicating $\pm 1SE$ across participants.

Above detection threshold, thresholds in the dekadactyl condition were significantly lower ($t_{7} = 6.63$, p < 0.01, Bonferroni-corrected) than those in the pentadactyl condition. On average, the thresholds decreased by a factor of approximately 1.27 (2.1 dB). Additionally, thresholds in the half-dekadactyl condition, where the baseline stimulus vibrated ten digits, but the target stimulus only vibrated five digits, were higher than those in the dekadactyl condition. These findings could be interpreted as a summation effect when the target inputs were doubled. However, the psychometric function is linearised from the bottom of the dip onwards, which might increase the effects of probability summation (14). We return to this point in the modelling section. In the dichodactyl condition, thresholds increased across all baseline intensity levels, with thresholds elevated by a factor of 7.19 (17.14 dB) at the highest baseline intensity level (32%). This result is consistent with a suppression effect when adding a mask between digits, where the target stimulus could only be detected when it approached the baseline intensity.

The slopes of the psychometric function for each condition are illustrated in Figure 1b. At detection threshold, all conditions exhibited relatively steep slopes, around $\beta = 4$. At low baseline intensity levels (0 to 4%), except for in the dichodactyl condition (green triangles), the slopes decreased with increasing baseline intensity level, approaching $\beta = 1$ at a baseline intensity level of 4%. At higher baseline intensity levels (4% to 32%), the slopes for these

three conditions remained shallow, consistent with previous studies using the same paradigm in other senses (10, 16). In contrast, the slopes in the dichodactyl condition remained steep across all baseline intensity levels, with slight variations in the range $2 < \beta < 5$. This pattern differs from that observed in dichoptic masking in vision (10, 17), where slopes were steep at detection threshold, became shallow at lower contrast levels, and then became very steep again at higher contrast levels. The very steep slopes ($\beta \sim 6$) in dichoptic masking are attributed to mandatory physiological summation between the eyes (18). Therefore, the approximately constant slopes observed in the dichodactyl condition suggest that mandatory physiological summation between digits may not occur here.

Summation and suppression of neural responses

The average amplitude spectra and scalp distributions for four conditions of Experiment 2 are shown in Figure 2a-d. The steady-state EEG signals were strongest at fronto-central electrodes for both frequencies, aligning with findings from previous studies involving finger vibration (19, 20). Therefore, we averaged the EEG responses across six electrodes (F1, F2, Fz, FC1, FC2, FCz) to calculate intensity-response functions at both 23 Hz and 26 Hz.

In the pentadactyl and dekadactyl conditions, where a 26 Hz stimulus was used, we observed a peak at 26 Hz in both Figure 2a and b, with a stronger activity at the fronto-central region in the dekadactyl condition. A similar pattern was observed in the cross-pentadactyl condition, where a 23 Hz stimulus resulted in a peak at 23 Hz (Figure 2c). In the cross-dekadactyl condition (Figure 2d), when two different frequencies were simultaneously presented, peaks were observed at the original frequencies (26 Hz (F1) and 23 Hz (F2)) as well as at specific intermodulation frequencies (20 Hz ($2 \times F2 - F1$) and 29 Hz ($2 \times F1 - F2$)). Additionally, the distribution of activity across the scalp was similar in the cross-dichodactyl and cross-dekadactyl conditions.

Responses as a function of vibration intensity showed monotonic increases for most conditions (Figure 2e,f). Two 6 (condition) \times 5 (intensity) repeated measures ANOVAs were conducted on the EEG amplitudes at each frequency separately. At 26 Hz, significant main effects of condition (F = 67.32, p < 0.001, $\eta_G^2 = 0.309$, Greenhouse-Geisser corrected), intensity level (F = 66.6, p < 0.001, $\eta_G^2 = 0.288$, Greenhouse-Geisser corrected), and a significant interaction effect (F = 25.61, p < 0.001, $\eta_G^2 = 0.115$) were observed. In the pentadactyl condition (blue circles), EEG amplitudes increased monotonically with increasing intensity level (Figure 2e). In the dekadactyl condition (red squares), doubling the inputs led to stronger responses. Compared to the pentadactyl condition, average response amplitudes were higher by a factor of 1.41 across all intensity levels—reflected as a multiplicative scaling of the red line. This suggests a sub-linear summation, where the combined response is greater than in the pentadactyl condition, but less than would be expected from perfect linear summation. If adjacent digit inputs were combined linearly without suppression, we would expect a doubling of response amplitude (i.e., a factor of 2). In the dichodactyl condition (green triangles), the target stimulus was presented to Set A, while a fixed vibration at 32% of maximum intensity

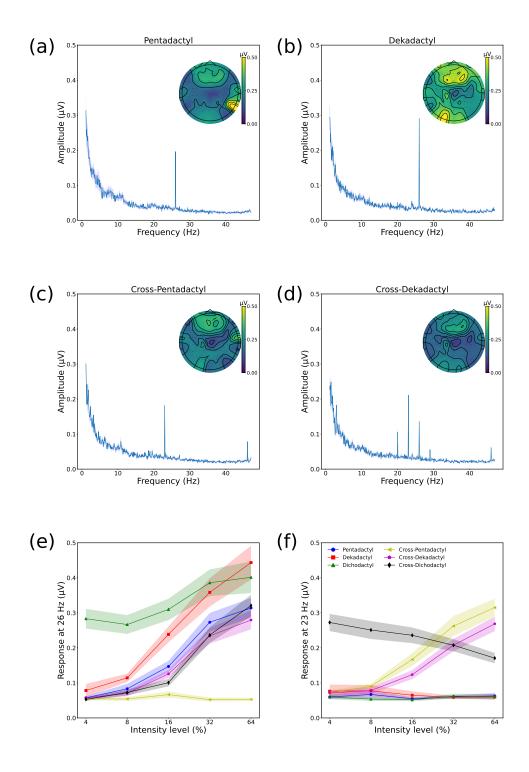


Figure 2: Results of the EEG experiment. Panels (a-d) show Fourier spectra and inset scalp topographies for a subset of four conditions at the highest intensity. Panels (e,f) show intensity-response functions fo&all conditions at 26Hz (e) and 23Hz (f). Data are averaged across N=30 participants, and shaded regions indicate ±1SE across participants.

was presented to Set B, resulting in a high baseline response, and responses that increased with intensity level. At higher intensity levels (32 to 64%), the responses in the dichodactyl condition approximated those in the dekadactyl condition. In the cross-dekadactyl (pink pentagons) and cross-dichodactyl (black diamonds) conditions, two different frequencies were presented simultaneously. Instead of summing, they suppressed each other, leading to weaker responses compared to the pentadactyl condition.

At 23 Hz (Figure 2f), we also found significant main effects of condition (F = 68.27, p < 0.001, $\eta_G^2 = 0.402$, Greenhouse-Geisser corrected), intensity level (F = 33.07, p < 0.001, $\eta_G^2 = 0.069$), as well as a significant interaction effect (F = 28.98, p < 0.001, $\eta_G^2 = 0.255$, Greenhouse-Geisser corrected). Further evidence of suppression was observed in the cross-dekadactyl condition (pink pentagons), where simultaneous 23 Hz and 26 Hz stimuli led to reduced responses compared to the cross-pentadactyl condition (yellow triangles). In the cross-dichodactyl condition (black diamonds), we observed a strong initial response to the 23 Hz mask at 4% target intensity level. However, as the intensity of the 26 Hz target increased, the overall response decreased (F = 14.27, p < 0.001, $\eta_G^2 = 0.33$, Greenhouse-Geisser corrected). This negative trend suggests that the stronger the 26 Hz target, the more it suppressed the response to the 23 Hz mask (Busse et al., 2009). The resulting pattern reflects a masking effect and inter-digit suppression, rather than summation, leading to weaker responses as intensity levels increase. As expected, the three conditions involving only a 26 Hz vibration did not show any measurable responses at 23 Hz (Figure 2f).

Computational modelling results

We began by fitting the data of Experiment 1 using the model of Meese et al. (10), with seven free parameters including the weight of suppression between channels (ω in Equation 1 and Equation 2). Because the combination across channels is linear (following an initial transducer stage), we refer to this as the Linear summation model. The model gave a reasonable fit, as shown in Figure 3a, with an RMS error of 1.79dB (see Table 1 for parameter values). However, two systematic shortcomings are apparent. At detection threshold, the model overestimates the amount of summation (notice the red curve is below the data points for the first three baseline intensity levels). Also, suppression between channels is relatively strong ($\omega = 0.817$), but this results in the slope of the dichodactyl condition (green curve) being steeper than in the empirical data (green triangles).

To address these shortcomings, we added a further parameter to the model - an exponent at the summation stage (see Equation 5), which is the defining feature of the Minkowski summation model. The Minkowski exponent determines how multiple sensory inputs are combined at the perceptual level. At high values, it serves as an approximation of probability summation, which has traditionally been modelled using a MAX operator within a 2IFC signal detection framework (14). As the Minkowski exponent increases, the model shifts from linear integration toward a MAX-like operation, where the strongest input dominates the response.

This provides a flexible way to capture both linear and nonlinear integration, depending on the value of the exponent. The Minkowski summation model provides a much more satisfactory fit (see Figure 3b), with an RMS error of 0.89dB, and no obvious systematic issues with the fit. The Minkowski exponent was estimated at $\gamma = 15.484$ - substantially greater than than the implicit value of $\gamma = 1$ in the Linear summation model, and consistent with the low levels of summation at threshold in the data. Several other parameter values also differ between the models (see Table 1), most notably the weight of suppression (ω) reduces to near-zero. With this architecture, threshold elevation in the dichodactyl condition is caused by the MAX-like operation from the high Minkowski exponent (a true MAX operator would have an exponent of $\gamma = \infty$), meaning that explicit suppression is not required.

To predict the psychometric slopes, we used the estimated parameters from the threshold fitting for each of the two models separately. For each model, we simulated model responses across a range of target stimulus levels. For each target level and condition, we calculated d-prime (d') as the signal difference divided by the internal noise, and obtained the predicted probability of a correct response by passing d' divided by $\sqrt{2}$ through the cumulative normal distribution. The resulting predicted psychometric function was fitted with a cumulative Gaussian using the psignifit, and the predicted slope parameters were extracted from the fitted functions. The results of psychometric slope estimates are shown in Figure 3c and 3d. Both models capture the general features of the slope data. Slopes start steep ($\beta = 4$) at detection threshold, and are linearised to around $\beta = 1.3$ at higher baseline intensities in all but the dichodactyl condition. The dichodactyl slopes remain steep ($\beta > 2$) across the full range of baseline intensities. We note that the additional nonlinearity in the Minkowski model does cause the slope values around detection threshold to be slightly overestimated, but the general trend is correct. Because these slope values are predicted with no additional free parameters, based on the fits at detection threshold (see also ((10))), this increases our confidence in the accuracy of the models.

The absence of suppression in the Minkowski model does not necessarily mean that there is no suppression between digits - since psychophysical responses are assumed to be based on the most sensitive subset of neurons relevant to a given task, it is possible that they directly tap mechanisms that are suppression-free. Our EEG data measure responses from the whole neural population, and so we next model these results to obtain a more general estimate of suppression. The model used to fit the EEG data omits the output nonlinearity (Equation 4), and adds a scaling parameter (R_{max}), resulting in 5 free parameters. It produced an excellent account of the results at both temporal frequencies, and across all 6 stimulus conditions (see Figure 3e,f), with an RMS error of $0.02\mu V$. The model correctly captures the sub-linear summation between channels (i.e. the red curve in Figure 3e is less than a factor of two greater than the blue curve), and the suppression evident in the cross-dekadactyl and cross-dichodactyl conditions. The weight of suppression ($\omega = 0.518$) was intermediate between the two dipper models, as well as being in between previously published values for vision ($\omega = 1$; (1)) and hearing ($\omega = 0$; (2)).

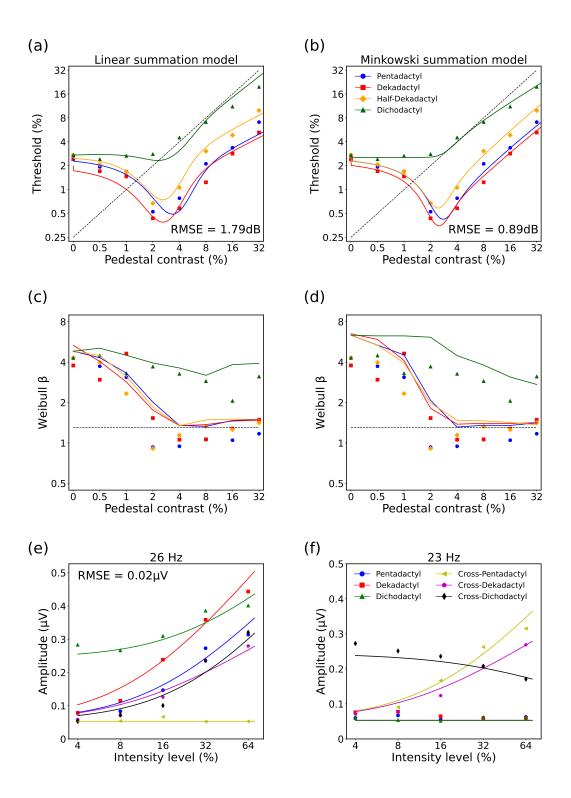


Figure 3: Summary of model fitting. Panel (a) shows the fit of a model in which summation is linear (following an early transducer), and panel (b) shows the fit of the Minkowski summation model. Panels (c) and (th) show the best model fit to the EEG data at 26Hz (c) and 23Hz (d).

Table 1: Summary of fitted model parameters for three computational models. Brackets indicate fixed values, and dashes denote parameters not included in a given model.

Model	R_{max}	p	q	m	S	Z	ω	k	γ	RMSE
Linear summation	-	9.845	8.845	1.416	0.067	106.408	0.817	0.264	(1.0)	1.79
Minkowski summation	-	19.149	16.0	1.081	0.976	0.039	0.004	0.142	15.484	0.89
EEG model	0.053	-	-	1.263	25.955	-	0.518	0.139	-	0.02

Discussion

In this study, we present evidence detailing the processes of signal summation and suppression in vibrotactile signal combination. In the psychophysical experiment, we observed that doubling the inputs resulted in a slight reduction in detection and discrimination thresholds, indicating a weak summation effect. Additionally, adding a masking stimulus led to increased discrimination thresholds, indicating a suppression process. Furthermore, the EEG experiment demonstrated that adding the same frequency increases brain activity, whereas adding a different frequency decreases it. These findings allow us to quantify the summation and suppression effect between digits. Our computational model fitting results show that at a population level, responses to two vibrotactile inputs suppress each other, though our psychophysical data are more consistent with probability summation rather than neural/physiological summation. The weight of suppression between digits is around $\omega = 0.5$, which is intermediate between the corresponding values observed in visual (1) and auditory (2) signal combination. Overall, our results suggest the presence of suppression in vibrotactile signal combination, with a suppression effect distinct from that observed in visual and auditory signal combination. In the remainder of this discussion, we consider the underlying mechanisms of vibrotactile signal combination and the differences across sensory modalities.

Our findings are consistent with previous studies (12, 21, 22) that suggest doubling inputs can reduce the vibration detection threshold. However, the summation effect observed in our study is weaker than that reported in these studies, which found a 3 dB reduction in detection threshold when using vibrations above 40 Hz and doubling the contactor size. This discrepancy may be attributed to the different vibration frequencies used in the studies, and our choice to stimulate alternating fingers rather than to vary stimulus area. Some psychophysical studies have proposed that four distinct mechanoreceptive channels mediate vibration perception: Pacinian (P), Non-Pacinian I (NP I), Non-Pacinian II (NP II), and Non-Pacinian III (NP III) (22, 23). Each channel has unique characteristics and responds to specific frequency ranges. For instance, the P channel is more sensitive to higher frequencies (e.g., greater than 40 Hz) and is the only channel that possesses the property of spatial summation (21, 23, 24). In contrast, vibrations between 2 and 40 Hz are mediated by the NP I channel, which has been shown not to exhibit spatial summation (22, 23, 25). Consequently, the weak summation effect observed in our study may be attributed to the 26 Hz vibration, which is determined by the NP I channel that lacks spatial summation. Additionally, unlike the study by (12), which used varying contactor sizes to stimulate random areas within a test region, thereby preventing participants from knowing the exact location of stimulation, our study specifically involved the stimulation of individual digits, with participants aware of which digits were being stimulated in some conditions. This methodological difference likely contributed to the observed discrepancy between the studies.

The results of our EEG experiment are broadly consistent with those of the psychophysical study. Doubling the digits at the same frequency elicited stronger brain responses, though the increase was less than twofold. These findings correspond with previous studies, demonstrating that brain responses to concurrent stimuli at the same frequencies are stronger than those elicited by individual stimuli, suggesting a summation effect between inputs (4, 26, 27). However, the observed response is less than the anticipated summed response, generally falling between 10% and 50% of the expected value, signifying a suppression effect between inputs (4, 28). In contrast, adding a masking stimulus at a different frequency resulted in a reduction in brain activity. These results provide further evidence of suppression between digits and are consistent with previous neuroimaging studies investigating the interaction between different frequencies (29, 30). For instance, (29) examined the suppression effect by vibrating two fingers at the same (18 Hz) or different frequencies (18 vs. 22 Hz, 18 vs. 26 Hz). Their findings revealed that the event-related potential (ERP) and SSSEP responses to simultaneous stimulation of both fingers were significantly lower than the linear sum of individual responses, with no difference in suppression based on frequency variation. This ruled out the hypothesis that suppression is due to neuronal occlusion from overlapping cortical areas, as stronger suppression would be expected at the same frequency if this were the case (4, 31). Instead, the results support the alternative explanation of lateral inhibition, where activation of one cortical neuron suppresses neighbouring neurons' activity (32–36). This inhibitory mechanism has been extensively observed in both animal and human studies (3, 4, 11, 37, 38).

Another interesting finding is that we observed an intermediate level of suppression between vibrotactile stimuli compared with vision and audition. In visual perception, the forward-facing positioning of the eyes results in substantially overlapping visual fields. To merge these overlapping inputs from each eye (monocular vision) into a cohesive single image (binocular single vision), neural signals from both eyes must exhibit strong mutual inhibition to achieve 'ocularity invariance', ensuring the constancy of perception through one or both eyes (39). This is consistent with recent findings indicating that some neurons in the primary visual cortex are monocularly excitable, responding exclusively to the dominant eye, while binocular stimulation can suppress their activity (40). In contrast, the lateral placement of the ears results in minimal overlap between auditory inputs, reducing the necessity for strong interaural inhibition to integrate these signals into a unified percept, as is required in visual processing. Instead, binaural perception benefits from the comparison and integration of these disparate inputs to localise sound sources and discern subtle differences in timing and intensity (41, 42). Although prior evidence supports the existence of binaural suppression (2, 43, 44), the extent of this suppression may differ depending on hemispheric laterality (45, 46).

Tactile perception involves the stimulation of each of the ten fingers individually, creating a more complex signal integration compared to binocular or binaural perception. The primary

somatosensory cortex (S1) is divided into four distinct Brodmann areas (BA 3a, 3b, 1, and 2), each responsible for mapping different parts of the body surface. Evidence suggests that receptive field of each finger is arranged in somatotopic order in BA 3b, while in BA 1/2, they are arranged in clusters with large overlap (27, 31, 47). Although SSSEPs reflect activity across the whole scalp, EEG (30, 48) and MEG (11, 27, 49) studies also support overlapping finger representations in S1. Notably, the overlap between adjacent fingers is greater than between non-adjacent ones, indicating that suppression between fingers depends on their spatial proximity. Additionally, hand posture plays a significant role in signal summation and suppression. For instance, a study (50) found that a "CLOSE" posture (thumb and index finger positioned as if to pick something up) produces stronger suppression than an "OPEN" posture (hand fully open). In the present study, finger posture and inter-finger distance were controlled by placing the fingertips in a fixed position on solenoids, suggesting that the amount of suppression may vary depending on finger arrangements or hand posture. Furthermore, studies have shown that blind individuals exhibit stronger somatosensory evoked potentials compared to sighted individuals, potentially indicating an expanded S1 region (51, 52). This suggests that use-dependent cortical reorganisation may occur across different body regions, and the amount of suppression may vary depending on the body part involved.

Conclusion

In summary, we demonstrate that vibrotactile signal combination involves both probability summation and suppression, as evidenced by psychophysical thresholds and EEG activity. A computational model further characterizes this process, indicating that the strength of suppression between digits is intermediate — weaker than in vision but stronger than in audition. These findings establish a foundational framework for understanding vibrotactile integration and provide a basis for future research to explore whether the weight of suppression varies across different body parts, offering deeper insights into somatosensory processing and clinical conditions in which tactile processing or body experience is affected (e.g., chronic hand pain).

Materials and Methods

Participants

Eight adult subjects participated in the psychophysics experiment, and thirty-one adult subjects participated in the EEG experiment. All participants self-reported as healthy, with no diagnosed neurological disorders, and no history of exposure to severe hand-transmitted vibration. Both experiments were approved by the Ethics Committee of the Department of Psychology at the University of York (application IDs 2277 and 2303). Written informed consent was obtained from all participants prior to conducting the experiments.

Apparatus & stimuli

Vibration stimuli were generated by a specially constructed board with ten fixed solenoids ('tactor' devices, from Dancer Design Ltd.) controlled by a computer (Figure 4c). Each solenoid could be independently driven by a pair of 6-channel USB sound cards to vibrate each finger. The outputs of the sound cards were amplified by a 10-channel linear amplifier, which produced a maximum output modulation of ± 7.5 V, for a maximum vibration amplitude of ± 0.375 N. All the stimuli were generated and presented using MATLAB and Psychtoolbox 3 (53, 54). Any sounds produced by the vibrations were rendered inaudible by playing a 440 Hz tone on the remaining two sound card outputs, which was delivered to participants over a pair of headphones.

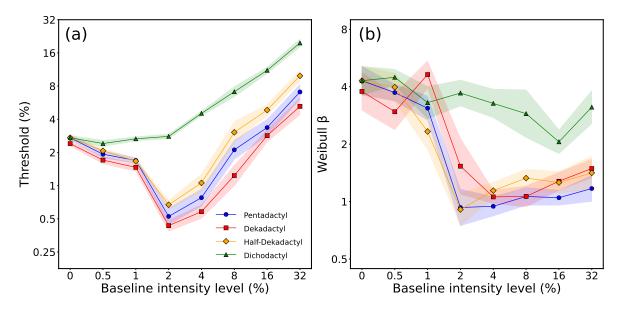


Figure 4: Overview of methods details. Panel (a) illustrates the arrangements of pedestal and target stimuli in the two intervals of a trial in Experiment 1, for four stimulus arrangements (rows). Panel (b) shows an example 'dipper' function. Panel (c) shows the board containing the ten tactors. Panel (d) illustrates the allocation of digits into two sets. Panel (e) illustrates the stimulus conditions used in Experiment 2.

EEG signals were recorded using a 64-channel electrode cap and an ANT Neuroscan (ANT Neuro, Netherlands) amplifier sampling at 1kHz. Electrodes were arranged according to the 10-20 system, and impedances were kept below $5k\Omega$. Digital triggers were sent to the EEG amplifier using a USB TTL module (Black Box Toolkit Ltd., UK), signifying the start of the trial. The whole head average was used as a reference for the EEG data, and the ground electrode was located at position AFz.

Psychophysical procedures

In Experiment 1, a two-interval forced-choice (2IFC) task was used to measure detection and discrimination thresholds. During the experiment, participants were instructed to place their ten digits on the corresponding solenoids, and a series of 26Hz vibration stimuli were delivered to their hands. The digits on each hand were coded 1 to 5 from the thumb to the little finger in that order. The digits 1, 3 and 5 on the left hand and 2 and 4 on the right hand are denoted "Set A", and the digits 2 and 4 on the left hand, and 1, 3 and 5 on the right hand are denoted "Set B" (illustrated in Figure 4d).

Each trial consisted of two 500 ms intervals: one containing the pedestal stimulus and the other containing the pedestal stimulus plus a target increment, separated by a 400 ms interstimulus interval. The next trial began 200 ms after the participant responded. To mask any sound produced by the solenoids and indicate the stimulus intervals, a 440 Hz beep sound was delivered through headphones simultaneously with the vibration stimuli. The order of the two intervals was randomised, and participants were required to determine which interval contained the target increment by pressing a foot pedal. Feedback was provided by a coloured square on the computer screen, with green indicating a correct response and red indicating an incorrect one. The amplitude of the target increment was determined using a pair of 3-down-1-up staircases, with a step size of 3 dB (where dB units are defined as $20 \times log_{10}(100 \times C)$, and C is the stimulus intensity expressed as a proportion of the maximum system output), aiming to distribute trials around the detection threshold at 75% correct. Threshold measurement was terminated after either 70 trials or 12 reversals, whichever occurred first.

The pedestal and target stimuli were presented under four conditions (illustrated in Figure 4a) and at eight pedestal levels (0, 1, 2, 4, 8, 16, 32, 64%), with the pedestal level expressed as a percentage of the maximum vibration (0.375N). In the "pentadactyl" condition (meaning five-fingered in Greek), the pedestal and target stimuli vibrated only "Set A" (analogous to the stimulation of one eye or one ear). In the "dekadactyl" (ten-fingered) condition, the pedestal and target stimuli vibrated both "Set A" and "Set B" (analogous to the stimulation of both eyes or both ears). Comparing the "pentadactyl" and "dekadactyl" conditions reveals the summation effect of doubling the number of inputs. In the "dichodactyl" condition (named for consistency with dichoptic conditions in vision experiments, where different stimuli are shown to the two eyes), the pedestal stimulus vibrated "Set A" and the target stimulus vibrated "Set B", permitting the measurement of masking effects across digits. The "half-dekadactyl" condition involved vibrating all ten digits for the pedestal stimulus, while only "Set A" vibrated for the target stimulus, enabling measurement of summation (by comparison with the dekadactyl condition) while controlling the number of digits receiving the pedestal stimulus (see also the half-binocular condition of Meese et al. 10). In all conditions, the vibration frequency for both pedestal and target stimuli was 26 Hz. "Set A" and "Set B" were counterbalanced across trials. Each pedestal level was tested in a single block lasting approximately 15 minutes and repeated three times. The entire experiment took around 7 hours per participant, resulting in a total of 60438 trials (7555 per participant on average), and was completed over multiple days.

EEG procedures

After EEG cap set-up, participants in Experiment 2 were exposed to a series of vibrations under six different conditions (illustrated in Figure 4e) at five intensity levels (4, 8, 16, 32, 64%). Steady-state somatosensory evoked potential (SSSEP) signals were recorded throughout the experiment. During each trial, participants received an 11-s vibration with a 3-s interstimulus interval, and were required to keep their hands still until designated break periods. The "Set A" and "Set B" allocations were the same as those used in the psychophysical experiment (see Figure 4d) and were counterbalanced across trials. The order of conditions was randomised, and each condition was repeated twice for each set, resulting in a total of 120 trials. The entire experiment lasted approximately 30 minutes, split into four 7-minute blocks with rest breaks between blocks.

Two different frequencies were used: 26 Hz (F1) and 23 Hz (F2). F1 is considered the primary frequency, as SSSEP responses are greatest around 26Hz when vibration is delivered to the hands (55). Using two distinct frequencies enables measurement of both the separate responses to each frequency and the interactions between them. In the "pentadactyl" condition, F1 only vibrated "Set A"; in the "dekadactyl" condition, F1 vibrated both "Set A" and "Set B"; in the "dichodactyl" condition, F1 vibrated "Set A" while a mask at 26 Hz with an intensity level of 32% vibrated "Set B". These three conditions contributed to the observation of summation and suppression effects at the same frequency.

In the remaining three conditions, a second frequency (F2) was introduced to investigate interactions between different frequencies. In the "cross-pentadactyl" condition, F2 vibrated "Set A", providing a comparison with the "pentadactyl" condition and serving as a baseline for other cross-frequency conditions. In the "cross-dekadactyl" condition, F1 vibrated "Set A" and F2 vibrated "Set B", permitting measurement of suppression effects between different frequencies. In the "cross-dichodactyl" condition, F1 vibrated "Set A" while the F2 mask (intensity level of 32%) vibrated "Set B", again to measure suppression between digits (see Figure 4e for a diagram of all conditions).

Data analysis

For both experiments, off-line analysis and statistical testing was performed in Python 3. For psychophysical data, the *psignifit* 4 package (56) was used to estimate thresholds (at 75% correct) and slope parameters of the psychometric functions by fitting a cumulative Gaussian. We then converted the slope parameter (σ) to equivalent Weibull β values using the approximation $\beta = 10.3/\sigma$.

For EEG data, all preprocessing was conducted using MNE-Python (57). For each trial, the initial 1000 ms post-stimulus presentation was discarded to eliminate onset transients. The

remaining 10 s were Fourier transformed and the amplitudes were averaged across repetitions and participants. After removing one outlier, data from 30 participants remained for calculating the intensity-response functions and performing statistical analysis. The amplitudes from six electrodes centred on the area of greatest response (F1, F2, Fz, FC1, FC2, FCz) were then averaged to plot the amplitude spectra and intensity-response functions. The primary dependent variables were the Fourier amplitudes at 26 Hz and 23 Hz.

Computational modelling

The psychophysical data were fitted using the two stage model of Meese et al (10), as outlined in equations 1-4, with 7 free parameters $(m, S, \omega, p, q, Z \text{ and } k)$. The final parameter (k) determines the threshold criteria, such that the model response in the target interval must exceed that in the null interval by k for threshold to be reached. It is proportional to additive noise in the model. We also considered a modified model, in which the summation process described by Equation 3 involved an additional exponent:

$$binsum = (Stage1_L^{\gamma} + Stage1_R^{\gamma})^{1/\gamma}$$
 (5)

The Minkowski exponent (γ) is implicitly 1 in Equation 3, but was free to vary in our second model.

To fit the EEG data, we used a simpler model described by Equations 1-3, but omitting the output nonlinearity described by Equation 4, which serves primarily to determine the shape of the dipper function in psychophysical studies, but is not required for EEG data (1). The output was instead defined as:

$$resp = R_{max} \times binsum + k \tag{6}$$

where R_{max} is a scaling parameter on the output, and k again represents additive noise. The simpler model had 5 free parameters $(m, S, \omega, R_{max} \text{ and } k)$. We used a downhill simplex algorithm to minimize the squared error between model and data. Fitting for each model was repeated 100 times from random starting vectors, and the parameters that gave the best numerical fit were selected.

Data and code availability

All experiment code, raw data, processed data and analysis code are available at the project repository: https://doi.org/10.17605/OSF.IO/M79D2. The linked GitHub repository also contains a fully computationally reproducible version of this manuscript in Quarto format.

Acknowledgements

We thank Mark Green for constructing the vibration board, and Kirralise Hansford for her support during EEG data collection. This work was supported by the China Scholarship Council [202308510049], and by BBSRC grant BB/V007580/1 awarded to DHB and ARW.

References

- 1. D. H. Baker, A. R. Wade, Evidence for an optimal algorithm underlying signal combination in human visual cortex. *Cerebral Cortex* **27**, 254–264 (2017).
- 2. D. H. Baker, et al., Binaural summation of amplitude modulation involves weak interaural suppression. Sci Rep 10, 3560 (2020).
- 3. K. Biermann, et al., Interaction of finger representation in the human first somatosensory cortex: A neuromagnetic study. Neuroscience Letters 251, 13–16 (1998).
- 4. S. C. Gandevia, L. A. Hall, D. I. McCloskey, E. K. Potter, Proprioceptive sensation at the terminal joint of the middle finger. *J Physiol* **335**, 507–17 (1983).
- 5. M. Ide, S. Hidaka, Tactile stimulation can suppress visual perception. *Scientific Reports* 3, 3453 (2013).
- 6. S. Hidaka, M. Ide, Sound can suppress visual perception. Scientific Reports 5, 10483 (2015).
- 7. D. H. Baker, F. A. Lygo, T. S. Meese, M. A. Georgeson, Binocular summation revisited: Beyond √2. Psychol Bull 144, 1186–1199 (2018).
- 8. F. W. Campbell, D. G. Green, Monocular versus Binocular Visual Acuity. *Nature* **208**, 191–192 (1965).
- 9. J. A. Solomon, The history of dipper functions. Atten Percept Psychophys **71**, 435–43 (2009).
- 10. T. S. Meese, M. A. Georgeson, D. H. Baker, Binocular contrast vision at and above threshold. *Journal of Vision* **6(11)**, 7 (2006).
- 11. K. Hoechstetter, et al., Interaction of Tactile Input in the Human Primary and Secondary Somatosensory Cortex—A Magnetoencephalographic Study. NeuroImage 14, 759–767 (2001).
- 12. G. A. Gescheider, B. GüÇlü, J. L. Sexton, S. Karalunas, A. Fontana, Spatial summation in the tactile sensory system: Probability summation and neural integration. Somatosensory & Motor Research 22, 255–268 (2005).
- 13. C. Gu, M. J. Griffin, Spatial summation of vibrotactile sensations at the foot. *Medical Engineering & Physics* **35**, 1221–1227 (2013).
- 14. C. W. Tyler, C.-C. Chen, Signal detection theory in the 2AFC paradigm: Attention, channel uncertainty and probability summation. *Vision Research* **40**, 3121–3144 (2000).

- 15. R. F. Quick, A vector-magnitude model of contrast detection. *Kybernetik* **16**, 65–67 (1974).
- 16. J. M. Foley, G. E. Legge, Contrast detection and near-threshold discrimination in human vision. *Vision Res* **21**, 1041–53 (1981).
- 17. D. H. Baker, et al., Binocular integration of chromatic and luminance signals. J Vis **24(12)**, 7 (2024).
- 18. D. H. Baker, T. S. Meese, M. A. Georgeson, Paradoxical psychometric functions ("swan functions") are explained by dilution masking in four stimulus dimensions. *I-Perception* 4, 17–35 (2013).
- 19. E. Porcu, C. Keitel, M. M. Müller, Visual, auditory and tactile stimuli compete for early sensory processing capacities within but not between senses. *NeuroImage* **97**, 224–235 (2014).
- J. R. Timora, T. W. Budd, Steady-State EEG and Psychophysical Measures of Multisensory Integration to Cross-Modally Synchronous and Asynchronous Acoustic and Vibrotactile Amplitude Modulation Rate. *Multisensory Research* 31, 391–418 (2018).
- 21. G. A. Gescheider, S. J. Bolanowski, J. V. Pope, R. T. Verrillo, A four-channel analysis of the tactile sensitivity of the fingertip: Frequency selectivity, spatial summation, and temporal summation. Somatosensory & Motor Research 19, 114–124 (2002).
- 22. R. T. Verrillo, Effect of Contactor Area on the Vibrotactile Threshold. The Journal of the Acoustical Society of America 35, 1962–1966 (1963).
- 23. S. J. Bolanowski, G. A. Gescheider, R. T. Verrillo, C. M. Checkosky, Four channels mediate the mechanical aspects of touch. *The Journal of the Acoustical Society of America* 84, 1680–1694 (1988).
- 24. R. T. Verrillo, Temporal Summation in Vibrotactile Sensitivity. The Journal of the Acoustical Society of America 37, 843–846 (1965).
- 25. G. A. Gescheider, S. J. Bolanowski, K. L. Hall, K. E. Hoffman, R. T. Verrillo, The Effects of Aging on Information-Processing Channels in the Sense of Touch: I. Absolute Sensitivity. *Somatosensory & Motor Research* 11, 345–357 (1994).
- 26. K. Hoechstetter, H.-M. Meinck, P. Henningsen, M. Scherg, A. Rupp, Psychogenic sensory loss: Magnetic source imaging reveals normal tactile evoked activity of the human primary and secondary somatosensory cortex. *Neurosci Lett* **323**, 137–40 (2002).
- 27. H. Ishibashi, et al., Differential interaction of somatosensory inputs in the human primary sensory cortex: A magnetoencephalographic study. Clinical Neurophysiology 111, 1095–1102 (2000).
- 28. Ching-Liang Hsieh, Fumio Shima, Shozo Tobimatsu, Shu-Jian Sun, Motohiro Kato, The interaction of the somatosensory evoked potentials to simultaneous finger stimuli in the human central nervous system. A study using direct recordings. *Electroencephalography and Clinical Neurophysiology/Evoked Potentials Section* **96**, 135–142 (1995).

- 29. M. Severens, J. Farquhar, P. Desain, J. Duysens, C. Gielen, Transient and steady-state responses to mechanical stimulation of different fingers reveal interactions based on lateral inhibition. *Clinical Neurophysiology* **121**, 2090–2096 (2010).
- 30. C. Y. Pang, M. M. Mueller, Competitive interactions in somatosensory cortex for concurrent vibrotactile stimulation between and within hands. *Biological Psychology* **110**, 91–99 (2015).
- 31. T. Krause, et al., Representational overlap of adjacent fingers in multiple areas of human primary somatosensory cortex depends on electrical stimulus intensity: An fMRI study. Brain Research 899, 36–46 (2001).
- 32. S. E. Laskin, W. A. Spencer, Cutaneous masking. II. Geometry of excitatory and inhibitory receptive fields of single units in somatosensory cortex of the cat. *Journal of Neurophysiology* 42, 1061–1082 (1979).
- 33. J. C. Brumberg, D. J. Pinto, D. J. Simons, Spatial gradients and inhibitory summation in the rat whisker barrel system. *Journal of Neurophysiology* **76**, 130–140 (1996).
- 34. J. DiCarlo, K. O. Johnson, S. S. Hsiao, Structure of Receptive Fields in Area 3b of Primary Somatosensory Cortex in the Alert Monkey. *The Journal of Neuroscience* 18, 2626–2645 (1998).
- 35. R. W. Dykes, P. Landry, R. Metherate, T. P. Hicks, Functional role of GABA in cat primary somatosensory cortex: Shaping receptive fields of cortical neurons. *Journal of Neurophysiology* **52**, 1066–1093 (1984).
- 36. G. Mirabella, Integration of Multiple-whisker Inputs in Rat Somatosensory Cortex. *Cerebral Cortex* **11**, 164–170 (2001).
- 37. Y. Iwamura, M. Tanaka, Functional organization of receptive fields in the cat somatosensory cortex II: Second representation of the forepaw in the ansate region. *Brain Research* **151**, 61–72 (1978).
- 38. Y. Iwamura, M. Tanaka, M. Sakamoto, O. Hikosaka, Vertical neuronal arrays in the postcentral gyrus signaling active touch: A receptive field study in the conscious monkey. *Experimental Brain Research* 58 (1985).
- 39. D. H. Baker, T. S. Meese, M. A. Georgeson, Binocular interaction: Contrast matching and contrast discrimination are predicted by the same model. *Spat Vis* **20**, 397–413 (2007).
- 40. K. Dougherty, M. A. Cox, J. A. Westerberg, A. Maier, Binocular Modulation of Monocular V1 Neurons. *Current Biology* **29**, 381–391.e4 (2019).
- 41. J. F. Brugge, M. M. Merzenich, Responses of neurons in auditory cortex of the macaque monkey to monaural and binaural stimulation. *Journal of Neurophysiology* **36**, 1138–1158 (1973).
- 42. D. A. Benson, D. C. Teas, Single unit study of binaural interaction in the auditory cortex of the chinchilla. *Brain Research* **103**, 313–338 (1976).

- 43. J. Tiihonen, R. Hari, E. Kaukoranta, M. Kajola, Interaural Interaction in the Human Auditory Cortex. International Journal of Audiology 28, 37–48 (1989).
- 44. R. Gransier, A. Van Wieringen, J. Wouters, Binaural Interaction Effects of 30–50 Hz Auditory Steady State Responses. *Ear & Hearing* **38**, e305–e315 (2017).
- 45. K. Kaneko, N. Fujiki, R. Hari, Binaural interaction in the human auditory cortex revealed by neuromagnetic frequency tagging: No effect of stimulus intensity. *Hearing Research* **183**, 1–6 (2003).
- 46. N. Fujiki, V. Jousmäki, R. Hari, Neuromagnetic Responses to Frequency-Tagged Sounds: A New Method to Follow Inputs from Each Ear to the Human Auditory Cortex during Binaural Hearing. *The Journal of Neuroscience* 22, RC205–RC205 (2002).
- 47. R. Kurth, et al., fMRI shows multiple somatotopic digit representations in human primary somatosensory cortex: NeuroReport 11, 1487–1491 (2000).
- 48. I. Arslanova, K. Wang, H. Gomi, P. Haggard, Somatosensory evoked potentials that index lateral inhibition are modulated according to the mode of perceptual processing: Comparing or combining multi-digit tactile motion. *Cognitive Neuroscience* 13, 47–59 (2022).
- 49. L. Tamè, F. Pavani, C. Papadelis, A. Farnè, C. Braun, Early integration of bilateral touch in the primary somatosensory cortex. *Human Brain Mapping* **36**, 1506–1523 (2015).
- 50. Y. Hamada, R. Suzuki, Hand posture modulates neuronal interaction in the primary somatosensory cortex of humans. *Clinical Neurophysiology* **114**, 1689–1696 (2003).
- 51. D. Giriyappa, R. M. Subrahmanyam, S. Rangashetty, R. Sharma, Index finger somatosensory evoked potentials in blind braille readers. *Neurol Neurochir Pol* 43, 439–45 (2009).
- 52. H. Burton, R. J. Sinclair, D. G. McLaren, Cortical activity to vibrotactile stimulation: An fMRI study in blind and sighted individuals. *Human Brain Mapping* **23**, 210–228 (2004).
- 53. M. Kleiner, D. H. Brainard, D. G. Pelli, What's new in psychtoolbox-3? *Perception* **36S**, 14 (2007).
- 54. D. H. Brainard, The psychophysics toolbox. Spat Vis 10, 433–6 (1997).
- 55. A. Z. Snyder, Steady-state vibration evoked potentials: Description of technique and characterization of responses. *Electroencephalography and Clinical Neurophysiology/Evoked Potentials Section* 84, 257–268 (1992).
- 56. H. H. Schütt, S. Harmeling, J. H. Macke, F. A. Wichmann, Painfree and accurate Bayesian estimation of psychometric functions for (potentially) overdispersed data. *Vision Research* **122**, 105–123 (2016).
- 57. A. Gramfort, MEG and EEG data analysis with MNE-Python. Frontiers in Neuro-science 7, 267 (2013).