# riseset Group

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SHA-256: 2d19f300cc61c986c7caa9db0e3708c782e95515f012b824cb06f15658d7d052

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## Contents

riseset Overview	2
riseset Interface	4
riseset Source Code	5
=: Index	38

#### riseset Overview

riseset is a collection of basic astronomical algorithms that compute the rise, transit, and set times of IAU-named stars. The motivation for composing this group is twofold.

- 1. Provide a *reference* implementation for a LEAN4 program that replicates the J code shown here. I want a *hello world* program that is not entirely trivial, does something interesting and is small enough that it can be easily adjusted as LEAN4 matures.
- 2. Address one of my goals of calling out all the bright named stars visible from my current location on a given date.

Many of the algorithms are taken from Jean Meeus's book Astronomical Algorithms. A PDF copy of this book is available here:

https://ia802807.us.archive.org/20/items/astronomicalalgorithmsjeanmeeus1991/

also here:

Nutation algorithms are from Jay Tanner's site:

https://neoprogrammics.com/nutations/index.php

Markdown versions of Tanner's algorithms are stored in the JOD futs and utils dictionaries — see:

- 1. nutation\_in\_longitude\_dPsi\_md
- 2. nutation\_in\_obliquity\_of\_ecliptic\_dEpsDeg\_md

```
in:
```

```
https://github.com/bakerjd99/joddumps/blob/master/futs.ijs https://github.com/bakerjd99/joddumps/blob/master/utils.ijs Delta T (\DeltaT) is computed using polynomial expressions by Espenak and Meeus, see: https://eclipse.gsfc.nasa.gov/SEhelp/deltatpoly2004.html A markdown version of the Delta T (\DeltaT) algorithm is in futs see:
```

```
1. nasa_polynomial_expressions_for_delta_t_md
```

You can display the markdown referenced about with the JOD expressions:

```
load 'general/jod'
od ;:'futs utils'
NB. display markdown documents
4 disp ; }.@(4&dn1)&.> 'nutation_';'nasa_'
```

Many examples showing how to use various riseset words are in the JOD futs test suite riseset. You can display all the test cases with the JOD expressions:

```
3 grp 'riseset' NB. test cases in suite
3 disp 'riseset' NB. display test suite
```

riseset Interface RISESET OVERVIEW

4

#### riseset Interface

```
iau_tonight [17] named IAU stars visible tonight
loadstars [20] loads riseset star data
riseset [31] rise, transit, set times of stars
```

#### riseset Source Code

```
NB.*riseset s-- compute rise, transit and set times of IAU named stars.
NB.
NB. verbatim: interface word(s):
NB. -----
NB. iau_tonight - named IAU stars visible tonight
NB. loadstars - loads riseset star data
NB. riseset - rise, transit, set times of stars
NB.
NB. created: 2023mar09
NB. changes: -----
NB. 23mar28 (iau_tonight) added
coclass 'riseset'
NB. *end-header
NB. Byte Order Mark: UTF-8 EF,BB,BF (hex) or 239 187 191 (dec)
BOM=: 239 187 191{a.
NB. carriage return character
CR=: 13\{a.
NB. seconds per day
DAYSECS=: 86400
```

5

```
NB. interface words (IFACEWORDSriseset) group
IFACEWORDSriseset=: <;. 1 ' iau tonight loadstars riseset'</pre>
NB. horizon limit in degrees
I.TMTTHORZ=: 20
NB. limiting magnitude
LIMITMAG=: 3.
NB. approximate epoch J2000 obliquity of the ecliptic degrees, minutes, seconds
OBLIQUITYDMS2000=: 23 26 21.4480000000000004
NB. observer latitude longitude, west longitudes negative
OBSLOCATION=: 116.375956000000002 43.6467749999999981
NB. root words (ROOTWORDSriseset) group
ROOTWORDSriseset=: <;._1 ' IFACEWORDSriseset ROOTWORDSriseset VMDriseset iau_tonight yyyymmfd'
NB. standard altitude stars - compensates for horizon atmospheric refraction
STDALTITUDE=: 0.56669999999999992
NB. UTC time zone offset in hours
UTCOFFSET=: 6
NB. version, make count and date
VMDriseset=: '0.8.0';5;'28 Mar 2023 13:59:30'
```

```
NB. all zero, first, second, ... nth differences of nl: alldifs ?.10#100
alldifs=: ([: >: [: i. [: - #) {.&.> [: <"1 (}. - }:)^:(i.0#0[)
apparRADEC=: 4 : 0
NB.*apparRADEC v-- apparent RA and DEC for epoch (x) from J2000.0
NB. RA and DEC.
NB.
NB. This verb adjusts J2000 RA and DEC coordinates to another
NB. epoch. The method is based on Meeus (20.3) pg 126. This
NB. calculation ignores stellar proper motions and assumes that
NB. (y) RA DEC values are J2000.0. The resulting positions are
NB. accurate enough for basic rise, transit,
NB. calculations.
NB.
NB. \ dyad: ft = . flYmd \ apparRADEC \ ftRADEC
NB.
     2028 11 13.19 apparRADEC 41.054063 ,. 49.227750
NB.
NB.
     (\{."1 \ ciau\} =: \{:"1 \ ciau\})
NB.
     2023 4 22 apparRADEC RA_J2000 ,: Dec_J2000
NB.
'zet z th'=. zetzthT0 x NB. final epoch t
                        NB. J2000 ra, dec
'ra dec'=. y
NB. meeus (20.4) pg. 126
A=. (cosd dec)*sind ra + zet
B=. ((cosd th)*(cosd dec)*cosd ra + zet) - (sind th)*sind dec
```

```
C=. ((sind th)*(cosd dec)*cosd ra + zet) + (cosd th)*sind dec
NB. NIMP star close celestial poles
NB. new dec, ra
ran=. z + atan2 A ,: B [ decn=. dfr arcsin C
ran ,: decn
)
NB. seconds correction apparent sidereal time - meeus pq. 84 - (\Delta psi * cos(eps))/15
apparsecs=: 15 %~ (3600 * nutation_longitude_dPsi) * [: cosd meanobliquityjd0
NB. apparent Greenwich sidereal - hms: apparsidjd0 julfrcal |: 2023 1 3,:1991 2 8.5
apparsidjd0=: ([: dmsfrdd 15 %~ [: nth0 meansidjd0) + 0 0 ,"1 [: ,. apparsecs
NB. applies the verb in string (x) to (y)
apply=: 128!:2
NB. arc cosine
arccos=: 2&o.
NB. arc sine
arcsin=: _1&o.
NB. arc tangent
arctan=: _3&o.
```

```
NB. signal with optional message
assert=: 0 0" $ 13!:8^:((0: e. ]) (12" ))
atan2=: 3 : 0
NB.*atan2 v-- arctangent of (Y % X) in degrees.
NB.
NB. FORTRAN (ATN2) variation of the standard (arctan) (_3&o.) for
NB. ratios. Based on a PASCAL function from Astronomy on the
NB. Personal Computer by Montenbruck and Pfleger ISBN
NB. 0-387-52754-0 pq. 9.
NB.
NB. Result is between _180 <: atn2 <: 180 degrees
NB.
NB. monad: fl = atan2 fl YX
NB.
     atan2 1 ,: 1 NB. 45 degrees
NB.
     atan2 1 ,: %: 3 NB. 30 degrees
NB.
NB.
     NB. random ratios comparing two atan2 verbs
NB.
     r=: ?. 2 500$50
NB.
     r=: r * (\$r) \$ (?.~*/\$r) { (*/\$r)\$ 1 1}
NB.
NB.
     (atan2b /.r) -: atan2 r
NB.
     NB. surprisingly (atan2) is faster than (atan2b)
NB.
     NB. (j 9.41 2023) but (atan2b) consumes less memory
NB.
     NB. 1000 ts"1 'atan2b r',:'atan2 |.r'
NB.
```

```
NB. vector J
                            NB. scalar PASCAL
rad=. 0.0174532925199432955
                            NB. CONST RAD=0.0174532925199433;
r=. 0 #~ {: $y
b0=. *./0=y
                            NB. IF (X=0.0) AND (Y=0.0) THEN ATN2:= 0.0
ir=. i. #r=. 0 (I. b0)} r
if. +./b1=. -.b0 do.
 t=. |(I. b1) {"1 y
                     NB. AX =: ABS(X); AY =: ABS(Y)
 it=. (I. b1) { ir
                       NB. IF (AX>AY) THEN PHI=: ARCTAN(AY/AX)/RAD
 b2=. (1{t}) > 0{t}
 s=. (I. b2) {"1 t
 r=. (rad %~ arctan %/s) (b2#it)} r
 s=. (I. -.b2) {"1 t}
                     NB. ELSE PHI=: 90.0-ARCTAN(AX/AY)/RAD;
 r=. (90 - rad %~ arctan %/ |.s) (it #~ -.b2)} r
end.
x10=. I. b1 *. (1{y}) < 0
                            NB. IF (X<0.0) THEN PHI=: 180.0-PHI;
r=. (180 - x10{r}) (x10)} r
y10=. I. b1 *. (0{y}) < 0
                            NB. IF (Y<0.0) THEN PHI=: -PHI;
r=. (-y10{r}) (y10)} r
r
NB. boxes open nouns
```

```
boxopen=: <^:(L. = 0:)
cold_iau_named_stars=: 3 : 0
NB.*cold_iau_named_stars v-- convert IAU btcl to column dictionary.
NB.
NB. monad: bt =. cold iau named stars btcl
NB.
     iau=.; {: , > {: 4 get 'iau_named_stars_2022_txt'
NB.
      ciau=. cold iau named stars parse iau named stars iau
NB.
NB.
     NB. define columns
NB.
     (0 {"1 ciau)=: 1 {"1 ciau
NB.
c=. 0{"1 t=. |: y}
pO=. c i. ;:'Vmag RA J2000 Dec J2000'
d=. _999&".&> p0 { t=. }."1 t
'invalid mag, ra, dec' assert -. _999 e. d
p1=. c i. ;: 'IAU Name Designation Bayer Name'
c ,. (<"1 ] p1 { t) , <"1 d
NB. cosine radians
cos=: 2\&o.
NB. cosine degrees
cosd=: cos@rfd
```

```
NB. decimal degrees from degrees, minutes, seconds - inverse (dmsfrdd)
ddfrdms=: (60"_ #. ]) % 3600"_
deltaT0=: 3 : 0
NB.*deltaTO v-- dynamical time \Delta T in seconds.
NB.
NB. Returns the difference in seconds between UT and TD based on
NB. polynomial expressions by Espenak and Meesus.
                                                             This
NB. calculation is useful for the years -1999 to 3000: a five
NB. thousand year period.
NB.
NB. see: https://eclipse.gsfc.nasa.gov/SEhelp/deltatpoly2004.html
NB.
NB. also in (futs): nasa_polynomial_expressions_for_delta_t_md
NB.
NB. monad: flSecs = deltaTO flYd
NB.
      ymd=. |: (3 {. 6!:0 ''), _1812 3 12 , _12 12 11 , 2137 12 13, 1700 1 1 ,: 35 7 6
NB.
      /: ymd , deltaTO deltaTdy ymd
NB.
NB. (ry) time intervals are (l,u]
NB. before -500:
NB. \Delta T = -20 + 32 * u^2; where: u = (y-1820)/100
ry=. ,: 1999 500
t1=. {{ 20 + 32 * U^2 [U=. (y - 1820) \% 100 }}
```

```
NB. between -500 and +500:
     \Delta T = 10583.6 - 1014.41 * u + 33.78311 * u^2 - 5.952053 * u^3
NB.
           -0.1798452 * u^4 + 0.022174192 * u^5 + 0.0090316521 * u^6; where: u = y/100
NB.
      NOTE: for the year -500 set value of 17190 to 17203.7
ry=. ry , 500 500
 t2 = . \{ \{ 10583.6 - (1014.41*U) + (33.78311*U^2) - (5.952053*U^3) - (0.1798452*U^4) + (0.022174192*U^5) + 0. \} \} 
>..>0090316521*U^6 [ U=. y % 100 }}
NB. between +500 and +1600:
      \Delta T = 1574.2 - 556.01 * u + 71.23472 * u^2 + 0.319781 * u^3
NB.
           -0.8503463 * u^{2} - 0.005050998 * u^{5} + 0.0083572073 * u^{6}; where: u = (y-1000)/100
ry=. ry , 500 1600
t3=. {{ 1574.2 - (556.01*U) + (71.23472*U^2) + (0.319781*U^3) - (0.8503463*U^4) - (0.005050998*U^5) + 0.00}
>..>83572073*U^6 [ U=. (y-1000) % 100 }}
NB. between +1600 and +1700:
NB. \Delta T = 120 - 0.9808 * t - 0.01532 * t^2 + t^3 / 7129; where: t = y - 1600
ry=. ry , 1600 1700
t4=. \{\{120 - (0.9808*t) - (0.01532*t^2) + (t^3)\%7129 [t=.y-1600]\}\}
NB. between +1700 and +1800:
NB. \Delta T = 8.83 + 0.1603 * t - 0.0059285 * t^2 + 0.00013336 * t^3 - t^4 / 1174000; where: <math>t = y - 1700
ry=. ry , 1700 1800
t5=. {{ 8.83 + (0.1603*t) - (0.0059285*t^2) + (0.00013336*t^3) - (t^4)%1174000 [t=.y-1700}}
NB. between +1800 and +1860:
NB. \Delta T = 13.72 - 0.332447 * t + 0.0068612 * t^2 + 0.0041116 * t^3 - 0.00037436 * t^4
```

```
NB.
                            + 0.0000121272 * t^5 - 0.0000001699 * t^6 + 0.000000000875 * t^7; where: t = y - 1800
ry = . ry , 1800 1860
t6=. {{ 13.72 - (0.332447*t) + (0.0068612*t^2) + (0.0041116*t^3) - (0.00037436*t^4) + (0.0000121272*t^5) - (0.0000121272*t^5) - (0.0000121272*t^5) + (0.0000121272*t^5) - (0.000012*t^5) 
>..> (0.0000001699*t^6) + 0.000000000875*t^7 [ t=. y - 1800 }}
NB. between 1860 and 1900:
             \Delta T = 7.62 + 0.5737 * t - 0.251754 * t^2 + 0.01680668 * t^3
                             -0.0004473624 * t^4 + t^5 / 233174; where: t = y - 1860
NB.
ry=. ry , 1860 1900
t7=. {{ 7.62 + (0.5737*t) - (0.251754*t^2) + (0.01680668*t^3) - (0.0004473624*t^4) + (t^5)\%233174 [ t=. v
>..>- 1860 }}
NB. between 1900 and 1920:
NB. \Delta T = -2.79 + 1.494119 * t - 0.0598939 * t^2 + 0.0061966 * t^3 - 0.000197 * t^4; where: t = y - 1900
ry=. ry , 1900 1920
t8=. \{\{-2.79 + (1.494119*t) - (0.0598939*t^2) + (0.0061966*t^3) - 0.000197*t^4 [ t=. y - 1900 \}\}
NB. between 1920 and 1941:
NB. \Delta T = 21.20 + 0.84493*t - 0.076100 * t^2 + 0.0020936 * t^3; where: t = y - 1920
ry=. ry , 1920 1941
t9=. \{\{ 21.20 + (0.84493*t) - (0.076100*t^2) + 0.0020936*t^3 [ t=. y - 1920 \} \}
NB. between 1941 and 1961:
NB. \Delta T = 29.07 + 0.407*t - t^2/233 + t^3/2547; where: t = y - 1950
ry=. ry , 1941 1961
t10=. \{\{29.07 + 0.407*t - ((t^2)\%233) + (t^3)\%2547 [t=.v-1950]\}\}
```

```
NB. between 1961 and 1986:
NB. \Delta T = 45.45 + 1.067*t - t^2/260 - t^3 / 718; where: t = y - 1975
ry=. ry , 1961 1986
t11=. \{ \{ 45.45 + (1.067*t) - ((t^2)\%260) - (t^3)\%718 [ t=. y - 1975 \} \}
NB. between 1986 and 2005:
      \Delta T = 63.86 + 0.3345 * t - 0.060374 * t^2 + 0.0017275 * t^3 + 0.000651814 * t^4
           + 0.00002373599 * t^5; where: t = y - 2000
NB.
ry=. ry , 1986 2005
t12=. {{ 63.86 + (0.3345*t) - (0.060374*t^2) + (0.0017275*t^3) + (0.000651814*t^4) + 0.00002373599*t^5 [ <math>t
>...>=. v - 2000 }}
NB. between 2005 and 2050:
NB. \Delta T = 62.92 + 0.32217 * t + 0.005589 * t^2; where: t = y - 2000
ry=. ry , 2005 2050
t13=. \{\{62.92 + (0.32217*t) + 0.005589*t^2 [t=.y-2000]\}\}
NB. between 2050 and 2150:
NB. \Delta T = -20 + 32 * ((y-1820)/100)^2 - 0.5628 * (2150 - y)
ry=. ry , 2050 2150
t14=. \{\{ 20 + (32 * ((y-1820)\%100)^2) - 0.5628 * 2150 - y \} \}
NB. after 2150:
NB. \Delta T = -20 + 32 * u^2; where: u = (y-1820)/100
ry=. ry , 2150 3000
t15=. \{\{ 20 + 32 * U^2 [ U=. (y-1820)\%100 \}\}
```

```
\it NB. NOTE: the \it t(i) verbs match the intervals
ti=. (rb=. /:~ ~. ,ry) I. y
'year range 1999 to 3000 exceeded' assert -. (0, #rb) e. ti
NB. t(i) gerund
tg=. t1`t2`t3`t4`t5`t6`t7`t8`t9`t10`t11`t12`t13`t14`t15
NB. apply t(i) verbs to appropriate intervals
(;ti </. i.#y) { ;(tg {~ <: ~.ti) apply&.> ti </. y
NB. delta \Delta T decimal year: deltaTdy 2023 3 12 ,. 1959 12 11
deltaTdy=: (0 { ]) + 12 %~ 0.5 -~ 1 { ]
NB. degrees from radian
dfr=: *&57.2957795130823229
NB. degrees, minutes, seconds from decimal degrees - inverse (ddfrdms)
dmsfrdd=: <. (,.) 60 60 #: 3600 * 1 | ,
NB. fractional day from hms: 0.80625 = fdfrhms 19 21 0
fdfrhms=: 24 %~ (60"_ #. ]) % 3600"_
NB. fractional centuries from epoch J2000 Meeus pg. 83: qT0jd julfrcal 1957 10 4.81
gT0jd=: 36525 %~ 2451545. -~ ]
```

```
NB. fractional centuries from epoch J2000 Meeus pg. 83: gT0ymd 1957 10 4.81
gTOymd=: 36525 %~ 2451545. -~ julfrcal
NB. hours, minutes from decimal seconds: hmfrds dsfrhms 20 27 43.23
hmfrds=: [: 24 60&#: 60 %~ ]
iau_tonight=: 3 : 0
NB.*iau_tonight v-- named IAU stars rising/setting tonight.
NB.
NB. monad: bt =. iau_tonight uuIgnore
NB.
NB.
      iau tonight O
NB.
NB. dyad: bt =. blYmd LB UO LMAG LHORZ iau tonight uuIgnore
NB.
      NB. date of Uluru star party diner
NB.
      YMD=. 2022 10 19
NB.
NB.
      ULURU=. 131.01941 _25.34301
      UTC=. _9.5
NB.
     LMAG=. 6.0
NB.
     LHORZ=. 5
NB.
NB.
      (YMD; ULURU; UTC; LMAG; LHORZ) iau_tonight 0
((3 {. 6!:0 ''); OBSLOCATION; UTCOFFSET; LIMITMAG; LIMITHORZ) iau tonight y
NB. date, location, UTC offset, magnitude, horizon
```

```
'YMD LB UO LMAG LHORZ'=. x
NB. IAU star data
({."1 IAU)=. {:"1 IAU [ 'IAU NAV'=. loadstars 0
NB. !(*)=. Vmaq IAU Name
NB. brighter than limiting magnitude
stars=. (LMAG > Vmag) # IAU Name
Rsiau=. (YMD; UO; LB) riseset stars
NB. retain rising setting - circumpolar NIMP
Rsiau=. Rsiau #~ -. ; 1 {"1 Rsiau
NB. name ,. transit altitude, hour minutes
Rsiau=. (0 {"1 Rsiau) ,. (0 2 3)&{&.> 1&{&.> 2 {"1 Rsiau}}}
NB. retain above local horizon
Rsiau=. Rsiau #~ LHORZ < 0&{&> 1 {"1 Rsiau
NB. sort by transit time
Rsiau \{ ~/: \}."1 > 1 \{ "1 Rsiau \}
intr3p=: 4 : 0
NB.*intr3p v-- interpolate three values - meeus pg 25.
NB.
NB. dyad: fln intr3p fl
```

18

```
NB.
NB.
      NB. meeus pq. 24
NB.
      yi=. 0.884226 0.877366 0.870531
NB.
      0.05 intr3p yi
NB. y = y2 + (n/2)(a + b nc)
NB. a b c are differences
'only 3 values' assert 3=#y
d=. 1 2{alldifs y
'a b'=. >0{d [ c=. ,/ >1{d}
(1{y}) + (x%2) * a + b + x*c
julfrcal=: 3 : 0
\it NB.*julfrcal \it v-- \it Julian dates from calendar dates.
NB.
NB. Astronomical Julian date. Similiar to (tojulian) but handles
NB. the fact that Julian days start at noon rather than midnight
NB. for calendar days.
NB.
NB. monad: fl =. julfrcal ilyyyyMMDD / ftyyyyMMDD
NB.
      julfrcal 2001 9 11
NB.
NB.
      julfrcal 1776 1941 1867 , 7 12 7 ,: 4 7 1
NB.
```

```
NB.
     NB. Meeus (Astronomical Algorithms) test cases (pg. 61)
     NB. NOTE: the fractional day representation of time
NB.
NB.
     2436116.31 = julfrcal 1957 10 4.81 NB. 7.a Sputnik 1
NB.
     1842713.0 = julfrcal 333 1 27.5
                                      NB. 7.b
NB.
NB.
     NB. zero date is roughly the age of the oldest bristlecone pines (coincidence?)
     julfrcal -4711 10 29.5
NB.
NB. vector J
                              NB. scalar BASIC
'v m d'=. v
                              NB. INPUT "Y,M,D";Y,M,D
g=. 1582 <: y
                              NB. G=1: IF Y<1582 THEN G=0
f=. (d - d1) - 0.5 [d1=. <. d
                              NB. D1=INT(D): F=D-D1-0.5
j=. - <. 7 * 4 %~ <.y + 12 %~ m+9 NB. J=-INT(7*(INT((M+9)/12)+Y)/4)
                               NB. IF G=0 THEN 805
s=. * m-9 [ a=. | m-9]
                              NB. S=SGN(M-9): A=ABS(M-9)
j3=. <. y + s * <. a\%7
                              NB. J3=INT(Y+S*INT(A/7))
j=. j+(<.275*m/9)+d1+g*j3 NB. 805 J=J+INT(275*M/9)+D1+G*J3
j=. j+1721027+(2*g)+367*y NB. J=J+1721027+2*G+367*Y
                              NB. IF F>=0 THEN 825
b=. f >: 0
f = . f + b [ j = . j - b]
                             NB. F=F+1: J=J-1
f + j
loadstars=: 3 : 0
NB.*loadstars v-- loads riseset star data.
NB.
```

```
NB. monad: blIAU_Nav =. loadstars uuIgnore
NB.
NB.
     NB. needs (futs, utils) dictionaries
      od;: 'futs utils' [ 3 od'' [ require 'general/jod'
NB.
NB.
      loadstars 0
NB.
NB. dyad: blIAU Nav=. pa loadstars uuIqnore
NB.
NB.
     1 loadstars 0 NB. define columns
NB.
     loadstars~ 1 NB. shorter idiom
0 loadstars y
NB. load IAU stars !(*)=. get
ciau=.; {: , > {: MACRO_ajod_get 'iau_named_stars_2022_txt'
ciau=. cold iau named stars parse iau named stars ciau
NB. load navigation stars
cnavs=. parsetd (; {: , > {: MACRO ajod get 'Navigation Stars txt') -. CR
cnavs=. (0 { cnavs) ,. <"1 |: }. cnavs</pre>
'star column overlap' assert 0 = \#(0 \{ \text{"1 cnavs}) ([-. -.) 0 \{ \text{"1 ciau} \})
NB. define columns - override mixed assignments (<:)=:
if. x -: 1 do.
  (0 {"1 ciau)=: 1 {"1 ciau
  (0 {"1 cnavs)=: 1 {"1 cnavs
end.
```

```
(<ciau), <cnavs
meanobliquityT0=: 3 : 0
NB. *meanobliquityTO v-- mean obliquity of the ecliptic IAU in degrees.
NB.
NB. monad: fl = .meanobliquityTO flT
NB. units are decimal arc seconds
ea=. +/3600 60 1 * OBLIQUITYDMS2000
NB. meeus (21.2) pg. 135
3600 \% ea - (46.8150*y) - (0.00059*y^2) + 0.001813*y^3
meanobliquityT1=: 3 : 0
NB.*meanobliquityT1 v-- mean obliquity of the ecliptic Laskar in
NB. degrees.
NB.
NB. Mean obliquity using Laskar's polynomial. This expression is
NB. more accurate than (meanobliquityT0): see Meeus (21.2) pg.
NB. 135.
NB.
NB. \ monad: \ fl = . \ meanobliquityT1 \ flT
```

```
NB. units are decimal arc seconds
ea=. +/3600 60 1 * OBLIQUITYDMS2000
NB. time units 10000 Julian years
U=. y % 100
e0=. (39.05*U^6) + (7.12*U^7) + (27.87*U^8) + (5.79*U^9) + 2.45*U^10
3600 \% ea - (4680.93*U) - (1.55*U^2) + (1999.25*U^3) - (51.38*U^4) - (249.67*U^5) - e0
)
meanobliquityjd0=: 3 : 0
NB. *meanobliquity id0 v-- mean obliquity ecliptic for Julian date (y) degrees.
NB.
NB. monad: fl = meanobliquityjd0 flJD
NB.
     NB. meeus pq. 136
NB.
      e0=. ,dmsfrdd meanobliquityjd0 2446895.5
NB.
NB.
NB.
      NB. matches to 3 decimals
      23 26 27.407 -: 0.001 round e0
NB.
NB.
NB. \ dyad: \ fl = . \ pa \ meanobliquityjd0 \ flJD
NB.
NB.
     NB. Laskar algorithm
      el=. ,dmsfrdd 1 meanobliguityjd0 2446895.5
NB.
```

```
0 meanobliquityjd0 y
meanobliquityT0`meanobliquityT1@.(x) gT0jd y
meansid0=: 4 : 0
NB.*meansid0 \ v-- \ mean \ sidereal \ time \ at \ Greenwich \ for \ T \ (x) \ JD \ (y).
NB.
NB.\ dyad:\ flDegs = .\ flT\ meansid\ flJD
NB. meeus (11.4) pg 84
280.46061837 + (360.98564736629 * y - 2451545.0) + (0.000387933 * x^2) - 38710000 %~ x^3
)
meansidjd0=: 3 : 0
NB. *meansidjd0 v-- mean sidereal time at Greenwich for julian day (y) in degrees.
NB.
NB. \ monad: \ fl = . \ meansidjd0 \ flJD
NB.
      NB. julian day for April 10, 1987 19h:24m:00s UT
NB.
      JD=. julfrcal 1987 4,10 + fdfrhms 19 21 0
NB.
      meansidjd0 JD
NB.
(gT0jd y) meansid0 y
```

```
NB. normalize negative degree sidereal time: nnth0 -1677831.2621266
nnth0=: ] + 360 * [: | [: (<.) 360 %~ ]
NB. normalize positive degree sidereal time: npth0 1677831.2621266
npth0=: ] - 360 * [: (<.) 360 %~ ]
NB. normalize degree sidereal time: nth0 _35555 77777
nth0=: npth0`nnth0@.(0&>:@[)
nutation longitude dPsi=: 3 : 0
NB.*nutation_longitude_dPsi v-- nutation in ecliptical longitude in degrees (1980 iau theory).
NB.
NB. NOTE: the pseudo-code is vector ready and easily converted to J.
NB.
NB. verbatim: algorithm from Jay Tanner https://neoprogrammics.com/nutations/
NB.
      see: nutation in longitude dPsi md
NB.
NB.
NB. monad: flDeq =. nutation_longitude_dPsi flJD
NB.
      ymd=. |: 2023 3 12 , 1959 12 11 , 2135 12 13, 1700 1 1 ,: 1935 7 6
NB.
NB.
      JD=. julfrcal ymd NB. no delT adj.
     2460015.5 = 0{JD}
NB.
      nutation longitude dPsi JD
NB.
NB.
NB.
     NB. see (futs) test: (riseset_tanner_smoke) for examples
```

```
T=. (y - 2451545) % 36525 NB. T = (JD - 2451545) / 36525
T2=. T*T
                          NB. T2 = T*T
T3=. T*T2
                          NB. T3 = T*T2
NB. DegToRad = 3.1415926535897932 / 180
DegToRad=. 3.1415926535897932 % 180
NB. w1 = 297.85036 + 445267.11148*T - 0.0019142*T2 + (T3 / 189474)
w1=.297.85036 + (445267.11148*T) - (0.0019142*T2) + (T3 % 189474)
w1=. DegToRad*(w1)
                       NB. w1 = DegToRad*(w1)
NB. \ w2 = 357.52772 + 35999.05034*T - 0.0001603*T2 - (T3 / 300000)
w2=. 357.52772 + (35999.05034*T) - (0.0001603*T2) - (T3 % 300000)
w2=. DegToRad*(w2)
                          NB. w2 = DeqToRad*(w2)
NB. w3 = 134.96298 + 477198.867398*T + 0.0086972*T2 + (T3 / 56250)
w3=. 134.96298 + (477198.867398*T) + (0.0086972*T2) + (T3 % 56250)
w3=. DegToRad*(w3)
                          NB. w3 = DegToRad*(w3)
NB. w4 = 93.27191 + 483202.017538*T - 0.0036825*T2 + (T3 / 327270)
w4=. 93.27191 + (483202.017538*T) - (0.0036825*T2) + (T3 % 327270)
w4=. DegToRad*(w4)
                          NB. w4 = DeqToRad*(w4)
NB. w5 = 125.04452 - 1934.136261*T + 0.0020708*T2 + (T3 / 450000)
w5=. 125.04452 - (1934.136261*T) + (0.0020708*T2) + (T3 % 450000)
w5=. DegToRad*(w5) 
 NB. w5 = DegToRad*(w5)
```

```
w=. (\sin w5)*((174.2*T) - 171996)
                                    NB. w = sin(w5)*(-174.2*T - 171996)
w=. \ w + (\sin 2 * w4 + w5 - w1)*((_1.6*T) - 13187) \ NB. \ w = w + sin(2*(w4 + w5 - w1))*(-1.6*T - 13187)
w=. w + (\sin 2 * w4 + w5)*(2274 - 0.2*T)
                                                NB. w = w + \sin(2*(w4 + w5))*(-2274 - 0.2*T)
w=. w + (\sin 2 * w5)*((0.2*T) + 2062)
                                                NB. w = w + \sin(2 * w5)*(0.2*T + 2062)
w=. w + (\sin w2)*(1426 - 3.4*T)
                                                NB. w = w + \sin(w2)*(1426 - 3.4*T)
w=. w + (\sin w3)*((0.1*T) + 712)
                                                 NB. w = w + \sin(w3)*(0.1*T + 712)
NB. w = w + \sin(2*(w4 + w5 - w1) + w2)*(1.2*T - 517)
w=. w + (\sin (2 * w4 + w5 - w1) + w2)*((1.2*T) - 517)
w=. w + (\sin (2*w4) + w5)*((_0.4*T) - 386)
NB. w = w + \sin(2*w4 + w5)*(-0.4*T - 386)
NB. w = w + \sin(2*(w4 + w5 - w1) - w2)*(217 - 0.5*T)
w=. w + (\sin (2 * w4 + w5 - w1) - w2)*(217 - 0.5*T)
w=. w + (\sin (2*w4 - w1) + w5)*(129 + 0.1*T)
                                             NB. w = w + \sin(2*(w4 - w1) + w5)*(129 + 0.1*T)
                                                NB. w = w + \sin(w3 + w5)*(0.1*T + 63)
w=. w + (\sin w3 + w5)*((0.1*T) + 63)
w=. w + (\sin w5 - w3)*((0.1*T) - 58)
                                            NB. w = w + \sin(w5 - w3)*(-0.1*T - 58)
w=. w + (\sin 2*w2)*(17 - 0.1*T)
                                                  NB. w = w + \sin(2*w2)*(17 - 0.1*T)
w=. w + (\sin 2 * w^2 + w^4 + w^5 - w^1)*((0.1*T) - 16) NB. w = w + \sin(2*(w^2 + w^4 + w^5 - w^1))*(0.1*T - 16)
w=. w - 301*(sin (2 * w4 + w5) + w3)
                                                 NB. w = w - 301*sin(2*(w4 + w5) + w3)
w=. w - 158*(sin w3 - 2*w1)
                                                 NB. w = w - 158*sin(w3 - 2*w1)
w=. w + 123*(sin (2 * w4 + w5) - w3)
                                                 NB. w = w + 123*sin(2*(w4 + w5) - w3)
w=. w + 63*(sin 2*w1)
                                                  NB. w = w + 63*sin(2*w1)
                                                 NB. w = w - 59*sin(2*(w1 + w4 + w5) - w3)
w=. w - 59*(sin (2 * w1 + w4 + w5) - w3)
                                                  NB. w = w - 51*sin(2 * w4 + w3 + w5)
w=. w - 51*(sin (2*w4) + w3 + w5)
```

```
NB. w = w + 48*sin(2*(w3 - w1))
w=. w + 48*sin(2 * w3 - w1)
w=. w + 46*(sin (2 * w4 - w3) + w5)
                                                NB. w = w + 46*sin(2*(w4 - w3) + w5)
w=. w - 38*(sin 2 * w1 + w4 + w5)
                                                 NB. w = w - 38*sin(2*(w1 + w4 + w5))
                                                 NB. w = w - 31*sin(2*(w3 + w4 + w5))
w=. w - 31*(sin 2 * w3 + w4 + w5)
w=. w + 29*(sin 2*w3)
                                                 NB. w = w + 29*sin(2*w3)
w=. w + 29*(sin (2 * w4 + w5 - w1) + w3)
                                                 NB. w = w + 29*sin(2*(w4 + w5 - w1) + w3)
w=. w + 26*(sin 2*w4)
                                                 NB. w = w + 26*sin(2*w4)
                                                 NB. w = w - 22*sin(2*(w4 - w1))
w=. w - 22*(sin 2* w4 - w1)
w=. w + 21*(sin (2*w4) + w5 - w3)
                                                 NB. w = w + 21*sin(2*w4 + w5 - w3)
w=. w + 16*(sin (2*w1) - w3 + w5)
                                                 NB. \ w = w + 16*sin(2*w1 - w3 + w5)
w=. w - 15*(sin w2 + w5)
                                                 NB. w = w - 15*sin(w2 + w5)
w=. w - 13*(\sin w3 + w5 - 2*w1)
                                                 NB. w = w - 13*sin(w3 + w5 - 2*w1)
w=. w - 12*(\sin w5 - w2)
                                                 NB. w = w - 12*sin(w5 - w2)
                                                 NB. w = w + 11*sin(2*(w3 - w4))
w=. w + 11*(sin 2 * w3 - w4)
w=. w - 10*(sin (2 * w4 + w1) + w5 - w3)
                                                 NB. w = w - 10*sin(2*(w4 + w1) + w5 - w3)
                                                 NB. w = w - 8*sin(2*(w4 + w1 + w5) + w3)
w=. w - 8*(sin (2 * w4 + w1 + w5) + w3)
                                                 NB. w = w + 7*sin(2*(w4 + w5) + w2)
w=. w + 7*(sin (2 * w4 + w5) + w2)
w=. w - 7*(\sin w3 - (2*w1) + w2)
                                                 NB. w = w - 7*sin(w3 - 2*w1 + w2)
                                                 NB. w = w - 7*sin(2*(w4 + w5) - w2)
       7*(\sin (2 * w4 + w5) - w2)
w=, w -
                                                 NB. w = w - 7*sin(2*w1 + 2*w4 + w5)
w=. w - 7*(sin (2*w1) + (2*w4) + w5)
w=. w + 6*(sin (2*w1) + w3)
                                                 NB. w = w + 6*sin(2*w1 + w3)
w=. w + 6*(sin 2 * w3 + w4 + w5 - w1)
                                                 NB. w = w + 6*sin(2*(w3 + w4 + w5 - w1))
w=. w + 6*(sin (2 * w4 - w1) + w3 + w5)
                                                 NB. w = w + 6*sin(2*(w4 - w1) + w3 + w5)
                                                 NB. w = w - 6*sin(2*(w1 - w3) + w5)
w=. w - 6*(sin (2 * w1 - w3) + w5)
w=. w - 6*(sin (2*w1) + w5)
                                                 NB. w = w - 6*sin(2*w1 + w5)
w=. w + 5*(sin w3 - w2)
                                                 NB. \ w = w + 5*sin(w3 - w2)
w=. w - 5*(sin (2* w4 - w1) + w5 - w2)
                                                 NB. w = w - 5*sin(2*(w4 - w1) + w5 - w2)
```

```
5*(\sin w5 - 2*w1)
                                                 NB. w = w - 5*sin(w5 - 2*w1)
w=. w -
        5*(sin (2 * w3 + w4) + w5)
                                                NB. w = w - 5*sin(2*(w3 + w4) + w5)
w=. w + 4*(sin (2 * w3 - w1) + w5)
                                                NB. w = w + 4*sin(2*(w3 - w1) + w5)
       4*(\sin (2 * w4 - w1) + w2 + w5)
                                                NB. w = w + 4*sin(2*(w4 - w1) + w2 + w5)
                                                NB. w = w + 4*sin(w3 - 2*w4)
       4*(\sin w3 - 2*w4)
       4*(\sin w3 - w1)
                                                NB. \ w = w - 4*sin(w3 - w1)
       4*(\sin w2 - 2*w1)
                                                NB. w = w - 4*sin(w2 - 2*w1)
       4*(sin w1)
                                                NB. w = w - 4*sin(w1)
w=. w -
w=. w + 3*(sin (2*w4) + w3)
                                                NB. w = w + 3*sin(2*w4 + w3)
        3*(\sin 2*w4+w5-w3)
                                                NB. w = w - 3*sin(2*(w4 + w5 - w3))
w=. w -
                                                NB. \ w = w - 3*sin(w3 - w1 - w2)
w=. w - 3*(\sin w3 - w1 - w2)
w=. w - 3*(\sin w2 + w3)
                                                NB. w = w - 3*sin(w2 + w3)
w=. w - 3*(sin (2 * w4 + w5) + w3 - w2)
                                                NB. w = w - 3*sin(2*(w4 + w5) + w3 - w2)
w=. w - 3*(sin (2 * w1 + w4 + w5) - w2 - w3)
                                               NB. w = w - 3*sin(2*(w1 + w4 + w5) - w2 - w3)
w=. w - 3*(sin (2 * w4 + w5) + 3*w3)
                                                NB. w = w - 3*sin(2*(w4 + w5) + 3*w3)
w=. w - 3*(sin (2 * w1 + w4 + w5) - w2)
                                               NB. w = w - 3*sin(2*(w1 + w4 + w5) - w2)
dPsiDeg=. w \% 36000000.0 NB. dPsiDeg = w / 36000000.0
)
parse_iau_named_stars=: 3 : 0
NB.*parse\_iau\_named\_stars\ v--\ IAU\ named\ star\ list\ to\ btcl\ header
NB. table.
NB.
NB. Original star name data was downloaded from:
NB.
NB. https://www.iau.org/public/themes/naming_stars/
```

```
NB.
NB. and slightly adjusted in Excel. The data stored in (futs) is
NB. a Unicode UTF-8 CSV export.
NB.
NB. monad: btcl =. parse_iau_named_stars clTxt
NB.
NB.
     NB. get stars from (futs)
     NB. od ;:'futs utils'
NB.
NB.
     iau=.; {: , > {: 4 get 'iau_named_stars_2022_txt'
     parse iau named stars iau
NB.
NB. remove any byte order mark
t=. parsecsv y \}.~ (BOM -: (#BOM){.y}{0,#BOM}
NB. extract relevant columns
c=. ;:'IAU Name Designation Bayer Name Vmag RA J2000 Dec J2000'
t=. t {"1~ (0 { t) i. c
NB. scrub objects with questionable magnitude
t #~ ~: 999&".&> (c i. <'Vmag') {"1 t
)
parsecsv=: 3 : 0
NB.*parsecsv v-- parses comma delimited files. (x) is the field
NB. delimiter. Lines are delimited with either CRLF or LF
NB.
NB. \ monad: \ btcl = . \ parsecsv \ cl
```

```
NB. dyad: btcl = ca parsecsv cl
NB.
NB.
     ',' parsecsv read 'c:\comma\delimted\text.csv'
',' parsecsv y
'separater cannot be the " character' assert -. x -: '"'
NB. CRLF delimited *.csv text to char table
y=. x ,. ];._2 y -. CR
NB. bit mask of unquoted " field delimiters
b=. -. }. ~:/\ '"' e.~ ' ' , , y
b=. ($y) $ b *. , x = y
NB. use masks to cut lines
b <;._1"1 y
NB. parse TAB delimited table text - see long document
parsetd=: [: <;. 2&> (a.{~9}) ,&.>~ [: <;. 2 [: (] , ((10{a.)" = {:) }. (10{a.)" ) (13{a.) -.~ ]
NB. radians from degrees
rfd=: *&0.0174532925199432955
riseset=: 4 : 0
```

```
NB.*riseset v-- rise, transit, set times of IAU named stars.
NB.
NB. dyad: blYmdUtoLB riseset blclStarNames
NB.
NB.
      LB=. _116.375956 43.646775
                                     NB. Meridian
NB.
      YMD=. 2023 3 27
NB.
      UO=. 6
     (YMD; UO; LB) riseset 'Algol'
NB.
NB.
      (YMD; UO; LB) riseset 'Algol'; 'Rigel'; 'Spica'
NB. local time, UT offset (O=Greenwich), Latitude Longitude
'ymfd uo LB'=. x
NB. convert LB to meeus convention
LB=. _1 1 * LB
NB. local time to UT
UT=. ymfd + 0 0,uo%24
NB. look up RA, Dec
'IAU Navigation'=. loadstars 0
NB. IAU stars !(*)=. IAU Name RA J2000 Dec J2000
(\{."1 \text{ IAU})=. \{:"1 \text{ IAU}\}
Stars=. boxopen y
if. 0 e. b=. Stars e. IAU_Name do.
  smoutput 'not in IAU named stars -> '; Stars #~ -.b
```

```
else.
  ix=. IAU Name i. Stars
 RA=. <ix{RA J2000 [ Dec=. <ix{Dec J2000
 riseset calc UT; LB; (<Stars), RA, Dec
end.
riseset calc=: 3 : 0
NB.*riseset calc v-- rise, transit, set times of stars.
NB.
NB. Main rise/set calculations. Argument (y) set in (riseset).
NB.
NB. monad: bt =. riseset calc blyMD LB OBJ RA Dec
'ymd LB obj ra dec'=. ,&.> y
NB. (L) longitude, west positive
NB. (B) latitude, north positive
'L B'=. LB
obj=. obj ,"O 1 a:,a: NB. result table
NB. dynamical time \Delta T in fractional days NOTE: \Delta T is not
NB. going to change a lot over the interpolation period
dTfd=. (,/deltaT0 deltaTdy ymd) % DAYSECS
NB. apparent sidereal time Greenwich at Oh in degrees
```

```
th0=. ,/ddfrdms 15 * apparsidjd0 julfrcal ymd
NB. TD times \Delta T + UT = TD
TD=. (2 {. ymd),"1 0 (_1 0 1 + {:ymd) + dTfd
NB. apparent ra, dec for _1 0 1 days around rise/set
rdi=. |: TD apparRADEC"1 _ ra ,: dec
hO=. STDALTITUDE
NB. approximate times (14.1) meeus pq. 98
cosH0=. ((sind h0) - (sind B)*sind (<a:;1;1){rdi} % (cosd B)*cosd (<a:;1;1){rdi}
NB. 1 indicates above or below horizon
bhrz=. 1 < |cosH0|
obj=. (<"0 bhrz) (<a:;1)} obj
obj=. (<'above or below horizon') (<(I. bhrz);2)} obj
ix=. I. -. bhrz NB. objects that rise and set
NB. m(i) are fractional day times (1/) puts mi in [0,1]
HO=. dfr arccos ix{cosHO
m0=. 1|360 \% (((ix;0;1){rdi}) + L - th0)
m1=. 1 | m0 - H0 \% 360
m2=. 1 | m0 + H0 \% 360
NB. rise, transit, setting
m=. m1,. m0,. m2
```

```
NB. sidereal time at Greenwich - meeus pg. 99
th=. nth0 th0 + 360.985647*m
NB. adjusted ra, dec
rda=. nu intr3p"1 ix{rdi [ nu=. dTfd + m
NB. local hour angles
rax=. <a:;0 [ decx=. <a:;1
H=. (th - L) - rax{rda
NB. body's altitude (12.6) meeus pq. 89
sih=. ((sind B)*sind decx{rda) + (cosd B)*(cosd decx{rda)*cosd H
NB. degree altitudes positive
h=. |dfr arcsin sih
NB. corrections for transits (trx), rise/sets (rsx)
dltm=. ($m)$0
trx=. <a:;1 [ rsx=. <a:;0 2
dltm=. (-(trx{H})\%360) trx} dltm
drs=. rsx { (h - h0) \% 360 * (cosd decx{rda})*(cosd B)*sind H
dltm=. drs rsx} dltm
m=. m + dltm
NB. objects, above/below, altitudes, fractional day UT, UT hours/minutes
(<"2 (,."1 ] 0.5 round h) ,"1 (,."1 m) ,"1 ] 1 round hmfrds DAYSECS*m) (<ix;2)} obj
)
```

```
NB. round (y) to nearest (x) (e.g. 1000 round 12345)
round=: [ * [: (<.) 0.5 + %~
NB. sine radians
sin=: 1&o.
NB. sin degrees
sind=: sin@rfd
NB. session manager output
smoutput=: 0 0 $ 1!:2&2
zetzthT0=: 3 : 0
NB.*zetzthTO v-- epoch adjustment terms for J2000 RA DEC in degrees.
NB.
NB.\ monad:\ fT = .\ zetzthTO\ ftYYYYMMDD
NB.
NB.
      zetzthT0 2028 11 13.19
NB.
      zetzthT0 2023 4 23 , 1988 3 20 ,: 1987 4,10 + fdfrhms 19 21 0
NB.
t=. gTOymd y
't2 t3'=. t (^"1 0) 2 3 NB. t^2 and t^3
NB. meeus (20.3) pg. 126
```

```
zet=. (2306.2181*t) + (0.30188*t2) + 0.017988*t3
    (2306.2181*t) + (1.09468*t2) + 0.018203*t3
z=.
th=. (2004.3109*t) + (0.42665*t2) + 0.041833*t3
NB. insure degree result rank matches (y) rank
3600 % zet , z (,\,\;)@.(2=#$y) th
NB.POST_riseset post processor.
smoutput IFACE=: (0 : 0)
NB. (riseset) interface word(s): 20230328j135930
NB. -----
NB. iau tonight NB. named IAU stars visible tonight
NB. loadstars NB. loads riseset star data
NB. riseset NB. rise, transit, set times of stars
NB. smoutput 'NB. vmd: ' , ,'0,p<; >q<; >0,0' (8!:2) VMDriseset
cocurrent 'base'
coinsert 'riseset'
NB. high print precision
(9!:11) 16
NB. test stars
NB. smoutput loadstars O
```

## $\mathbf{Index}$

()=:, <u>21</u>	dmsfrdd, 16	npth0, 25 nth0, 25
alldifs, 7	fdfrhms, 16	nutation_longitude_dPsi, 25
apparRADEC, 7	TO:1 16	
apparsecs, 8	gT0jd, 16	OBLIQUITYDMS2000, 6
apparsidjd0, 8	gT0ymd, 17	OBSLOCATION, 6
apply, 8	hmfrds, 17	named in named stans 20
arccos, 8	111111111111111111111111111111111111111	parse_iau_named_stars, 29
arcsin, 8	iau_tonight, 17	parsecsv, 30
arctan, 8	IFACE, 37	parsetd, $31$
assert, 9	IFACEWORDSriseset, 6	rfd, 31
atan2, 9	intr3p, 18	riseset, 31
BOM, 5	:]f] 10	${\tt riseset\_calc}, 33$
boxopen, 11	julfrcal, 19	ROOTWORDSriseset, $6$
20110F011, 21	LIMITHORZ, 6	round, 36
${\tt cold\_iau\_named\_stars}, 11$	LIMITMAG, 6	-: 26
$\cos, 11$	loadstars, 20	sin, 36
cosd, 11	,	sind, 36
CR, 5	meanobliquityjd0, 23	smoutput, 36
DAVGEGG	meanobliquityT0, 22	STDALTITUDE, 6
DAYSECS, 5	meanobliquityT1, 22	UTCOFFSET, 6
ddfrdms, 12	$meansid0, \frac{24}{}$	, ,
deltaT0, 12	$meansidjd0, \frac{24}{}$	VMDriseset, 6
deltaTdy, 16		+-+hTO 26
dfr, 16	nnth0, 25	zetzthT0, 36