Module Interface Specification for Tamias2D : A 2D Game Physics Library

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1 Revision History

Date	Version	Notes
Nov. 15, 2018	1.0	Updates throughout document; siimplifying document
Nov 20, 2018	1.1	Notes

2 Symbols, Abbreviations and Acronyms

See SRS Documentation at https://github.com/smiths/caseStudies/blob/master/CaseStudies/gamephys/docs/SRS/GamePhysicsSRS.pdf

Contents

3 Introduction

The following document details the Module Interface Specifications for the implemented modules in the Tamias2D Game Physics Library. It is intended to ease navigation through the program for design and maintenance purposes. Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at https://github.com/smiths/caseStudies/tree/master/CaseStudies/gamephys

4 Notation

For instance, the symbol := is used for a multiple assignment statement and conditional rules follow the form $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | ... | c_n \Rightarrow r_n)$.

The following table summarizes the primitive data types used by Tamias2D .

Data Type	Notation	Description
boolean	$\mathbb{B}$	An element of {true, false}.
character	char	A single symbol or digit.
real	$\mathbb{R}$	Any number in (-∞, ∞).
integer	$\mathbb{Z}$	A number without a fractional component in (-∞, ∞).
natural number	$\mathbb{N}$	A number without a fractional component in $[1, \infty)$.

Tamias2D also uses non-primitive data types such as arrays, enumerations, pointers (references), strings, structures, unions. These are summarized in the following table.

Data Type	Notation	Description
Array	array(T)	A list of a given data type T.
Enumeration	enum	A data type containing named, constant values.
Pointer	T*	A reference to an object of data type T.
String	string/array(char)	An array of characters.
Structure	struct	A data type that can store multiple fields of different data types in one variable.
Union	union	Similar to a structure, but only one field can contain a value at any given time.

Finally, Tamias2D uses two more important type-related concepts: void and function pointers. Void is not a data type in itself; however, functions that do not return any value are assigned a return type of void, and void pointers, denoted by void*, are used for references

to objects of an unspecified data type. Tamias2D also allows passing functions to other functions through the use of function pointers, which hold references to function definitions. Each function pointer is denoted by the name of their function type and is defined by a specific function signature, such as:

$$\text{Function Type} : \text{Arg}_1 \times \text{Arg}_2 \times ... \times \text{Arg}_n \rightarrow \text{Return Type}$$

For example, an inequality operator would have the signature "Inequality : $\mathbb{R} \times \mathbb{R} \rightarrow \mathbb{B}$".

5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	**Level 2**	**Level 3**
Hardware-Hiding Module		
Behaviour-Hiding Module	Rigid Body	
	Shape	
		Circle
		Segment
		Polygon
	Space	
Software Decision Module	Vector	
	Collision Solver	

Table 3: Module Hierarchy

6 MIS of the Rigid Body Module

6.1 Module Name: Body

6.2 Uses

Shape Module, Space Module, Vector Module

6.3 Syntax

6.3.1 Exported Constants

N/A

6.3.2 Exported Access Programs

Name	In	Out	Exceptions
bodyInit	Body*, $\mathbb{R}$, $\mathbb{R}$	Body*	-
update	Body*	$\mathbb{R}$	-
apply_force	Body*	Vec2*	-
apply_torque	Body*	$\mathbb{R}$	-
set_space	Body*	Space*	-
set_angular_accler	Body*	$\mathbb{R}$	-

6.4 Semantics

6.4.1 State Variables

BodyType $\in$ {DYNAMIC, STATIC}

Body:

type: BodyType
mass: $\mathbb{R}$
massInv: $\mathbb{R}$
moment: $\mathbb{R}$
momentInv: $\mathbb{R}$
position: Vector
velocity: Vector
force: Vector
angle: $\mathbb{R}$
angular_accler: $\mathbb{R}$
torque: $\mathbb{R}$
space: Space*

6.4.2 State Invariant

For dynamic bodies, the following invariants apply. Any value in $\mathbb{R}$ means that it must be a valid and finite real number:

- Body.mass $\in [0, \infty)$
- Body.moment $\in [0, \infty)$
- |Body.position.x| $\in \mathbb{R} \wedge$ |Body.position.y| $\in \mathbb{R}$
- |Body.vel.x| $\in \mathbb{R} \wedge$ |Body.vel.y| $\in \mathbb{R}$
- |Body.force.x| $\in \mathbb{R} \wedge$ |Body.force.y| $\in \mathbb{R}$
- |Body.angle| $\in \mathbb{R}$
- |Body.angular_accler| $\in \mathbb{R}$
- |Body.torque| $\in \mathbb{R}$

6.5 Environment Variables

N/A

6.5.1 Assumptions

All input pointers are also assumed to be non-null.

6.5.2 Access Routine Semantics

bodyInit:	**Transition:**	bodyInit allocates a new Body and initializes its mass, moment, bodyType, restitution, angle and shape with the input values. Other fields are zero-initialized and kinematic functions are set to default ones.
	Output:	bodyInit returns a pointer to the initialized Body.
	Exceptions:	None.
Update :	**Transition:**	Update will update Body's position and all other parameters(bodyInit) associated to the body after each cycle.
	Output:	None.
	Exceptions:	None

6.5.3 Local Functions

N/A

7 MIS of the Shape Module

7.1 Module Name: Shape

7.2 Uses

Rigid Body Module, Space Module, Vector Module,

7.3 Syntax

7.3.1 Exported Constants

N/A

7.3.2 Exported Access Programs

Name	In	Out	Exceptions
set_angle	Shape*	$\mathbb{R}$	-
set_pos	Shape*	$\mathbb{R}$	-
get_centre	Shape*	Vec2*	-

7.4 Semantics

7.4.1 State Variables

ShapeType $\in$ {CIRCLE, POLYGON}
ShapeClass:

type: ShapeType

Shape:

Colshape: ShapeClass* type: CollisionType
space: Space*
body: Body*

7.4.2 Assumptions

All input pointers are assumed to be non-null. Also see 7.8.2, 7.12.2.

7.4.3 Access Program Semantics

7.5 Submodule Name: CircleShape

7.6 Uses

Rigid Body Module, Shape Module, Vector Module

7.7 Syntax

7.7.1 Exported Data Types

CircleShape: struct

7.7.2 Exported Access Programs

Name	In	Out	Exceptions
circleShapeInit	CircleShape*, Body*, double, Vector	CircleShape*	-
get_center	Shape*	double	NotCircleShape
circleShapeNew	Body*, double, Vector	Shape*	-
circleShapeGetRadius	Shape*	double	NotCircleShape
circleShapeSetRadius	Shape*, double	-	NotCircleShape $\vee$ IllegalBody
momentForCircle	double, double, double, Vector	double	-
areaForCircle	double, double	double	-

7.8 Semantics

7.8.1 State Variables

CircleShape:

shape: Shape
center: Vector
radius: $\mathbb{R}$

7.8.2 Assumptions

circleShapeNew have been called before any other access programs. All input pointers are also assumed to be non-null.

7.8.3 Access Program Semantics

circleShapeInit:

Input: circleShapeInit accepts a CircleShape pointer, a Body pointer, a double and a Vector as inputs.

Exceptions: None.

Transition: circleShapeInit initializes the input CircleShape. It sets the radius to the input double, the center to the input Vector, and then initializes the rest of the variables using shapeInit and the input Body.

Output: circleShapeInit returns a pointer to the initialized CircleShape.

circleShapeNew:	**Input:**	circleShapeNew accepts a Body pointer, a double and a Vector as inputs.
	Exceptions:	None.
	Transition:	circleShapeNew allocates and initializes a new CircleShape object using the input paramters.
	Output:	circleShapeNew returns a pointer to the new CircleShape.
circleShapeGet:	**Input:**	Each circleShapeGet function accepts a Shape pointer as input.
	Exceptions:	Each circleShapeGet function may throw a NotCircleShape exception if the input Shape pointer is not of the CircleShape class.
	Transition:	None.
	Output:	Each circleShapeGet function returns the value of their corresponding parameter.
circleShapeSet:	**Input:**	Each circleShapeSet function accepts a Shape pointer and their corresponding parameter as inputs.
	Exceptions:	Each circleShapeSet function may throw a NotCircleShape exception if the input Shape pointer is not of the CircleShape class, or if the Body associated with the Shape violates an invariant in 6.4.2 after the transitions are complete.
	Transition:	Each circleShapeSet function sets their corresponding parameter with the input value, updates the mass information of the Shape and recalculates the mass of its associated Body.
	Output:	None.
momentForCircle:	**Input:**	momentForCircle accepts three doubles for mass, inner radius and outer radius, and a Vector as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	momentForCircle returns the calculated moment from the input parameters as a double.

areaForCircle:	**Input:**	areaForCircle accepts two double values for the inner radius and outer radius as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	areaForCircle returns the calculated area from the input parameters as a double.

7.8.4 Local Constants

CircleShapeClass: ShapeClass
CircleShapeClass := {CIRCLE_SHAPE, circleShapeCacheData, NULL}

7.8.5 Local Functions

circleShapeCacheData:	**Input:**	circleShapeCacheData accepts a CircleShape pointer and a Transform matrix as inputs.
	Exceptions:	None.
	Transition:	circleShapeCacheData updates the transformed center of the input CircleShape using the input Transform matrix and generates a new BB with the CircleShape's properties. Default cacheData method of the CircleShapeClass.
	Output:	circleShapeCacheData returns the new BB as output.
circleShapeMassInfo:	**Input:**	circleShapeMassInfo accepts two double values for mass and radius and a Vector as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	circleShapeMassInfo is a convenience constructor which returns a new ShapeMassInfo structure for CircleShapes, initialized using the input values.

7.9 Submodule Name: PolyShape

7.10 Uses

Rigid Body Module, Shape Module, Vector Module,

7.11 Syntax

7.11.1 Exported Data Types

PolyShape: struct

7.11.2 Exported Access Programs

Name	In	Out	Exceptions
polyShapeInit	PolyShape*, Body*, int, Vector*, double, Transform	PolyShape*	-

boxShapeInit	PolyShape*, Body*, double, double, double	PolyShape*	-
boxShapeInit2	PolyShape*, Body*, double, BB	PolyShape*	-
polyShapeNew	Body*, int, Vector*, double	Shape*	-
polyShapeNewRaw	Body*, int, Vector*, double, Transform	Shape*	-
boxShapeNew	Body*, double, double, double	Shape*	-
boxShapeNew2	Body*, double, BB	Shape*	-
polyShapeGetCount	Shape*	int	NotPolyShape
polyShapeGetVert	Shape*, int	Vector	NotPolyShape $\vee$ IndexOutOf-Bounds
polyShapeGetRadius	Shape*	double	NotPolyShape
polyShapeSetVerts	Shape*, int, Vector*, Transform	-	NotPolyShape $\vee$ IllegalBody
polyShapeSetVertsRaw	Shape*, int, Vector*	-	NotPolyShape $\vee$ IllegalBody
polyShapeSetRadius	Shape*, double	-	NotPolyShape
momentForPoly	double, int, Vector*, Vector, double	double	-
areaForPoly	int, Vector*, double	double	-
centroidForPoly	int, Vector*	Vector	-

7.12 Semantics

7.12.1 State Variables

PolyShape:

shape: Shape
count: $\mathbb{Z}$
radius: $\mathbb{R}$

7.12.2 Assumptions

polyShapeNew/polyShapeNewRaw, or boxShapeNew/boxShapeNew2, have been called before any other access programs. All input pointers are also assumed to be non-null.

7.12.3 Semantics

polyShapeInit:	**Input:**	polyShapeInit accepts a PolyShape pointer, a Body pointer, an integer, a pointer to a Vector array, a double and a Transform matrix as inputs.
	Exceptions:	None.
	Transition:	polyShapeInit transforms each vertex from the input array with the input Transform matrix, places the resultant vertices in a new array, calculates the size of the convex hull containing the new vertices and initializes the input PolyShape using this array, the hull size and the remaining parameters.
	Output:	polyShapeInit returns a pointer to the initialized PolyShape.
polyShapeInit Raw:	**Input:**	polyShapeInitRaw accepts a PolyShape pointer, a Body pointer, an integer, a pointer to a Vector array and a double as inputs.
	Exceptions:	None.
	Transition:	polyShapeInitRaw initializes the input PolyShape using shapeInit and the input parameters, sets its vertices to the given array and integer (which represents the length of the array), and sets its radius to the input double.
	Output:	polyShapeInitRaw returns a pointer to the initialized PolyShape.
boxShapeInit:	**Input:**	boxShapeInit accepts a PolyShape pointer, Body pointer and three doubles as inputs.
	Exceptions:	None.
	Transition:	boxShapeInit calculates values for half-width and half-height using the last two input doubles as width and height, respectively. It then initializes the input PolyShape using a new BB generated from the calculated half-dimensions and the remaining parameters.
	Output:	boxShapeInit returns a pointer to the initialized PolyShape.

boxShapeInit2:	**Input:**	boxShapeInit2 accepts a PolyShape pointer, Body pointer, a double and a BB as inputs.
	Exceptions:	None.
	Transition:	boxShapeInit2 creates a Vector array containing the vertices of the box, determined from the input BB. It then initializes the input PolyShape as a box using the array and number of vertices, as well as the remaining parameters.
	Output:	boxShapeInit2 returns a pointer to the initialized PolyShape.
polyShapeNew:	**Input:**	Each polyShapeNew function accepts a Body pointer, an integer, a pointer to a Vector array and a double as inputs. In addition, polyShapeNew (not Raw) accepts a Transform matrix as its last input.
	Exceptions:	None.
	Transition:	Each polyShapeNew function allocates and initializes a new PolyShape object using the input parameters.
	Output:	Each polyShapeNew function returns a pointer to the new PolyShape.
boxShapeNew:	**Input:**	Each boxShapeNew function accepts a Body pointer and a double as inputs. In addition, boxShapeNew accepts two additional doubles, while boxShapeNew2 accepts an additional BB as input.
	Exceptions:	None.
	Transition:	Each boxShapeNew function allocates and initializes a new PolyShape object as a box using the input parameters.
	Output:	Each boxShapeNew function returns a pointer to the new PolyShape.
polyShapeGet:	**Input:**	Each polyShapeGet function accepts a Shape pointer as input. polyShapeGetVert also accepts an additional integer as input.
	Exceptions:	Each polyShapeGet function may throw a NotPolyShape exception if the input Shape pointer is not of the PolyShape class. polyShapeGetVert may also throw an exception if the input integer is greater than or equal to the number of vertices of the input Shape.
	Transition:	None.

	Output:	Each polyShapeGet function returns the value of their corresponding parameter.
polyShapeSet:	**Input:**	Each polyShapeSet function accepts a Shape pointer and their corresponding parameter as inputs. Specifically, each polyShapeSetVerts function accepts an integer (for the number of vertices) and a pointer to a Vector array (holding the vertices) as inputs, and polyShapeSetVerts (not Raw) accepts an additional Transform matrix.
	Exceptions:	Each polyShapeSet function may throw a NotPolyShape exception if the input Shape pointer is not of the PolyShape class. Each polyShapeSetVerts function may throw an IllegalBody exception if the Body associated with the Shape violates an invariant in 6.4.2 after the transitions are complete.
	Transition:	Each polyShapeSet function sets their corresponding parameter with the input value. More specifically, polyShapeVerts transforms the vertices in the input array with the input Transform matrix, places the resultant vertices in a new array, determines the size of the convex hull containing these vertices, and calls polyShapeSetVertsRaw with the new array and hull size. polyShapeVertsRaw frees the current vertices of the input PolyShape, sets its new vertices, updates the mass information of the Shape and recalculates the mass of the associated Body.
	Output:	None.
momentForPoly:	**Input:**	momentForPoly accepts a double for mass, an integer for number of vertices, a pointer to a Vector array containing these vertices, a Vector for offset, and a double for radius as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	momentForPoly returns the calculated moment from the input parameters as a double.
areaForPoly:	**Input:**	areaForPoly accepts an integer for number of vertices, a pointer to a Vector array containing these vertices, and a double for radius as inputs.
	Exceptions:	None.

	Transition:	None.
	Output:	areaForPoly returns the calculated area from the input parameters as a double.
centroidForPoly:	**Input:**	centroidForPoly accepts an integer for number of vertices and a pointer to a Vector array containing these vertices as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	centroidForPoly returns the calculated centroid from the input parameters as a Vector.

7.12.4 Local Constants

PolyShapeClass: ShapeClass
PolyShapeClass := {POLY_SHAPE, polyShapeCacheData, polyShapeDestroy}

7.12.5 Local Functions

setVerts:	**Input:**	setVerts accepts a PolyShape pointer, an integer, and a pointer to a Vector array as inputs.
	Exceptions:	None.
	Transition:	setVerts sets the input PolyShape's number of vertices to the input integer. If this is less than or equal to POLY_SHAPE_INLINE_ALLOC, the PolyShape uses its default _planes array for its vertices. Otherwise, it heap-allocates a new array with the length of the input integer. Finally, the function iterates through the planes array and sets the vertices and their calculated edge normals from the input array. Called by polyShapeInitRaw and polyShapeSetVertsRaw to mutate vertices.
	Output:	None.

8 MIS of the Space Module

8.1 Module Name: Space

8.2 Uses

Rigid Body Module, Shape Module, Vector Module, Collision Solver Module

8.3 Interface Syntax

8.3.1 Exported Constants

collisionHandlerDoNothing: CollisionHandler
collisionHandlerDoNothing := {WILDCARD_COLLISION_TYPE, WILDCARD_COLLISION_TYPE, alwaysCollide, alwaysCollide, doNothing, doNothing, NULL}

CONTACTS_BUFFER_SIZE: $\mathbb{Z}^+$
CONTACTS_BUFFER_SIZE := (BUFFER_BYTES - sizeof(ContactBufferHeader)) / sizeof(Contact)

8.3.2 Exported Access Programs

Name	In	Out	Exceptions
spaceInit	Space*	Space*	-
spaceSetGravity	Space*, Vector	-	-
spaceGetBodies	Space*	array*	-
spaceAddCollisionHandler	Space*, CollisionType, CollisionType	CollisionHandler*	-
spaceAddBody	Space*, Body*	Body*	-
spaceCollideShapes	Shape*, Shape*, CollisionID, Space*	CollisionID	-
spaceStep	Space*, double	-	-

8.4 Semantics

8.4.1 State Variables

Space:

iterations: $\mathbb{Z}$
gravity: Vector
Bodies: Array*
stamp: Timestamp

CollisionHandler:

typeA: CollisionType	preSolveFunc: CollisionPreSolveFunc	separateFunc: CollisionSeparateFunc
typeB: CollisionType	postSolveFunc: CollisionPostSolveFunc	userData: DataPointer
beginFunc: CollisionBeginFunc		

ContactBufferHeader:

stamp: Timestamp
next: ContactBufferHeader*
numContacts: $\mathbb{Z}^+$

ContactBuffer:

header: ContactBufferHeader
contacts: array(Contact)

8.4.2 Assumptions

spaceInit is called before any other access programs.

8.4.3 Semantics

spaceInit:	**Input:**	spaceInit accepts a Space pointer as input.
	Exceptions:	None.
	Transition:	spaceInit initializes the input Space, allocating new data structures accordingly and zero-initializing all other variables.
	Output:	spaceInit returns a pointer to the initialized Space.
spaceCollideShapes:	**Input:**	spaceCollideShapes accepts two Shape pointers, a Collision ID and a Space pointer as inputs.
	Exceptions:	None.

Transition: spaceCollideShapes tests if the input Shapes can be collided using queryReject. If it fails, it returns the input ID. Otherwise, it performs collision detection and makes a new CollisionInfo structure. If a collision occurs, the function modifies the number of Contacts for the input Space, updates the Arbiter for the input Shapes, calls the Arbiter's collision handler functions and updates the Arbiter's timestamp. Otherwise, no further transitions are made. In either case, the function returns the ID of the generated CollisionInfo structure.

Output: spaceCollideShapes returns a CollisionID as output.

spaceStep:

Input: spaceStep accepts a Space pointer and a as inputs.

Exceptions: None.

Transition: spaceStep updates the input Space following the specified timestep (input double). If the timestep is zero, the function exits immediately. Otherwise, it updates the Space's timestamp and current timestep, resets space lists and locks the Space. While the Space is locked, the function calculates new positions of Bodies in the Space and collides Shapes as necessary. before unlocking the Space without running post-step callbacks. Next, it locks the Space once again, clears cached Arbiters, pre-processes the Arbiters, updates the velocities of Bodies in the Space, applies cached impulses, runs the impulse solver, and then runs post-solve callbacks on the Arbiters. Finally, it unlocks the Space and runs post-step callbacks.

Output: None.

8.4.4 Local Functions

spaceUse WildcardDefaultHandler:

Input: spaceUseWildcardDefaultHandler accepts a Space pointer as input.

Exceptions: None.

Transition: The function sets the Space to use wildcards and copies collisionHandlerDefault to the Space's default handler. Called by spaceAddDefaultCollisionHandler.

	Output:	None.
spaceAlloc Contact-Buffer:	**Input:**	spaceAllocContactBuffer accepts a Space pointer as input.
	Exceptions:	None.
	Transition:	spaceAllocContactBuffer heap-allocates a new contact buffer and adds it to the input Space's allocated buffers. Called by spacePushFreshContactBuffer to allocate a new ContactBufferHeader.
	Output:	spaceAllocContactBuffer returns a pointer to the allocated ContactBuffer as output, cast as a ContactBufferHeader pointer.
contactBuffer HeaderInit:	**Input:**	contactBufferHeaderInit accepts a ContactBufferHeader pointer, a Timestamp and another ContactBufferHeader pointer as input.
	Exceptions:	None.
	Transition:	contactBufferHeaderInit initializes the first input Contact-BufferHeader. It modifies its timestamp to the given Timestamp, its next header to be the next header of the second input ContactBufferHeader (or to the first input header if the second one is null), and its number of Contacts to zero. Called by spacePushFreshContactBuffer to initialize a ContactBufferHeader.
	Output:	contactBufferHeaderInit returns a pointer to the initialized ContactBufferHeader.

9 MIS of the Vector Module

9.1 Module Name: Vector

9.2 Uses

This module only uses standard libraries.

9.3 Interface Syntax

9.3.1 Exported Constants

VECT_ERR, zeroVect: Vector
VECT_ERR := {INT_MAX, INT_MIN}
zeroVect := {0.0, 0.0}
PI:= $\mathbb{R}$

9.3.2 Exported Access Programs

Name	In	Out	Exceptions
vect	double, double	Vector	-
vectEqual	Vector, Vector	Boolean	-
vectAdd	Vector, Vector	Vector	-
vectSub	Vector, Vector	Vector	-
vectMult	Vector, double	Vector	-
vectNeg	Vector	Vector	-
vectDot	Vector, Vector	double	-
vectCross	Vector, Vector	double	-
vectPerp	Vector	Vector	-
vectRPerp	Vector	Vector	-
vectProject	Vector, Vector	Vector	-
vectForAngle	double	Vector	-
vectToAngle	Vector	double	-
vectRotate	Vector, Vector	Vector	-
vectUnrotate	Vector, Vector	Vector	-
vectLengthSq	Vector	double	-
vectLength	Vector	double	-
vectNormalize	Vector	Vector	-

vectClamp	Vector, double	Vector	-
vectLerp	Vector, Vector, double	Vector	-
vectDistSq	Vector, Vector	double	-
vectDist	Vector, Vector	double	-
vectNear	Vector, Vector, double	Boolean	-

9.4 Semantics

9.4.1 State Variables

Vector:

x: $\mathbb{R}$
y: $\mathbb{R}$

9.4.2 Semantics

vect:
- **Input:** vect accepts two doubles as input.
- **Exceptions:** None.
- **Transition:** None.
- **Output:** vect returns a new Vector created from the input doubles.

vectEqual:
- **Input:** vectEqual accepts two Vectors as input.
- **Exceptions:** None.
- **Transition:** None.
- **Output:** vectEqual compares the values of the input Vectors and returns true if they are equal, and false otherwise.

vectAdd:
- **Input:** vectAdd accepts two Vectors as input.
- **Exceptions:** None.
- **Transition:** None.
- **Output:** vectAdd returns the sum of the input Vectors.

vectSub:
- **Input:** vectSub accepts two Vectors as input.
- **Exceptions:** None.
- **Transition:** None.

	Output:	vectSub returns the difference of the input Vectors.
vectMult:	**Input:**	vectMult accepts a Vector and a double as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	vectMult returns the scalar multiple of the input Vector with the input double.
vectNeg:	**Input:**	vectNeg accepts a Vector as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectNeg returns the negative of the input Vector.
vectDot:	**Input:**	vectDot accepts two Vectors as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	vectDot returns the dot product of the input Vectors.
vectCross:	**Input:**	vectCross accepts two Vectors as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	vectCross calculates the cross product of the input Vectors and returns the z-component of the product as a double.
vectPerp:	**Input:**	vectPerp accepts a Vector as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectPerp rotates the input Vector by 90 degrees clockwise and returns the resultant Vector as output.
vectRPerp:	**Input:**	vectRPerp accepts a Vector as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectRPerp rotates the input Vector by 90 degrees anti-clockwise and returns the resultant Vector as output.
vectProject:	**Input:**	vectProject accepts two Vectors as inputs.

	Exceptions:	None.
	Transition:	None.
	Output:	vectProject projects the first input Vector onto the second and returns the resultant Vector as output.
vectForAngle:	**Input:**	vectForAngle accepts a double as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectForAngle computes the Vector corresponding to the input angle (double), measured from the x-axis, and returns the result.
vectToAngle:	**Input:**	vectToAngle accepts a Vector as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectToAngle calculates the angle between the input Vector and the x-axis and returns the result as a double.
vectRotate:	**Input:**	vectRotate accepts two Vectors as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	vectRotate rotates the first input Vector by the second using complex multiplication returns the resultant Vector as output.
vectUnrotate:	**Input:**	vectUnrotate accepts two Vectors as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	vectUnrotate is the inverse operation of vectRotate; it returns the original Vector before it was rotated by another Vector using vectRotate.
vectLength:	**Input:**	Each vectLength function accepts a Vector as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectLength and vectLengthSq calculates the regular and squared length of the input Vector, respectively, and returns the result as a double.
vectNormalize:	**Input:**	vectNormalize accepts a Vector as input.
	Exceptions:	None.

	Transition:	None.
	Output:	vectNormalize converts the input Vector into a unit vector and returns the normalized Vector as output.
vectClamp:	**Input:**	vectClamp accepts a Vector and a double as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	vectClamp restricts the input Vector to a length specified by the input double. If the length of the input Vector is less than the input length, vectClamp returns the input Vector. Otherwise, it shrinks the Vector to the specified length and returns the resultant Vector.
vectLerp:	**Input:**	vectLerp accepts two Vectors and a double as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	vectLerp linearly interpolates between the two input Vectors for a percentage specified by the input double, and returns the new interpolated Vector as output.
vectDist:	**Input:**	Each vectDist function accepts two Vectors as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectDist and vectDistSq calculates the regular and squared distance, respectively, between the two input Vectors and returns the result as a double.
vectNear:	**Input:**	vectNear accepts two Vectors and a double as input.
	Exceptions:	None.
	Transition:	None.
	Output:	vectNear returns true if the distance between the input Vectors is less than the distance specified by the input double, and false otherwise.

10 MIS of the Collision Solver Module

10.1 Module Name: Collision

10.2 Uses

Rigid Body Module, Shape Module, Vector Module

10.3 Syntax

10.3.1 Exported Constants

N/A

10.3.2 Exported Access Programs

Name	In	Out	Exceptions
relative_velocity	Body*, Body*, Vector, Vector	Vector	-
normal_relative_velocity	Body*, Body*, Vector, Vector, Vector	double	-
apply_impulse	Body*, Vector, Vector	-	-
apply_impulses	Body*, Body*, Vector, Vector, Vector	-	-
apply_bias_impulse	Body*, Vector, Vector	-	-
apply_bias_impulses	Body*, Body*, Vector, Vector, Vector	-	-
k_scalar_body	Body*, Vector, Vector	double	-
k_scalar	Body*, Body*, Vector, Vector, Vector	double	UnsolvableCollision
collide	Shape*, Shape*, CollisionID, Contact*	CollisionInfo	-

shapesCollide	Shape*, Shape*	ContactPointSet	-

10.4 Interface Semantics

10.4.1 State Variables

SupportPoint:

p: Vector
index: CollisionID

MinkowskiPoint:

a: Vector
b: Vector
ab: Vector
id: CollisionID

SupportContext:

shape1: Shape*
shape2: Shape*
func1: SupportPointFunc
func2: SupportPointFunc

EdgePoint:

p: Vector
hash: HashValue

Edge:

a: EdgePoint
b: EdgePoint
radius: $\mathbb{R}$
normal: Vector

ClosestPoints:

a: Vector	n: Vector	d: $\mathbb{R}$
b: Vector		id: CollisionID

10.4.2 Access Program Semantics

relative_velocity:	**Input:**	relative_velocity accepts two Body pointers and two Vectors as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	relative_velocity calculates the relative velocity of the second input Body relative to the first input Body with the input parameters and returns the result as a Vector.
normal_relative_velocity:	**Input:**	normal_relative_velocity accepts two Body pointers and three Vectors as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	normal_relative_velocity calculates the dot product of the relative velocity between the two input Bodies and the normal (third input Vector) and returns the result as a double.
apply_impulse:	**Input:**	apply_impulse accepts a Body pointer and two Vectors as inputs.
	Exceptions:	None.
	Transition:	apply_impulse recalculates the input Body's linear and angular velocity using the impulse (first input Vector) and point of application (second input Vector).
	Output:	None.
apply_impulses:	**Input:**	apply_impulses accepts two Body pointers and three Vectors as inputs.
	Exceptions:	None.
	Transition:	apply_impulses applies the input impulse (third input Vector) to the two input Bodies, in opposite directions, to recalculate their linear and angular velocities, using their points of application (first and second input Vectors).

	Output:	None.
apply_bias_impulse:	**Input:**	apply_bias_impulse accepts a Body pointer and two Vectors as inputs.
	Exceptions:	None.
	Transition:	apply_bias_impulse recalculates the input Body's linear and angular bias velocities using the impulse (first input Vector) and point of application (second input Vector).
	Output:	None.
apply_bias_impulses:	**Input:**	apply_bias_impulses accepts two Body pointers and three Vectors as inputs.
	Exceptions:	None.
	Transition:	apply_bias_impulses applies the input impulse (third input Vector) to the two input Bodies, in opposite directions, to recalculate their linear and angular bias velocities, using their points of application (first and second input Vectors).
	Output:	None.
k_scalar_body:	**Input:**	k_scalar_body accepts a Body pointer and two Vectors as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	k_scalar_body first calculates the cross product of the two input Vectors. Then, it computes the product of the inverse momentum of the input Body and the squared cross product of the input Vectors. Finally, it calculates the sum of this quantity and the Body's inverse mass, and returns the final result as a double.
k_scalar:	**Input:**	k_scalar accepts two Body pointers and three Vectors as inputs.
	Exceptions:	k_scalar may throw an UnsolvableCollision exception if the calculated value is equal to zero.
	Transition:	None.

	Output:	k_scalar calculates k_scalar_body for the first input Body with the first and last input Vector, and for the second input Body with the second and last input Vector. It then calculates the sum of these results and returns the above sum as a double.
collide:	**Input:**	collide accepts two Shape pointers, a CollisionID and a Contact pointer as inputs.
	Exceptions:	None.
	Transition:	collide creates a new CollisionInfo structure with the input parameters and other fields zero-initialized. The function will then reorder the structure's Shape types as necessary, and apply the appropriate collision function from CollisionFuncs to it.
	Output:	collide returns the new CollisionInfo structure as output.
shapesCollide:	**Input:**	shapesCollide accepts two Shape pointers as inputs.
	Exceptions:	None.
	Transition:	shapesCollide declares a new Contact array and generates a CollisionInfo structure for the input Shapes using the collide function and the Contact array, modifying the array in the process. Next, it declares a new ContactPointSet structure for the collision and sets the number of points and normal accordingly. Finally, the function will iterate through the Contact array to set the points for the ContactPointSet.
	Output:	shapesCollide returns the new ContactPointSet as output.

10.4.3 Local Constants

BuiltinCollisionFuncs: array(CollisionFunc)
BuiltinCollisionFuncs := {CircleToCircle, CollisionError, CollisionError, CircleToSegment, SegmentToSegment, CollisionError, CircleToPoly, SegmentToPoly, PolyToPoly}
CollisionFuncs := BuiltinCollisionFuncs

10.4.4 Local Functions

collisionInfo PushContact:	**Input:**	collisionInfoPushContact accepts a CollisionInfo pointer, two Vectors and a HashValue as inputs.

	Exceptions:	collisionInfoPushContact may throw a CollisionContactOverflow exception when the number of Contacts of the input CollisionInfo exceeds MAX_CONTACTS_PER_ARBITER.
	Transition:	collisionInfoPushContact pushes a new Contact structure into the input CollisionInfo's Contacts array with the other input parameters and updates its number of Contacts accordingly. Called by the ShapeToShape collision functions to add new contact points and by closestPoints in the collision functions for SegmentShapes and PolyShapes.
	Output:	None.
SupportPoint:	**Input:**	Each SupportPoint function accepts a Shape pointer of the Shape type corresponding to the function's prefix and a Vector as inputs.
	Exceptions:	None.
	Transition:	None.
	Output:	Each SupportPoint creates a new SupportPoint with the input Shape's transformed center (CircleShapes), endpoint (SegmentShape) or vertex (PolyShape), with the appropriate index of the point as its CollisionID. Each corresponding function is used by the appropriate ShapeToShape function in generating the SupportPointContext to be passed to GJK.
support:	**Input:**	support accepts a SupportContext pointer and a Vector as inputs.
	Exceptions:	None.
	Transition:	support calculates the maximal point on the Minkowski difference of two shapes along a particular axis. It generates two SupportPoints using the SupportPointFunc functions and Shapes contained in the input SupportContext and the input Vector, and creates a new MinkowskiPoint with these SupportPoints. Used in the calculations of GJK and EPA.
	Output:	support returns the new MinkowskiPoint as output.
supportEdgeFor:	**Input:**	Each supportEdgeFor function accepts a Shape pointer of the corresponding Shape type and a Vector as inputs.

	Exceptions:	None.
	Transition:	Each supportEdgeFor function computes the dot products of the input Shape's vertices (for PolyShapes) or normal (for SegmentShapes) with the input Vector to calculate a support edge for the input Shape, which is an edge of a SegmentShape or PolyShape that is in contact with another Shape. Called by some ShapeToShape functions to determine contact points for SegmentShapes and PolyShapes.
	Output:	Each supportEdgeFor function generates a new Edge structure containing information about the calculated support edge and returns it as output.
closestT:	**Input:**	closestT accepts two Vectors as inputs.
	Exceptions:	None.
	Transition:	closestT finds the closest $\mathbf{p}(t)$ to the origin $(0, 0)$, where $\mathbf{p}(t) = \frac{a(1-t)+b(1+t)}{2}$, a and b are the two input Vectors and $t \in [-1, 1]$. The function clamps the result to this interval. Used for the computation of closest points in closestPointsNew.
	Output:	closestT returns a double as output.
lerpT:	**Input:**	lerpT accepts two Vectors and a double as inputs.
	Exceptions:	None.
	Transition:	lerpT functions similarly to vectLerp, except the parameter t, the last input double, is constrained to the interval $[-1, 1]$. Used for the computation of closest points in closestPointsNew.
	Output:	lerpT returns a Vector as output.
closestPoints New:	**Input:**	closestPointsNew accepts two MinkowskiPoint structures as inputs.
	Exceptions:	None.

Transition: closestPointsNew finds the closest edge to the origin (0, 0) on the Minkowski difference of two Shapes, which is obtained by using closestT and lerpT with the input MinkowskiPoints. This is used to calculate the closest points on the surface of two Shapes, as well as the distance and the minimum separating axis between them. The function then generates a new ClosestPoints structure using the calculated data and the concatenated IDs of the input MinkowskiPoints. Used to compute closest points in EPA and GJK.

Output: closestPointsNew returns the new ClosestPoints as output.

EPA:

Input: EPA accepts a SupportContext pointer, and three MinkowskiPoint structures as inputs.

Exceptions: EPA may throw a SameVertices exception when the EPA vertices are the same. It may also raise HighIterWarning when the number of iterations reaches the WARN_EPA_ITERATIONS threshold.

Transition: EPA recursively finds the closest points on the surface of two overlapping Shapes using the EPA (Expanding Polytope Algorithm). The function initializes a convex hull array of vertices and each recursion adds a point to the hull until the function obtains the closest points on the surfaces of the Shapes.

Output: EPA generates a new ClosestPoints structure containing information about the computed closest points and returns it as output.

GJK:

Input: GJK accepts a SupportContext pointer and a CollisionID pointer as inputs.

Exceptions: GJK may raise a HighIterWarning when the number of iterations reaches the WARN_GJK_ITERATIONS threshold, or WARN_EPA_ITERATIONS when EPA needs to be called.

Transition: GJK recursively finds the closest points between two shapes using the (Gilbert-Johnson-Keerthi) algorithm. If the collision Shapes are found to overlap at some iteration of the algorithm, the function will then execute EPA to find the closest points.

	Output:	GJK generates a new ClosestPoints structure containing information about the computed closest points and returns it as output.
contactPoints:	**Input:**	contactPoints accepts two Edge structures, a ClosestPoints structure and a CollisionInfo pointer as inputs.
	Exceptions:	None.
	Transition:	contactPoints finds contact point pairs on the surfaces of the input support Edges and pushes a new Contact structure into the input CollisionInfo's Contacts array. This is used in ShapeToShape functions involving SegmentShapes and PolyShapes (except for CircleToPoly).
	Output:	None.
ShapeToShape:	**Input:**	Each ShapeToShape function accept two pointers to the corresponding Shape types and a CollisionInfo pointer as inputs.
	Exceptions:	None.
	Transition:	Each ShapeToShape function calls GJK to find the ClosestPoints for the two input Shapes and uses it to check if the current distance between the two Shapes is less than the minimum collision distance (usually determined by the sum of the Shapes' radii). If so, the function pushes a new Contact structure containing information about the Shapes' contact points into the Contacts array of the input CollisionInfo. These functions are stored in the exported CollisionFuncs array, and the appropriate function will be called by collide.
	Output:	None.
CollisionError:	**Input:**	CollisionError accepts two Shape pointers and a CollisionInfo pointer as inputs.
	Exceptions:	CollisionError throws an eponymous exception when the types of the input Shapes are not in sorted order.
	Transition:	CollisionError throws an exception and aborts the program. This function is stored in the exported CollisionFuncs array and called by collide when the colliding Shape types are not in order.

Output: None.