Software Stability Analysis: System Verification and Validation Plan

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1 Revision History

Date	Version	Notes
10/10/18	1.0	Initial template fill-ins

2 Symbols, Abbreviations and Acronyms

The symbols, abbreviations, and acronyms used in this document include those defined in the table below, as well as any defined in the tables found in Section 2 of the Software Requirements Specification (SRS) document.

symbol	description
j	index representing a single coordinate
MIS	Module Interface Specification
MG	Module Guide
TC	Test Case
VnV	Verification and Validation

Contents

List of Tables

List of Figures

This document outlines the system verification and validation plan for the software. General information regarding the system under test and the objectives of the verification and validation activities is provided in Section 3. Overviews of verification plans for the SRS, design, and implementation are given in Section 4, along with a summary of the validation plan for the software. Section 5 details specific system test cases for verifying the requirements outlined in Section 6 of the SRS. A summary of planned static verification activities can be found in Section 6 of this document.

3 General Information

3.1 Summary

The software being tested is the Slope Stability Analysis Program (SSP). Based on user-defined slope geometry and material properties, SSP determines the critical slip surface of the given slope, the corresponding factor of safety, and interslice normal and shear forces along the critical slip surface.

3.2 Objectives

The purpose of the verification and validation activities is to confirm that SSP exhibits desired software qualities. The primary objective is to build confidence in the correctness of the software. The tests described in this document cannot definitively prove correctness, but they can build confidence by verifying that the software is correct for the cases covered by tests. Other important qualities to be verified are the understandability, maintainability, and reusability of the software.

3.3 References

Extensive information about the purpose and requirements of SSP can be found in the SRS document. This System VnV Plan is complemented by the System VnV Report, where the results of the tests planned in this document are discussed. For more details on test cases specific to the implementation of SSP, consult the Unit VnV Plan document. The latest documentation for SSP can be found on GitHub, at
https://github.com/smiths/caseStudies/tree/master/CaseStudies/ssp.

4 Plan

4.1 Verification and Validation Team

Brooks MacLachlan is responsible for the verification and validation of SSP, though input from various students and the professor, Dr. Spencer Smith, of CAS 741 will also contribute.

4.2 SRS Verification Plan

SRS verification will be carried out by reviews. Brooks MacLachlan will extensively review the SRS, including reviewing the sources to confirm that the theories and models described in the SRS are correct. Any issues identified during this review will be fixed immediately by Brooks MacLachlan. This review will be followed up by additional reviews by Dr. Spencer Smith and Vajiheh Motamer, a student in CAS 741. Any issues identified by these reviewers will be recorded through the issue tracker on GitHub, and addressed by Brooks MacLachlan. Brooks MacLachlan will also informally present the SRS to the entire class of CAS 741. Any issues discovered during this presentation will be subsequently fixed by Brooks MacLachlan. A focus of these reviews will be to verify the non-functional requirements of correctness and understandability by identifying information in the SRS that is incorrect or ambiguous.

4.3 Design Verification Plan

The design of SSP is outlined in the Module Guide (MG) and Module Interface Specification (MIS) documents. The design will be verified by review of these documents. Brooks MacLachlan will extensively review both documents. To verify correctness, part of this review will be to ensure that every module traces to a requirement and that every requirement is traced to by a module. To evaluate the modularity of the design, "uses" relationships between modules will be examined to ensure modules do not mutually use each other. The review will also check that each module hides exactly one secret. Ensuring the program is well-modularized contributes to verification of the non-functional requirements of maintainability and reusability. Any issues identified during these reviews will be fixed immediately by Brooks MacLachlan. Dr. Spencer Smith will also review both documents. An ad-

ditional review will be conducted by students in CAS 741: Karol Serkis for the MG and Malavika Srinivasan for the MIS. Any issues identified by these reviews will be recorded through the issue tracker on GitHub, and addressed by Brooks MacLachlan. Brooks MacLachlan will also informally present the MG to the entire class of CAS 741. Any design issues discovered during this presentation will be subsequently fixed by Brooks MacLachlan. Reviews of these design documents will also focus on ensuring understandability by identifying descriptions and specifications that are ambiguous.

4.4 Implementation Verification Plan

The implementation of SSP will be verified by review and by testing. Brooks MacLachlan will extensively review the implementation. Any issues identified during these reviews will be fixed immediately by Brooks MacLachlan. This review will be followed up by reviews by Dr. Spencer Smith and Robert White, a student in CAS 741. Any issues identified by these reviews will be recorded through the issue tracker on GitHub, and addressed by Brooks MacLachlan. Brooks MacLachlan will also informally present the implementation to the entire class of CAS 741. Any implementation issues discovered during this presentation will be subsequently fixed by Brooks MacLachlan. These reviews will contribute to verifying correctness and understandability of the software by identifying code that is not traceable to any specifications described in the SRS, MG, or MIS.

The implementation will also be verified by testing. Specific test cases are outlined in Section 5 of this document. Test cases that are directly dependent on implementation details are outlined in an accompanying document, the Unit VnV Plan. All tests will be written (where applicable), reviewed, executed, and reported on by Brooks MacLachlan.

4.5 Software Validation Plan

There is no validation plan for SSP.

5 System Test Description

The values in Table 1 will be used as input for many of the test cases described throughout this section. These values were taken from the User's Guide for this project by Karchewski (8 January 2012). Individual test cases will reference the table as input but specify new values for any input parameter that should have a different value than specified by the table.

5.1 Tests for Functional Requirements

5.1.1 User Input Tests

Valid User Input
The following set of test cases is intended to cover different forms of valid user input. Valid user input includes: slopes with or without a water table, slopes with one layer or multiple layers, slopes that increase or decrease as x increases, slopes described by the minimum number of points, 2, or more than the minimum number of points, and slopes solved with f as a constant or as a half-sine.

TC1: test-valid_input_decreasing

Control: Automatic

Initial State: New session

Input: As described in Table 1.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

TC2: test-valid_input_increasing

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with slope coordinates $\{(x_{us}, y_{us})\}$ increasing as x increases, as follows: $\{(0, 15), (30, 15), (40, 20), (50, 25), (70, 25)\}$.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

Input	Unit	Value
$\{(x_{\mathrm{us}}, y_{\mathrm{us}})\}$	m	$\{(0, 25), (20, 25), (30, 20), (40, 15), (70, 15)\}$
$\{(x_{\mathrm{wt}}, y_{\mathrm{wt}})\}$	m	$\{(0, 22), (10.87, 21.28), (21.14, 19.68), (31.21, 17.17), (38.69, 14.56), (40, 14), (70, 14)\}$
$x_{\mathrm{slip}}^{\mathrm{minStart}}$	m	10
$x_{\mathrm{slip}}^{\mathrm{maxStart}}$	m	24
$x_{\mathrm{slip}}^{\mathrm{minEnd}}$	m	34
$x_{\mathrm{slip}}^{\mathrm{maxEnd}}$	m	53
$y_{\mathrm{slip}}^{\mathrm{min}}$	m	5
$y_{\mathrm{slip}}^{\mathrm{max}}$	m	26
c'	Pa	5000
φ'	°	20
γ	$\mathrm{N\,m^{-3}}$	15000
γ_{Sat}	$\mathrm{N\,m^{-3}}$	15000
γ_{w}	$\mathrm{N\,m^{-3}}$	9800
Boolean representing the form of the interslice variation function f. 1 means f is constant, 0 means f is a half-sine	N/A	0

Table 1: Input to be used for test cases

TC3: test-valid_input_multiple

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with an additional slope layer

5

described by the following coordinates: $\{(0, 20), (36, 17), (40, 15), (70, 15)\}$.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

TC4: test-valid_input_noWT

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with no water table vertices $\{(x_{\text{wt}}, y_{\text{wt}})\}$.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

TC5: test-valid_input_minimal

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with except with only 2 slope coordinates $\{(x_{\text{us}}, y_{\text{us}})\}$, as follows: $\{(0, 25), (20, 25)$. Also, with no water table vertices $\{(x_{\text{wt}}, y_{\text{wt}})\}$.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

TC6: test-valid_input_fConstant

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with f as a constant. This is accomplished by setting the Boolean-type input to 1.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

TC7: test-valid_input_xMinStartEqual

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with $x_{\text{slip}}^{\text{minStart}}$ set to 0.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

TC8: test-valid_input_xMaxEndEqual

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with $x_{\text{slip}}^{\text{maxEnd}}$ set to 70.

Output: SSP runs to completion with no errors

How test will be performed: Automated test on unit testing framework

Invalid User Input

The test cases described in Table 2 are intended to cover all invalid input possibilities. Invalid input is input that defies the data constraints described in Section 5.2.6 of the SRS. These test cases are identical to each other with the exception of their input. The input for each is specified in Table 2. For each test case, the inputs not specified in this table are specified in Table 1. The control method for these test cases is automatic. The initial state for each is a new session. The expected output is the generation of an exception. The tests will be performed as automated tests on a unit testing framework.

Test Case	Test Name	Input	Value
TC9	test-invalid_slope_decToInc	$\{(x_{\text{us}}, y_{\text{us}})\}$	$\{(0, 25), (20, 25), (30, 20), (40, 25), (70, 25)\}$
TC10	test-invalid_slope_incToDec	$\{(x_{\text{us}}, y_{\text{us}})\}$	$\{(0, 15), (20, 15), (30, 20), (40, 15), (70, 15)\}$
TC11	test-invalid_slope_diffStart	$\{(x_{\text{us}}, y_{\text{us}})\}$	$\{(0, 15), (20, 15), (30, 20), (40, 25), (70, 25)\}, \{(10, 15), (20, 15), (30, 20), (40, 25), (70, 25)\}$
TC12	test-invalid_slope_diffEnd	$\{(x_{\text{us}}, y_{\text{us}})\}$	$\{(0, 15), (20, 15), (30, 20), (40, 25), (70, 25)\}, \{(10, 15), (20, 15), (30, 20), (40, 25), (60, 25)\}$

TC13	test-invalid_slope_onePt	$\{(x_{\text{us}}, y_{\text{us}})\}$	$\{(0,\ 15)\}$
TC14	test-invalid_slope_diffStartWT	$\{(x_{\text{wt}}, y_{\text{wt}})\}$	$\{(10,\ 22),\ (10.87,\ 21.28),\ (21.14,\ 19.68),\ (31.21,\ 17.17),\ (38.69,\ 14.56),\ (40,\ 14),\ (70,\ 14)\}$
TC15	test-invalid_slope_diffEndWT	$\{(x_{\text{wt}}, y_{\text{wt}})\}$	$\{(0,\ 22),\ (10.87,\ 21.28),\ (21.14,\ 19.68),\ (31.21,\ 17.17),\ (38.69,\ 14.56),\ (40,\ 14),\ (60,\ 14)\}$
TC16	test-invalid_slope_onePtWT	$\{(x_{\text{wt}}, y_{\text{wt}})\}$	$\{(0,\ 22)\}$
TC17	test-invalid_slip_xMinStart	$x_{\text{slip}}^{\text{minStart}}$	-5
TC18	test-invalid_slip_xMaxStart	$x_{\text{slip}}^{\text{maxStart}}$	5
TC19	test-invalid_slip_xMinEnd	$x_{\text{slip}}^{\text{minStart}}$	20
TC20	test-invalid_slip_xMaxEnd	$x_{\text{slip}}^{\text{minStart}}$	30
TC21	test-invalid_slip_xMaxEndOut	$x_{\text{slip}}^{\text{minStart}}$	75
TC22	test-invalid_slip_yMin	$y_{\text{slip}}^{\text{min}}$	30
TC23	test-invalid_slip_yMax	$y_{\text{slip}}^{\text{min}}$	0
TC24	test-invalid_slip_yEqual	$y_{\text{slip}}^{\text{min}}$	5
TC25	test-invalid_cohesion_0	c'	0
TC26	test-invalid_cohesion_negative	c'	-5
TC27	test-invalid_angFric_0	φ'	0
TC28	test-invalid_angFric_negative	φ'	-5
TC29	test-invalid_angFric_90	φ'	90
TC30	test-invalid_angFric_obtuse	φ'	100
TC31	test-invalid_unitWt_0	γ	0
TC32	test-invalid_unitWt_negative	γ	-5
TC33	test-invalid_unitWtSat_0	γ_{Sat}	0

TC34	test-invalid_unitWtSat_negative	γ_{Sat}	-5
TC35	test-invalid_unitWtWater_0	γ_{w}	0
TC36	test-invalid_unitWtWater_negative	γ_{w}	-5

Table 2: Faulty Input Test Cases

5.1.2 Calculation Tests

The tests in this section verify that SSP correctly determines critical slip surfaces and calculates factors of safety by comparing results obtained from SSP to results reported in literature or results obtained by the original version of SSP for some specific example problems. In each test case, the sources to compare to are specified.

TC37: test-ex1_FS

    Control: Automatic

    Initial State: New session

    Input: As described in Table 3.

    Output: Relative error between factor of safety calculated by SSP and factor of safety from literature, as described below.

Source	Factor of Safety
Greco (1 July 1996)	1.3270
Malkawi et al. (1 August 2001)	1.2380
Cheng et al. (27 Decemeber 2006)	1.3250
Li et al. (25 June 2010)	1.3270

    How test will be performed: Automated test on unit testing framework

TC38: test-ex1_slip

    Control: Automatic

    Initial State: New session

    Input: As described in Table 3.

Input	Unit	Value
$\{(x_{\mathrm{us}}, y_{\mathrm{us}})\}$	m	$\{(0, 5), (5, 5), (15, 10), (25, 10)\}$
$\{(x_{\mathrm{wt}}, y_{\mathrm{wt}})\}$	m	N/A
$x_{\mathrm{slip}}^{\mathrm{minStart}}$	m	0
$x_{\mathrm{slip}}^{\mathrm{maxStart}}$	m	10
$x_{\mathrm{slip}}^{\mathrm{minEnd}}$	m	10
$x_{\mathrm{slip}}^{\mathrm{maxEnd}}$	m	20
$y_{\mathrm{slip}}^{\mathrm{min}}$	m	0
$y_{\mathrm{slip}}^{\mathrm{max}}$	m	12
c'	Pa	9800
φ'	°	10
γ	$\mathrm{N\,m^{-3}}$	17640
γ_{Sat}	$\mathrm{N\,m^{-3}}$	17640
γ_{w}	$\mathrm{N\,m^{-3}}$	N/A
Boolean representing the form of the interslice variation function f. 1 means f is constant, 0 means f is a half-sine	N/A	0

Table 3: Input to be used for literature comparison test cases

Output: Distance error between critical slip surface determined by SSP and critical slip surfaces from from literature. Distance error is calculated by dividing the critical slip surfaces into 10 evenly spaced vertices, calculating the distance between respective vertices from SSP and from literature, and adding the distance for all 10 vertices together. For brevity, the table below gives only the starting and ending x values of the critical slip surfaces from literature. More complete descriptions of the slip surface can be found by referring to the source.

Source	Starting x value	Ending x value
Greco (1 July 1996)	4.8077	18.2911
Malkawi et al. (1 August 2001)	3.5400	20.1419
Cheng et al. (27 Decemeber 2006)	4.5258	18.3943
Li et al. (25 June 2010)	4.6000	18.5300

How test will be performed: Automated test on unit testing framework

TC39:   test-origProg_FS

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with an additional slope layer described by the following coordinates: {(0, 20), (36, 17), (40, 15), (70, 15)}.

Output: Relative error between the factor of safety calculated by SSP and the factor of safety calculated by the original version of SSP, 1.3937, which is assumed to be correct and can be found at https://github.com/smiths/caseStudies/tree/master/CaseStudies/ssp/misc

How test will be performed: Automated test on unit testing framework

TC40:   test-origProg_slip

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with an additional slope layer described by the following coordinates: {(0, 20), (36, 17), (40, 15), (70, 15)}.

Output: Distance error between the critical slip surface calculated by SSP and the critical slip surface calculated by the original version of SSP, which is assumed to be correct and can be found at https://github.com/smiths/caseStudies/tree/master/CaseStudies/ssp/misc. Distance error is calculated by dividing the critical slip surfaces into 10 evenly spaced vertices, calculating the distance between respective vertices from SSP and from the original SSP, and adding the distance for all 10 vertices together. The critical slip surface calculated by the original version of SSP is shown in Figure 1
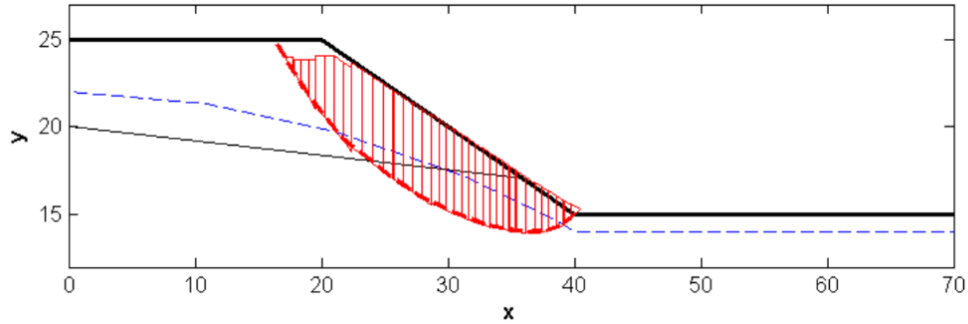
Figure 1: The critical slip surface for TC40 calculated by the original version of SSP

How test will be performed: Automated test on unit testing framework

TC41: test-origProg_normal

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with an additional slope layer described by the following coordinates: {(0, 20), (36, 17), (40, 15), (70, 15)}.

Output: Relative error between the interslice normal force calculated by SSP and the interslice normal force calculated by the original version of SSP, which is assumed to be correct and can be found at https://github.com/smiths/caseStudies/tree/master/CaseStudies/ssp/misc. The relative error will be calculated at 10 evenly spaced points spanning the critical slip surface and averaged to obtain the relative error to consider for this test case. The interslice normal forces along the critical slip surface calculated by the original SSP are shown in Figure 2.

How test will be performed: Automated test on unit testing framework

TC42: test-origProg_shear

Control: Automatic

Initial State: New session

Input: As described in Table 1, except with an additional slope layer described by the following coordinates: {(0, 20), (36, 17), (40, 15), (70, 15)}.

Output: Relative error between the interslice shear force calculated by SSP and the interslice shear force calculated by the original version of SSP, which is assumed to be correct and can be found at https://github.com/smiths/caseStudies/tree/master/CaseStudies/ssp/misc. The relative error will be calculated at 10 evenly spaced points spanning the critical slip surface and averaged to obtain the relative error to consider for this test case. The interslice shear forces along the critical slip surface calculated by the original SSP are shown in Figure 2.

How test will be performed: Automated test on unit testing framework
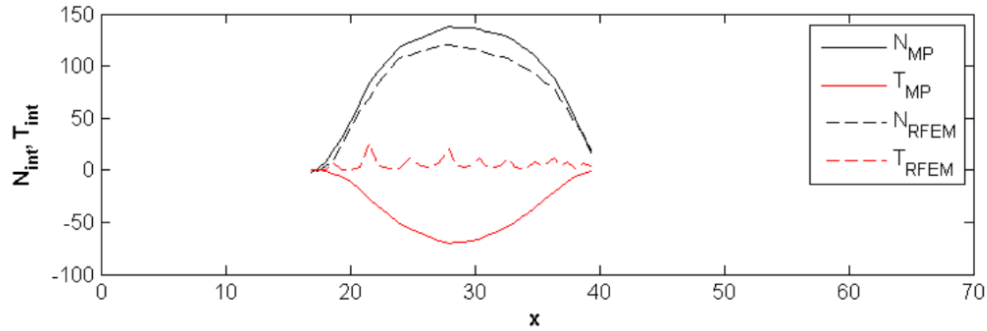
Figure 2: The interslice normal and shear forces for TC41 and TC42 calculated by the original version of SSP, where N_{MP} is the interslice normal force and T_{MP} is the interslice shear force

[I wanted to add tests for the correctness NFR in Section 5.2 but felt that it was already covered by these functional requirement test cases. Is that true? —BM]

5.1.3 Output Tests

Output Delivery Tests
The following set of test cases are intended to verify that all expected outputs are delivered by SSP.

13

TC43: test-output_FS

> Control: Automatic
>
> Initial State: New session
>
> Input: As described in Table 1.
>
> Output: SSP reports a value for the factor of safety of the critical slip surface
>
> How test will be performed: Automated test on unit testing framework

TC44: test-output_slip

> Control: Automatic
>
> Initial State: New session
>
> Input: As described in Table 1.
>
> Output: SSP reports the coordinates of the critical slip surface for the slope.
>
> How test will be performed: Automated test on unit testing framework

TC45: test-output_normal

> Control: Automatic
>
> Initial State: New session
>
> Input: As described in Table 1.
>
> Output: SSP reports the interslice normal force along the critical slip surface for the slope.
>
> How test will be performed: Automated test on unit testing framework

TC46: test-output_shear

> Control: Automatic
>
> Initial State: New session
>
> Input: As described in Table 1.
>
> Output: SSP reports the interslice shear force along the critical slip surface for the slope.
>
> How test will be performed: Automated test on unit testing framework

Output Verification Tests

The following set of test cases are intended to verify that that the output of SSP obeys the physical constraints described in Section 5.2.6 of the SRS.

TC47: test-valid_output_FS

> Control: Automatic
>
> Initial State: New session
>
> Input: As described in Table 1.
>
> Output: The factor of safety reported by SSP is greater than 0.
>
> How test will be performed: Automated test on unit testing framework

TC48: test-valid_output_slip

> Control: Automatic
>
> Initial State: New session
>
> Input: As described in Table 1.
>
> Output: The slope between consecutive coordinates of the critical slip surface are always increasing. In mathematical terms, if j is an index representing a single coordinate and $j + 1$ represents the consecutive coordinate in the positive x-direction,
> $\left(\frac{y_{\mathrm{cs}_{j+2}} - y_{\mathrm{cs}_{j+1}}}{x_{\mathrm{cs}_{j+2}} - x_{\mathrm{cs}_{j+1}}} \right) - \left(\frac{y_{\mathrm{cs}_{j+1}} - y_{\mathrm{cs}_j}}{x_{\mathrm{cs}_{j+1}} - x_{\mathrm{cs}_j}} \right) > 0.$
>
> How test will be performed: Automated test on unit testing framework

TC49: test-valid_output_normal

> Control: Automatic
>
> Initial State: New session
>
> Input: As described in Table 1.
>
> Output: The interslice normal forces reported by SSP are always greater than 0 across the entire critical slip surface.
>
> How test will be performed: Automated test on unit testing framework

TC50: test-valid_output_shear

> Control: Automatic
>
> Initial State: New session

Input: As described in Table 1.

Output: The interslice shear forces reported by SSP are always less than 0 across the entire critical slip surface.

How test will be performed: Automated test on unit testing framework

5.2 Tests for Nonfunctional Requirements

5.2.1 Maintainability test

TC51: test-maintainability

Type: Manual

Initial State: Test subject has a completed MG for SSP

Input/Condition: MG for SSP and the following question "If you were tasked with modifying SSP to accept an imposed surface load as an input and incorporate this additional force into the computation, which module(s) would you change?"

Output/Result: Input Module, Input Verification Module, Calculation Module

[Subject to change since design has not been completed yet —BM]

How test will be performed: Test subject will be asked the question described in "Input/Condition" and must answer only by consulting the MG. Their answer will be recorded and compared with the correct answer outlined in "Output/Result". If the subject answers correctly, the test passes and confidence in the maintainability of SSP is increased. If the subject answers incorrectly, the test fails and the documentation or implementation of SSP must be updated to be more maintainable.

5.2.2 Reusability test

TC52: test-reusability

Type: Manual

Initial State: There is a completed implementation of SSP

Input/Condition: Code that prompts the user for command-line inputs related to slope stability analysis.

Output/Result: An alternative version of SSP that uses the input code. All modules in the alternative version should be identical to the existing SSP modules, with the exception of the Input Module.

How test will be performed: The alternative version of SSP will be developed by Brooks MacLachlan. If only the Input Module is changed from the existing version, then the test passes and confidence in the reusability of SSP's modules is increased. If other modules need to be changed, the test fails and the other modules must be modified to be completely reusable.

5.3 Traceability Between Test Cases and Requirements

The purpose of the traceability matrix shown in Table 4 is to provide easy references on which requirements are verified by which test cases, and which test cases need to be updated if a requirement changes. If a requirement is changed, the items in the column of that requirement that are marked with an "X" may have to be modified as well.

	R1	R2	R3	R4	R5	R6	R7	R8	R9	R10
TC1 - TC8	X									
TC9 - TC36		X								
TC37 - TC40			X	X	X					
TC41									X	
TC42										X
TC43							X			
TC44								X		
TC45									X	
TC46										X
TC47 - TC50						X				

Table 4: Traceability Matrix Showing the Connections Between Requirements and Test Cases

6 Static Verification Techniques

The reviews described in Section 4.4 will employ the static verification techniques of code walkthroughs and code inspection to attempt to uncover issues with the implementation.

7 References

Y. M. Cheng, Liang Li, Shi chun Chi, and W. B. Wei. Particle swarm optimization algorithm for the location of the critical non-circular failure surface in two-dimensional slope stability analysis. *Computers and Geotechnics*, (24):92–103, 27 Decemeber 2006.

Venanzio R. Greco. Efficient monte carlo technique for locating critical slip surface. *J. Geotech. Engrg.*, (122):517–525, 1 July 1996.

Brandon Karchewski. Slope stability program (ssp) user's guide 1.0, 8 January 2012.

Yu-Chao Li, Yun-Min Chen, Tony L.T Zhan, Dao-Sheng Ling, and Peter John Cleall. An efficient approach for locating the critical slip surface in slope stability analyses using a real-coded genetic algorithm. *Can. Geotech. J.*, (47):806–820, 25 June 2010.

Abdallah I. Husein Malkawi, Waleed F. Hassan, and Sarada K. Sarma. Global search method for locating general slip surface using monte carlo techniques. *J. Geotech. Geoenviron. Eng.*, (127):688–698, 1 August 2001.