

1) Given an array of  $[4, -2, 5, 3, 10, 5, 2, 8, -3, 6, 7, -4, 1, 9, -9, 10, -6, 8, 11, 9]$  integers find the maximum and minimum product that can be obtained by multiply two integers from the array

sol array is  $[4, -2, 5, 3, 10, 5, 2, 8, -3, 6, 7, -4, 1, 9, -9, 10, -6, 8, 11, 9]$   
we need to consider the largest and smallest product that can be formed by selecting two numbers from the array

1) Sort the array

Sorted array

$[-9, -8, -6, -5, -4, -3, -2, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11]$

- ⇒ Identify possible candidates for maximum product
- ⇒ Identify possible candidates for minimum product

Calculating maximum product

- \* The two largest positive numbers are 10 and 11  $10 \times 11 = 110$
- \* The two smallest negative numbers are -9 and -8  $-9 \times -8 = 72$

the maximum product

Calculating minimum product:-

The largest positive and negative numbers 11 and -9

$$11 \times -9 = -99$$

The smallest positive and negative numbers are

$$-9 \times 8 = -72$$

-99 is smaller than -72

maximum product = 110 and minimum product = -99

2) Demonstrate the priority search method to search for the key = 23 from the array = {2, 5, 8, 12, 16, 23, 38, 56, 72, 91}

sol. given array = {2, 5, 8, 12, 16, 23, 38, 56, 72, 91}

1, initialize pointers

low = 0 and high = 9

calculate  $mid = \left\lfloor \frac{low + high}{2} \right\rfloor = \frac{0 + 9}{2} = 4$

Compare  $arr[mid]$  with key:

$arr[4] = 16$

Since  $16 < 23$  update  $low = mid + 1 = 5$

calculate  $arr[mid]$  with key:

$arr[7] = 56$

Since  $56 > 23$  update  $high = mid - 1 = 6$

$mid = \left\lfloor \frac{5 + 6}{2} \right\rfloor = 5$

$arr[mid] = arr[5] = 23$

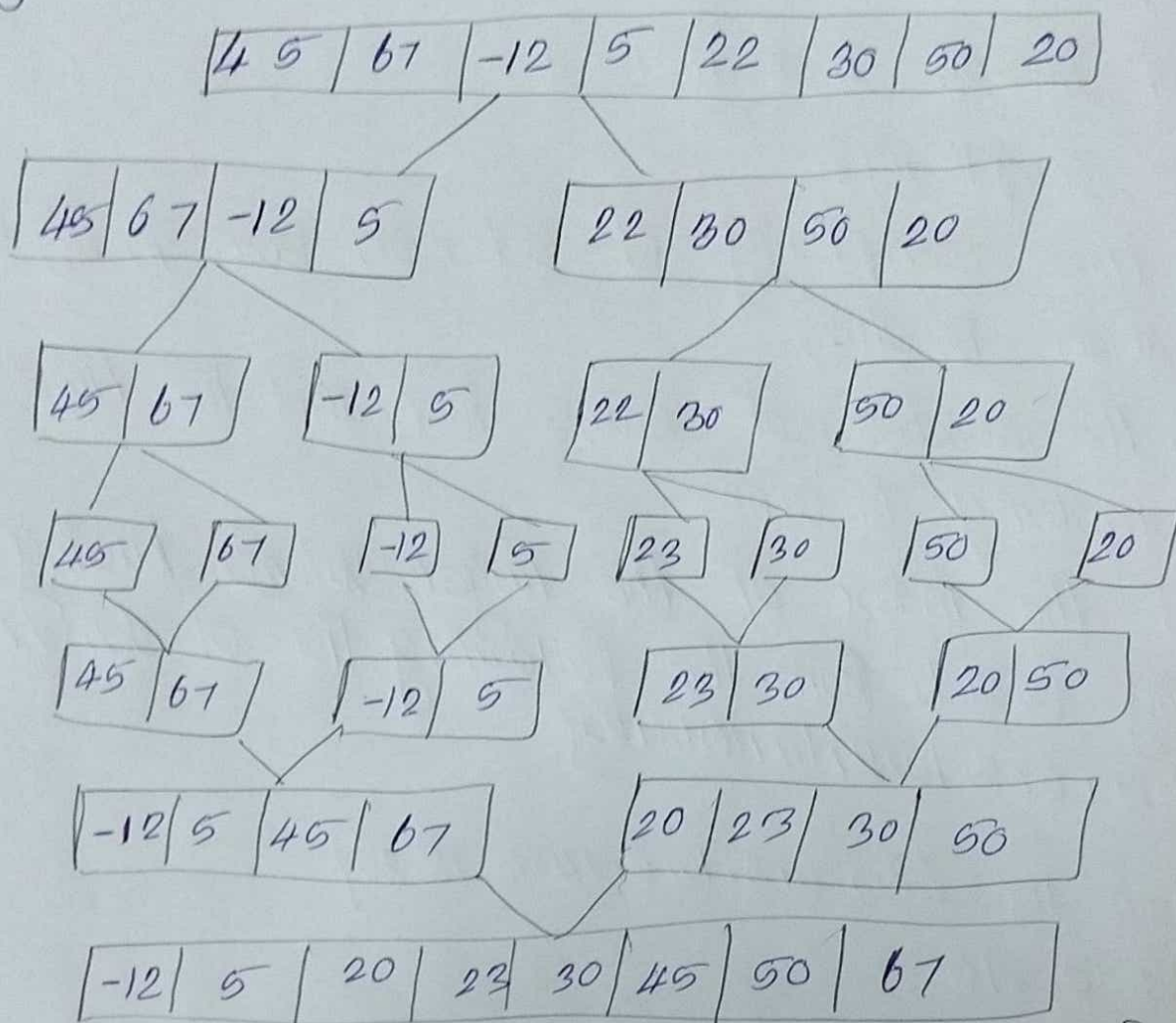
$23 = 23$  The is found at index = 5

$\therefore$  The key = 23 is found at index 5

3) Apply merge sort and other list of 8 elements, Data  $d = \{4, 5, 6, 7, -12, 5, 22, 30, 50, 20\}$ . Set up a recursive relation for the number of key comparisons made by merge sort



merge sort



$\therefore$  The sorted list =  $(-12, 5, 20, 23, 30, 45, 50, 67)$

- 4) Find the no. of times to perform solving swapping for selection sort also estimate the time complexity for the order of notation set  $S(12, 7, 5, -2, 8, 6, 13, 4)$ .  
The selection sort algorithm always makes exactly  $n-1$  swaps in the worst case, where  $n$  is the no. of element in the list.  
Given  $S = \{12, 7, 5, -2, 8, 6, 13, 4\}$

No. of Element,  $n = 8$

No. of swaps  $n = 8$   $n - 1 = 7$

Time complexity:-

The time complexity of selection sort in Big-O notation is  $O(n^2)$

So, the numbers of swaps is 7, and the time complexity is  $O(n^2)$

5) Find the index of the target value using binary search from the following list of elements  
[2, 4, 6, 8, 10, 12, 14, 16, 18, 20]

Given list = [2, 4, 6, 8, 10, 12, 14, 16, 18, 20]

Value = 10

Low = 0 and high = 9

$$\text{mid} = \frac{\text{low} + \text{high}}{2} = \frac{0 + 9}{2} = 4$$

Ex:- List(4) mid = 10, mid = value

Since  $10 == 10$  the target is found at index 4

The target value = 10 is found at index 4,